### Data 621 - Homework 4

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### 11/21/2021

### Overview

In this homework assignment, you will explore, analyze and model a data set containing approximately 8000 records representing a customer at an auto insurance company. Each record has two response variables. The first response variable, TARGET\_FLAG, is a 1 or a 0. A "1" means that the person was in a car crash. A zero means that the person was not in a car crash. The second response variable is TARGET\_AMT. This value is zero if the person did not crash their car. But if they did crash their car, this number will be a value greater than zero.

Your objective is to build multiple linear regression and binary logistic regression models on the training data to predict the probability that a person will crash their car and also the amount of money it will cost if the person does crash their car. You can only use the variables given to you (or variables that you derive from the variables provided). Below is a short description of the variables of interest in the data set:

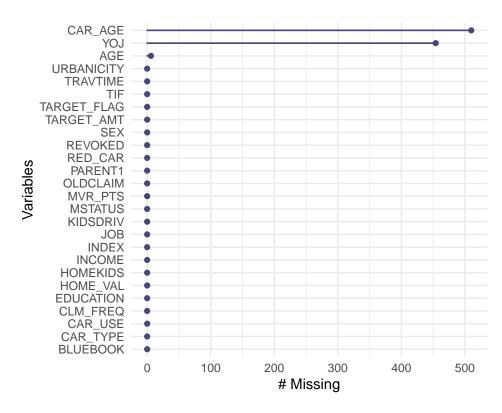
### **Exploratory Data Analysis**

Below is a glimpse of the Insurance Training data.

```
## Rows: 8,161
## Columns: 26
        $ INDEX
                                                  <int> 1, 2, 4, 5, 6, 7, 8, 11, 12, 13, 14, 15, 16, 17, 19, 20, 2~
        $ TARGET_FLAG <int> 0, 0, 0, 0, 0, 1, 0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 0, 0, 0, 1~
        $ TARGET AMT
                                                  <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 2946.000, 0.000, 4021.0~
        $ KIDSDRIV
                                                  <int> 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0~
                                                  <int> 60, 43, 35, 51, 50, 34, 54, 37, 34, 50, 53, 43, 55, 53, 45~
## $ AGE
        $ HOMEKIDS
                                                  <int> 0, 0, 1, 0, 0, 1, 0, 2, 0, 0, 0, 0, 0, 0, 3, 0, 3, 2, 1~
                                                  <int> 11, 11, 10, 14, NA, 12, NA, NA, 10, 7, 14, 5, 11, 11, 0, 1~
##
        $ YOJ
                                                  <chr> "$67,349", "$91,449", "$16,039", "", "$114,986", "$125,301~
        $ INCOME
                                                  <chr> "No", "No", "No", "No", "Yes", "No", "No",
       $ PARENT1
                                                  <chr> "$0", "$257,252", "$124,191", "$306,251", "$243,925", "$0"~
        $ HOME VAL
## $ MSTATUS
                                                  <chr> "z_No", "z_No", "Yes", "Yes", "Yes", "z_No", "Yes", "Yes", "
                                                  <chr> "M", "M", "z_F", "M", "z_F", "z_F", "z_F", "M", "z_F", "M"~
       $ SEX
                                                  <chr> "PhD", "z_High School", "z_High School", "<High School", "~
## $ EDUCATION
                                                  <chr> "Professional", "z_Blue Collar", "Clerical", "z_Blue Colla~
       $ JOB
                                                  <int> 14, 22, 5, 32, 36, 46, 33, 44, 34, 48, 15, 36, 25, 64, 48,~
## $ TRAVTIME
       $ CAR USE
                                                  <chr> "Private", "Commercial", "Private", "Private", "Private", ~
## $ BLUEBOOK
                                                  <chr> "$14,230", "$14,940", "$4,010", "$15,440", "$18,000", "$17~
                                                  <int> 11, 1, 4, 7, 1, 1, 1, 1, 7, 1, 7, 7, 6, 1, 6, 6, 7, 4, ~
##
        $ TIF
                                                  <chr> "Minivan", "Minivan", "z_SUV", "Minivan", "z_SUV", "Sports~
## $ CAR_TYPE
## $ RED CAR
                                                  <chr> "yes", "yes", "no", "yes", "no", "no", "no", "yes", "no", ~
                                                  <chr> "$4,461", "$0", "$38,690", "$0", "$19,217", "$0", "$0", "$~
## $ OLDCLAIM
       $ CLM_FREQ
                                                  <int> 2, 0, 2, 0, 2, 0, 0, 1, 0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 2~
                                                  <chr> "No", "No", "No", "Yes", "No", "Yes", "No", "Yes", "No", "No
        $ REVOKED
                                                  <int> 3, 0, 3, 0, 3, 0, 10, 0, 1, 0, 0, 3, 3, 3, 0, 0, 0, 0, ~
## $ MVR_PTS
                                                  <int> 18, 1, 10, 6, 17, 7, 1, 7, 1, 17, 11, 1, 9, 10, 5, 13, 16,~
## $ CAR AGE
                                                  <chr> "Highly Urban/ Urban", "Highly Urban/ Urban", "Highly Urba~
## $ URBANICITY
```

There are 8161 observations in this data set and 26 columns. We know that INDEX, TARGET\_FLAG and TARGET\_AMT are not predictor variables. This gives us 8161 observations with 23 predictors that are a combination of int, double and character data types. We also see that the character variables will have to converted to factors in order for us to explore their distributions. Variables such and INCOME, HOME\_VAL, BLUEBOOK, OLDCLAIM will be converted to numeric because they are numbers with values that have meaning in their hierarchy.

### Missing Values



There are missing variables in the columns Car\_AGE, AGE and YOJ. None of these exceed the 10% missing data so we will continue with all variables for noe (not dropping any of them due to missing data)

### DATA CLEANING - CONVERTING DATA TYPES

- Let's remove the \$, z\_, and , and put in a different variable name from numeric strings.
- Let's also change all other character variables into factors.

Let's glimpse the data to confirm the data cleaning.

```
## Rows: 8,161
  Columns: 26
  $ INDEX
                <int> 1, 2, 4, 5, 6, 7, 8, 11, 12, 13, 14, 15, 16, 17, 19, 20, 2~
  $ TARGET_FLAG <fct> 0, 0, 0, 0, 0, 1, 0, 1, 1, 0, 1, 0, 0, 1, 1, 0, 0, 0, 0, 1~
                <dbl> 0.000, 0.000, 0.000, 0.000, 0.000, 2946.000, 0.000, 4021.0~
  $ TARGET_AMT
  $ KIDSDRIV
                <int> 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0 ~
  $ AGE
                <int> 60, 43, 35, 51, 50, 34, 54, 37, 34, 50, 53, 43, 55, 53, 45~
##
                <int> 0, 0, 1, 0, 0, 1, 0, 2, 0, 0, 0, 0, 0, 0, 0, 3, 0, 3, 2, 1~
  $ HOMEKIDS
                <int> 11, 11, 10, 14, NA, 12, NA, NA, 10, 7, 14, 5, 11, 11, 0, 1~
## $ YOJ
## $ INCOME
                <dbl> 67349, 91449, 16039, NA, 114986, 125301, 18755, 107961, 62~
                $ PARENT1
  $ HOME VAL
                <dbl> 0, 257252, 124191, 306251, 243925, 0, NA, 333680, 0, 0, 0,~
## $ MSTATUS
                <fct> No, No, Yes, Yes, Yes, No, Yes, Yes, No, No, No, Yes, Yes,~
## $ SEX
                <fct> M, M, F, M, F, F, F, M, F, M, F, F, M, M, F, F, M, F, F, F~
```

```
## $ EDUCATION
                <fct> PhD, High School, High School, <High School, PhD, Bachelor~
## $ JOB
                 <fct> Professional, Blue Collar, Clerical, Blue Collar, Doctor, ~
## $ TRAVTIME
                 <int> 14, 22, 5, 32, 36, 46, 33, 44, 34, 48, 15, 36, 25, 64, 48,~
                 <fct> Private, Commercial, Private, Private, Private, Commercial~
## $ CAR_USE
                 <dbl> 14230, 14940, 4010, 15440, 18000, 17430, 8780, 16970, 1120~
## $ BLUEBOOK
                 <int> 11, 1, 4, 7, 1, 1, 1, 1, 7, 1, 7, 7, 6, 1, 6, 6, 7, 4, ~
## $ TIF
## $ CAR_TYPE
                 <fct> Minivan, Minivan, SUV, Minivan, SUV, Sports Car, SUV, Van,~
                 <fct> yes, yes, no, yes, no, no, no, yes, no, no, no, no, yes, y~
## $ RED_CAR
                 <dbl> 4461, 0, 38690, 0, 19217, 0, 0, 2374, 0, 0, 0, 0, 5028, 0,~
## $ OLDCLAIM
                 <int> 2, 0, 2, 0, 2, 0, 0, 1, 0, 0, 0, 0, 2, 0, 0, 0, 0, 0, 2~
## $ CLM FREQ
                 <fct> No, No, No, No, Yes, No, No, Yes, No, No, No, No, Yes, No,~
## $ REVOKED
                 <int> 3, 0, 3, 0, 3, 0, 10, 0, 1, 0, 0, 3, 3, 3, 0, 0, 0, 0, ~
## $ MVR PTS
## $ CAR_AGE
                 <int> 18, 1, 10, 6, 17, 7, 1, 7, 1, 17, 11, 1, 9, 10, 5, 13, 16,~
## $ URBANICITY
                <fct> Highly Urban/ Urban, Highly Urban/ Urban, Highly Urban/ Ur~
```

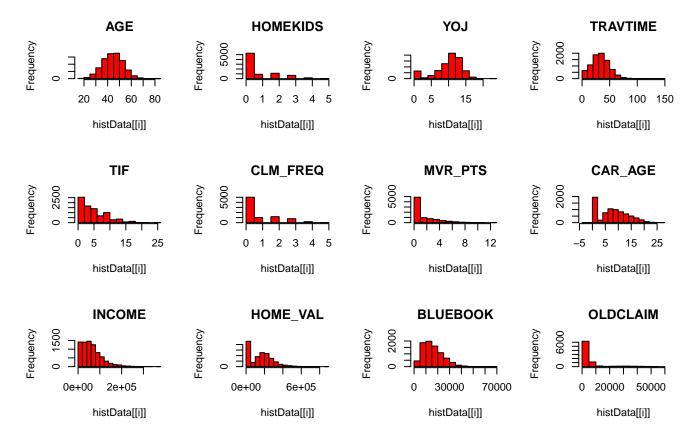
Display summary statistics again to confirm data cleaning.

##	INDEX	TARGET_FLAG T	ARGET_AMT	KIDSDRIV	AGE
##	Min. : 1	0:6008 Min	_	Min. :0.0000	Min. :16.00
##	1st Qu.: 2559		Qu.: 0	1st Qu.:0.0000	1st Qu.:39.00
##	Median: 5133		ian: 0	Median :0.0000	
##	Mean : 5152	Mea		Mean :0.1711	
##	3rd Qu.: 7745		Qu.: 1036	3rd Qu.:0.0000	
##	Max. :10302	Max	•	Max. :4.0000	•
##	11dx10002	nax	107000	11dA: .1.0000	NA's :6
##	HOMEKIDS	YOJ	INCOME	PARENT1	HOME_VAL
##	Min. :0.0000		Min. :	0 No :7084	Min. : 0
##	1st Qu.:0.0000		1st Qu.: 280		1st Qu.: 0
##	Median :0.0000	•	Median : 540		Median :161160
##	Mean :0.7212		Mean : 618		Mean :154867
##	3rd Qu.:1.0000		3rd Qu.: 859		3rd Qu.:238724
##	Max. :5.0000		Max. :3670		Max. :885282
##	Max5.0000	NA's :454	NA's :445	.50	NA's :464
##	MSTATUS SEX		ATION	JOB	TRAVTIME
##	No :3267 F:43		_	Collar :1825	Min. : 5.00
##	Yes:4894 M:3	•		rical :1271	1st Qu.: 22.00
##	100.1001 11.0	High School		essional:1117	Median : 33.00
##		Masters		ger : 988	Mean : 33.49
##		PhD	: 728 Lawy	_	3rd Qu.: 44.00
##		1 112	Stud		Max. :142.00
##			(Oth		
##	CAR_USE	BLUEB00K	TIF		AR_TYPE
##	Commercial:302	9 Min. : 1500	Min. : 1	.000 Minivan	:2145
##	Private :513	2 1st Qu.: 9280	1st Qu.: 1	.000 Panel Tr	uck: 676
##		Median :14440	Median : 4	.000 Pickup	:1389
##		Mean :15710	Mean : 5	.351 Sports C	ar : 907
##		3rd Qu.:20850	3rd Qu.: 7	.000 SUV	:2294
##		Max. :69740	Max. :25	.000 Van	: 750
##					
##	RED_CAR	OLDCLAIM C	LM_FREQ	REVOKED M	VR_PTS
##	no:5783 Min	. : 0 Min.	:0.0000	No :7161 Min.	: 0.000
##	yes:2378 1st	Qu.: 0 1st	Qu.:0.0000	Yes:1000 1st	Qu.: 0.000
##	Med	ian: O Medi	an :0.0000	Medi	an : 1.000
##	Mean	n : 4037 Mean	:0.7986	Mean	: 1.696
##	3rd	Qu.: 4636 3rd	Qu.:2.0000	3rd	Qu.: 3.000
##	Max	. :57037 Max.	:5.0000	Max.	:13.000
##					
##	CAR_AGE		URBANICITY		
##	Min. :-3.000	Highly Rural/	Rural:1669		
##	1st Qu.: 1.000	Highly Urban/	Urban:6492		

## Median: 8.000 ## Mean: 8.328 ## 3rd Qu::12.000 ## Max.:28.000 ## NA's:510

We get a better sense of the information available in each variable now with the data type changes.

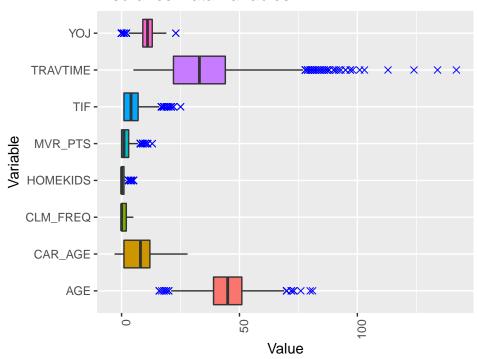
Let's plot the distribution of the numerical variables using histograms.



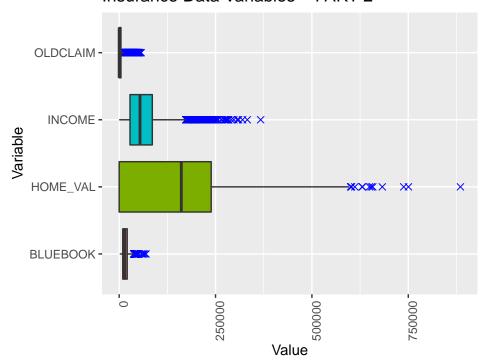
From the above histagrams of numerical data we can see that most numerical variables have a right skew, which may indicate that a transformation will be helpful for these variables.

Let's identify the variables with outlier values using boxplots.

### Insurance Data Variables - PART 1



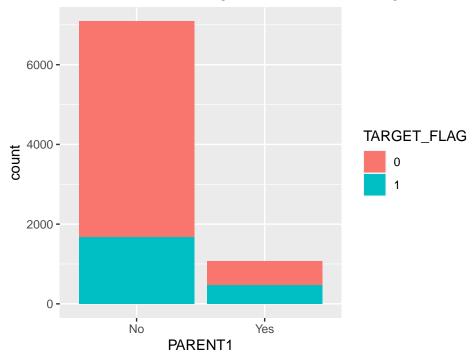
### Insurance Data Variables - PART 2



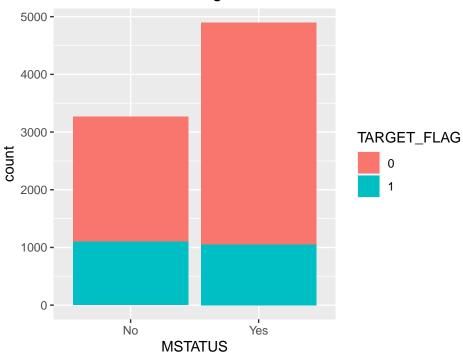
From these initial box plots we can see that there are some outliers. In particular, TRAVTIME, INCOME, and HOME\_VAL have many outliers which are spread out more compared to the other variables.

### Categorical Predictors - with target variable

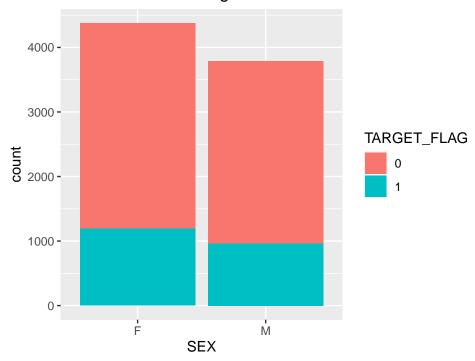
# Insurance Data Categorical Variables - Single Parent (I



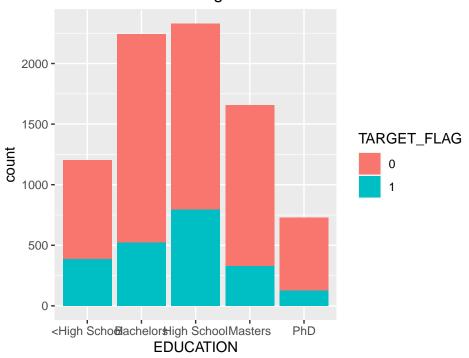
# Insurance Data Categorical Variables - Marital Status



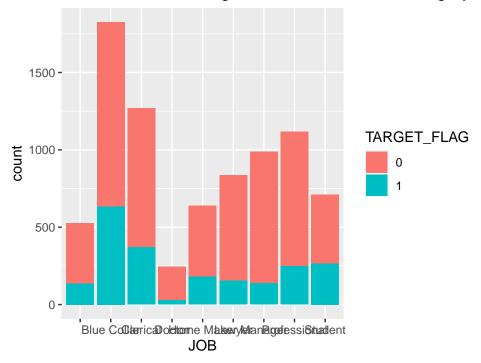
# Insurance Data Categorical Variables - SEX



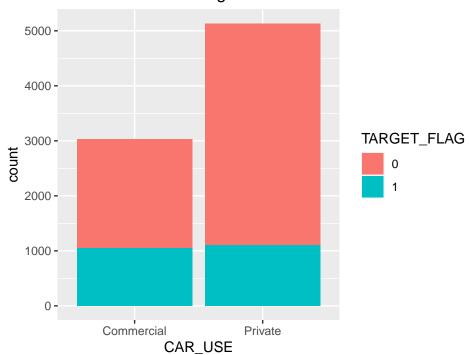
# Insurance Data Categorical Variables - Max Education



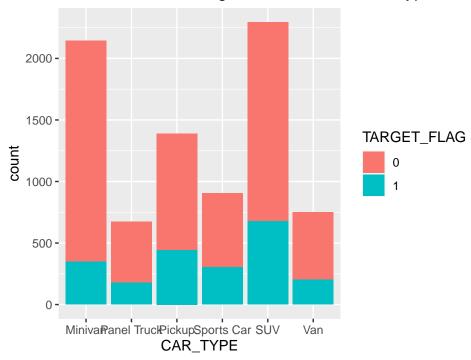
# Insurance Data Categorical Variables – Job Category



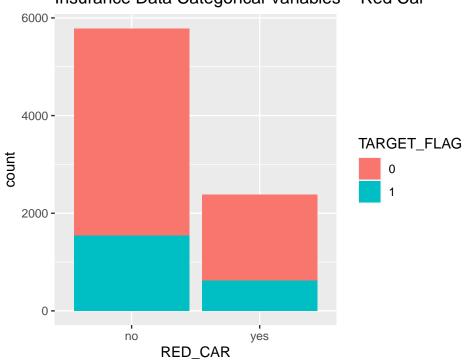
# Insurance Data Categorical Variables - Vehicle Use



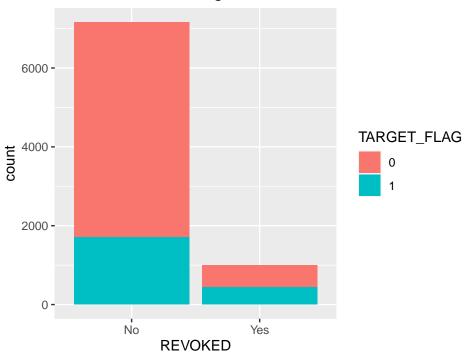
# Insurance Data Categorical Variables - Car Type



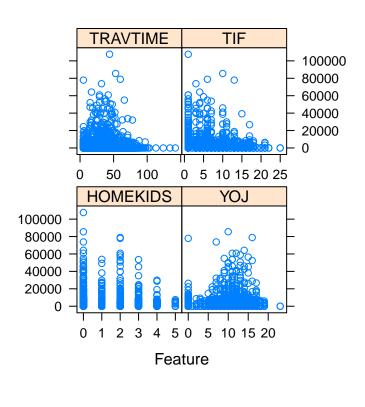
# Insurance Data Categorical Variables - Red Car

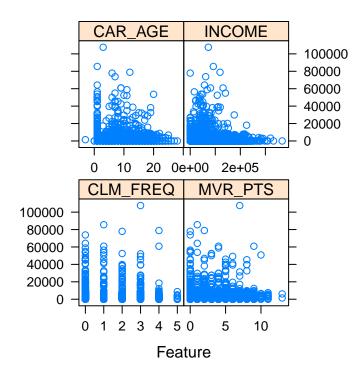


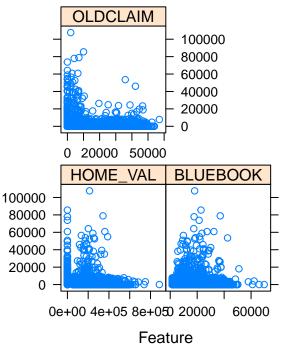
# Insurance Data Categorical Variables – Licensed Revol



### Numeric Data - Relationship to Target

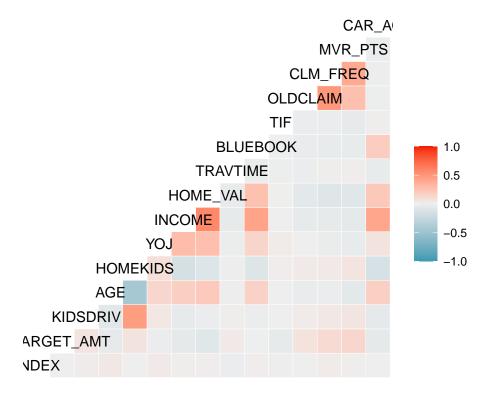






### Correlation

Let's use a heat map to see the level of correlation of the numeric predictor variables.



Let's check if there are any highly correlated variables (correlation higher than 0.75) and drop them if necessary.

```
## All correlations <= 0.75
## character(0)</pre>
```

### **Data Preparation**

### **Data Cleaning**

- Missing values are handled by imputing them as follows:
  - Use the mean to impute missing values for Age and YOJ.
  - Use the median to impute missing values for HOME\_VAL, INCOME, and CAR\_AGE.
- Outlier values non-factor variables are being normalized.

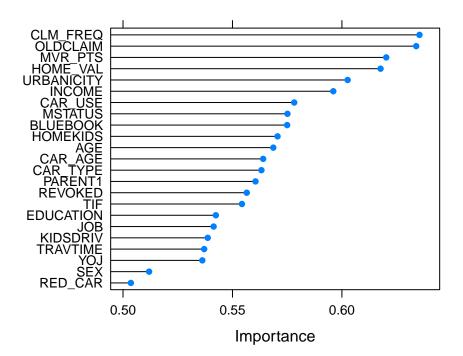
### Variable Importance

To determine the variable importance the following steps were taken:

- A training data frame prepTrainA was prepared for the TARGET\_FLAG response variable and its associated predictor variables.
- A training data frame prepTrainB was prepared for the TARGET\_AMT response variable and its associated predictor variables.
- Using the prepTrainA data frame, a classification model modelA was trained using the Learning Vector Quantization (1vq) method. From it, the variable importance was summarized and plotted.

```
## ROC curve variable importance
##
## Importance
## CLM_FREQ 0.6354
```

```
## OLDCLAIM
                   0.6339
## MVR_PTS
                   0.6202
## HOME_VAL
                   0.6176
  URBANICITY
                   0.6026
##
  INCOME
                   0.5961
  CAR_USE
                   0.5782
## MSTATUS
                   0.5751
  BLUEBOOK
                   0.5750
## HOMEKIDS
                   0.5706
  AGE
                   0.5686
## CAR_AGE
                   0.5640
  CAR_TYPE
                   0.5632
## PARENT1
                   0.5605
  REVOKED
                   0.5565
  TIF
                   0.5543
##
  EDUCATION
                   0.5424
##
##
  JOB
                   0.5414
  KIDSDRIV
                   0.5387
  TRAVTIME
                   0.5371
##
  YOJ
                   0.5362
## SEX
                   0.5119
## RED_CAR
                   0.5036
```

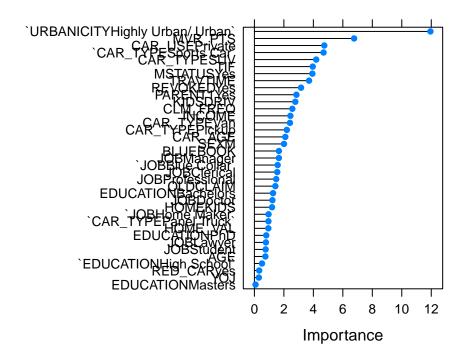


According to the plots above, we can predict which variables would contribute best to the categorical predictions for TARGET\_FLAG. We can use this to inform our data transformations.

• Using the prepTrainB data frame, a classification/regression model modelB was trained using the Generalized Linear Model (glm) method. From it, the variable importance was summarized and plotted.

```
## glm variable importance
##
## only 23 most important variables shown (out of 37)
##
## Overall
## 'URBANICITYHighly Urban/ Urban' 11.944
```

##	MVR_PTS	6.764
##	CAR_USEPrivate	4.741
##	'CAR_TYPESports Car'	4.692
##	CAR_TYPESUV	4.193
##	TIF	3.958
##	MSTATUSYes	3.932
##	TRAVTIME	3.708
##	REVOKEDYes	3.166
##	PARENT1Yes	2.852
##	KIDSDRIV	2.776
##	CLM_FREQ	2.574
##	INCOME	2.441
##	CAR_TYPEVan	2.413
##	CAR_TYPEPickup	2.200
##	CAR_AGE	2.096
##	SEXM	2.007
##	BLUEBOOK	1.663
##	JOBManager	1.660
##	'JOBBlue Collar'	1.578
##	JOBClerical	1.550
##	JOBProfessional	1.478
##	OLDCLAIM	1.420



According to the plots above, we can predict which variables would contribute best to the numerical predictions for TARGET\_AMT. We can use this to inform our data transformations.

### Train Test Split

We partition the training data in two data sets. One to be used for training purposes and one for validation/testing purposes.

### Models

Using the training data set, build at least two different multiple linear regression models and three different binary logistic regression models, using different variables (or the same variables with different transformations). You may select the variables

manually, use an approach such as Forward or Stepwise, use a different approach such as trees, or use a combination of techniques. Describe the techniques you used. If you manually selected a variable for inclusion into the model or exclusion into the model, indicate why this was done.

Discuss the coefficients in the models, do they make sense? For example, if a person has a lot of traffic tickets, you would reasonably expect that person to have more car crashes. If the coefficient is negative (suggesting that the person is a safer driver), then that needs to be discussed. Are you keeping the model even though it is counter intuitive? Why? The boss needs to know.

### **Binary Logistic Regression**

### Binary Logistic Regression Model 1

For this model, we only include the predictor variables that have theoretical effect on probability of collition, which was provided as part of the definition of the variables.

Additionally, we remove the variables that were deemed as

- "urban legends", such as RED\_CAR and SEX.
- having a theoretical "unknown effect" on probability of collision, such as EDUCATION.

Also, from our importance variable model importanceA, we know that the variables RED\_CAR and SEX ranked in the bottom 2 items of the importance list of 23 items. Hence, we don't include them.

```
##
## Call:
  glm(formula = TARGET_FLAG ~ AGE + CAR_USE + CLM_FREQ + HOME VAL +
##
      INCOME + JOB + KIDSDRIV + MSTATUS + MVR_PTS + REVOKED + TIF +
##
      TRAVTIME + YOJ, family = binomial(link = "logit"), data = train)
##
## Deviance Residuals:
##
      Min
                1Q
                     Median
                                  3Q
                                          Max
##
  -2.0607
           -0.7577
                    -0.5370
                              0.8177
                                       2.8031
##
## Coefficients:
##
                    Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                  -6.265e-02 2.593e-01 -0.242 0.809111
## AGE
                  -1.202e-02 3.727e-03 -3.225 0.001258 **
## CAR USEPrivate -5.537e-01 7.862e-02 -7.043 1.88e-12 ***
## CLM FREQ
                   2.581e-01 2.677e-02
                                         9.641 < 2e-16 ***
## HOME_VAL
                  -1.327e-06 3.610e-07 -3.675 0.000238 ***
## INCOME
                  -4.107e-06 1.080e-06 -3.804 0.000143 ***
## JOBBlue Collar
                   2.759e-01 1.452e-01
                                         1.900 0.057447 .
## JOBClerical
                   1.945e-01 1.690e-01
                                         1.151 0.249816
## JOBDoctor
                  -2.060e-01 2.650e-01 -0.777 0.436982
## JOBHome Maker
                   4.789e-02 2.004e-01
                                          0.239 0.811094
## JOBLawyer
                   1.522e-02 1.784e-01
                                          0.085 0.932011
## JOBManager
                  -4.282e-01 1.715e-01 -2.496 0.012546 *
## JOBProfessional 3.635e-02 1.598e-01
                                          0.227 0.820111
## JOBStudent
                   2.181e-02 1.899e-01
                                          0.115 0.908548
## KIDSDRIV
                   3.511e-01 5.551e-02
                                          6.324 2.54e-10 ***
## MSTATUSYes
                  -5.051e-01 7.465e-02 -6.765 1.33e-11 ***
                   1.374e-01 1.435e-02
                                          9.579 < 2e-16 ***
## MVR PTS
## REVOKEDYes
                   7.957e-01 8.529e-02
                                          9.329 < 2e-16 ***
## TIF
                  -5.016e-02 7.687e-03 -6.525 6.78e-11 ***
## TRAVTIME
                   6.508e-03 1.903e-03
                                         3.420 0.000625 ***
## YOJ
                  -9.587e-03 8.753e-03 -1.095 0.273386
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## (Dispersion parameter for binomial family taken to be 1)
##
## Null deviance: 7533.1 on 6527 degrees of freedom
## Residual deviance: 6528.6 on 6507 degrees of freedom
## AIC: 6570.6
##
## Number of Fisher Scoring iterations: 4
```

### Binary Logistic Regression Model 2

In order to improve on our first model, we use all the variables from Model 1, but we exclude the variables YOJwhich proved to be the least statistically significant for our Model 1.

Additionally, we include the variables OLDCLAIM and URBANICITY, which ranked 4th and 5th in our list of 23 predictor variable importance model importanceA,

```
## ROC curve variable importance
##
##
    only 5 most important variables shown (out of 23)
##
             Importance
##
## CLM_FREQ
                 0.6354
## OLDCLAIM
                 0.6339
## MVR PTS
                 0.6202
## HOME VAL
                 0.6176
## URBANICITY
                 0.6026
##
## Call:
  glm(formula = TARGET_FLAG ~ AGE + CAR_USE + CLM_FREQ + HOME_VAL +
##
##
      INCOME + JOB + KIDSDRIV + MSTATUS + MVR_PTS + REVOKED + TIF +
##
      TRAVTIME + OLDCLAIM + URBANICITY, family = binomial(link = "logit"),
##
      data = train)
##
## Deviance Residuals:
      Min
           1Q Median
                                  3Q
                                          Max
## -2.4277 -0.7374 -0.4179 0.7057
                                       2.9863
##
## Coefficients:
##
                                  Estimate Std. Error z value Pr(>|z|)
                                -2.375e+00 2.857e-01 -8.313 < 2e-16 ***
## (Intercept)
                                -1.132e-02 3.890e-03 -2.911 0.003607 **
## AGE
## CAR_USEPrivate
                                -6.694e-01 8.269e-02 -8.095 5.70e-16 ***
                                 1.795e-01 3.138e-02
## CLM_FREQ
                                                       5.721 1.06e-08 ***
## HOME_VAL
                                -1.341e-06 3.724e-07 -3.602 0.000316 ***
## INCOME
                                -4.800e-06 1.107e-06 -4.338 1.44e-05 ***
                                 5.527e-01 1.475e-01
                                                      3.748 0.000178 ***
## JOBBlue Collar
## JOBClerical
                                 6.551e-01 1.737e-01
                                                        3.771 0.000162 ***
                                -1.763e-01 2.650e-01 -0.665 0.506038
## JOBDoctor
## JOBHome Maker
                                 5.915e-01 2.032e-01
                                                      2.910 0.003610 **
## JOBLawyer
                                 9.474e-02 1.805e-01
                                                      0.525 0.599711
## JOBManager
                                -4.475e-01 1.721e-01 -2.601 0.009296 **
                                 2.014e-01 1.621e-01
## JOBProfessional
                                                       1.242 0.214274
## JOBStudent
                                 5.903e-01 1.941e-01
                                                        3.041 0.002357 **
## KIDSDRIV
                                 4.586e-01 5.971e-02
                                                        7.681 1.57e-14 ***
                                -6.311e-01 7.810e-02 -8.080 6.48e-16 ***
## MSTATUSYes
## MVR PTS
                                 1.194e-01 1.496e-02
                                                        7.976 1.51e-15 ***
## REVOKEDYes
                                 8.145e-01 1.006e-01
                                                       8.096 5.66e-16 ***
## TIF
                                -5.477e-02 7.983e-03 -6.862 6.80e-12 ***
## TRAVTIME
                                 1.408e-02 2.061e-03
                                                       6.833 8.31e-12 ***
```

```
## OLDCLAIM -1.145e-05 4.332e-06 -2.643 0.008227 **

## URBANICITYHighly Urban/ Urban 2.329e+00 1.237e-01 18.819 < 2e-16 ***

## ---

## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1

##

## (Dispersion parameter for binomial family taken to be 1)

##

## Null deviance: 7533.1 on 6527 degrees of freedom

## Residual deviance: 6009.2 on 6506 degrees of freedom

## AIC: 6053.2

##

## Number of Fisher Scoring iterations: 5
```

We can see a significant improvement on the Residual deviance and AIC values.

#### Binary Logistic Regression Model 3

In order to improve on our previous model, we add the variables BLUEBOOK and HOMEKIDS, which ranked 9th and 10th in our list of 23 predictor variable importance model importanceA,

At this point, the top 10 most statistically important of our set of 23 predictor variables are included in this model.

```
## ROC curve variable importance
##
##
     only 10 most important variables shown (out of 23)
##
##
              Importance
                 0.6354
## CLM FREQ
## OLDCLAIM
                  0.6339
                  0.6202
## MVR_PTS
## HOME_VAL
                  0.6176
## URBANICITY
                 0.6026
## INCOME
                 0.5961
## CAR_USE
                 0.5782
## MSTATUS
                 0.5751
## BLUEBOOK
                 0.5750
## HOMEKIDS
                 0.5706
##
## Call:
## glm(formula = TARGET_FLAG ~ AGE + CAR_USE + CLM_FREQ + HOME_VAL +
##
       INCOME + JOB + KIDSDRIV + MSTATUS + MVR_PTS + REVOKED + TIF +
       TRAVTIME + OLDCLAIM + URBANICITY + BLUEBOOK + HOMEKIDS, family = binomial(link = "logit"),
##
##
      data = train)
##
## Deviance Residuals:
      Min
            1Q
                    Median
                                   3Q
                                           Max
##
## -2.4244 -0.7320 -0.4164 0.6821
                                        2.9748
## Coefficients:
                                  Estimate Std. Error z value Pr(>|z|)
##
## (Intercept)
                                 -2.258e+00 3.086e-01 -7.315 2.58e-13 ***
## AGE
                                 -4.528e-03 4.333e-03 -1.045 0.295999
                                 -7.865e-01 8.546e-02 -9.204 < 2e-16 ***
## CAR_USEPrivate
## CLM_FREQ
                                 1.739e-01 3.151e-02
                                                       5.520 3.39e-08 ***
                                 -1.337e-06 3.743e-07 -3.571 0.000356 ***
## HOME_VAL
## INCOME
                                -3.486e-06 1.133e-06 -3.076 0.002101 **
                                 4.131e-01 1.492e-01
## JOBBlue Collar
                                                        2.769 0.005626 **
## JOBClerical
                                  5.702e-01 1.746e-01
                                                        3.265 0.001093 **
```

```
## JOBDoctor
                                -2.424e-01 2.667e-01 -0.909 0.363280
## JOBHome Maker
                                5.065e-01 2.042e-01 2.481 0.013105 *
## JOBLawyer
                                3.755e-02 1.811e-01 0.207 0.835692
                                -4.971e-01 1.727e-01 -2.879 0.003992 **
## JOBManager
## JOBProfessional
                                1.571e-01 1.628e-01 0.965 0.334521
                                4.097e-01 1.966e-01 2.084 0.037134 *
## JOBStudent
## KIDSDRIV
                               3.808e-01 6.792e-02 5.607 2.06e-08 ***
                               -6.547e-01 7.869e-02 -8.320 < 2e-16 ***
## MSTATUSYes
## MVR_PTS
                                1.184e-01 1.502e-02 7.880 3.28e-15 ***
## REVOKEDYes
                                8.031e-01 1.011e-01 7.942 1.99e-15 ***
                               -5.633e-02 8.020e-03 -7.024 2.15e-12 ***
## TTF
## TRAVTIME
                                1.439e-02 2.069e-03
                                                      6.953 3.57e-12 ***
                                -1.120e-05 4.345e-06 -2.578 0.009938 **
## OLDCLAIM
## URBANICITYHighly Urban/ Urban 2.358e+00 1.243e-01 18.965 < 2e-16 ***
                                -2.650e-05 4.511e-06 -5.875 4.22e-09 ***
## BLUEBOOK
## HOMEKIDS
                                 9.684e-02 3.580e-02
                                                      2.705 0.006830 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
      Null deviance: 7533.1 on 6527 degrees of freedom
## Residual deviance: 5967.0 on 6504 degrees of freedom
## AIC: 6015
##
## Number of Fisher Scoring iterations: 5
```

This time, we can see an even more significant improvement on the Residual deviance and AIC values.

#### Binary Logistic Regression Model 4

In order to improve on our previous model, we add the variables CAR\_AGE, PARENT1 and EDUCATION, which ranked 12th, 14th and 17th in our list of 23 predictor variable importance model importanceA,

We also remove the variables AGE and HOMEKIDS, which from the previous models do not seem to contribute much. i.e. do not seem to be statistically significant for most of the models.

```
##
## Call:
## glm(formula = TARGET FLAG ~ CAR USE + CLM FREQ + HOME VAL + INCOME +
      JOB + KIDSDRIV + MSTATUS + MVR_PTS + REVOKED + TIF + TRAVTIME +
##
      OLDCLAIM + URBANICITY + BLUEBOOK + CAR_AGE + CAR_TYPE + PARENT1 +
##
##
      EDUCATION, family = binomial(link = "logit"), data = train)
##
## Deviance Residuals:
##
      Min
            1Q
                   Median
                                  3Q
                                          Max
## -2.6408 -0.7109 -0.3978
                                       3.1562
                              0.6333
##
## Coefficients:
##
                                  Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                -3.027e+00 3.095e-01 -9.780 < 2e-16 ***
## CAR_USEPrivate
                               -7.907e-01 1.023e-01 -7.733 1.05e-14 ***
                                                      5.393 6.94e-08 ***
                                1.722e-01 3.194e-02
## CLM_FREQ
## HOME_VAL
                                -1.425e-06 3.780e-07 -3.769 0.000164 ***
## INCOME
                               -2.484e-06 1.189e-06 -2.088 0.036772 *
                                3.677e-01 2.080e-01 1.767 0.077146 .
## JOBBlue Collar
## JOBClerical
                                4.621e-01 2.200e-01
                                                      2.100 0.035696 *
## JOBDoctor
                               -2.734e-01 2.895e-01 -0.944 0.344937
## JOBHome Maker
                               3.776e-01 2.293e-01 1.647 0.099562 .
                                1.694e-01 1.913e-01 0.886 0.375636
## JOBLawyer
```

```
## JOBManager
                               -4.761e-01 1.925e-01 -2.473 0.013383 *
## JOBProfessional
                               2.565e-01 2.001e-01 1.282 0.199867
## JOBStudent
                              3.529e-01 2.366e-01 1.491 0.135860
                              4.086e-01 6.263e-02 6.524 6.84e-11 ***
## KIDSDRIV
## MSTATUSYes
                               -4.904e-01 8.931e-02 -5.491 4.00e-08 ***
                               1.135e-01 1.520e-02 7.470 8.05e-14 ***
## MVR PTS
## REVOKEDYes
                               7.962e-01 1.025e-01 7.769 7.92e-15 ***
                               -5.623e-02 8.136e-03 -6.912 4.79e-12 ***
## TIF
## TRAVTIME
                               1.484e-02 2.102e-03 7.061 1.66e-12 ***
## OLDCLAIM
                               -1.135e-05 4.391e-06 -2.586 0.009714 **
## URBANICITYHighly Urban/ Urban 2.449e+00 1.263e-01 19.386 < 2e-16 ***
## BLUEBOOK
                               -2.274e-05 5.312e-06 -4.282 1.85e-05 ***
                               -3.642e-03 8.405e-03 -0.433 0.664791
## CAR_AGE
## CAR_TYPEPanel Truck
                              5.734e-01 1.706e-01 3.360 0.000779 ***
## CAR_TYPEPickup
                              5.400e-01 1.124e-01 4.805 1.55e-06 ***
## CAR_TYPESports Car
                               1.026e+00 1.194e-01
                                                    8.593 < 2e-16 ***
                               7.482e-01 9.578e-02 7.812 5.63e-15 ***
## CAR_TYPESUV
## CAR_TYPEVan
                              7.281e-01 1.349e-01 5.399 6.71e-08 ***
                              5.309e-01 1.049e-01 5.060 4.19e-07 ***
## PARENT1Yes
## EDUCATIONBachelors
                               -4.417e-01 1.293e-01 -3.416 0.000636 ***
## EDUCATIONHigh School
                             -5.730e-02 1.069e-01 -0.536 0.591870
## EDUCATIONMasters
                               -3.846e-01 2.007e-01 -1.916 0.055385 .
                               -2.537e-01 2.364e-01 -1.073 0.283095
## EDUCATIONPhD
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 7533.1 on 6527 degrees of freedom
## Residual deviance: 5831.7 on 6495 degrees of freedom
## AIC: 5897.7
##
## Number of Fisher Scoring iterations: 5
```

At this point, we can see most significant improvement on the Residual deviance and AIC values.

### Binary Logistic Regression Model 5

Just out of curiosity, what if we ignored all the statistical correlation and variable importance that we used for the previous four models. We use a model that includes all the predictor variables and the response variable TARGET\_FLAG.

```
##
## Call:
## glm(formula = TARGET_FLAG ~ . - TARGET_AMT, family = binomial(link = "logit"),
##
      data = train)
##
## Deviance Residuals:
     Min 1Q Median
                                 3Q
                                         Max
  -2.6207 -0.7138 -0.3982 0.6320
##
                                      3.1760
##
## Coefficients:
##
                                 Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                               -2.794e+00 3.811e-01 -7.331 2.29e-13 ***
## KIDSDRIV
                                3.954e-01 6.933e-02 5.703 1.18e-08 ***
## AGE
                               -3.360e-03 4.509e-03 -0.745 0.456212
                                2.628e-02 4.177e-02 0.629 0.529287
## HOMEKIDS
                               -1.639e-02 9.646e-03 -1.699 0.089301 .
## YOJ
## INCOME
                               -2.356e-06 1.194e-06 -1.972 0.048596 *
## PARENT1Yes
                                4.746e-01 1.226e-01 3.871 0.000108 ***
```

```
## HOME_VAL
                                 -1.381e-06
                                             3.795e-07
                                                        -3.640 0.000273 ***
## MSTATUSYes
                                 -4.922e-01
                                             9.386e-02
                                                        -5.244 1.57e-07 ***
## SEXM
                                  6.883e-02
                                             1.256e-01
                                                         0.548 0.583642
## EDUCATIONBachelors
                                 -4.420e-01
                                             1.295e-01
                                                        -3.413 0.000643 ***
                                 -5.567e-02
                                             1.070e-01
                                                        -0.520 0.602836
## EDUCATIONHigh School
## EDUCATIONMasters
                                 -3.802e-01 2.010e-01
                                                        -1.891 0.058579
## EDUCATIONPhD
                                 -2.484e-01 2.370e-01
                                                        -1.048 0.294649
  JOBBlue Collar
                                  3.697e-01
                                             2.081e-01
                                                          1.777 0.075644
## JOBClerical
                                  4.590e-01 2.202e-01
                                                          2.085 0.037058 *
## JOBDoctor
                                 -2.672e-01 2.901e-01
                                                        -0.921 0.357022
## JOBHome Maker
                                  3.097e-01 2.358e-01
                                                          1.314 0.188979
## JOBLawyer
                                  1.798e-01
                                             1.916e-01
                                                          0.938 0.348195
                                            1.928e-01
## JOBManager
                                 -4.673e-01
                                                        -2.424 0.015348 *
## JOBProfessional
                                  2.623e-01
                                            2.002e-01
                                                          1.310 0.190294
## JOBStudent
                                  2.746e-01
                                             2.409e-01
                                                          1.140 0.254280
## TRAVTIME
                                  1.493e-02
                                             2.105e-03
                                                         7.091 1.33e-12 ***
## CAR_USEPrivate
                                 -7.869e-01
                                             1.025e-01
                                                        -7.680 1.59e-14 ***
## BLUEBOOK
                                 -2.070e-05 5.921e-06
                                                        -3.496 0.000473 ***
## TIF
                                 -5.618e-02
                                             8.141e-03
                                                        -6.901 5.17e-12 ***
## CAR_TYPEPanel Truck
                                  5.310e-01
                                             1.829e-01
                                                          2.903 0.003694 **
  CAR_TYPEPickup
                                  5.420e-01
                                             1.125e-01
                                                          4.818 1.45e-06 ***
## CAR_TYPESports Car
                                  1.067e+00
                                             1.446e-01
                                                          7.377 1.62e-13 ***
## CAR TYPESUV
                                  7.894e-01
                                             1.239e-01
                                                          6.369 1.91e-10 ***
## CAR_TYPEVan
                                  7.015e-01
                                             1.403e-01
                                                          5.002 5.68e-07 ***
## RED_CARyes
                                 -1.634e-02 9.674e-02
                                                        -0.169 0.865834
## OLDCLAIM
                                             4.394e-06
                                 -1.115e-05
                                                        -2.537 0.011172 *
## CLM FREQ
                                  1.718e-01
                                             3.196e-02
                                                          5.377 7.55e-08 ***
## REVOKEDYes
                                  7.916e-01 1.026e-01
                                                         7.715 1.21e-14 ***
## MVR PTS
                                  1.124e-01
                                             1.523e-02
                                                          7.381 1.57e-13 ***
## CAR_AGE
                                 -3.696e-03 8.409e-03
                                                        -0.440 0.660251
## URBANICITYHighly Urban/ Urban 2.449e+00
                                             1.263e-01
                                                        19.388 < 2e-16 ***
##
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
  (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 7533.1
                              on 6527
                                       degrees of freedom
## Residual deviance: 5827.2
                              on 6490
                                       degrees of freedom
##
  AIC: 5903.2
##
## Number of Fisher Scoring iterations: 5
```

The results above show the best improvement so far.

Even after seeing the most significant improvement of all models, we still see that variables AGE, HOMEKIDS, SEX, and RED\_CAR (yes) are not statistically significant. Which, lead us to believe that it might be true that deeming the variables RED\_CAR and SEX as "urban legends" might be just urban legends. Those variable show little to no correlation to the probability of collision.

The variable EDUCATION seems to be statistically significant. At least for the values "Bachelors" and "Masters" we see that, based on the sign of their coefficients, they have a negative correlation to the theoretical probability of collision. So, it appears that people with higher education tend to have fewer accidents.

### **Linear Regression Models**

#### Linear Regression Model 1

We begin with a baseline model that includes all the predictor variables and the response variable TARGET\_AMT.

```
##
## Call:
## lm(formula = TARGET_AMT ~ . - TARGET_FLAG, data = train)
##
  Residuals:
##
     Min
             1Q Median
                          30
##
   -5952 -1694 -762
                          352 103691
##
## Coefficients:
##
                                 Estimate Std. Error t value Pr(>|t|)
                                -6.848e+01 6.487e+02 -0.106 0.915928
## (Intercept)
                                                      2.517 0.011852 *
## KIDSDRIV
                                3.233e+02 1.284e+02
                                5.760e+00 7.980e+00
## AGE
                                                      0.722 0.470441
## HOMEKIDS
                                5.912e+01 7.359e+01
                                                     0.803 0.421818
                                -8.437e+00 1.709e+01 -0.494 0.621472
## YOJ
## INCOME
                                -4.093e-03 2.015e-03 -2.031 0.042292 *
                                7.032e+02 2.278e+02
                                                     3.086 0.002034 **
## PARENT1Yes
## HOME_VAL
                               -6.449e-04 6.619e-04 -0.974 0.329934
                               -5.344e+02 1.638e+02 -3.263 0.001109 **
## MSTATUSYes
## SEXM
                                4.437e+02 2.076e+02
                                                      2.137 0.032619 *
## EDUCATIONBachelors
                               -4.616e+02 2.309e+02 -1.999 0.045621 *
## EDUCATIONHigh School
                               -1.545e+02 1.948e+02 -0.793 0.427742
                               -1.577e+02 3.407e+02 -0.463 0.643392
## EDUCATIONMasters
                                                      0.206 0.836881
## EDUCATIONPhD
                                8.225e+01 3.995e+02
## JOBBlue Collar
                                2.763e+02 3.644e+02
                                                      0.758 0.448271
## JOBClerical
                               2.679e+02 3.863e+02
                                                      0.694 0.487944
                               -6.130e+02 4.577e+02 -1.339 0.180560
## JOBDoctor
## JOBHome Maker
                                2.059e+02 4.123e+02
                                                      0.499 0.617610
## JOBLawyer
                                9.217e+01 3.354e+02
                                                       0.275 0.783475
## JOBManager
                               -6.918e+02 3.283e+02 -2.107 0.035141 *
## JOBProfessional
                                3.274e+02 3.507e+02
                                                       0.933 0.350668
                                9.435e+01 4.233e+02
## JOBStudent
                                                      0.223 0.823627
                                1.127e+01 3.625e+00
## TRAVTIME
                                                      3.109 0.001885 **
                               -8.458e+02 1.851e+02 -4.570 4.97e-06 ***
## CAR_USEPrivate
## BLUEBOOK
                                1.762e-02 9.787e-03
                                                      1.800 0.071865 .
                               -5.279e+01 1.362e+01 -3.875 0.000108 ***
## TIF
## CAR_TYPEPanel Truck
                               -1.110e+02 3.170e+02 -0.350 0.726208
                                3.659e+02 1.913e+02
## CAR_TYPEPickup
                                                      1.912 0.055891
## CAR_TYPESports Car
                                9.907e+02 2.452e+02
                                                      4.040 5.42e-05 ***
## CAR TYPESUV
                               7.973e+02 2.021e+02
                                                     3.944 8.09e-05 ***
## CAR TYPEVan
                               5.866e+02 2.397e+02
                                                      2.447 0.014433 *
                               -1.247e+02 1.678e+02 -0.743 0.457580
## RED_CARyes
## OLDCLAIM
                               -1.191e-02 8.465e-03 -1.408 0.159304
## CLM_FREQ
                                1.114e+02 6.196e+01
                                                     1.798 0.072230
                                4.205e+02 1.961e+02
## REVOKEDYes
                                                       2.145 0.032007 *
## MVR PTS
                                1.754e+02 2.927e+01
                                                      5.992 2.18e-09 ***
                                -2.352e+01 1.446e+01 -1.626 0.103938
## CAR AGE
## URBANICITYHighly Urban/ Urban 1.726e+03 1.565e+02 11.029 < 2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4589 on 6490 degrees of freedom
## Multiple R-squared: 0.07099,
                                 Adjusted R-squared: 0.06569
## F-statistic: 13.4 on 37 and 6490 DF, p-value: < 2.2e-16
```

#### Linear Regression Model 2

For our second model, we only include the top 10 most important predictor variables that we gathered from our importance trained model model model model model.

```
##
## Call:
## lm(formula = TARGET_AMT ~ URBANICITY + MVR_PTS + CAR_USE + CAR_TYPE +
      CAR_TYPE + TIF + MSTATUS + TRAVTIME + REVOKED + PARENT1,
      data = train)
##
##
## Residuals:
##
    Min
            1Q Median
                         3Q
##
   -5989 -1671 -852
                        249 103828
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
                                         267.099 0.852 0.394365
## (Intercept)
                               227.510
## URBANICITYHighly Urban/ Urban 1407.279
                                         145.912 9.645 < 2e-16 ***
                                         27.108 7.773 8.86e-15 ***
## MVR_PTS
                               210.704
## CAR_USEPrivate
                              -971.332
                                         139.845 -6.946 4.13e-12 ***
                                         255.789 -0.171 0.864166
## CAR_TYPEPanel Truck
                               -43.760
## CAR_TYPEPickup
                               369.661
                                       185.113 1.997 0.045872 *
                                         ## CAR_TYPESports Car
                               799.531
## CAR_TYPESUV
                               615.412
                                       155.300
                                                 3.963 7.49e-05 ***
                                       ## CAR_TYPEVan
                              590.626
                               -53.139
                                         13.671 -3.887 0.000103 ***
## TIF
                                         132.811 -3.423 0.000624 ***
## MSTATUSYes
                              -454.592
## TRAVTIME
                                12.849
                                          3.632 3.537 0.000407 ***
## REVOKEDYes
                               384.468
                                         176.236 2.182 0.029178 *
## PARENT1Yes
                               990.605
                                       192.623 5.143 2.79e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 4616 on 6514 degrees of freedom
## Multiple R-squared: 0.05666, Adjusted R-squared: 0.05478
## F-statistic: 30.1 on 13 and 6514 DF, p-value: < 2.2e-16
```

### Linear Regression Model 3

For our third model, we only include the predictor variables that have theoretical probably of effecting the payout if there is a crash, which was provided as part of the definition of the variables.

```
##
## Call:
  lm(formula = TARGET_AMT ~ BLUEBOOK + CAR_AGE + CAR_TYPE + CLM_FREQ +
##
      OLDCLAIM, data = train)
##
## Residuals:
    Min
            1Q Median
                          3Q
                                Max
##
   -3763 -1597 -1117
                        -297 104469
##
## Coefficients:
##
                       Estimate Std. Error t value Pr(>|t|)
                      1.042e+03 1.967e+02 5.295 1.23e-07 ***
## (Intercept)
## BLUEBOOK
                      1.810e-03 8.597e-03 0.210 0.833307
                      -4.808e+01 1.072e+01 -4.486 7.37e-06 ***
## CAR AGE
## CAR_TYPEPanel Truck 7.741e+02 2.612e+02 2.963 0.003054 **
## CAR_TYPEPickup
                      6.882e+02 1.822e+02 3.777 0.000160 ***
## CAR_TYPESports Car 7.034e+02 2.115e+02 3.326 0.000886 ***
                      5.532e+02 1.611e+02 3.435 0.000597 ***
## CAR TYPESUV
## CAR_TYPEVan
                      9.643e+02 2.268e+02 4.253 2.14e-05 ***
## CLM_FREQ
                      4.042e+02 5.779e+01
                                             6.995 2.93e-12 ***
## OLDCLAIM
                      4.720e-03 7.728e-03 0.611 0.541369
```

```
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4705 on 6518 degrees of freedom
## Multiple R-squared: 0.01945, Adjusted R-squared: 0.01809
## F-statistic: 14.36 on 9 and 6518 DF, p-value: < 2.2e-16</pre>
```

### Model Selection

### Binary logistic regression

#### **Confusion Matrices**

We generate confusion matrices for our five models using a p = 0.5 cutoff.

#### Confusion Matrix for Model 1:

```
## Confusion Matrix and Statistics
##
##
            Reference
## Prediction 0 1
           0 4517 1267
##
           1 289 455
##
##
##
                  Accuracy : 0.7616
##
                    95% CI: (0.7511, 0.7719)
      No Information Rate: 0.7362
##
      P-Value [Acc > NIR] : 1.325e-06
##
##
##
                    Kappa: 0.2496
##
##
   Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.2642
               Specificity: 0.9399
##
##
           Pos Pred Value: 0.6116
##
           Neg Pred Value: 0.7809
                Prevalence: 0.2638
##
           Detection Rate: 0.0697
##
     Detection Prevalence : 0.1140
##
        Balanced Accuracy: 0.6020
##
##
          'Positive' Class: 1
```

#### Confusion Matrix for Model 2:

```
## Confusion Matrix and Statistics
##
##
            Reference
## Prediction
              0
##
           0 4428 1040
##
           1 378 682
##
##
                  Accuracy : 0.7828
##
                    95% CI: (0.7726, 0.7927)
##
      No Information Rate: 0.7362
##
      P-Value [Acc > NIR] : < 2.2e-16
```

```
##
##
                     Kappa : 0.3621
##
##
    Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.3961
##
               Specificity: 0.9213
            Pos Pred Value: 0.6434
##
            Neg Pred Value: 0.8098
##
##
                Prevalence: 0.2638
            Detection Rate: 0.1045
##
      Detection Prevalence: 0.1624
##
         Balanced Accuracy: 0.6587
##
##
##
          'Positive' Class : 1
##
Confusion Matrix for Model 3:
## Confusion Matrix and Statistics
##
##
             Reference
               0 1
## Prediction
            0 4422 1035
            1 384 687
##
##
##
                  Accuracy : 0.7826
                    95% CI : (0.7724, 0.7926)
##
       No Information Rate: 0.7362
##
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa : 0.3631
##
##
   Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.3990
##
               Specificity: 0.9201
##
            Pos Pred Value : 0.6415
            Neg Pred Value: 0.8103
                Prevalence: 0.2638
##
##
            Detection Rate: 0.1052
##
      {\tt Detection\ Prevalence}\ :\ {\tt 0.1641}
##
         Balanced Accuracy: 0.6595
##
##
          'Positive' Class : 1
##
Confusion Matrix for Model 4:
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction
               0
                      1
##
            0 4434
                    986
##
            1 372 736
##
##
                  Accuracy: 0.792
##
                    95% CI: (0.7819, 0.8018)
```

No Information Rate: 0.7362

##

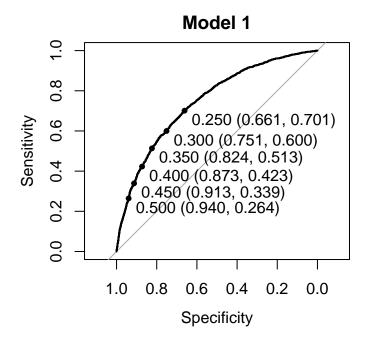
```
P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                     Kappa: 0.3952
##
   Mcnemar's Test P-Value : < 2.2e-16
##
##
##
               Sensitivity: 0.4274
               Specificity: 0.9226
##
            Pos Pred Value: 0.6643
##
##
           Neg Pred Value: 0.8181
                Prevalence: 0.2638
##
            Detection Rate: 0.1127
##
##
     Detection Prevalence : 0.1697
##
         Balanced Accuracy: 0.6750
##
          'Positive' Class : 1
##
##
```

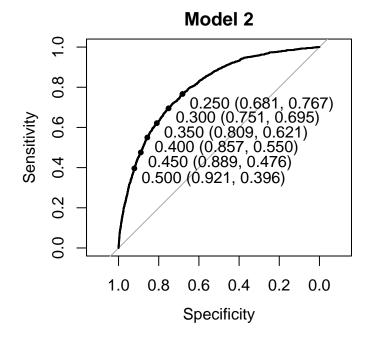
#### Confusion Matrix for Model 5:

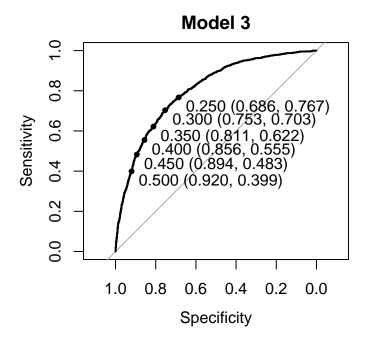
```
## Confusion Matrix and Statistics
##
##
            Reference
               0
## Prediction
            0 4434 973
##
##
            1 372 749
##
##
                  Accuracy: 0.794
                    95% CI: (0.7839, 0.8037)
##
##
      No Information Rate: 0.7362
      P-Value [Acc > NIR] : < 2.2e-16
##
##
##
                     Kappa: 0.4026
##
##
   Mcnemar's Test P-Value : < 2.2e-16
##
##
               Sensitivity: 0.4350
               Specificity: 0.9226
##
##
            Pos Pred Value : 0.6682
           Neg Pred Value: 0.8200
##
##
                Prevalence: 0.2638
##
            Detection Rate: 0.1147
##
     Detection Prevalence: 0.1717
##
         Balanced Accuracy: 0.6788
##
##
          'Positive' Class : 1
##
```

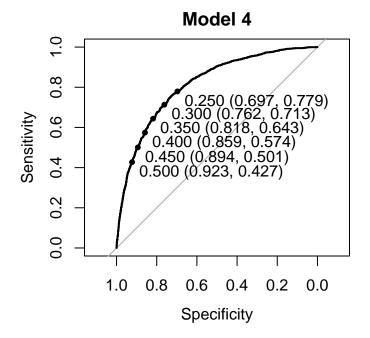
#### **ROC Curves**

We generate the ROC curves for all of our models.









## 

### Conclusions

# Code Appendix