

### 0.0.1 Append At

The Primitive *appendAt* uses the Primitive *atDepth* to navigated into a nested collection *coll?* (called *coll* bellow). The Value *v?* passed to *appendAt* will be appended to *coll* at *idxs?*<sub>*j*</sub>. This results in a *coll!* which is equivalent to *coll?* except for at the value at the path *idxs?*<sub>*i*</sub> .. *idxs?*<sub>*j*</sub> ∈ *coll?*.

<pre> AppendAt[Collection, Collection, V] _____ AtDepth coll?, coll!, idxs?: Collection v?: V appendAt_ : Collection × Collection × V → Collection  appendAt = ⟨atDepth_, append_, ⟨atDepth_, remove_, append_⟩#idxs?-1⟩ coll! = appendAt(coll?, idxs?, v?) •   let coll == append(atDepth(coll?, idxs? ⋖ idxs?_j), v?, idxs?_j) •     ∀n : i .. j - 1 • j = first(last(idxs?))   ∃ c_n •       let c_i == atDepth(coll?, (idxs?   i)) ⇒ atIndex(coll?, idxs?_i)       c_n == atDepth(c_{n-1}, (idxs?   n))       c_{j-1} == atDepth(c_n, (idxs?   j - 1)) ⇔ n = j - 2       c_j == append(c_{j-1}, v?, (idxs?   j)) ⇒ c_j = coll = coll!_j       coll!_{j-1} == append(remove(c_{j-2}, idxs?_{j-1}), c_j, idxs?_{j-1})       coll!_n == append(remove(c_{n-1}, idxs?_n), coll!_{n+1}, idxs?_n)       coll!_i == append(remove(c_i, idxs?_i), coll!_n, idxs?_i) ⇔ n = i + 1       = append(remove(coll?, idxs?_i), coll!_i, idxs?_i) </pre>
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The relationship described above  $coll? \triangleleft idxs_i = coll! \triangleleft idxs_i$  is described above as  $\langle atDepth\_ , remove\_ , append\_ \rangle \# idxs?^{-1}$ . The variables  $coll!_{i..j}$  were used to describe the sub Collections which have to have a single index updated given *idxs?*. Those subcollections are combined together to produce *coll!* such that the only difference between *coll?* ∧ *coll!* is found at path *idxs?*. The following examples demonstrate the properties of *appendAt* described above.

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X = ⟨x0, x1, x2⟩
x0 = 0
x1 = foo
x2 = ⟨a, b, c⟩
appendAt(X, ⟨1, 3⟩, z) = ⟨x0, fooz, x2⟩ ⇒ foo = ⟨f, o, o⟩
appendAt(X, ⟨1⟩, 5) = ⟨⟨0, 5⟩, x1, x2⟩ [existing item gets 0 index]
appendAt(X, ⟨1, 0⟩, 5) = ⟨⟨5, 0⟩, x1, x2⟩ [overwriting default behavior]
appendAt(X, ⟨2, 0⟩, d) = ⟨x0, x1, ⟨d, a, b, c⟩⟩
appendAt(X, ⟨2⟩, d) = ⟨x0, x1, ⟨a, b, c, d⟩⟩

```