Introduction

some stand in intro text

1 xAPI Formal Specification

The current formal specification only defines xAPI statements abstractly within the context of Z. A concrete definition for xAPI statements is outside the scope of this document.

1.1 Basic Types

 $IFI ::= mbox \mid mbox_sha1sum \mid openid \mid account$

• Type unique to Agents and Groups, The concrete definition of the listed values is outside the scope of this specification

 $OBJECTTYPE := Agent \mid Group \mid SubStatement \mid StatementRef \mid Activity$

A type which can be present in all activities as defined by the xAPI specification

 $INTERACTIONTYPE ::= true-false \mid choice \mid fill-in \mid long-fill-in \mid matching \mid performance \mid sequencing \mid likert \mid numeric \mid other$

• A type which represents the possible interaction Types as defined within the xAPI specification

 $INTERACTIONCOMPONENT ::= choices \mid scale \mid source \mid target \mid steps$

- A type which represents the possible interaction components as defined within the xAPI specification
- the concrete definition of the listed values is outside the scope of this specification

 $CONTEXTTYPES ::= parent \mid grouping \mid category \mid other$

• A type which represents the possible context types as defined within the xAPI specification

[STATEMENT]

• Basic type for an xAPI data point

[AGENT, GROUP]

• Basic types for Agents and collections of Agents

1.2 Id Schema

```
Id = id : \mathbb{F}_1 \# 1
```

• the schema *Id* introduces the component *id* which is a non-empty, finite set of 1 value

1.3 Schemas for Agents, Groups and Actors

```
\begin{array}{c} Agent \\ agent : AGENT \\ objectType : OBJECTTYPE \\ name : \mathbb{F}_1 \# 1 \\ ifi : IFI \\ \\ objectType = Agent \\ agent = \{ifi\} \cup \mathbb{P}\{name, objectType\} \end{array}
```

• The schema *Agent* introduces the component *agent* which is a set consisting of an *ifi* and optionally an *objectType* and/or *name*

```
Member \_\_\_\_
Agent
member : \mathbb{F}_1
member = \{a : AGENT \mid \forall a_n : a_i...a_j \bullet i \leq n \leq j \bullet a = agent\}
```

• The schema Member introduces the component member which is a set of objects a, where for every a within $a_0...a_n$, a is an agent

```
Group = Group = Group : GROUP \\ objectType : OBJECTTYPE \\ if i : IFI \\ name : \mathbb{F}_1 \# 1 \\ \hline objectType = Group \\ group = \{objectType, name, member\} \lor \{objectType, member\} \lor \\ \{objectType, if i\} \cup \mathbb{P}\{name, member\}
```

• The schema *Group* introduces the component *group* which is of type *GROUP* and is a set of either *objectType* and *member* with optionaly *name* or *objectType* and *ifi* with optionally *name* and/or *member*

```
Actor \_\_\_\_
Agent
Group
actor : AGENT \lor GROUP
actor = agent \lor group
```

• The schema *Actor* introduces the component *actor* which is either an *agent* or *group*

1.4 Verb Schema

```
 \begin{array}{c} \_Verb \_ \\ Id \\ display, verb : \mathbb{F}_1 \\ \hline \\ verb = \{id, display\} \lor \{id\} \end{array}
```

• The schema *Verb* introduces the component *verb* which is a set that consists of either *id* and the non-empty, finite set *display* or just *id*

1.5 Object Schema

```
Extensions \\ = extensions, extensionVal : \mathbb{F}_1 \\ extensionId : \mathbb{F}_1 \#1 \\ \hline extensionS = \{e : (extensionId, extensionVal) \mid \forall e_n : e_i..e_j \bullet i \leq n \leq j \bullet \\ (extensionId_i, extensionVal_i) \lor (extensionId_i, extensionVal_j) \land \\ (extensionId_j, extensionVal_i) \lor (extensionId_j, extensionVal_j) \land \\ extensionId_i \neq extensionId_j \}
```

- The schema *Extensions* introduces the component *extensions* which is a non-empty, finite set that consists of ordered pairs of *extensionId* and *extensionVal*. Different *extensionId*s can have the same *extensionVal* but there can not be two identical *extensionId* values
- extension Id is a non-empty, finite set with one value
- \bullet extensionVal is a non-empty, finite set

```
\label{eq:linear_constraint} $\_InteractionActivity $\_\_interactionType: INTERACTIONTYPE$$ correctResponsePattern: seq_1 $ interactionComponent: INTERACTIONCOMPONENT$$ interactionActivity = \{interactionType, correctReponsePattern, interactionComponent\} $$ \{interactionType, correctResponsePattern\}$$
```

• The schema InteractionActivity introduces the component interactionActivity which is a set of either interactionType and correctResponsePattern or interactionType and correctResponsePattern and interactionComponent

• The schema *Definition* introduces the component *definition* which is the non-empty, finite power set of *name*, *description*, *type*, *moreInfo* and *extensions*

```
Object
Id
Definition \\
Agent
Group
Statement
objectTypeA, objectTypeS, objectTypeSub, objectType:OBJECTTYPE
substatement: STATEMENT \\
object: \mathbb{F}_1
substatement = statement \\
objectTypeA = Activity
objectTypeS = StatementRef
objectTypeSub = SubStatement
objectType = objectTypeA \lor objectTypeS
object = \{id\} \lor \{id, objectType\} \lor \{id, objectTypeA, definition\}
         \vee \{id, definition\} \vee \{agent\} \vee \{group\} \vee \{objectTypeSub, substatement\}
         \vee \{id, objectTypeA\}
```

- The schema Object introduces the component object which is a non-empty, finite set of either id, id and objectType, id and objectTypeA, id and objectTypeA and definition, agent, group, or substatement
- The schema *Statement* and the corresponding component *statement* will be defined later on in this specification

1.6 Result Schema

```
Score = Score : \mathbb{F}_1
scaled, min, max, raw : \mathbb{Z}
scaled = \{n : \mathbb{Z} \mid -1.0 \le n \le 1.0\}
min = n < max
max = n > min
raw = \{n : \mathbb{Z} \mid min \le n \le max\}
score = \mathbb{P}_1 \{scaled, raw, min, max\}
```

• The schema *Score* introduces the component *score* which is the non-empty powerset of min, max, raw and scaled

• The schema Result introduces the component result which is the nonempty power set of score, success, completion, response, duration and extensions

1.7 Context Schema

• The schema *Instructor* introduces the component *instructor* which can be ether an *agent* or a *group*

```
Team
Group
team: GROUP
team = group
```

• The schema Team introduces the component team which is a group

```
Context_{-}
Instructor
Team
Object
Extensions \\
registration, revision, platform, language : \mathbb{F}_1 \# 1
parentT, groupingT, categoryT, otherT: CONTEXTTYPES
contextActivities, statement: \mathbb{F}_1
statement = object \setminus (id, objectType, agent, group, definition)
parentT = parent
qroupingT = qrouping
categoryT = category
otherT = other
contextActivity = \{ca: object \setminus (agent, group, objectType, objectTypeSub, substatement)\}
contextActivityParent = (parentT, contextActivity)
contextActivityCategory = (categoryT, contextActivity)
contextActivityGrouping = (groupingT, contextActivity)
contextActivityOther = (otherT, contextActivity)
contextActivities = \mathbb{P}_1\{contextActivityParent, contextActivityCategory,
                        contextActivityGrouping, contextActivityOther\}
context = \mathbb{P}_1\{registration, instructor, team, contextActivities, revision, \}
              platform, language, statement, extensions}
```

- The schema Context introduces the component context which is the non-empty powerset of registration, instructor, team, contextActivities, revision, platform, language, statement and extensions
- The notation $object \setminus agent$ represents the component object except for its subcomponent agent

1.8 Timestamp and Stored Schema

```
Timestamp \\ timestamp : \mathbb{F}_1 \# 1 Stored \\ stored : \mathbb{F}_1 \# 1
```

• The schema *Timestamp* and *stored* introduce the components *timestamp* and *stored* respectively. Each are non-empty, finite sets containing one value

1.9 Attachements Schema

- The schema Attachements introduces the component attachements which is a non-empty, finite set of the component attachement
- The component attachment is a non-empty, finite set of the components usageType, display, contentType, length, sha2 with optionally description and/or fileUrl

1.10 Statement and Statements Schema

```
Statement \\ Id \\ Actor \\ Verb \\ Object \\ Result \\ Context \\ Timestamp \\ Stored \\ Attachements \\ statement : STATEMENT \\ \\ statement = \{actor, verb, object, stored\} \cup \\ \mathbb{P}\{\mathrm{id}, result, context, timestamp, attachments\}
```

- The schema *Statement* introduces the component *statement* which consists of the components *actor*, *verb*, *object* and *stored* and the optional components *id*, *result*, *context*, *timestamp*, and/or *attachments*
- The schema *Statement* allows for subcomponent of *statement* to refrenced via the . (selection) operator

```
Statements \\ IsoToUnix \\ statements : \mathbb{F}_1 statements = \{s : statement \mid \forall s_n : s_i...s_j \bullet i \leq n \leq j \\ \bullet convert(s_i.timestamp) \leq convert(s_j.timestamp)\}
```

• The schema *Statements* introduces the component *statements* which is a non-empty, finite set of the component *statement* which are in chronological order.

2 Timeline Of Learner Success

As learners engage in activities supported by a learning ecosystem, they will build up a history of learning experiences. When the digital resources of that learning ecosystem adhere to a framework dedicated to supporting and understanding the learner, such as the Total Learning Architecture (TLA), it becomes possible to retell their learning story through data and data visualization. One important aspect of that story is the learners history of success.

2.1 Ideal Statements

In order to accurately portray a learner's timeline of success, there are a few base requirements of the data produced by a Learning Record Provider (LRP). They are as follows:

- the learner must be uniquely and consistently identified across all statements
- learning activities which evaluate a learner's understanding of material must report if the learner was successful or not
 - the grade earned by the learner must be reported
 - the minimum and maximum possible grade must be reported
- The learning activities must be uniquely and consistently identified across all statements
- The time at which a learner completed a learning activity must be recorded
 - The timestamp should contain an appropriate level of specificity.
 - ie. Year, Month, Day, Hour, Minute, Second, Timezone

2.2 Input Data Retrieval

How to query an LRS via a GET request to the Statements Resource via curl. The following section contains the appropriate parameters with example values as well as the curl command necessary for making the request.¹²³

 $^{^1}$ S is the set of all statements parsed from the statements array within the HTTP response to the Curl request(s). It may be possible that multiple Curl requests are needed to retrieve all query results. If multiple requests are necessary, S is the result of concatenating the result of each request into a single set

 $^{^2}$ Querying an LRS will not be defined within the following Z specifications but the results of the query will be utilized

³ If you want to query across the entire history of a LRS, omit Since and Until from the endpoint(s) and remove the associated & symbols.

```
Agent = "agent={"account":
    {"homePage": "https://example.homepage",
        "name": 123456}}"

Since = "since=2018-07-20T12:08:47Z"

Until = "until=2018-07-21T12:08:47Z"

Base = "https://example.endpoint/statements?"

endpoint = Base + Agent + "&" + Since + "&" + Until

Auth = Hash generated from basic auth

S = curl -X GET -H "Authorization: Auth"
-H "Content-Type: application/json"
-H "X-Experience-API-Version: 1.0.3"
Endpoint
```

2.3 Statement Parameters to Utilize

The statement parameter locations here are written in JSONPath. This notation is also compatable with the xAPI Z notation due to the defined hierarchy of components. Within the Z specifications, a variable name will be used instead of the \$

- \$.timestamp
- \bullet \$.result.success
- \$.result.score.raw
- \bullet \$.result.score.min
- \bullet \$.result.score.max
- \bullet \$.verb.id

2.4 2018 Pilot TLA Statement Problems

The initial pilot test data supports this algorithm. This section may require updates pending future data review following iterations of the TLA testing.

2.5 Summary

1. Query an LRS via a GET request to the statements endpoint using the parameters agent, since and until

- 2. Filter the results to the set of statements where:
 - \$.verb.id is one of:
 - http://adlnet.gov/expapi/verbs/passed
 - https://w3id.org/xapi/dod-isd/verbs/answered
 - http://adlnet.gov/expapi/verbs/completed
 - \$.result.success is true
- 3. process the filtered data
 - extract \$.timestamp
 - extract the score values from \$.result.score.raw, \$.result.score.min and \$.result.score.max and convert them to the scale 0..100
 - create a pair of [\$.timestamp, #]

2.6 Formal Specification

2.6.1 Basic Types

```
\begin{split} &COMPLETION :== \\ &\{ http: //adlnet.gov/expapi/verbs/passed \} \mid \\ &\{ https: //w3id.org/xapi/dod-isd/verbs/answered \} \mid \\ &\{ http: //adlnet.gov/expapi/verbs/completed \} \\ &SUCCESS :== \{ true \} \end{split}
```

2.6.2 System State

- The set S_{all} is a non-empty, finite set and is the component statements
- The sets $S_{completion}$ and $S_{success}$ are both finite sets
- the set $S_{completion}$ is a subset of S_{all} which may contain every value within S_{all}
- the set $S_{success}$ is a subset of $S_{completion}$ which may contain every value within $S_{completion}$
- the set $S_{processed}$ is a finite set of pairs where each contains a statement.timestamp and a natural number

2.6.3 Initial System State

```
InitTimelineLearnerSuccess \\ \hline S_{all} \neq \emptyset \\ S_{completion} = \emptyset \\ S_{success} = \emptyset \\ S_{processed} = \emptyset
```

- The set S_{all} is a non-empty set
- The sets $S_{completion}$, $S_{success}$ and $S_{processed}$ are all initially empty

2.6.4 Filter for Completion

```
Completion \\ Statement \\ completion: STATEMENT \rightarrow \mathbb{F} \\ s?: STATEMENT \\ s!: \mathbb{F} \\ \\ \hline s? = statement \\ s! = completion(s?) \\ completion(s?) = \mathbf{if} \ s? .verb.id: COMPLETION \\ \mathbf{then} \ s! = s? \\ \mathbf{else} \ s! = \emptyset \\ \\ \hline
```

- The schema *Completion* inroduces the function *completion* which takes in the variable s? and returns the variable s!
- The variable s? is the component statement
- s! is equal to s? if \$.verb.id is of the type COMPLETION otherwise s! is an empty set

```
Filter For Completion \\ \Delta Timeline Learner Success \\ Completion \\ completions: \mathbb{F} \\ \hline completions \subseteq S_{all} \\ completions' = \{s: STATEMENT \mid completion(s) \neq \emptyset\} \\ S'_{completion} = S_{completion} \cup completions' \\ \hline \end{cases}
```

 \bullet the set completions is a subset of S_{all} which may contain every value within S_{all}

- The set completions' is the set of all statements s where the result of completion(s) is not an empty set
- the updated set $S'_{completion}$ is the union of the previous state of set $S_{completion}$ and the set completions'

2.6.5 Filter for Success

```
Success = Statement
success : STATEMENT \rightarrow \mathbb{F}
s? : STATEMENT
s! : \mathbb{F}
s? = statement
s! = success(s?)
success(s?) = \mathbf{if} \ s? .result.success : SUCCESS
\mathbf{then} \ s! = s?
\mathbf{else} \ s! = \emptyset
```

- the schema *Success* introduces the function *success* which takes in the variable s? and returns the variable s!
- the variable s? is the component statement
- s! is equal to s? if \$.result.success is of the type SUCCESS otherwise s! is an empty set

```
FilterForSuccess \\ \Delta TimelineLearnerSuccess \\ Success \\ successes : \mathbb{F} \\ \hline successes \subseteq S_{completion} \\ successes' = \{s: STATEMENT \mid success(s) \neq \emptyset\} \\ S'_{success} = S_{success} \cup successes' \\ \hline
```

- \bullet the set successes is a subset of $S_{completion}$ which may contain every value within $S_{completion}$
- The set successes' contains elements s of type STATEMENT where success(s) is not an empty set
- The updated set $S'_{success}$ is the union of the previous state of $S_{success}$ and successes'

2.6.6 Processes Results

```
Scale \\ scaled!: \mathbb{N} \\ raw?, min?, max?: \mathbb{Z} \\ scale: \mathbb{Z} \to \mathbb{N} \\ \\ scaled! = scale(raw?, min?, max?) \\ scale(raw?, min?, max?) = \\ (raw?*((0.0 - 100.0) div(min? - max?))) + \\ (0.0 - (min?*((0.0 - 100.0) div(min? - max?))))) \\ \\ \end{cases}
```

• The schema *Scale* introduces the function *scale* which takes 3 arguments, raw?, min? and max?. The function converts raw? from the range min?..max? to 0.0..100.0

```
 \begin{array}{l} ProcessStatements \\ \Delta TimelineLearnerSuccess \\ Scale \\ FilterStatements \\ processed : \mathbb{F} \\ \\ \hline processed \subseteq S_{success} \\ processed' = \{p: (\mathbb{F}_1 \# 1, \mathbb{N}) \mid \\ & \quad \text{let } \{processed_i.processed_j\} == \{s_i..s_j\} \bullet \\ & \quad i \leq n \leq j \bullet \forall s_n: s_i..s_j \bullet \exists \ p_n: p_i..p_j \bullet \\ & \quad first \ p_n = s_n.timestamp \land \\ & \quad second \ p_n = scale(s_n.result.score.raw, \\ & \quad s_n.result.score.min, \\ & \quad s_n.result.score.max) \} \\ S'_{processed} = S_{processed} \cup processed' \\ \end{array}
```

- The operation ProcessStatements introduces the variable processed which is a subset of $S_{success}$ which may contain every value within $S_{success}$
- $S_{success}$ is the result of the operation FilterStatements
- The operation defines the variable processed' which is a set of objects p which are ordered pairs of (1) a finite set containing one value and (2) a single positive number.
- The first component of every object p, is the timestamp from the associated statement within processed ie. s.timestamp
- The second component of every object p is the result of the function scale. The score values contained within the associated $statement\ s$ are the arugments passed to scale. ie scale(s.result.score.raw, s.result.score.min, s.result.score.max)
- The result of the operation ProcessStatements is to updated the set $S_{processed}$ with the values contained within processed'

2.6.7 Sequence of Operations

 $Filter Statements \stackrel{\frown}{=} Filter For Completion \, {}^\circ_{\mathbb{S}} \, Filter For Success$

- \bullet The schema FilterStatements is the sequential composition of operation schemas FilterForCompletion and FilterForSuccess
- \bullet FilterForCompletion happens before FilterForSuccess

 $ProcessedStatements \triangleq FilterStatements \approx ProcessStatements$

- ullet The schema ProcessedStatements is the sequential composition of operation schemas FilterStatements and ProcessStatements
- \bullet Filter Statements happens before Process Statements

2.6.8 Return

```
Return \subseteq \Xi Timeline Learner Success Processed Statements S_{processed}!: \mathbb{F} S_{processed}! = S_{processed}
```

• The returned variable $S_{processed}$! is equal to the current state of variable $S_{processed}$ after the operations FilterForCompletion, FilterForSuccess and ProcessStatements

2.7 Pseudocode

Algorithm 1: Timeline of Learner Success

```
Input: S_{all}
Result: coll'
coll = [];
while S_{all} \neq \emptyset do
     foreach s \in S_{all} do
           if s.verb.id = COMPLETION then
                S'_{completion} \leftarrow s \cup S_{completion};
                S'_{all} \leftarrow S_{all} \setminus s;
                recur S'_{completion}, S'_{all};
           else
                do
               S'_{all} \leftarrow S_{all} \setminus s;
recur S'_{all};
           end
     \quad \text{end} \quad
end
 \begin{aligned} \textbf{while} \ S'_{completion} \neq \emptyset \ \textbf{do} \\ \big| \ \ \textbf{foreach} \ sc \in S'_{completion} \ \textbf{do} \end{aligned} 
           if sc.result.success = SUCCESS then
                S'_{success} \leftarrow sc \cup S_{success};
                S'_{completion} \leftarrow S_{completion} \setminus sc;
                recur S'_{success}, S'_{completion};
          else
                do
                S'_{completion} \leftarrow S_{completion} \setminus sc;
               recur S'_{completion};
          \mathbf{end}
     end
end
for
each ss \in S'_{success} do
     raw? \leftarrow ss.result.score.raw;
     max? \leftarrow ss.result.score.max;
     min? \leftarrow ss.result.score.min;
     scaled \leftarrow scale(raw?, min?, max?);
     subVec \leftarrow [ss.timestamp, scaled];
     coll' \leftarrow coll \cap subVec;
     \mathbf{recur}\ coll'
\mathbf{end}
return \ coll'
```

- The Z schemas are used within this pseudocode
- The return value coll is an array of arrays, each containing a *statement.timestamp* and a scaled score.

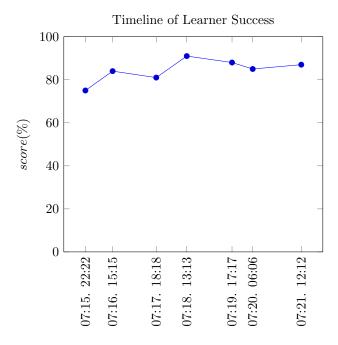
2.8 JSON Schema

```
{"type":"array",
    "items":{"type":"array",
        "items":[{"type":"string"}, {"type":"number"}]}}
```

2.9 Visualization Description

The **Timeline of Learner Success** visualization will be a line chart where the domain is time and the range is score on a scale of 0.0 to 100.0. Every subarray will be a point on the chart. The domain of the graph should be in chronological order.

2.10 Visualization prototype



2.11 Prototype Improvement Suggestions

Additional features may be implemented on top of this base specification but they would require adding aditional values to each subarray returned by the algorithm. These additional values can be retrieved via (1) performing metadata lookup within or independently of the algorithm (2) by utilizing additional xAPI statement paramters and/or (3) by performing additional computations. The following examples assume the metadata is contained within each statement available to the algorithm.

- A tooltip containing the name of an activity when hovering over a specific point on the chart
 - this would require utilizing \$.object.definition.name
- A tooltip containing the device on which the activity was experienced
 - this would require utilizing \$.context.platform
- A tooltip containing the instructor associated with a particular data point
 - this would require utilizing \$.context.instructor

Appendex A: Visualization Exemplars

Appendex A includes a typology of data visualizations which may be supported within DAVE workbooks. These visualizations can either be one to one or one to many in regards to the algorithms defined within this document. Future iterations of this document will increasingly include these typologies within the domain-question template exemplars.

Line Charts

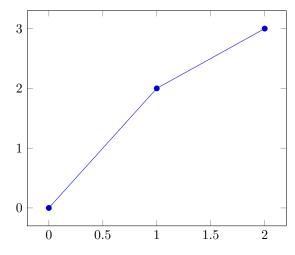


Figure 1: Line Chart

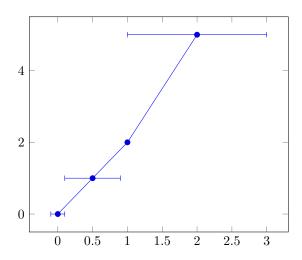


Figure 2: Line Chart with Error

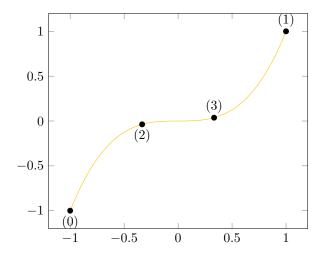


Figure 3: Spline Chart



Figure 4: Quiver Chart

Grouping Charts

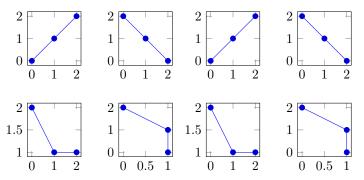


Figure 5: Grouped Line Charts

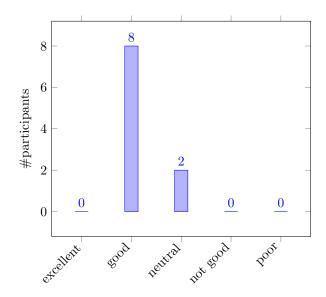


Figure 6: Histogram

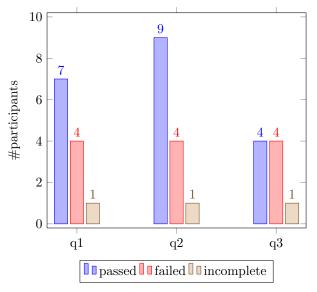


Figure 7: Bar Chart

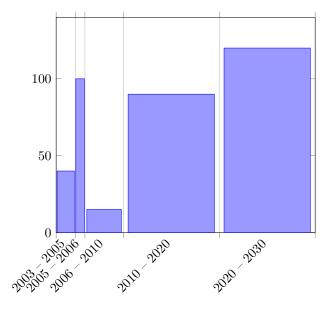


Figure 8: Bar Chart Grouped by Time Range

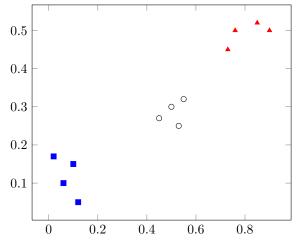


Figure 9: Scatter Plot

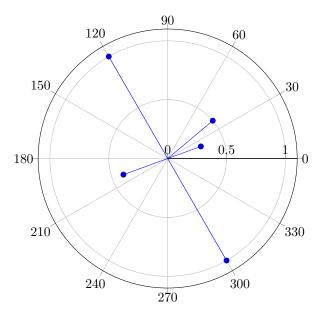


Figure 10: Polar Chart

Specialized Charts

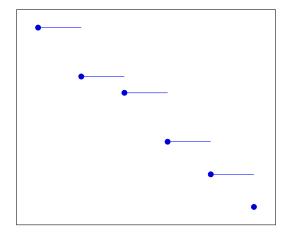


Figure 11: Gantt Chart

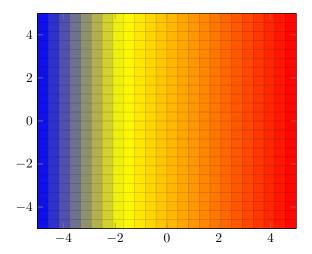


Figure 12: Heat Map

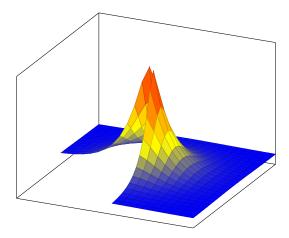
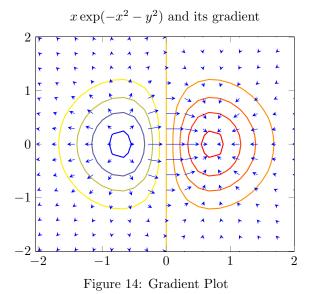


Figure 13: 3D Plot



27