## 0.0.1 At Key

The operation atKey will return the Value v at some specified Key k.

```
AtKey[KV, K] = m?: KV
v!: V
k?: K
atKey_{-}: KV \times K \rightarrow V
v! = atKey(m?, k?) \bullet
let coll == ((seq m?) \upharpoonright (k?, m?_{k?})) \Rightarrow \langle (k?, m?_{k?}) \rangle \iff k? \in \text{dom } m?
= (second(head(coll)) \iff k? \mapsto m?_{k?} \in coll) \vee
(\emptyset \iff k? \not\in \text{dom } m?)
```

In the schema above, coll is the result of filtering for  $(k?, m?_{k?})$  within seq m?. If the mapping was in the original m?, it will also be in the sequence of mappings. This means we can filter over the sequence to look for the mapping and if found, it is returned as  $\langle (k?, m?_{k?}) \rangle$ . To return the mapping itself, head(coll) is used to extract the mapping such that the value mapped to k? can be returned.

$$v! = atKey(m?, k?) = second(head(coll)) = m?_{k?} \bullet m?_{k?} : V \iff k? \in dom m?$$

The follow examples demonstrate the properties of atKey

$$M = \langle \langle k_0 v_{k_0}, k_1 v_{k_1} \rangle \rangle$$

$$k_0 = abc \land v_{k_0} = 123 \qquad [k_0 v_{k_0} = abc \mapsto 123]$$

$$k_1 = def \land v_{k_1} = xyz \mapsto 456 \qquad [k_1 v_{k_1} = def \mapsto xyz \mapsto 456]$$

$$atKey(M, abc) = 123$$

$$atKey(M, def) = xyz \mapsto 456$$

$$atKey(M, foo) = \emptyset$$