Data 621 Homework 3

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Libraries

```
library(tidyverse)
## Warning: package 'tidyverse' was built under R version 4.0.5
## Warning: package 'ggplot2' was built under R version 4.0.5
## Warning: package 'tibble' was built under R version 4.0.5
## Warning: package 'tidyr' was built under R version 4.0.5
## Warning: package 'readr' was built under R version 4.0.5
## Warning: package 'dplyr' was built under R version 4.0.5
## Warning: package 'forcats' was built under R version 4.0.5
library(ggplot2)
library(VIM)
## Warning: package 'VIM' was built under R version 4.0.5
## Warning: package 'colorspace' was built under R version 4.0.5
library(GGally)
## Warning: package 'GGally' was built under R version 4.0.5
library(caret)
## Warning: package 'caret' was built under R version 4.0.5
```

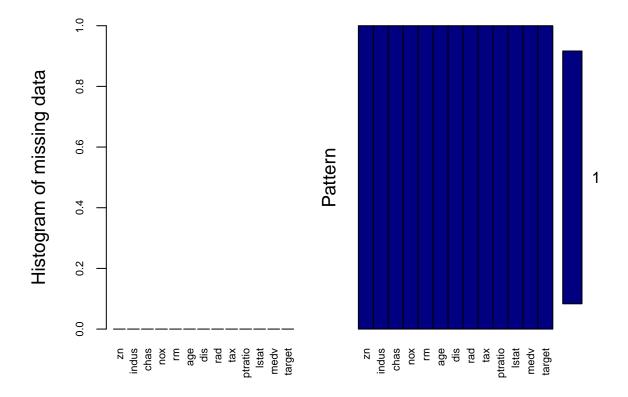
```
library(broom)
```

EDA

```
# Load data
# Training
rawTrain <- read.csv("https://raw.githubusercontent.com/MsQCompSci/Data621Group4/main/HW3/crime-trainin
#Testing data
rawTest <- read.csv("https://raw.githubusercontent.com/MsQCompSci/Data621Group4/main/HW3/crime-evaluati
# check to see if we need to clean the data
# gives us a sense of what each predictor is
glimpse(rawTrain)
## Rows: 466
## Columns: 13
## $ zn
            <dbl> 0, 0, 0, 30, 0, 0, 0, 0, 0, 80, 22, 0, 0, 22, 0, 0, 100, 20, 0~
## $ indus
            <dbl> 19.58, 19.58, 18.10, 4.93, 2.46, 8.56, 18.10, 18.10, 5.19, 3.6~
            ## $ chas
## $ nox
            <dbl> 0.605, 0.871, 0.740, 0.428, 0.488, 0.520, 0.693, 0.693, 0.515,~
## $ rm
            <dbl> 7.929, 5.403, 6.485, 6.393, 7.155, 6.781, 5.453, 4.519, 6.316,~
## $ age
            <dbl> 96.2, 100.0, 100.0, 7.8, 92.2, 71.3, 100.0, 100.0, 38.1, 19.1,~
            <dbl> 2.0459, 1.3216, 1.9784, 7.0355, 2.7006, 2.8561, 1.4896, 1.6582~
## $ dis
            <int> 5, 5, 24, 6, 3, 5, 24, 24, 5, 1, 7, 5, 24, 7, 3, 3, 5, 5, 24, ~
## $ rad
## $ tax
            <int> 403, 403, 666, 300, 193, 384, 666, 666, 224, 315, 330, 398, 66~
## $ ptratio <dbl> 14.7, 14.7, 20.2, 16.6, 17.8, 20.9, 20.2, 20.2, 20.2, 16.4, 19~
           <dbl> 3.70, 26.82, 18.85, 5.19, 4.82, 7.67, 30.59, 36.98, 5.68, 9.25~
## $ 1stat
            <dbl> 50.0, 13.4, 15.4, 23.7, 37.9, 26.5, 5.0, 7.0, 22.2, 20.9, 24.8~
## $ medv
## $ target <int> 1, 1, 1, 0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 0, 0, 0, 1, 1, 1, 1, 0,~
# All varaibles are numeric
# categorical variables
# chas
#dicrete
#rad, zn, tax
#all others are continuous
```

No Missing Values

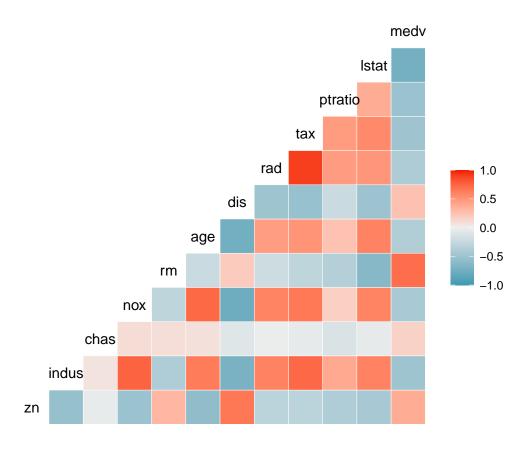
```
#plot missing values using VIM package
aggr(rawTrain , col=c('navyblue','red'), numbers=TRUE, sortVars=TRUE, labels=names(rawTrain), cex.axis=
```



```
##
##
    Variables sorted by number of missings:
##
    Variable Count
##
           zn
##
       indus
                   0
##
         chas
                   0
                   0
##
          nox
##
           rm
                   0
##
                   0
          age
##
          dis
                   0
##
          rad
##
                   0
          tax
##
     ptratio
       lstat
##
                   0
##
        medv
##
       target
                   0
```

Correlation

```
#correlation matrix for predictors
ggcorr(rawTrain%>% select(zn:medv))
```



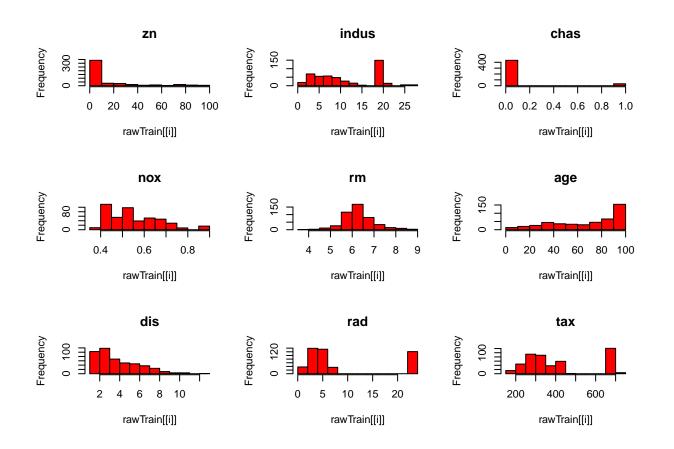
```
## Compare row 2 and column 4 with corr 0.76
## Means: 0.539 vs 0.416 so flagging column 2
## Compare row 4 and column 7 with corr 0.769
## Means: 0.487 vs 0.395 so flagging column 4
## Compare row 9 and column 8 with corr 0.906
## Means: 0.46 vs 0.377 so flagging column 9
## Compare row 6 and column 7 with corr 0.751
## Means: 0.417 vs 0.357 so flagging column 6
## All correlations <= 0.75
## [1] "indus" "nox" "tax" "age"</pre>
```

```
# There are 4 highly correlated variables
# I will drop the highest one which is tax which seems to be the most highly correlated
#tax and rad are 0.9 correlated lets look at their relationship to the predictor to see which one to dr
```

Distribution of Predictors

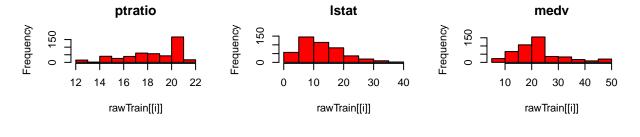
ADD VARIANCE AND INFLATION FACTORS TO THIS SECTION?

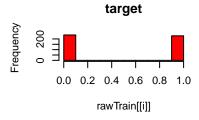
```
par(mfrow = c(3,3))
for(i in 1:ncol(rawTrain)) {#distribution of each variable
  hist(rawTrain[[i]], main = colnames(rawTrain[i]), col = "red")
}
```



indus, tax and rad
#all other variables ar skewed except RM

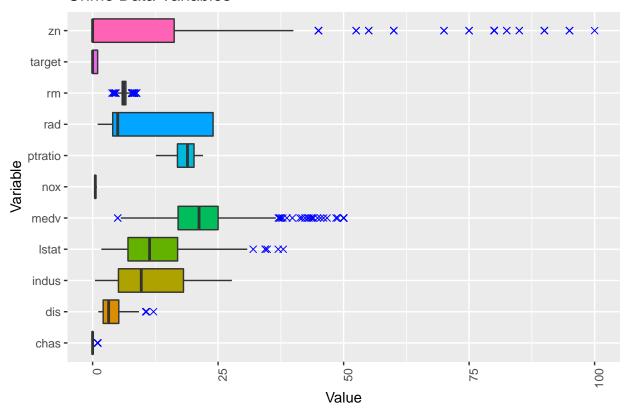
#binomial data





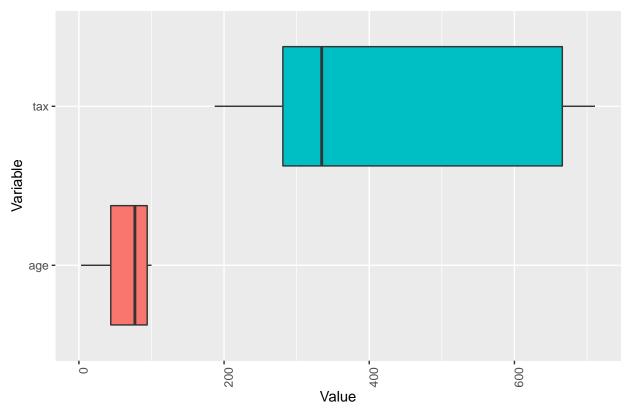
Box Plots

Crime Data Variables



#we can see that zn, medv and lstat has MANY outliers

Crime Data Variables



```
\# no outliers for tax and age
```

Model Building

##

Coefficients:

```
#remove Tax due to high correlation with other variables
modelOne <- glm(target ~ zn + indus + chas + nox + rm + age + dis + rad + ptratio + lstat + medv , data
modelOne

##
## Call: glm(formula = target ~ zn + indus + chas + nox + rm + age + dis +
## rad + ptratio + lstat + medv, family = "binomial", data = train)</pre>
```

```
## (Intercept)
                                 indus
                                               chas
                       zn
                                                            nox
                                                                          rm
##
    -49.98632
                  -0.06821
                                0.01524
                                            1.68171
                                                        62.41402
                                                                     -2.12008
##
          age
                       dis
                                   rad
                                            ptratio
                                                           lstat
                                                                      medv
##
      0.03982
                   1.05296
                                0.74014
                                            0.57939
                                                        -0.02528
                                                                    0.36244
## Degrees of Freedom: 119 Total (i.e. Null); 108 Residual
## Null Deviance:
                       163.6
## Residual Deviance: 50.73
                              AIC: 74.73
#remove Tax squared age and log lstat
modelTwo <- glm(target ~ zn + indus + chas + nox + rm + age^2 + dis + rad + ptratio + log2(lstat) + med
modelTwo
## Call: glm(formula = target ~ zn + indus + chas + nox + rm + age^2 +
      dis + rad + ptratio + log2(lstat) + medv, family = "binomial",
##
      data = train)
##
## Coefficients:
## (Intercept)
                                 indus
                        zn
                                               chas
                                                             nox
                                                                          rm
                                0.02560
    -45.70491
                  -0.07452
                                            1.71374
                                                        63.05722
                                                                     -2.59852
##
                       dis
                                   rad
                                            ptratio log2(lstat)
                                                                        medv
          age
##
      0.04930
                   1.10615
                               0.75558
                                            0.57837
                                                        -0.86561
                                                                    0.36131
##
## Degrees of Freedom: 119 Total (i.e. Null); 108 Residual
## Null Deviance:
                       163.6
## Residual Deviance: 50.29
                               AIC: 74.29
#This one has a litter lower AIC
summary(modelTwo)
##
## Call:
## glm(formula = target ~ zn + indus + chas + nox + rm + age^2 +
      dis + rad + ptratio + log2(lstat) + medv, family = "binomial",
##
      data = train)
##
## Deviance Residuals:
                 1Q
                        Median
                                     3Q
                                              Max
## -1.98060 -0.24172 -0.01038 0.00038
                                          2.51026
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
## (Intercept) -45.70491 19.85879 -2.301 0.02136 *
              -0.07452 0.06833 -1.091 0.27548
## zn
## indus
               0.02560 0.11069 0.231 0.81708
## chas
               1.71374 1.51011 1.135 0.25644
              63.05722 21.23483 2.970 0.00298 **
## nox
## rm
              -2.59852 1.79138 -1.451 0.14690
```

0.04930 0.03390 1.454 0.14584

1.10615 0.55339 1.999 0.04562 *

age

dis

```
## rad
                0.75558
                            0.29663
                                    2.547 0.01086 *
                                    1.979 0.04786 *
                0.57837
                            0.29231
## ptratio
## log2(lstat) -0.86561
                            1.24316 -0.696 0.48624
                 0.36131
## medv
                            0.15789
                                    2.288 0.02212 *
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 163.645 on 119 degrees of freedom
## Residual deviance: 50.286 on 108 degrees of freedom
## AIC: 74.286
## Number of Fisher Scoring iterations: 9
\#log10(zn + 1), log10(dis) and deleted log2(lstat) - not significant
modelThree <- glm(target ~ log10(zn + 1) + indus + chas + nox + rm + age^2 + log10(dis) + rad + ptratio
modelThree
##
## Call: glm(formula = target ~ log10(zn + 1) + indus + chas + nox + rm +
       age^2 + log10(dis) + rad + ptratio + medv, family = "binomial",
##
       data = train)
##
## Coefficients:
##
     (Intercept)
                 log10(zn + 1)
                                         indus
                                                         chas
                                                                         nox
                                       0.05221
##
      -54.26269
                      -0.54972
                                                      1.41733
                                                                    63.80368
                                    log10(dis)
##
              rm
                            age
                                                          rad
                                                                     ptratio
##
       -1.92656
                        0.03476
                                       9.71029
                                                      0.77699
                                                                     0.60580
##
           medv
##
        0.36206
##
## Degrees of Freedom: 119 Total (i.e. Null); 109 Residual
## Null Deviance:
                       163.6
## Residual Deviance: 50.47
                               AIC: 72.47
#AIC is lower again (not sure if age 2 ishelpful)
summary(modelThree)
##
## Call:
## glm(formula = target \sim log10(zn + 1) + indus + chas + nox + rm +
       age^2 + log10(dis) + rad + ptratio + medv, family = "binomial",
##
##
       data = train)
##
## Deviance Residuals:
       Min
                   1Q
                         Median
                                       3Q
                                                Max
## -1.93941 -0.24838 -0.02038
                                0.00033
                                            2.59167
##
## Coefficients:
```

```
## chas
                 1.41733
                           1.50486
                                    0.942 0.34627
## nox
                63.80368 21.05195 3.031 0.00244 **
## rm
                -1.92656 1.51643 -1.270 0.20392
                          0.02594
                                    1.340 0.18025
## age
                 0.03476
## log10(dis)
                9.71029
                           4.81949 2.015 0.04393 *
                 ## rad
## ptratio
                 0.60580
                           0.30629 1.978 0.04794 *
                            0.15616 2.318 0.02042 *
## medv
                 0.36206
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 163.645 on 119 degrees of freedom
## Residual deviance: 50.466 on 109 degrees of freedom
## AIC: 72.466
##
## Number of Fisher Scoring iterations: 9
#combine rad and rm (multiplied) - they seemed to correspond in their distributions
modelFour<- glm(target ~ log10(zn + 1) + indus + chas + nox + age^2 + log10(dis) + rad*rm + ptratio +
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
modelFour
##
## Call: glm(formula = target ~ log10(zn + 1) + indus + chas + nox + age^2 +
      log10(dis) + rad * rm + ptratio + medv, family = "binomial",
      data = train)
##
##
## Coefficients:
##
    (Intercept) log10(zn + 1)
                                      indus
                                                      chas
                                                                     nox
##
      -39.69026
                     -0.39952
                                    0.05430
                                                   0.92790
                                                                80.55149
##
                   log10(dis)
                                        rad
                                                                 ptratio
            age
                                                       rm
                                                  -7.99103
##
        0.05098
                     11.14932
                                    -3.50163
                                                                 0.90573
##
           medv
                       rad:rm
##
        0.60249
                      0.72035
## Degrees of Freedom: 119 Total (i.e. Null); 108 Residual
## Null Deviance:
                      163.6
## Residual Deviance: 40.73
                              AIC: 64.73
#AIC is lower #Not sure what the rationale is for this working but it lowered the AIC number and Resid
summary(modelFour)
```

Estimate Std. Error z value Pr(>|z|)

0.10752 0.486 0.62725

(Intercept) -54.26269 19.75958 -2.746 0.00603 **
log10(zn + 1) -0.54972 0.96504 -0.570 0.56892

0.05221

##

##

indus

```
## Call:
## glm(formula = target \sim log10(zn + 1) + indus + chas + nox + age^2 +
      log10(dis) + rad * rm + ptratio + medv, family = "binomial",
      data = train)
##
## Deviance Residuals:
                        Median
                 10
                                      30
                                               Max
## -2.24476 -0.14203 -0.00414 0.00482
                                           2.05517
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
                           19.76088 -2.009 0.04459 *
## (Intercept)
                -39.69026
## log10(zn + 1) -0.39952
                             1.23407 -0.324 0.74613
## indus
                                      0.435 0.66375
                  0.05430
                           0.12491
## chas
                  0.92790
                           1.63062
                                       0.569 0.56933
## nox
                 80.55149
                            25.80599
                                       3.121 0.00180 **
## age
                           0.02896
                                       1.760 0.07834 .
                  0.05098
## log10(dis)
                 11.14932
                             5.21051
                                      2.140 0.03237 *
                             1.26718 -2.763 0.00572 **
## rad
                 -3.50163
## rm
                 -7.99103
                             3.14895 -2.538 0.01116 *
## ptratio
                  0.90573
                             0.37792
                                       2.397 0.01655 *
## medv
                  0.60249
                             0.22238
                                       2.709 0.00674 **
## rad:rm
                 0.72035
                             0.25034
                                       2.877 0.00401 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 163.645 on 119 degrees of freedom
## Residual deviance: 40.734 on 108 degrees of freedom
## AIC: 64.734
##
## Number of Fisher Scoring iterations: 9
#delte indus
modelFive<-glm(target ~ log10(zn+1)+ nox + age^2 + log10(dis) + rad*rm + ptratio + medv, data = train
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
modelFive
##
## Call: glm(formula = target \sim log10(zn + 1) + nox + age^2 + log10(dis) +
      rad * rm + ptratio + medv, family = "binomial", data = train)
##
##
## Coefficients:
##
    (Intercept)
                log10(zn + 1)
                                                                 log10(dis)
                                          nox
                                                         age
                                                                   10.66210
##
      -36.53958
                     -0.47587
                                     81.22921
                                                     0.05416
##
                                                                    rad:rm
            rad
                            rm
                                      ptratio
                                                        medv
##
                                      0.85851
                                                                    0.75086
       -3.65291
                      -8.36956
                                                     0.61188
##
## Degrees of Freedom: 119 Total (i.e. Null); 110 Residual
## Null Deviance:
                       163.6
## Residual Deviance: 41.49
                              AIC: 61.49
```

```
#AIC is higher #resiudal deviance is lower
# I looked at the histograms and looked for complementary shapes to decide what to multiply
```

Variable importance

##

```
summary(modelFive)
##
## Call:
## glm(formula = target \sim log10(zn + 1) + nox + age^2 + log10(dis) +
      rad * rm + ptratio + medv, family = "binomial", data = train)
##
## Deviance Residuals:
                                   3Q
                 1Q
                      Median
                                           Max
## -2.37810 -0.16278 -0.00419 0.00439
                                       1.97419
## Coefficients:
                Estimate Std. Error z value Pr(>|z|)
## (Intercept) -36.53958 16.42367 -2.225 0.02609 *
## log10(zn + 1) -0.47587 1.25809 -0.378 0.70524
## nox
              81.22921 24.73815 3.284 0.00103 **
## age
               0.05416 0.02809 1.928 0.05389 .
## log10(dis) 10.66210 4.89514 2.178 0.02940 *
## rad
               -3.65291 1.30703 -2.795 0.00519 **
## rm
               -8.36956 3.06969 -2.727 0.00640 **
## ptratio
               0.85851 0.35989 2.385 0.01706 *
## medv
                ## rad:rm
               ## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 163.645 on 119 degrees of freedom
## Residual deviance: 41.495 on 110 degrees of freedom
## AIC: 61.495
## Number of Fisher Scoring iterations: 9
#indus and zn are not important
#multiply ptratio*nox (remove squared from age)
modelSix<- glm(target ~ log10(zn + 1) + age + ptratio*nox + log10(dis) + rad*rm + medv, data = train,
## Warning: glm.fit: fitted probabilities numerically 0 or 1 occurred
modelSix
```

```
## Call: glm(formula = target ~ log10(zn + 1) + age + ptratio * nox +
##
       log10(dis) + rad * rm + medv, family = "binomial", data = train)
##
## Coefficients:
##
     (Intercept) log10(zn + 1)
                                                      ptratio
                                                                         nox
                                           age
##
      -50.42921
                     -0.48978
                                                      1.58424
                                                                   105.27247
                                       0.05554
##
     log10(dis)
                            rad
                                            rm
                                                         medv
                                                                 ptratio:nox
                       -3.59743
                                      -8.29831
##
                                                      0.61232
        10.68244
                                                                    -1.31047
##
          rad:rm
##
         0.74144
##
## Degrees of Freedom: 119 Total (i.e. Null); 109 Residual
## Null Deviance:
                        163.6
## Residual Deviance: 41.42
                                AIC: 63.42
```

#AIC is lower

summary(modelSix)

```
##
## Call:
## glm(formula = target ~ log10(zn + 1) + age + ptratio * nox +
##
      log10(dis) + rad * rm + medv, family = "binomial", data = train)
##
## Deviance Residuals:
       Min
                  10
                        Median
                                      3Q
                                               Max
                                           1.98426
## -2.34744 -0.15485 -0.00417
                               0.00479
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                -50.42921 55.18900 -0.914 0.36085
## log10(zn + 1) -0.48978
                            1.29626 -0.378 0.70555
                             0.02869
                                       1.936 0.05291 .
## age
                  0.05554
## ptratio
                  1.58424
                            2.76305
                                      0.573 0.56640
## nox
                                      1.106 0.26889
                105.27247
                            95.21624
## log10(dis)
                 10.68244
                            4.93429
                                       2.165 0.03039 *
## rad
                 -3.59743
                             1.32868 -2.708 0.00678 **
## rm
                             3.11600 -2.663 0.00774 **
                 -8.29831
## medv
                 0.61232
                             0.21790
                                       2.810 0.00495 **
                             4.92343 -0.266 0.79011
## ptratio:nox
                 -1.31047
## rad:rm
                  0.74144
                             0.26133
                                       2.837 0.00455 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 163.645 on 119 degrees of freedom
## Residual deviance: 41.421 on 109 degrees of freedom
## AIC: 63.421
##
## Number of Fisher Scoring iterations: 9
```

Test Models

```
#Make predictions
predOne = predict(modelOne,test, type = "response")
predTwo = predict(modelTwo,test, type = "response")
predThree = predict(modelThree,test, type = "response")
predFour = predict(modelFour,test, type = "response")
predFive = predict(modelFive,test, type = "response")
predSix = predict(modelSix,test, type = "response")
#Error Measures
data.frame(modelOne = postResample(pred = predOne, obs = test$target), modelTwo = postResample(pred = p
##
            modelOne modelTwo modelThree modelFour modelFive modelSix
           0.2787735 0.2791040 0.2725896 0.2868524 0.2814246 0.2796029
## Rsquared 0.6950779 0.6948205 0.7076774 0.6806475 0.6914870 0.6952936
## MAE
          0.1253909 0.1253186 0.1218843 0.1217098 0.1197176 0.1185218
#We can see RMSE is increasing which means the fit is better for every model - This doesnt reflect very
```

Confusion Matrix and Accuracy Measurment

```
#Extract Accuracy
#Model One
#format predictions to binary
resultsFitOne <- ifelse(predOne > 0.5,1,0)
resultsFitOne <- as.factor(resultsFitOne)</pre>
#Confusion Matrix to Extract Accuracy
cOne <- confusionMatrix(as.factor(test$target),resultsFitOne)</pre>
accOne <- as.data.frame(cOne$overall)[1]</pre>
accOne<- accOne %>%
  slice(1)
#Model Two
#format predictions to binary
resultsFitTwo <- ifelse(predTwo > 0.5,1,0)
resultsFitTwo <- as.factor(resultsFitTwo)</pre>
#Confusion Matrix to Extract Accuracy
cTwo <- confusionMatrix(resultsFitTwo, as.factor(test$target))</pre>
accTwo <- as.data.frame(cTwo$overall)[1]</pre>
accTwo<- accTwo %>%
 slice(1)
#Model Three
#format predictions to binary
```

```
resultsFitThree<- ifelse(predThree > 0.5,1,0)
resultsFitThree <- as.factor(resultsFitThree)</pre>
#Confusion Matrix to Extract Accuracy
cThree <- confusionMatrix(resultsFitThree, as.factor(test$target))</pre>
accThree <- as.data.frame(cThree$overall)[1]</pre>
accThree<- accThree%>%
 slice(1)
#Model Four
#format predictions to binary
resultsFitFour<- ifelse(predFour > 0.5,1,0)
resultsFitFour <- as.factor(resultsFitFour)</pre>
#Confusion Matrix to Extract Accuracy
cFour <- confusionMatrix(resultsFitFour, as.factor(test$target))</pre>
accFour <- as.data.frame(cFour$overall)[1]</pre>
accFour<- accFour%>%
 slice(1)
#Model Five
#format predictions to binary
resultsFitFive<- ifelse(predFive > 0.5,1,0)
resultsFitFive <- as.factor(resultsFitFive)</pre>
#Confusion Matrix to Extract Accuracy
cFive <- confusionMatrix(resultsFitFive, as.factor(test$target))
accFive <- as.data.frame(cFive$overall)[1]</pre>
accFive<- accFive%>%
 slice(1)
#Model Six
#format predictions to binary
resultsFitSix<- ifelse(predSix > 0.5,1,0)
resultsFitSix <- as.factor(resultsFitSix)</pre>
#Confusion Matrix to Extract Accuracy
cSix<- confusionMatrix(resultsFitSix, as.factor(test$target))</pre>
accSix <- as.data.frame(cSix$overall)[1]</pre>
accSix<- accSix%>%
slice(1)
#create a table with accuracies
data.frame(c(accOne, accTwo, accThree, accFour,accFive, accSix))
##
     cOne.overall cTwo.overall cThree.overall cFour.overall cFive.overall
## 1
        0.8843931
                     0.8815029
                                   0.8959538
                                                    0.8901734
                                                                   0.8988439
##
   cSix.overall
## 1
        0.9017341
```

#Here we see that our best models are Five and Six in terms of accuracy

WE NEED QQ PLOTS OR SOME OTHER VISUAL TO HELP US TALK ABOUT GOODNESS OF FIT GETTING HIGHER ALTHOUGH THE ACCURACY IS NOT CHANGING SO WE CAN CHOOSE ONE (FIVE OR SIX)

AUC or ROC curve