


Ex7.s6: Repeated subsequences




Find all repeated substrings of length $\geq m$ in a string s by identifying positions i and j where

$s[i..i+m] == s[j..j+m]$

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 For simplicity, let's say $s = \text{"banana banana"}; m=3$




1. Generate all suffixes of string s :

i	suffix
0	banana banana
1	anana banana
2	nana banana
3	ana banana
4	na banana
5	a banana
6	banana
7	banana
8	anana
9	nana
10	ana
11	na
12	a

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2. Sort all suffixes alphabetically:

i	suffix
6	banana
12	a
5	a banana
10	ana
3	ana banana
1	anana banana
8	anana
0	banana banana
7	banana
2	nana banana
9	nana
11	na
4	na banana

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💡 now, **any repeated substring of length ≥ 3** must appear as a common prefix between **neighbouring suffixes** in this sorted list

2. Sort all suffixes alphabetically:

i	suffix
6	banana
12	a
5	a banana
10	ana
3	ana banana
1	anana banana
8	anana
0	banana banana
7	banana
2	nana banana
9	nana
11	na
4	na banana

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→ For each pair of neighbours, check whether they share more than 3 characters at the beginning

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i	suffix
6	banana
12	a
5	a banana
10	ana
3	ana banana
1	anana banana
8	anana
0	banana banana
7	banana
2	nana banana
9	nana
11	na
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2. Sort all suffixes alphabetically:

i	suffix
6	0 banana
12	0 a 1
5	1 a banana
10	1 ana 3
3	3 ana banana
1	3 anana banana 5
8	0 anana
0	0 banana banana 6
7	0 banana
2	0 nana banana 4
9	2 nana
11	2 na 2
4	na banana

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2. Sort all suffixes alphabetically:

i	suffix
6	0 banana
12	0 a 1
5	1 a banana
10	1 ana 3 ✓
3	3 ✓ ana banana
1	3 ✓ anana banana 5 ✓
8	0 anana
0	0 banana banana 6 ✓
7	0 banana
2	0 nana banana 4 ✓
9	2 nana
11	2 na 2
4	na banana

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Running time

- Sorting n suffixes: $O(n \log n)$ comparisons (Quicksort), where each comparison takes $O(m)$ (because we sort by the first m characters)

\Rightarrow total: $O(n \log n) \cdot O(m)$