Data Analytics and Visualization Environment for xAPI and the Total Learning Architecture: DAVE Learning Analytics Algorithms

Yet Analytics September 10, 2019

Introduction

This report introduces the initial learning analytics algorithms, **timeline of learner success**, which assessment questions are the most difficult and rate of completions. In doing so, it establishes a set of style guidelines for the reporting of algorithms and associated visualization templates. This document will be updated to include additional learning analytics questions presented elsewhere within this github repo in addition to other learning analytics algorithms which have yet to be defined. Updates may also address refinement of these algorithms and this document should be understood to be an example of algorithm presentation and not the final state of any defined algorithm.

The structure of this documents is as follows:

- 1. A formal specification for xAPI written in Z and referenced within the formal specifications of learning analytics algorithms
- 2. An algorithm definition which will consist of:
 - (a) an introduction for the algorithm
 - (b) the structure of the ideal input data
 - (c) how to retrieve input data from an LRS
 - (d) the statement parameters which the algorithm will utilize
 - (e) notices regarding data collected during the 2018 pilot test of the TLA
 - (f) a summary of the algorithm
 - (g) the formal specification of the algorithm
 - (h) pseudocode representation of the algorithm
 - (i) JSONSchema for the output of the algorithm
 - (j) a description of the associated visualization
 - (k) a prototype of the visualization
 - (l) a collection of suggestions describing how the algorithm could be adapted to improve the quality of the visualization prototype

1 xAPI Formal Specification

The current formal specification only defines xAPI statements abstractly within the context of Z. A concrete definition for xAPI statements is outside the scope of this document.

1.1 Basic Types

 $IFI ::= mbox \mid mbox_sha1sum \mid openid \mid account$

• Type unique to Agents and Groups, The concrete definition of the listed values is outside the scope of this specification

 $OBJECTTYPE := Agent \mid Group \mid SubStatement \mid StatementRef \mid Activity$

A type which can be present in all activities as defined by the xAPI specification

 $INTERACTIONTYPE ::= true-false \ | \ choice \ | \ fill-in \ | \ long-fill-in \ | \ matching \ | \ performance \ | \ sequencing \ | \ likert \ | \ numeric \ | \ other$

• A type which represents the possible interaction Types as defined within the xAPI specification

 $INTERACTIONCOMPONENT ::= choices \mid scale \mid source \mid target \mid steps$

- A type which represents the possible interaction components as defined within the xAPI specification
- the concrete definition of the listed values is outside the scope of this specification

 $CONTEXTTYPES ::= parent \mid grouping \mid category \mid other$

• A type which represents the possible context types as defined within the xAPI specification

[STATEMENT]

• Basic type for an xAPI data point

[AGENT, GROUP]

• Basic types for Agents and collections of Agents

1.2 Id Schema

```
Id = id : \mathbb{F}_1 \# 1
```

• the schema *Id* introduces the component *id* which is a non-empty, finite set of 1 value

1.3 Schemas for Agents, Groups and Actors

```
\begin{array}{c} Agent \\ agent : AGENT \\ objectType : OBJECTTYPE \\ name : \mathbb{F}_1 \# 1 \\ ifi : IFI \\ \\ objectType = Agent \\ agent = \{ifi\} \cup \mathbb{P}\{name, objectType\} \end{array}
```

• The schema *Agent* introduces the component *agent* which is a set consisting of an *ifi* and optionally an *objectType* and/or *name*

```
Member \_\_\_\_
Agent
member : \mathbb{F}_1
member = \{a : AGENT \mid \forall a_n : a_i...a_j \bullet i \leq n \leq j \bullet a = agent\}
```

• The schema Member introduces the component member which is a set of objects a, where for every a within $a_0...a_n$, a is an agent

```
Group = Group = Group : GROUP \\ objectType : OBJECTTYPE \\ if i : IFI \\ name : \mathbb{F}_1 \# 1 \\ \hline objectType = Group \\ group = \{objectType, name, member\} \lor \{objectType, member\} \lor \\ \{objectType, if i\} \cup \mathbb{P}\{name, member\}
```

• The schema *Group* introduces the component *group* which is of type *GROUP* and is a set of either *objectType* and *member* with optionaly *name* or *objectType* and *ifi* with optionally *name* and/or *member*

```
Actor \_\_\_\_
Agent
Group
actor : AGENT \lor GROUP
actor = agent \lor group
```

• The schema *Actor* introduces the component *actor* which is either an *agent* or *group*

1.4 Verb Schema

```
 \begin{array}{c} \_Verb \_ \\ Id \\ display, verb : \mathbb{F}_1 \\ \hline \\ verb = \{id, display\} \lor \{id\} \end{array}
```

• The schema *Verb* introduces the component *verb* which is a set that consists of either *id* and the non-empty, finite set *display* or just *id*

1.5 Object Schema

```
Extensions \\ = extensions, extensionVal : \mathbb{F}_1 \\ extensionId : \mathbb{F}_1 \#1 \\ \hline extensionS = \{e : (extensionId, extensionVal) \mid \forall e_n : e_i..e_j \bullet i \leq n \leq j \bullet \\ (extensionId_i, extensionVal_i) \lor (extensionId_i, extensionVal_j) \land \\ (extensionId_j, extensionVal_i) \lor (extensionId_j, extensionVal_j) \land \\ extensionId_i \neq extensionId_j \}
```

- The schema *Extensions* introduces the component *extensions* which is a non-empty, finite set that consists of ordered pairs of *extensionId* and *extensionVal*. Different *extensionId*s can have the same *extensionVal* but there can not be two identical *extensionId* values
- extension Id is a non-empty, finite set with one value
- \bullet extensionVal is a non-empty, finite set

```
\label{eq:linear_constraint} $\_InteractionActivity $\_\_interactionType: INTERACTIONTYPE$$ correctResponsePattern: seq_1 $ interactionComponent: INTERACTIONCOMPONENT$$ interactionActivity = \{interactionType, correctReponsePattern, interactionComponent\} $$ \{interactionType, correctResponsePattern\}$$
```

• The schema InteractionActivity introduces the component interactionActivity which is a set of either interactionType and correctResponsePattern or interactionType and correctResponsePattern and interactionComponent

• The schema *Definition* introduces the component *definition* which is the non-empty, finite power set of *name*, *description*, *type*, *moreInfo* and *extensions*

```
Object
Id
Definition \\
Agent
Group
Statement
objectTypeA, objectTypeS, objectTypeSub, objectType:OBJECTTYPE
substatement: STATEMENT \\
object: \mathbb{F}_1
substatement = statement \\
objectTypeA = Activity
objectTypeS = StatementRef
objectTypeSub = SubStatement
objectType = objectTypeA \lor objectTypeS
object = \{id\} \lor \{id, objectType\} \lor \{id, objectTypeA, definition\}
         \vee \{id, definition\} \vee \{agent\} \vee \{group\} \vee \{objectTypeSub, substatement\}
         \vee \{id, objectTypeA\}
```

- The schema Object introduces the component object which is a non-empty, finite set of either id, id and objectType, id and objectTypeA, id and objectTypeA and definition, agent, group, or substatement
- The schema *Statement* and the corresponding component *statement* will be defined later on in this specification

1.6 Result Schema

```
Score = Score : \mathbb{F}_1
scaled, min, max, raw : \mathbb{Z}
scaled = \{n : \mathbb{Z} \mid -1.0 \le n \le 1.0\}
min = n < max
max = n > min
raw = \{n : \mathbb{Z} \mid min \le n \le max\}
score = \mathbb{P}_1 \{scaled, raw, min, max\}
```

• The schema *Score* introduces the component *score* which is the non-empty powerset of *min*, *max*, *raw* and *scaled*

• The schema Result introduces the component result which is the nonempty power set of score, success, completion, response, duration and extensions

1.7 Context Schema

• The schema *Instructor* introduces the component *instructor* which can be ether an *agent* or a *group*

```
Team
Group
team: GROUP
team = group
```

• The schema Team introduces the component team which is a group

```
Context_{-}
Instructor
Team
Object
Extensions \\
registration, revision, platform, language : \mathbb{F}_1 \# 1
parentT, groupingT, categoryT, otherT: CONTEXTTYPES
contextActivities, statement: \mathbb{F}_1
statement = object \setminus (id, objectType, agent, group, definition)
parentT = parent
qroupingT = qrouping
categoryT = category
otherT = other
contextActivity = \{ca: object \setminus (agent, group, objectType, objectTypeSub, substatement)\}
contextActivityParent = (parentT, contextActivity)
contextActivityCategory = (categoryT, contextActivity)
contextActivityGrouping = (groupingT, contextActivity)
contextActivityOther = (otherT, contextActivity)
contextActivities = \mathbb{P}_1\{contextActivityParent, contextActivityCategory,
                        contextActivityGrouping, contextActivityOther\}
context = \mathbb{P}_1\{registration, instructor, team, contextActivities, revision, \}
              platform, language, statement, extensions}
```

- The schema Context introduces the component context which is the non-empty powerset of registration, instructor, team, contextActivities, revision, platform, language, statement and extensions
- The notation $object \setminus agent$ represents the component object except for its subcomponent agent

1.8 Timestamp and Stored Schema

```
Timestamp \\ timestamp : \mathbb{F}_1 \# 1 Stored \\ stored : \mathbb{F}_1 \# 1
```

• The schema *Timestamp* and *stored* introduce the components *timestamp* and *stored* respectively. Each are non-empty, finite sets containing one value

1.9 Attachements Schema

- The schema Attachements introduces the component attachements which is a non-empty, finite set of the component attachement
- The component attachment is a non-empty, finite set of the components usageType, display, contentType, length, sha2 with optionally description and/or fileUrl

1.10 Statement and Statements Schema

```
Statement \\ Id \\ Actor \\ Verb \\ Object \\ Result \\ Context \\ Timestamp \\ Stored \\ Attachements \\ statement : STATEMENT \\ \\ statement = \{actor, verb, object, stored\} \cup \\ \mathbb{P}\{\mathrm{id}, result, context, timestamp, attachments\}
```

- The schema *Statement* introduces the component *statement* which consists of the components *actor*, *verb*, *object* and *stored* and the optional components *id*, *result*, *context*, *timestamp*, and/or *attachments*
- The schema *Statement* allows for subcomponent of *statement* to refrenced via the . (selection) operator

```
Statements \\ IsoToUnix \\ statements : \mathbb{F}_1 statements = \{s : statement \mid \forall s_n : s_i...s_j \bullet i \leq n \leq j \\ \bullet convert(s_i.timestamp) \leq convert(s_j.timestamp)\}
```

• The schema *Statements* introduces the component *statements* which is a non-empty, finite set of the component *statement* which are in chronological order.

2 Timeline Of Learner Success

As learners engage in activities supported by a learning ecosystem, they will build up a history of learning experiences. When the digital resources of that learning ecosystem adhere to a framework dedicated to supporting and understanding the learner, such as the Total Learning Architecture (TLA), it becomes possible to retell their learning story through data and data visualization. One important aspect of that story is the learners history of success.

2.1 Ideal Statements

In order to accurately portray a learner's timeline of success, there are a few base requirements of the data produced by a Learning Record Provider (LRP). They are as follows:

- the learner must be uniquely and consistently identified across all statements
- learning activities which evaluate a learner's understanding of material must report if the learner was successful or not
 - the grade earned by the learner must be reported
 - the minimum and maximum possible grade must be reported
- The learning activities must be uniquely and consistently identified across all statements
- The time at which a learner completed a learning activity must be recorded
 - The timestamp should contain an appropriate level of specificity.
 - ie. Year, Month, Day, Hour, Minute, Second, Timezone

2.2 Input Data Retrieval

How to query an LRS via a GET request to the Statements Resource via curl. The following section contains the appropriate parameters with example values as well as the curl command necessary for making the request.¹²³

 $^{^1}$ S is the set of all statements parsed from the statements array within the HTTP response to the Curl request(s). It may be possible that multiple Curl requests are needed to retrieve all query results. If multiple requests are necessary, S is the result of concatenating the result of each request into a single set

 $^{^2}$ Querying an LRS will not be defined within the following Z specifications but the results of the query will be utilized

³ If you want to query across the entire history of a LRS, omit Since and Until from the endpoint(s) and remove the associated & symbols.

```
Agent = "agent={"account":
    {"homePage": "https://example.homepage",
        "name": 123456}}"

Since = "since=2018-07-20T12:08:47Z"

Until = "until=2018-07-21T12:08:47Z"

Base = "https://example.endpoint/statements?"

endpoint = Base + Agent + "&" + Since + "&" + Until

Auth = Hash generated from basic auth

S = curl -X GET -H "Authorization: Auth"
-H "Content-Type: application/json"
-H "X-Experience-API-Version: 1.0.3"
Endpoint
```

2.3 Statement Parameters to Utilize

The statement parameter locations here are written in JSONPath. This notation is also compatable with the xAPI Z notation due to the defined hierarchy of components. Within the Z specifications, a variable name will be used instead of the \$

- \$.timestamp
- \bullet \$.result.success
- \$.result.score.raw
- \bullet \$.result.score.min
- \bullet \$.result.score.max
- \bullet \$.verb.id

2.4 2018 Pilot TLA Statement Problems

The initial pilot test data supports this algorithm. This section may require updates pending future data review following iterations of the TLA testing.

2.5 Summary

1. Query an LRS via a GET request to the statements endpoint using the parameters agent, since and until

- 2. Filter the results to the set of statements where:
 - \$.verb.id is one of:
 - http://adlnet.gov/expapi/verbs/passed
 - https://w3id.org/xapi/dod-isd/verbs/answered
 - http://adlnet.gov/expapi/verbs/completed
 - \bullet \$.result.success is true
- 3. process the filtered data
 - extract \$.timestamp
 - extract the score values from \$.result.score.raw, \$.result.score.min and \$.result.score.max and convert them to the scale 0..100
 - create a pair of [\$.timestamp, #]

2.6 Formal Specification

2.6.1 Basic Types

```
\begin{split} &COMPLETION :== \\ &\{ http: //adlnet.gov/expapi/verbs/passed \} \mid \\ &\{ https: //w3id.org/xapi/dod-isd/verbs/answered \} \mid \\ &\{ http: //adlnet.gov/expapi/verbs/completed \} \\ &SUCCESS :== \{ true \} \end{split}
```

2.6.2 System State

- The set S_{all} is a non-empty, finite set and is the component statements
- The sets $S_{completion}$ and $S_{success}$ are both finite sets
- the set $S_{completion}$ is a subset of S_{all} which may contain every value within S_{all}
- the set $S_{success}$ is a subset of $S_{completion}$ which may contain every value within $S_{completion}$
- the set $S_{processed}$ is a finite set of pairs where each contains a statement.timestamp and a natural number

2.6.3 Initial System State

```
InitTimelineLearnerSuccess \\ \hline S_{all} \neq \emptyset \\ S_{completion} = \emptyset \\ S_{success} = \emptyset \\ S_{processed} = \emptyset
```

- The set S_{all} is a non-empty set
- The sets $S_{completion}$, $S_{success}$ and $S_{processed}$ are all initially empty

2.6.4 Filter for Completion

```
Completion \\ Statement \\ completion: STATEMENT \rightarrow \mathbb{F} \\ s?: STATEMENT \\ s!: \mathbb{F} \\ \\ \hline s? = statement \\ s! = completion(s?) \\ completion(s?) = \mathbf{if} \ s? .verb.id: COMPLETION \\ \mathbf{then} \ s! = s? \\ \mathbf{else} \ s! = \emptyset \\ \\ \hline
```

- The schema *Completion* inroduces the function *completion* which takes in the variable s? and returns the variable s!
- The variable s? is the component statement
- s! is equal to s? if \$.verb.id is of the type COMPLETION otherwise s! is an empty set

```
Filter For Completion \\ \Delta Timeline Learner Success \\ Completion \\ completions: \mathbb{F} \\ \hline completions \subseteq S_{all} \\ completions' = \{s: STATEMENT \mid completion(s) \neq \emptyset\} \\ S'_{completion} = S_{completion} \cup completions' \\ \hline \end{cases}
```

 \bullet the set completions is a subset of S_{all} which may contain every value within S_{all}

- The set completions' is the set of all statements s where the result of completion(s) is not an empty set
- the updated set $S'_{completion}$ is the union of the previous state of set $S_{completion}$ and the set completions'

2.6.5 Filter for Success

```
Success = Statement
success : STATEMENT \rightarrow \mathbb{F}
s? : STATEMENT
s! : \mathbb{F}
s? = statement
s! = success(s?)
success(s?) = \mathbf{if} \ s? .result.success : SUCCESS
\mathbf{then} \ s! = s?
\mathbf{else} \ s! = \emptyset
```

- the schema *Success* introduces the function *success* which takes in the variable s? and returns the variable s!
- the variable s? is the component statement
- s! is equal to s? if \$.result.success is of the type SUCCESS otherwise s! is an empty set

```
FilterForSuccess \\ \Delta TimelineLearnerSuccess \\ Success \\ successes : \mathbb{F} \\ \hline successes \subseteq S_{completion} \\ successes' = \{s: STATEMENT \mid success(s) \neq \emptyset\} \\ S'_{success} = S_{success} \cup successes' \\ \hline
```

- \bullet the set successes is a subset of $S_{completion}$ which may contain every value within $S_{completion}$
- The set successes' contains elements s of type STATEMENT where success(s) is not an empty set
- The updated set $S'_{success}$ is the union of the previous state of $S_{success}$ and successes'

2.6.6 Processes Results

```
Scale \\ scaled!: \mathbb{N} \\ raw?, min?, max?: \mathbb{Z} \\ scale: \mathbb{Z} \to \mathbb{N} \\ \\ scaled! = scale(raw?, min?, max?) \\ scale(raw?, min?, max?) = \\ (raw?*((0.0 - 100.0) div(min? - max?))) + \\ (0.0 - (min?*((0.0 - 100.0) div(min? - max?))))) \\ \\ \end{cases}
```

• The schema *Scale* introduces the function *scale* which takes 3 arguments, raw?, min? and max?. The function converts raw? from the range min?..max? to 0.0..100.0

```
 \begin{array}{l} ProcessStatements \\ \Delta TimelineLearnerSuccess \\ Scale \\ FilterStatements \\ processed : \mathbb{F} \\ \\ \hline processed \subseteq S_{success} \\ processed' = \{p: (\mathbb{F}_1 \# 1, \mathbb{N}) \mid \\ & \quad \text{let } \{processed_i.processed_j\} == \{s_i..s_j\} \bullet \\ & \quad i \leq n \leq j \bullet \forall s_n: s_i..s_j \bullet \exists \ p_n: p_i..p_j \bullet \\ & \quad first \ p_n = s_n.timestamp \land \\ & \quad second \ p_n = scale(s_n.result.score.raw, \\ & \quad s_n.result.score.min, \\ & \quad s_n.result.score.max) \} \\ S'_{processed} = S_{processed} \cup processed' \\ \end{array}
```

- The operation ProcessStatements introduces the variable processed which is a subset of $S_{success}$ which may contain every value within $S_{success}$
- $S_{success}$ is the result of the operation FilterStatements
- The operation defines the variable processed' which is a set of objects p which are ordered pairs of (1) a finite set containing one value and (2) a single positive number.
- The first component of every object p, is the timestamp from the associated statement within processed ie. s.timestamp
- The second component of every object p is the result of the function scale. The score values contained within the associated $statement\ s$ are the arugments passed to scale. ie scale(s.result.score.raw, s.result.score.min, s.result.score.max)
- The result of the operation ProcessStatements is to updated the set $S_{processed}$ with the values contained within processed'

2.6.7 Sequence of Operations

 $Filter Statements \stackrel{\frown}{=} Filter For Completion \, ^\circ_{\mathbb{S}} \, Filter For Success$

- \bullet The schema FilterStatements is the sequential composition of operation schemas FilterForCompletion and FilterForSuccess
- \bullet FilterForCompletion happens before FilterForSuccess

 $ProcessedStatements \triangleq FilterStatements \approx ProcessStatements$

- ullet The schema ProcessedStatements is the sequential composition of operation schemas FilterStatements and ProcessStatements
- \bullet Filter Statements happens before Process Statements

2.6.8 Return

```
Return \subseteq \Xi Timeline Learner Success Processed Statements S_{processed}!: \mathbb{F} S_{processed}! = S_{processed}
```

• The returned variable $S_{processed}$! is equal to the current state of variable $S_{processed}$ after the operations FilterForCompletion, FilterForSuccess and ProcessStatements

2.7 Pseudocode

Algorithm 1: Timeline of Learner Success

```
Input: S_{all}
Result: coll'
coll = [];
while S_{all} \neq \emptyset do
     foreach s \in S_{all} do
           if s.verb.id = COMPLETION then
                S'_{completion} \leftarrow s \cup S_{completion};
                S'_{all} \leftarrow S_{all} \setminus s;
                recur S'_{completion}, S'_{all};
           else
                do
               S'_{all} \leftarrow S_{all} \setminus s;
recur S'_{all};
           end
     \quad \text{end} \quad
end
 \begin{aligned} \textbf{while} \ S'_{completion} \neq \emptyset \ \textbf{do} \\ \big| \ \ \textbf{foreach} \ sc \in S'_{completion} \ \textbf{do} \end{aligned} 
           if sc.result.success = SUCCESS then
                S'_{success} \leftarrow sc \cup S_{success};
                S'_{completion} \leftarrow S_{completion} \setminus sc;
                recur S'_{success}, S'_{completion};
          else
                do
                S'_{completion} \leftarrow S_{completion} \setminus sc;
               recur S'_{completion};
          \mathbf{end}
     end
end
for
each ss \in S'_{success} do
     raw? \leftarrow ss.result.score.raw;
     max? \leftarrow ss.result.score.max;
     min? \leftarrow ss.result.score.min;
     scaled \leftarrow scale(raw?, min?, max?);
     subVec \leftarrow [ss.timestamp, scaled];
     coll' \leftarrow coll \cap subVec;
     \mathbf{recur}\ coll'
\mathbf{end}
return \ coll'
```

- The Z schemas are used within this pseudocode
- The return value coll is an array of arrays, each containing a *statement.timestamp* and a scaled score.

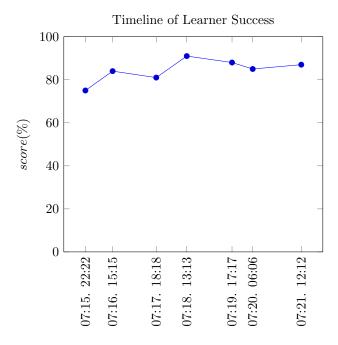
2.8 JSON Schema

```
{"type":"array",
    "items":{"type":"array",
        "items":[{"type":"string"}, {"type":"number"}]}}
```

2.9 Visualization Description

The **Timeline of Learner Success** visualization will be a line chart where the domain is time and the range is score on a scale of 0.0 to 100.0. Every subarray will be a point on the chart. The domain of the graph should be in chronological order.

2.10 Visualization prototype



2.11 Prototype Improvement Suggestions

Additional features may be implemented on top of this base specification but they would require adding aditional values to each subarray returned by the algorithm. These additional values can be retrieved via (1) performing metadata lookup within or independently of the algorithm (2) by utilizing additional xAPI statement paramters and/or (3) by performing additional computations. The following examples assume the metadata is contained within each statement available to the algorithm.

- A tooltip containing the name of an activity when hovering over a specific point on the chart
 - this would require utilizing \$.object.definition.name
- A tooltip containing the device on which the activity was experienced
 - this would require utilizing \$.context.platform
- A tooltip containing the instructor associated with a particular data point
 - this would require utilizing \$.context.instructor

3 Which Assessment Questions are the Most Difficult

As learners engage in activities supported by a learning ecosystem, they will experience learning content as well as assessment content. Assessments are designed to measure the effectiveness of learning content and help assess knowledge gained. It is possible that certain assessment questions do not accurately represent the concepts contained within learning content and this may be indicated by a majority of learners getting the question wrong. It is also possible that the question accurately represents the learning content but is very difficult. The following algorithm will identify these types of questions but will not be able to deduce why learners answer them incorrectly.

3.1 Ideal Statements

In order to accurately determine which assessment questions are the most dificult, there are a few requirements of the data produced by a LRP. They are as follows:

- statements describing a learner answering a question must report if the learner got the question correct or incorrect via \$.result.success
- if it is possible to get partial credit on a question, the amount of credit should be reported within the statement
 - the credit earned by the learner should be reported within \$.result.score.raw
 - the minimum and maximum possible credit amount should be reported within \$.result.score.min and \$.result.score.max respectively
- If it is possible to get partial credit on a question, it must still be reported if the learner reached the threshold of success via \$.result.success
- \bullet Statements describing a learner answering a question should contain activities of the type cmi.interaction
- activities must be uniquely and consistently identified across all statements
- Statements describing a learner answering a question should use the verb http://adlnet.gov/expapi/verbs/answered

 $^{^4}$ it is possible to use another verb iri but if another is used, that will need to be accounted for in data retrieval

3.2 Input Data Retrieval

How to query an LRS via a GET request to the Statements Resource via curl. The following section contains the appropriate parameters with example values as well as the curl command necessary for making the request.⁵⁶⁷

```
Verb = "verb=http://adlnet.gov/expapi/verbs/answered"

Since = "since=2018-07-20T12:08:47Z"

Until = "until=2018-07-21T12:08:47Z"

Base = "https://example.endpoint/statements?"

endpoint = Base + Verb + "&" + Since + "&" + Until

Auth = Hash generated from basic auth

S = curl -X GET -H "Authorization: Auth"
-H "Content-Type: application/json"
-H "X-Experience-API-Version: 1.0.3"
Endpoint
```

3.3 Statement Parameters to Utilize

The statement parameter locations here are written in JSONPath. This notation is also compatable with the xAPI Z notation due to the defined hierarchy of components. Within the Z specifications, a variable name will be used instead of the \$

- \bullet \$.result.success
- \$.object.id

3.4 2018 Pilot TLA Statement Problems

The initial pilot test data supports this algorithm. Given that the offical 2018 pilot test is scheduled to take place on July 27th, 2018, this section may require updates pending future data review.

3.5 Summary

1. Query an LRS via a GET request to the statements endpoint using the parameters verb, since and until

⁵ See footnote 1.

 $^{^6}$ See footnote 2.

⁷ See footnote 3.

- 2. Filter the results to the set of statements where:
 - \$.result.success is false
- 3. process the filtered data
 - group by \$.object.id
 - determine the count of each group
 - create a collection of pairs = [\$.object.id, #]

3.6 Formal Specification

3.6.1 Basic Types

```
INCORRECT :== \{false\}
```

3.6.2 System State

```
MostDifficultAssessmentQuestions \\ Statements \\ S_{all}: \mathbb{F}_1 \\ S_{incorrect}, S_{grouped}, S_{processed}: \mathbb{F} \\ \hline S_{all} = statements \\ S_{incorrect} \subseteq S_{all} \\ S_{grouped} = \{groups : \operatorname{seq}_1 statement\} \\ S_{processed} = \{pair : (id, \mathbb{N})\} \\ \hline
```

- The set S_{all} is a non-empty, finite set and is the component statements
- The sets $S_{incorrect}$, $S_{grouped}$ and $S_{processed}$ are all finite sets
- the set $S_{incorrect}$ is a subset of S_{all} which may contain every value within S_{all}
- the set $S_{grouped}$ is a finite set of objects groups which are non-empty, finite sequences of the component statement
- the set $S_{processed}$ is a finite set of pairs where each contains the component id and a natural number

3.6.3 Initial System State

```
InitMostDifficultAssessmentQuestions \\ MostDifficultAssessmentQuestions \\ \hline S_{all} \neq \emptyset \\ S_{incorrect} = \emptyset \\ S_{grouped} = \emptyset \\ S_{processed} = \emptyset
```

- The set S_{all} is a non-empty set
- The sets $S_{incorrect}$, $S_{grouped}$ and $S_{processed}$ are all initially empty

3.6.4 Filter for Incorrect

```
Incorrect \\ Statement \\ incorrect: STATEMENT \rightarrow \mathbb{F} \\ s?: STATEMENT \\ s!: \mathbb{F} \\ \\ s? = statement \\ s! = incorrect(s?) \\ incorrect(s?) = \mathbf{if} \ s? .result.success: INCORRECT \\ \mathbf{then} \ s! = s? \\ \mathbf{else} \ s! = \emptyset
```

- the schema *Incorrect* introduces the function *incorrect* which takes in the variable s? and returns the variable s!
- the variable s? is the component statement
- s! is equal to s? if \$.result.success is of the type INCORRECT otherwise s! is an empty set

- the set *incorrects* is a subset of S_{all} which may contain every value within S_{all}
- ullet The set incorrects' contains elements s of type STATEMENT where incorrect(s) is not an empty set
- The updated set $S'_{incorrect}$ is the union of the previous state of $S_{incorrect}$ and incorrects'

3.6.5 Processes Results

- The schema GroupByActivityId introduces the function group which has the input of g? and the output of g!
- The input variable g? is the component statements which implies its a set of objects g which are each a statement
- the output variable g! is a set of objects groups which are each a nonempty, finite sequence of statement where each member of the sequence $s_i...s_j$ has the same \$.object.id

```
CountPerGroup \\ Statement \\ c!: seq_1 statement \\ c!: \mathbb{N} \\ count: seq_1 statement \to \mathbb{N} \\ \hline \\ c! = count(c?) \\ c! \geq 1 \\ count(c?) = \forall c_n?: \langle c?_i ...c?_j \rangle \bullet i \leq n \leq j \land i = 0 \bullet \\ \exists_1 c!: \mathbb{N} \bullet \text{ if } n = i \text{ then } c! = n+1 \text{ else } c! = j+1 \\ \hline \\ \end{cases}
```

- The schema CountPerGroup introduces the function count which has the input of c? and the output of c!
- ullet The input variable c? is a non-empty, finite sequence in which each element is a statement
- The function *count* reads: for all elements $c?_n$ within the sequence $\langle c?_i ... c?_j \rangle$, such that n is greater than or equal to i and less than or equal to j, i is equal to zero and there exits a number c! which is equal to n+1 (when $n=i \Rightarrow n=0$) or equal to n

- \bullet The schema AggregateQuestionStatements introduces the variables grouped and processed
- grouped starts as an empty set but then becomes grouped' which is the output of applying the function group to the set of statements $S_{incorrect}$ created by the opperation FilterForIncorrect
- grouped' is a set of sequences. The elements of those sequences are statements which all have the same statement.object.id
- The set $S_{grouped}$ is updated to the set $S'_{grouped}$ which is the union of $S_{grouped}$ and grouped'
- the variable processed is a subset of $S'_{grouped}$ which can contain every value within $S'_{grouped}$
- the variable *processed* is updated to be the variable *processed'* which is a set of objects p which are ordered pairs of the component id and a natural number. p is defined as:
 - for all sequences $g_i..g_j$ within the set *processed*, there exists an ordered pair p_n such that:
 - * the first element of p_n is equal to the *object.id* of the first statement within the sequence g_n .
 - * The second element of p_n is equal to the value returned when g_n is passed to the function count.
- The set $S'_{processed}$ is the union of the sets $S_{processed}$ and processed'

3.6.6 Sequence of Operations

 $ProcessedQuestions \triangleq FilterForIncorrect$ % AggregateQuestionStatements

- ullet The schema ProcessedQuestions is the sequential composition of operation schemas FilterForIncorrect and AggregateQuestionStatements
- $\bullet \ \ Filter For Incorrect \ {\bf happens} \ \ {\bf before} \ \ Aggregate Question Statements$

3.6.7 Return

```
ReturnAggregate \_
\Xi MostDifficultAssessmentQuestions
ProcessedQuestions
S_{processed}!: \mathbb{F}
S_{processed}! = S_{processed}
```

• The returned variable $S_{processed}$! is equal to the current state of variable $S_{processed}$ after the operations FilterForIncorrect and AggregateQuestionStatements

3.7 Pseudocode

Algorithm 2: Most Difficult Assessment Questions

```
Input: S_{all}, displayN
Result: display"
context = \{\};
display = //;
while S_{all} \neq \emptyset do
     foreach s \in S_{all} do
          {f if}\ s.result.success = INCORRECT\ {f then}
               S'_{incorrect} \leftarrow s \cup S_{incorrect};
              S'_{all} \leftarrow S_{all} \setminus s;
              recur S'_{all}, S'_{incorrect};
          else
              S'_{all} \leftarrow S_{all} \setminus s;

recur S'_{all}
          end
     end
\mathbf{end}
while S'_{incorrect} \neq \emptyset do
     foreach si \in S'_{incorrect} do
          id \leftarrow si.object.id;
          if id \notin context then
               do
               count = 1;
               context' \leftarrow \{id : count\};
               S'_{incorrect} \leftarrow S_{incorrect} \setminus si;
              recur context', S'_{incorrect};
          else
               do
               count' \leftarrow inc(context.id);
               context' \leftarrow \{id : count'\};
              S'_{incorrect} \leftarrow S_{incorrect} \setminus si;
recur context', S'_{incorrect};
          end
     end
end
foreach id \in context' do
     IdToCount \leftarrow [id, context.id];
     display' \leftarrow display \cap IdToCount;
     recur display'
return display'' \leftarrow take(sortBySubArray(display'), displayN)
```

- The Z schemas are used within this pseudocode
- The return value display is an array of length display-n, where each element of display is an array of [statement.object.id, #] where # representing the number of times statement.object.id appeared within S'_incorrect

3.8 JSON Schema

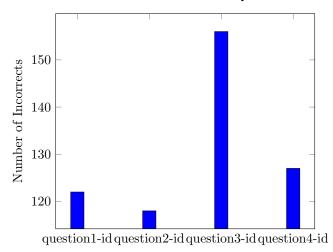
```
{"type":"array",
    "items":{"type":"array",
        "items":[{"type":"string"}, {"type":"number"}]}}
```

3.9 Visualization Description

The Most Difficult Assessment Questions visualization will be a bar chart where the domain consists of *statement.object.id* and the range is a number greater than or equal to 1. Every subarray within the array display will be a grouping within the bar chart. The pseudocode specifies an input paramter display-n which controls the length of the array display and therefor the number of groups contained within the visualization.

3.10 Visualization prototype





3.11 Prototype Improvement Suggestions

Additional features may be implemented on top of this base specification but they would require adding aditional values to each subarray returned by the algorithm. These additional values can be retrieved via (1) performing metadata lookup within or independently of the algorithm (2) by utilizing additional xAPI statement paramters and/or (3) by performing additional computations. The following examples assume the metadata is contained within each statement available to the algorithm.

- Use the name of the activity for the x-axis label instead of its id.
 - -\$.object.definition.name
 - grouping of statements should still happen by \$.object.id to ensure an accurate count
- a tooltip containing contextual information about the question such as:
 - The question text
 - * \$.object.definition.description
 - Interaction Type
 - * \$.object.definition which contains interaction properties
 - Answer choices
 - * \$.object.definition which contains interaction properties
 - Correct answer
 - * \$.object.definition which contains interaction properties
 - Most popular incorrect answer
 - * This would require an extra step of processing and all statements would need to utilize interaction properties within \$.object.definition
 - average partial credit earned (if applicable)
 - * \$.result.score.scaled
 - * The one potential issue with using scaled score is the calculation of scaled is not stricly defined by the xAPI specification but is instead up to the authors of the LRP. This results in the inability to reliably compare scaled scores across LRPs.
 - * if \$.result.score.raw , \$.result.score.min and \$.result.score.max are reported for all questions, it becomes possible to reliably compare scores across questions and LRPs.
 - average number of re-attempts
 - * this would require additional steps of processing so that \$.actor is considered as well
 - * due to the problem of actor unification, ie the same person being identified differently across statements, this metric may not be accurate.
 - average time spent on the question
 - * \$.result.duration
 - * this would require additional steps of processing to extract the duration and average it.

- a tooltip containing contextual information about the course and/or assessment the question was within
 - the instructor for the course
 - $* \ \$.context.instructor$
 - competency associated with the question and/or course
 - *~\$.context.contextActivities
 - metadata about the learning content associated with the question such as average time spent engaging with associated content before attempting the question.
 - this would require additional steps of processing to retrieve metadata about the content and its usage.
 - $* \ \$.context.contextActivities$

4 Rate of Completions

As learners engage in activities supported by a learning ecosystem, they will build up a history of learning experiences. When the digital resources of that learning ecosystem adhere to a framework dedicated to supporting and understanding the learner, such as the Total Learning Architecture (TLA), it becomes possible to retell their learning story through data and data visualization. One important aspect of that story is the rate of completion⁸ of the various digital resources within the learning ecosystem.

4.1 Ideal Statements

In order to accurately portray the rates of completion, there are a few base requirements of the data produced by a Learning Record Provider (LRP). They are as follows:

- statements describing a learner completing an activity should use the verb http://adlnet.gov/expapi/verbs/completed
- statements describing a learner completing an activity should report if the learner was successful or not via \$.result.success
- statement describing a learner completing a scored activity should report the learners score via \$.result.score.raw, \$.result.score.min and \$.result.score.max
- activites must be uniquely and consistently identified across all statements
- The time at which a learner completed a learning activity must be recorded
 - The timestamp should contain an appropriate level of specificity.
 - ie. Year, Month, Day, Hour, Minute, Second, Timezone
- statements describing a learner completing an activity should report the amount of time taken to complete the activity via \$.result.duration

4.2 Input Data Retrieval

How to query an LRS via a GET request to the Statements Resource via curl. The following section contains the appropriate parameters with example values as well as the curl command necessary for making the request. ¹⁰¹¹¹²

 $^{^8}$ Completion can be defined by the presence of the verb completed or by the presence of \$.result.completion set equal to true. In this algorithm, completion is defined by the presence of the verb completed regardless of \$.result.completion. This decision affects how statements are retrieved and filtered. In the case where completion is defined by \$.result.completion, the query to the LRS would not include the verb parameter and there would need to be a filtering process which looks for the presence of $\$.result.completion = {\rm true}$

 $^{^9}$ See footnote 4

 $^{^{10}}$ See footnote 1.

 $^{^{11}}$ See footnote 2.

¹² See footnote 3.

4.3 Statement Parameters to Utilize

The statement parameter locations here are written in JSONPath. This notation is also compatable with the xAPI Z notation due to the defined hierarchy of components. Within the Z specifications, a variable name will be used instead of the \$

- \$.timestamp
- \$.object.id

4.4 2018 Pilot TLA Statement Problems

The initial pilot test data supports the core requirements of this algorithm but completion statements only reports completion scores via \$.result.scaled instead of \$.result.score.raw, \$.result.score.min and \$.result.score.max. 13 Given that the offical 2018 pilot test is scheduled to take place on July 27th, 2018, this section may require updates pending future data review.

4.5 Summary

1. Query an LRS via a GET request to the statemetrs endpoint using the paramters verb, since and until.

 $^{^{13}}$ The one potential issue with using scaled score is the calculation of scaled is not stricly defined by the xAPI specification but is instead up to the authors of the LRP. This results in the inability to reliably compare scaled scores across LRPs. if \$.result.score.raw, \$.result.score.min and \$.result.score.max are reported for all questions, it becomes possible to reliably compare scores across LRPs by generating a scaled score in a consistent way.

- 2. group statements by their \$.object.id
- 3. select time range unit for use within rate calculation. Will default to day.
- 4. determine the amount of time between the first and last instance of a \$.object.id (in seconds) and divide it by the time unit. ie if the unit is minute, you would divide by 60.
- 5. calculate the rate by dividing the count of a group (2) by the number of time units covered by the statements (4) so that the rate is the number of completions per activity per time unit.

4.6 Formal Specification

4.6.1 Basic Types

```
TIMEUNIT :== \{second\} | \{minute\} | \{hour\} | \{day\} | \{week\} | \{month\} | \{year\} \} | \{minute\} | \{min
```

4.6.2 System State

```
RateOfCompletion \\ Statements \\ S_{completions}: \mathbb{F}_1 \\ S_{grouped}, S_{timeunit}, S_{processed}: \mathbb{F} \\ \\ S_{completions} = statements \\ S_{grouped} = \{byId: seq_1 \ statement\} \\ S_{withRate} = \{byGroup: (seq_1 \ statement, \mathbb{N})\} \\ S_{processed} = \{rate: (id, \mathbb{N}, TIMEUNIT)\} \\ \\
```

- The set $S_{completions}$ is a non-empty, finite set and is the component statements which contains the results of the query to the LRS.
- The sets $S_{qrouped}$, $S_{withRate}$ and $S_{processed}$ are all finite sets
- the set $S_{grouped}$ is a finite set of objects byId which are non-empty, finite sequences of the component statement
- the set $S_{withRate}$ is a finite set of objects byGroup which are ordered pairs of non-empty, finite sequences of the component statement and a natural number
- the set $S_{processed}$ is a finite set of objects rate where each contains the component id, a natural number and the type TIMEUNIT

4.6.3 Initial System State

```
InitRateOfCompletion RateOfCompletion T:TIMEUNIT S_{completions} \neq \emptyset S_{grouped} = \emptyset S_{withRate} = \emptyset S_{processed} = \emptyset T = \{day\}
```

- The set $S_{completions}$ is a non-empty set which contains the results of the GET request(s) to the LRS
- The sets $S_{grouped}$, $S_{withRate}$ and $S_{processed}$ are all initially empty
- the variable T has the type TIMEUNIT and the value $\{day\}$

4.6.4 Calculate Rate

- The schema *IsoToUnix* introduces the function *convert* which takes in a finit set of one thing (a timestamp) and converts it to a single natural number.
- the purpose of this function is to convert an ISO 8601 timestamp to the Unix epoch. The concrete definition of the conversion is outside the scope of this document
 - The Unix epoch is the number of seconds that have elapsed since January 1, 1970 (midnight UTC/GMT), not counting leap seconds.

```
 \begin{array}{l} -CalcRateByUnit \\ -Statement \\ -IsoToUnix \\ -CountPerGroup \\ -unit?: TIMEUNIT \\ s?, s!: \mathbb{F} \\ r: \mathbb{N} \\ -rate: (\mathbb{F}, TIMEUNIT) \to \mathbb{F} \\ \\ \hline \\ unit? = \{second\} \Rightarrow 1 \lor \{minute\} \Rightarrow 60 \lor \{hour\} \Rightarrow 3600 \lor \\ -\{day\} \Rightarrow 86400 \lor \{week\} \Rightarrow 604800 \lor \\ -\{month\} \Rightarrow 2629743 \lor \{year\} \Rightarrow 31556926 \\ s? = \{g: seq_1 statement\} \\ s! = rate(s?, unit?) \\ s! = \{s: (g, r) \mid \forall g_n: g_i..g_j \bullet i \leq n \leq j \bullet \exists s_n: (g_n, r_n) \bullet \\ -r_n = count(g_n) \div ((convert(last g_n.timestamp) - convert(head g_n.timestamp)) \div unit?) \} \end{array}
```

- The schema CalcRateByUnit introduces the function rate where the input s? is a set of objects g which are each a non-empty, finite sequence of statements and the input unit? represents a unit of time.
- for every g_n within the range $g_i...g_j$, there exists an associated object s_n which is an orderd pair of (g_n, r_n) where r_n is equal to the number of items within g_n divided by the number of unit?s within the time range of $last\ g_n.timestamp head\ g_n.timestamp$
- the output of the function rate is s!, the set of all s_n

4.6.5 Processes Results

```
AggergateCompletionStatements
\Delta RateOfCompletion
GroupByActivityId
CalcRateByUnit
grouped, processed, with Rate : \mathbb{F}
r:\mathbb{N}
T?: TIMEUNIT
T? = \{day\}
grouped = \emptyset
grouped' = group(S_{completions})
S'_{grouped} = S_{grouped} \cup grouped'
withRate \subseteq S'_{grouped}
withRate' = rate(withRate, T?)
S'_{withRate} = withRate' \cup S_{withRate}
processed \subseteq S'_{withRate}
processed' = \{p : (id, r, T?) \mid
                  let \{processed_i..processed_i\} == \{b_i..b_i\} \bullet
                  \forall b_n : b_i ... b_j \bullet i \le n \le j \bullet \exists p_n : (id_n, r_n, T?) \bullet
                  id_n = (head (first b_n)).object.id \land
                  r_n = (second \, b_n)
S'_{processed} = processed' \cup S_{processed}
```

- The schema AggergateCompletionStatements outlines how to calculate the rate of completion per \$.object.id per second|minute|hour|day|week|month|year
 - 1. $S'_{grouped}$ is the result of grouping the statements within $S_{completions}$ by their \$.object.id
 - 2. The groups from (1) are passed to the function *rate* with the variable *T*? which controls the unit of time, ie per day vs per week
 - 3. the result of (2) is then processed to create a triplet of \$.object.id, rate, unit of time for all unique \$.object.id within $S_{completions}$

4.6.6 Return

```
Return Aggergate Completion Statements \Xi Rate Of Completion Aggergate Completion Statements S_{processed}!: \mathbb{F} S_{processed}! = S_{processed}
```

• The return value $S_{processed}$! is equal to $S_{processed}$ after the operation described by AggergateCompletionStatements

4.7 Pseudocode

```
Algorithm 3: Rate of Completions
 Input: S_{completed}, timeUnit
 Result: ratePerObjTu'
  context = \{\};
  ratePerObjTu = //;
 while S_{completion} \neq \emptyset do
      for
each s \in S_{completion} do
          id \leftarrow s.object.id;
          ts \leftarrow convert(s.timestamp);
         if id \notin context then
              do
              times = [ts];
              context' \leftarrow \{id: times\};
              S'_{completion} \leftarrow S_{completion} \setminus s;
              recur context', S'_{completion};
          else
              do
              times' \leftarrow context.id \cap ts;
              context' \leftarrow \{id : times'\};
              S'_{completion} \leftarrow S_{completion} \setminus s;
              recur context', S'_{completion};
          end
      end
  end
 foreach k \in context' do
      allTs \leftarrow context'.k;
      totalDuration \leftarrow max(allTs) - min(allTs);
      totalCount \leftarrow count(allTs);
      rate \leftarrow totalCount \div (totalDuration \div timeUnit);
      subVec = [k, rate, timeUnit];
      ratePerObjTu' \leftarrow ratePerObjTu \cap subVec;
      recur ratePerObjTu';
  end
 return ratePerObjTu'
```

- Values from Z schemas are used within this pseudocode
- the result of the algorithm is an array of arrays where each subarray contains a *statement.object.id*, the *rate* and the *timeUnit* used to calculate *rate*.

4.8 JSON Schema

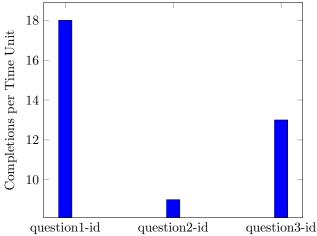
```
{"type":"array",
    "items":{"type":"array",
        "items":[{"type":"string"}, {"type":"number"},
{"type":"string"}]}
```

4.9 Visualization Description

The Rate of Completions visualization will be a bar chart where the domain consists of statement.object.id and the range is a number greater than 0 (the rate of completions for that statement.object.id). Every subarray within the array ratePerObjTu will be a grouping within the bar chart. The pseudocode specifies an input paramter timeUnit which controls the calculation of the rate (range of the visualization). timeUnit could be per minute, per day, per week, etc.

4.10 Visualization prototype





4.11 Prototype Improvement Suggestions

Additional features may be implemented on top of this base specification but they would require adding aditional values to each subarray returned by the algorithm. These additional values can be retrieved via (1) performing metadata lookup within or independently of the algorithm (2) by utilizing additional xAPI statement paramters and/or (3) by performing additional computations. The following examples assume the metadata is contained within each statement available to the algorithm.

- \bullet use statement.object.definition.name instead of statement.object.id for x axis label
- populate a tooltip with the people who have completed the activity. This could also include the number of times they have completed it.
- populate a tooltip with the breakdown of which devices or platforms the activity was completed on. This would require the device type or platform to be reported within *statement.context.platform*
- populate a tooltip with the breakdown of percentage successful for all completions of the activity. This would require statement.result.success
- populate a tooltip with the breakdown of scores earned (if appliciable) for the completions. This would require statement.result.score.raw, statement.result.score.min and statement.result.score.max
- populate a tooltip with the competency associated with the completed activities. The competency should be reported via statement.context.contextActivities
- populate a tooltip with the average duration spent to reach completions. This would require *statement.result.duration* to be reported.

5 How Often are Recommendations Followed

As learners engage in activities supported by a learning ecosystem, they will build up a history of learning experiences. When the digital resources of that learning ecosystem adhere to a framework dedicated to supporting and understanding the learner, such as the Total Learning Architecture (TLA), it becomes possible to retell their learning story through data and data visualization. One important aspect of that story is the recommendations provided to the learner and whether or not the learner follows those recommendations.

5.1 Ideal Statements

In order to accurately determine if a learner is following recommendations, there are a few requirements of the data produced by a LRP and the recommender itself. They are as follows:

- Every time the recommender makes a recommendation, a statement should be produced which uses the verb https: //w3id.org/xapi/dod-isd/verbs/recommended and has the recommended piece of content as the object.
 - the content should be uniquely and consistently identified across all statements.
- When a learner launches recommended content, the resulting launched statement should use the verb $http://adlnet.gov/expapi/verbs/launched^{15}$ and contain a refrence to the recommend content statement within \$.context.statement
 - Launching of content should use the above IRI regardless of why the content was launched
 - If it not possible to refrence the exact recommended content statement, the launch statement should have some indication that it was the result of a recommendation.¹⁶

¹⁴ See footnote 4

 $^{^{15}}$ See footnote $4\,$

¹⁶ It is possible to determine if recommendations are followed (with some level of error) without this explicit linking of launched to recommended but this severly complicates the algorithm. In this case, in order to optmize for accuracy, the algorithm would need to consider the actor and their general activity within a session, the object of both launched and recommended statements generated within the session, the time lapse between recommendations and launches with a predefined lapse value which determines if a launch was close enough in time to a recommendation to be considered a result of the recommendation. An additional constraint on the above case is the recommendation statements should contain a reference to to the person recieving the recommendation, otherwise determining the 1:1 relationships between recommendations and launches requires additional complexity and will still not be 100% accurate due to the reliance on the time lapse value.

5.2 Input Data Retrieval

How to query an LRS via a GET request to the Statements Resource via $\operatorname{curl}^{171819}$

```
R = "verb=https://w3id.org/xapi/dod-isd/verbs/recommended"
L = "verb=http://adlnet.gov/expapi/verbs/launched"
Since = "since = 2018 - 07 - 20T12 : 08 : 47Z"
Until = "until = 2018 - 07 - 21T12 : 08 : 47Z"
Base = "https://example.endpoint/statements?"
endpoint1 = Base + R + "\&" + Since + "\&" + Until
endpoint2 = Base + L + "&" + Since + "&" + Until
Auth = Hash generated from basic auth
SR = curl -X GET -H "Authorization: Auth"
         -H "Content-Type: application/json"
         -H "X-Experience-API-Version: 1.0.3"
         endpoint1
SL = curl -X GET -H "Authorization: Auth"
         -H "Content-Type: application/json"
         -H "X-Experience-API-Version: 1.0.3"
         endpoint2
S = SR + SL
```

5.3 Statement Parameters to Utilize

The statement parameter locations here are written in JSONPath. This notation is also compatable with the xAPI Z notation due to the defined hierarchy of components. Within the Z specifications, a variable name will be used instead of the \$

- \$.verb.id
- \$.context.statement

5.4 2018 Pilot TLA Statement Problems

At the time of writing this document, launched statements do not include a statement reference or any indication of a connection between recommendations and launches. The authors of this document do not have access to the LRS

¹⁷ footnote 1 applies to both S1 and S2.

 $^{^{18}}$ See footnote 2.

¹⁹ See footnote 3.

containing the recommended statements and thus can not draw any conclusions about any issues which may be present within those statements or any aspects of those statements which may correlate them to launch statements. The following algorithm is going to assume that the input set of statements follow the guidlines outlined in section 5.1 as the additional algorithmic considerations brought on by non ideal statements, as specified within footnote 16, result in an algorithm which is not optimal for near real time visualizations.

5.5 Summary

- 1. Query an LRS via a GET request to the statements endpoint using the paramters verb, since and until to gather all statements with the verb http://adlnet.gov/expapi/verbs/launched.
- 2. Query an LRS via a GET request to the statements endpoint using the paramters verb, since and until to gather all statements with the verb https://w3id.org/xapi/dod-isd/verbs/recommended.
- 3. Group all collections of statements by a TIMEUNIT
- 4. seperate the collection of grouped launched statements into a collection of those which were the result of a recommendation and those which were not.
- 5. Take the count of all groups of statements
 - Recommended statements per TIMEUNIT
 - Launches due to recommendations per TIMEUNIT
 - Launches not due to recommendations per TIMEUNIT
- 6. Calculate summary statistics for the overall time range and per TIMEUNIT
 - Divide launches due to recommendations by the total number of launches to determine the percentage of launches due to recommendations
 - Divide launches due to recommendations by the total number of recommendations to determine the percentage of recommendations which are followed.

 $^{^{20}}$ If since and until are specified, they should be the same in both requests.

5.6 Formal Specification

5.6.1 System State

```
FollowedRecommendations
Statements
CountPerGroup
S_{recommended}, S_{launched} : \mathbb{F}_1
ordered_L, ordered_R, grouped_{launched}, grouped_{recommended},
only Recommended, cPerGroup_{launched}, cPerGroup_{recommended}, \\
cPerGroup_{followed}, combined : seq
t_{start}, N_{launched}, N_{recommended}, N_{followed}, P_{followed}, P_{dueto} : \mathbb{N}
tr_{start}, tr_{end} : \mathbb{F}
unit?: TIMEUNIT
S_{recommended} = statements
S_{launched} = statements
combined = \langle (tr_{start}, tr_{end}, N_{launched}, N_{recommended}, N_{followed}, P_{followed}, P_{dueto}) \rangle
count(grouped_{launched}) = count(grouped_{recommended})
count(onlyRecommended) = count(grouped_{launched}) \Rightarrow
count(onlyRecommended) = count(grouped_{recommended})
count(cPerGroup_{launched}) = count(cPerGroup_{followed}) = count(cPerGroup_{recommended})
```

- $S_{recommended}$, $S_{launched}$ are both non-empty, finite sets.
 - $S_{recommended}$ and $S_{launched}$ contain the results of querying an LRS for recommended and launched statements respectively.
- $ordered_L$, $ordered_R$, $grouped_{launched}$, $grouped_{recommended}$, only Recommended, $cPerGroup_{launched}$, $cPerGroup_{recommended}$, $cPerGroup_{followed}$ and combined are all finite sequences.
 - $ordered_L$ and $ordered_R$ are the sequences of statements within $S_{launched}$ and $S_{recommended}$ respectively and sorted by timestamp.
 - $grouped_{launched}$ is the result of grouping the statements within $ordered_L$ by unit?.
 - $grouped_{recommended}$ is the result of grouping the statements within $ordered_R$ by unit?.
 - onlyRecommended is the result of filtering the statements within the sequence grouped_{launched} to only include statements where statement.context.statement is present
 - cPerGroup_{launched}, cPerGroup_{recommended}, cPerGroup_{followed} are all sequences of numbers which represent the count within each subsequence of grouped_{launched}, grouped_{recommended} and onlyRecommended respectively.

- combined is a sequence of ordered pairs where each pair consists of tr_{start} , tr_{end} , $N_{launched}$, $N_{recommended}$, $N_{followed}$, $P_{followed}$ and P_{dueto}
- t_{start} , $N_{launched}$, $N_{recommended}$, $N_{followed}$, $P_{followed}$, P_{dueto} are all natural numbers
- tr_{start} , tr_{end} are both timestamps which represent the start and end of the time range for each a group of statements.
- unit? is an input representing a time interval, ie day vs month vs hour.
- all sequences are the same length so that each subsequence represents the same time grouping. In other words, indexes are comparable across sequences.

5.6.2 Initial System State

```
InitFollowedRecommendations _
FollowedRecommendations
S_{recommended} \neq \emptyset
S_{launched} \neq \emptyset
unit? = \{day\}
ordered_L = \langle \rangle
ordered_R = \langle \dot{\rangle}
grouped_{launched} = \langle \rangle
grouped_{recommended} = \langle \rangle
onlyRecommended = \langle \rangle
cPerGroup_{launched} = \langle \rangle
cPerGropu_{recommended} = \langle \rangle
cPerGroup_{followed} = \langle \rangle
combined = \langle \rangle
t_{start}=0\,
N_{launched} = 0
N_{recommended} = 0
N_{followed} = 0
P_{followed} = 0
P_{dueto} = 0
```

- $S_{recommended}$ and $S_{launched}$ are initially not empty sets
- all sequences are initially empty
- all numbers are initially zero
- \bullet the default TIMEUNIT is set to day

5.6.3 Group by Timestamp

- The schema SortByTimestamp introduces the function orderByTimestamp which takes in a non-empty, finite set and returns a non-empty, finite sequence.
- orderByTimestamp is a sequence of statements ordered from earliest to

```
\begin{tabular}{ll} WithinRange & & withinRange : (\mathbb{N},\mathbb{N},\mathbb{N},TIMEUNIT) \rightarrow \mathbb{F}_1\#1\\ in?,start?,state?:\mathbb{N}\\ unit?:TIMEUNIT\\ out!:\{TRUE\}\lor\{FALSE\}\\ \\ \hline & unit?=\{second\}\Rightarrow 1\lor\{minute\}\Rightarrow 60\lor\{hour\}\Rightarrow 3600\lor\\ \{day\}\Rightarrow 86400\lor\{week\}\Rightarrow 604800\lor\\ \{month\}\Rightarrow 2629743\lor\{year\}\Rightarrow 31556926\\ out!=withinRange(in?,start?,state?,unit?)\\ withinRange(in?,start?,state?,unit?)=\\ & & \textbf{if}\ in?\leq start?+((state?+1)*unit?)\\ & & & \textbf{then}\ out!=\{TRUE\}\\ & & & \textbf{else}\ out!=\{FALSE\}\\ \end{tabular}
```

- The schema WithinRange introduces the function withinRange which takes in three numbers and a TIMEUNIT and returns either $\{TRUE\}$ or $\{FALSE\}$
- withinRange checks to see if in? is less than or equal to a start time start? plus the result of multiplying the numeric conversion for unit? by the state?.
- state? represents the current group, ie. day 1 vs day 2 vs day 3. The +1 is to account for array indexes starting at 0.

- The schema GroupByTimeUnit intorudces the function groupByTimeUnit which takes as arguments a non-empty, finite sequence, a natural number and a TIMEUNIT and outputs a non-empty, finite sequence of sequences.
- For every statement within the input sequence, groupByTimeUnit checks to see if the timestamp of that statement is within the range of t_{start} and unit?. If it is, that statement is removed from the input sequence g? and added to the current subsequence $\langle g_r \rangle$. If none of the remaining statements within the input sequence are within the range of t_{start} and unit?, then the variable state? is incremented, the current subsequence $\langle g_r \rangle$ is either a collection of matched statements or is an empty sequence and the search for remaining subsequences $\langle g_{r+state} \rangle$ continues.
- because the input sequence g? is orderd chronologically, this implies that once a statement does not fit into a range, the rest of the statements remaining in the input sequence will not fit into that range and state? must be incremented to generate a new subsequence $\langle g_{r+state}? \rangle$ so that the remaining statements can be grouped.

5.6.4 Processes Results

```
Order Statements \triangle Followed Recommendations Sort By Timestamp Ordered'_L = order By Timestamp(S_{launched}) Ordered'_R = order By Timestamp(S_{recommended}) Ordered'_{R} = order By Timestamp(S_{recommended}) Ordered'_{R} = order By Timestamp(S_{recommended}) Ordered'_{R} = order By Timestamp(S_{recommended})
```

- The schema *OrderStatements* updates the system state defined by the schema *FollowedRecommendations*.
- $ordered'_L$ is the result of ordering the statements contained within the set $S_{launched}$ chronologically.
- $ordered'_R$ is the result of ordering the statements contained within the set $S_{recommended}$ chronologically.
- t'_{start} is the timestamp from the first statement within $ordered'_L$ converted to unix time.

```
\begin{tabular}{l} $-GroupByTime $\_$ \\ $\Delta Followed Recommendations \\ $GroupByTimeUnit$ \\ \hline $grouped'_{launched} = groupByTimeUnit(ordered'_L, t'_{start}, 0, unit?)$ \\ $grouped'_{recommended} = groupByTimeUnit(ordered'_R, t'_{start}, 0, unit?)$ \\ \hline \end{tabular}
```

- \bullet The schema Group By Time updates the state defined by the schema Followed Recommendations.
- $grouped'_{launched}$ is the result of passing $ordered'_L$, t'_{start} , 0 and unit? to the function groupByTimeUnit.
- $grouped'_{recommended}$ is the result of passing $ordered'_R$, t'_{start} , 0 and unit? to the function groupByTimeUnit.

- ullet The schema OnlyRecommendedLaunches updates the state defined by the schema FollowedRecommendations.
- onlyRecommended' is the sequence of objects o where o is a sequence consisting of statements (or no statements) from the corresponding sequences within $grouped'_{launched}$ where statement.context.statement exists.
- only Recommended' maintains the same number and ordering of time groups (subsequences) as $grouped'_{launched}$ and $grouped'_{recommended}$.

```
GetCounts\_
 \Delta FollowedRecommendations
CountPerGroup
cPerGroup'_{launched} = \langle c : \mathbb{N} \, | \, \textbf{let} \, grouped'_{launched} == gl \Rightarrow \langle \langle gl_i \rangle .. \langle gl_j \rangle \rangle \bullet \\ \forall \langle gl_n \rangle : \langle gl_i \rangle .. \langle gl_j \rangle \bullet \exists_1 c_n : \mathbb{N} \bullet
                                                           if gl_n = \langle \rangle
                                                                       then c_n = 0
                                                                       else c_n = count(\langle gl_n \rangle) \rangle
cPerGroup'_{recommended} = \langle c : \mathbb{N} \mid \mathbf{let} \ grouped'_{recommended} == gr \Rightarrow \langle \langle gr_i \rangle .. \langle gr_j \rangle \rangle \bullet \\ \forall \langle gr_n \rangle : \langle gr_i \rangle .. \langle gr_j \rangle \bullet \exists_1 c_n : \mathbb{N} \bullet
                                                                       if gr_n = \langle \rangle
                                                                                   then c_n = 0
                                                                                   else c_n = count(\langle gr_n \rangle) \rangle
cPerGroup'_{followed} = \langle c : \mathbb{N} \mid \mathbf{let} \ onlyRecommended' == or \Rightarrow \langle \langle or_i \rangle ... \langle or_j \rangle \rangle \bullet
                                                           \forall \langle or_n \rangle : \langle or_i \rangle .. \langle or_j \rangle \bullet \exists_1 c_n : \mathbb{N} \bullet
                                                           if or_n = \langle \rangle
                                                                       then c_n = 0
                                                                       else c_n = count(\langle or_n \rangle) \rangle
```

- The schema GetCounts updates the state defined by the schema FollowedRecommednations.
- $cPerGroup'_{launched}$ is a sequence of numbers c where each c is either 0 or the result of passing the current subsequence of $grouped'_{launched}$ (gl_n) to the function count.
- $cPerGroup'_{recommended}$ is a sequence of numbers c where each c is either 0 or the result of passing the current subsequence of $grouped'_{recommended}$ (gr_n) to the function count.
- $cPerGroup'_{followed}$ is a sequence of numbers c where each c is either 0 or the result of passing the current subsequence of onlyRecommended' (or_n) to the function count.

```
Combine Sequences _
\Delta FollowedRecommendations
combined' = \langle c: (tr'_{start}, tr'_{end}, N'_{launched}, N'_{recommended}, N'_{followed}, P'_{followed}, P'_{dueto}) \mid
                      let grouped'_{launched} == gl \Rightarrow \langle \langle gl_i \rangle .. \langle gl_n \rangle .. \langle gl_j \rangle \rangle
                            cPerGroup'_{launched} == cl \Rightarrow \langle cl_i...cl_n...cl_j \rangle
                            cPerGroup'_{recommended} == cr \Rightarrow \langle cr_i..cr_n..cr_j \rangle
                            cPerGroup'_{followed} == cf \Rightarrow \langle cf_i..cf_n..cf_j \rangle
                      • \forall \langle gl_n \rangle : \langle gl_i \rangle ... \langle gl_j \rangle \bullet i \leq n \leq j \bullet
                      \exists_1 c_n : (tr_{startn}, tr_{endn}, N_{launchedn}, N_{recommendedn}, N_{followedn}, P_{followedn}, P_{dueton}) \bullet
                      tr_{startn} = (head gl_n).timestamp
                      tr_{endn} = (last gl_n).timestamp
                      N_{launchedn} = cl_n
                      N_{recommendedn} = cr_n
                      N_{followedn} = cf_n
                      P_{followedn} = cf_n \div cr_n
                      P_{dueton} = cf_n \div cl_n \rangle
```

- The schema CombineSequences changes the state defined by the schema FollowedRecommendations.
- combined' is a sequence of objects c where each c is an ordered pair of $tr'_{start}, tr'_{end}, N'_{launched}, N'_{recommended}, N'_{followed}, P'_{followed}, P'_{dueto}$.
- for each c_n :
 - $-\ tr'_{start} \leadsto tr_{startn}$ which is equal to the timestamp for the first statement within gl_n
 - $-tr'_{end} \sim tr_{endn}$ which is equal to the timestamp for the last statement within ql_n .
 - $-N'_{launched} \sim N_{launchedn}$ which is equal to the current count of launched statements within the nth time grouping aka cl_n .
 - $-N'_{recommended} \sim N_{recommendedn}$ which is equal to the current count of recommended statements within the nth time grouping aka cr_n .
 - $-N'_{followed} \sim N_{followedn}$ which is equal to the current count of recommended statements within the nth time grouping aka cf_n .
 - $-P'_{followed} \sim P_{followedn}$ which is equal to the result of dividing cf_n by cr_n .
 - $-P'_{dueto} \sim P_{dueton}$ which is equal to the result of dividing cf_n by cl_n .

5.6.5 Sequence of Operations

 $ProcessFollowedRecommendations \ \widehat{=} \\ OrderStatements \ _{\S} \ GroupByTime \ _{\S} \ OnlyRecommendedLaunches \ _{\S} \\ GetCounts \ _{\S} \ CombineSequences$

ullet The schema ProcessFollowedRecommendations defines the order of operations for the steps within the FollowedRecommendations algorithm.

5.6.6 Return

```
ReturnFollowedRecommendations
\Xi FollowedRecommendations
ProcessFollowedRecommendations
combined!: seq
combined! = combined'
```

- \bullet The schema Return Followed Recommendations describes the return value of the system defined by the schema Followed Recommendations
- \bullet The return value combined! is the variable combined' defined within the schema CombineSequences

5.7 Pseudocode

Algorithm 4: Followed Recommendations Input: $S_{recommended}$, $S_{launched}$ timeUnit Result: combined' $ordered'_{L} \leftarrow orderByTimestamp(S_{launched});$ $ordered'_{R} \leftarrow orderByTimestamp(S_{recommended});$ $t'_{start} \leftarrow convert((head\ ordered'_L).timestamp);$ $grouped'_{launched} \leftarrow groupByTimeUnit(ordered'_L, t'_{start}, 0, timeUnit);$ $grouped'_{recommended} \leftarrow$ $groupByTimeUnit(ordered'_R, t'_{start}, 0, timeUnit);$ $grouped_{followed} \leftarrow [];$ foreach G in $grouped'_{launched}$ do $curGrouping \leftarrow [];$ foreach G_n in G do if $G_n.context.statement \neq nil$ then $curGrouping' \leftarrow curGrouping \cap G_n;$ recur curGrouping' else | recur curGrouping' end $\quad \text{end} \quad$ $grouped'_{followed} \leftarrow grouped_{followed} \cap curGrouping';$ recur grouped'_{followed} end $C_{launched} \leftarrow \mathbf{map} \, \mathbf{count}() \, \mathbf{grouped'_{launched}};$ $C_{recommended} \leftarrow \mathbf{map\,count}()\,\mathbf{grouped'_{recommended}};$ $C_{followed} \leftarrow \mathbf{map \, count}() \, \mathbf{grouped'_{followed}};$ $combined \leftarrow [];$ for $i \leftarrow 0$ to $count(c_{launched})$ by 1 do $tr_{starti} \leftarrow (first(nth(grouped'_{launched}, i))).timestamp;$ $tr_{endi} \leftarrow (last(nth(grouped'_{launched}, i))).timestamp;$ $N_{Li} \leftarrow nth(C_{launched}, i);$ $N_{Ri} \leftarrow nth(C_{recommended}, i);$ $N_{Fi} \leftarrow nth(C_{followed}, i);$ $P_{Fi} \leftarrow N_{fi} \div N_{Ri};$ $P_{duetoi} \leftarrow N_{fi} \div N_{Li};$ $subVec_i \leftarrow [tr_{starti}, tr_{endi}, N_{Li}, N_{Ri}, N_{Fi}, P_{Fi}, P_{duetoi}];$

• map count() grouped'... means apply the function count() to every sequence within the sequence grouped... and put all results into a single array.

 $combined' \leftarrow combined \cap subVec_i$

end

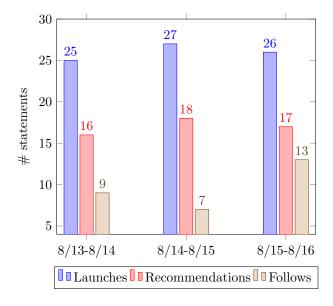
return combined'

5.8 JSON Schema

5.9 Visualization Description

The Followed Recommendations visualization can be a bar chart where the domain is time ranges and the range is a number representing the total count of statements recorded. For each time range, there will be three groups: 1) the number of launched statements 2) the number of recommended statements 3) the number of launches which are due to recommendations. Above each grouping or on hover, summary statistics can be desplayed which describe the percentage of launches due to recommendations and the percentage of recommendations which were followed.

5.10 Visualization prototype



• The percentages described in section 5.9 are not displayed here.

5.11 Prototype Improvement Suggestions

Additional features may be implemented on top of this base specification but they would require adding aditional values to each subarray returned by the algorithm. These additional values can be retrieved via (1) performing metadata lookup within or independently of the algorithm (2) by utilizing additional xAPI statement paramters and/or (3) by performing additional computations. The following examples assume the metadata is contained within each statement available to the algorithm.

- populate a tooltip with the most popular launched, recommended and followed activity.
- populate a tooltip with the number of actors associated with the launches and follows.
- populate a tooltip with the actor who most often and the actor who lease often follows recommendations.

Appendex A: Visualization Exemplars

Appendex A includes a typology of data visualizations which may be supported within DAVE workbooks. These visualizations can either be one to one or one to many in regards to the algorithms defined within this document. Future iterations of this document will increasingly include these typologies within the domain-question template exemplars.

Line Charts

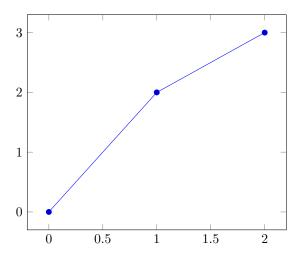


Figure 1: Line Chart

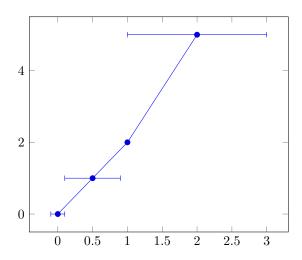


Figure 2: Line Chart with Error

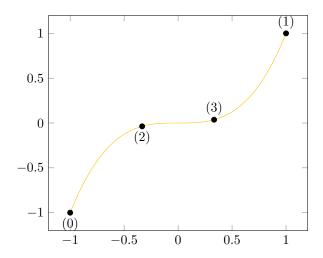


Figure 3: Spline Chart

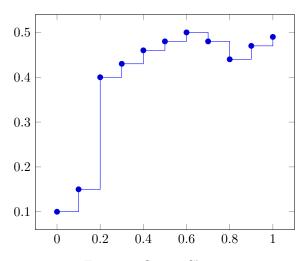


Figure 4: Quiver Chart

Grouping Charts

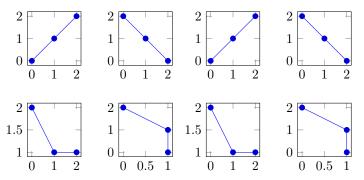


Figure 5: Grouped Line Charts

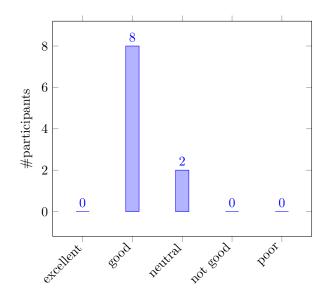


Figure 6: Histogram

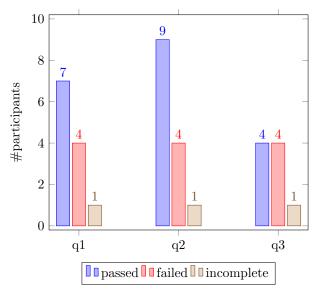


Figure 7: Bar Chart

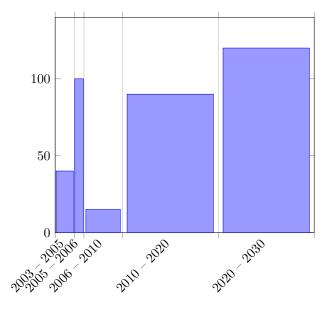


Figure 8: Bar Chart Grouped by Time Range

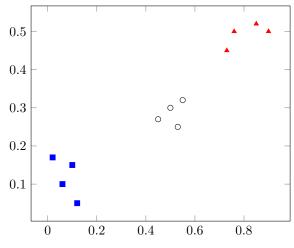


Figure 9: Scatter Plot

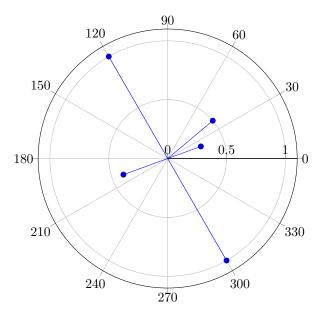


Figure 10: Polar Chart

Specialized Charts

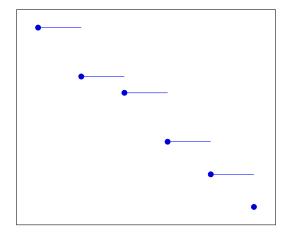


Figure 11: Gantt Chart

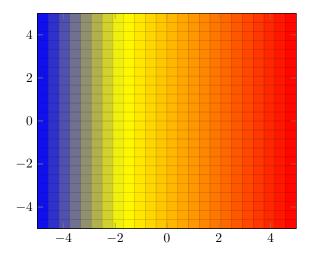


Figure 12: Heat Map

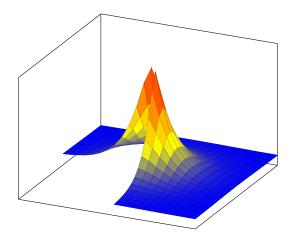
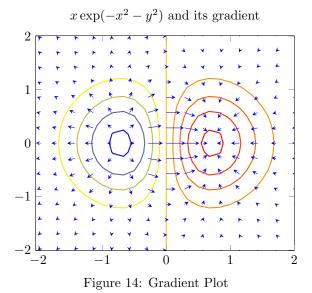


Figure 13: 3D Plot



61