## 0.0.1 At Key

The operation atKey will return the Value v at some specified

• Top level Key k within KV

$$atKey(KV, k) \rightarrow v$$

• Nested location  $K = \langle k_i..k_n..k_j \rangle$  within KV

$$atKey(KV,K) \rightarrow v$$

such that if KV is a collection of Key Value pair(s)  $\langle k_0 v_{k_0}, k_1 v_{k_1} \rangle$  where

$$k_0 = abc \land v_{k_0} = 123$$

$$\Rightarrow$$

$$k_0 v_{k_0} = abc \mapsto 123$$

and

$$k_1 = def \land v_{k_1} = xyz \mapsto 456$$
 
$$\Rightarrow$$
 
$$k_1v_{k_1} = def \mapsto xyz \mapsto 456$$

such that

$$KV = \langle abc \mapsto 123, \ def \mapsto xyz \mapsto 456 \rangle$$

When k is a single Key

•  $k \notin KV$ , atKey will return the representation of nothingness

$$atKey(KV, cba) = nil$$

•  $k \in KV$ , atKey will return  $v_k$ 

$$atKey(KV, k_0) \Rightarrow atKey(KV, abc) = 123$$
  
 $atKey(KV, k_1) \Rightarrow atKey(KV, def) = xyz \mapsto 456$ 

When K is a Collection of Key(s)

•  $K \notin KV$ , atKey will return the representation of nothingness

$$atKey(KV, \langle cba, 321 \rangle) = nil$$

•  $k_i \in KV \land k_i \notin KV$ , atKey will return the representation of nothingness

$$atKey(KV, < def, abc >) = nil$$

•  $k_i \in KV \land k_j \in KV$ , atKey will return the nested value

$$atKey(KV, \langle def, xyz \rangle) = 456$$