0.0.1 Map

The map operation accepts the following arguments

- Operation or Primitive
- A Collection
- Additional Arguments passed to the Operator or Primitive

and returns a collection of Operation $Operation(x_n, args) \lor Primitive(x_n, args)$ respectively

Given an input Collection X and a Operation o or Primitive p where

$$X = \langle x_i..x_n..x_j \rangle$$

and that collection consists of one or more members x_n within the range i..j

$$i \le n \le j \Rightarrow i \prec n \prec j \iff i \ne n \ne j$$

then

$$map(o, X, args) = Y \land map(p, X, args) = Y'$$

such that

$$Y = \langle o(x_i, args)...o(x_n, args)...o(x_i, args) \rangle$$

and

$$Y' = \langle p(x_i, args)...p(x_n, args)...p(x_i, args) \rangle$$

which establishes both Y and Y' are a Collection where each member y_n or y'_n is the result of passing x_n and args to o or p respectively.

In otherwords

$$o(x_i, args) \mapsto y_i \wedge o(x_n, args) \mapsto y_n \wedge o(x_i, args) \mapsto y_i$$

$$p(x_i, args) \mapsto y_i' \land p(x_n, args) \mapsto y_n' \land p(x_i, args) \mapsto y_i'$$

which implies both collections Y and Y' have the same ordering as collection X

$$i_{o(x,args)} = i_y \ \land \ n_{o(x,args)} = n_y \ \land \ j_{o(x,args)} = j_y$$

$$i_{p(x,args)} = i_{y'} \ \land \ n_{p(x,args)} = n_{y'} \ \land \ j_{p(x,args)} = j_{y'}$$

When X contains non-distinct values, o and p are unaffected.

$$o(x_n, args) = y_n$$

$$o(x_{n'}, args) = y_{n'}$$

$$o(x_{n'+1}, args) = y_{n'}$$

$$x_{n'} \equiv x_{n'+1} \land x_{n'} \not\equiv x_n$$

$$\Rightarrow$$

$$x_n \not\equiv x_{n'+1}$$

$$\Rightarrow$$

$$o(x_{n'}, args) = o(x_{n'+1}, args) \not= o(x_n, args)$$

Because p is just a composition of o's, the same property holds for primitives

$$p(x_n, args) = y'_n$$

$$p(x_{n'}, args) = y'_{n'}$$

$$p(x_{n'+1}, args) = y'_{n'}$$

$$\Leftrightarrow \Rightarrow$$

$$x_{n'} \equiv x_{n'+1} \land x_{n'} \not\equiv x_n$$

$$\Rightarrow$$

$$x_n \not\equiv x_{n'+1}$$

$$\Rightarrow$$

$$p(x_{n'}, args) = p(x_{n'+1}, args) \not= p(x_n, args)$$