Linked Structures

Linked Lists

The Concept

- Each element in a linked data structure is called a node
- A node contains two kind of fields:
 - The information field: Holds a reference to an element
 - Next link field(s): Hold reference(s) to one or more nodes in the structure

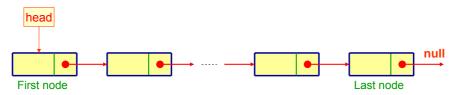
Node Information

Next Node's Link

One node in a linked structure

Example Linked List Structure

A linked list structure may look like this:

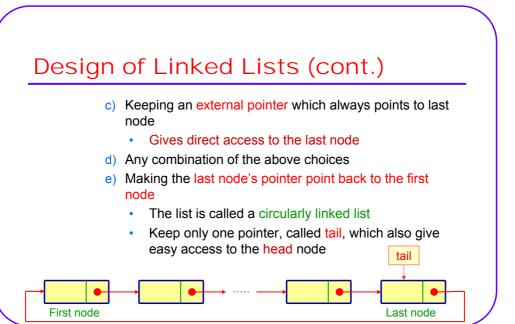


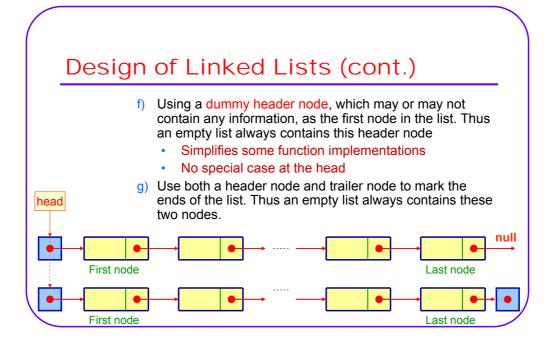
- The head pointer is an external reference to a node
- It always gives access to the first node in the list
- Access to other nodes is one-way and sequential through the stored links / pointers

Design of Linked Lists

Linked List Design Parameters:

- 1. How to mark the ends of the list?
 - A head pointer is always used to point to the first node
 - Possibilities for the last node are:
 - a) Using a null value in the pointer field of the last node
 - Expensive to locate the last node
 - b) Keeping a count of number of nodes in the list
 - Easy to get the size of the list
 - Still expensive to locate the last node





Design of Linked Lists (cont.)

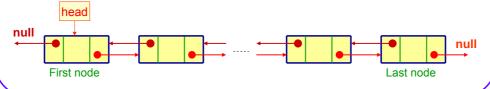
- 2. What external pointers give access to the list? and to which nodes?
 - At least one node of the list must be accessed through an external pointer (usually the first node)
 - Other possibilities include: A current pointer, a tail pointer, ..., and so on

Design of Linked Lists (cont.)

- 3. How many pointers should be stored in each node that point to related nodes?
 - At least one is necessary to point to the next node.
 The list is called "Singly Linked List"
 - Predecessor nodes are difficult to access
 - The list can only be traversed in one direction
 - Access at any point other than head node makes those before it inaccessible.

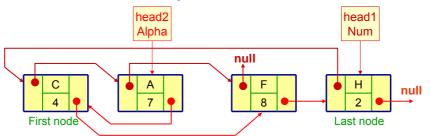
Design of Linked Lists (cont.)

- Other possibilities are:
 - a) Store two pointers in each node, one points to its successor and the other points to its predecessor
 - The list is called a "Doubly Linked List" if the ordering in one direction is the logical inverse of the other
 - The list can be traversed in both directions
 - · Easy to get the successor and predecessor of a node



Design of Linked Lists (cont.)

- b) Store two pointers in each node, each one giving a different ordering of the node
 - Such a list is called "Multi-Linked List" of order two
 - Useful to keep one physical order and have two different logical orders



Design of Linked Lists (cont.)

 Store more than two pointers (n pointers) in each node to get an extension of (b), called "Multi-Linked List" of order n.

Linked Structures

The Linear List

Abstract Definition

A Linear List is an ordered collection of elements from set S. The order is defined either by position or by other kind of ordering.

In other words, a linear list is either empty or can be written as:

$$(a_1, a_2, a_3, ..., a_n)$$

Where a_i are elements of some set S.

Specifications

- Each element of a list is assumed to have at least two fields, as shown:
- Keys are unique identities of the elements.

Key Field

Data Fields

• The list contains n elements.

Structure

- There is a linear relationship between elements.
- Each element in the list has a unique position.
- If the position of the first element is k, then the position of its successor is k+1.

Example:

Element X has position 2; Its successor is A, which has position 3.

| Position | 1 | 2 | 3 | 4 | 5 | 6 | 7 |
|----------|---|---|---|---|-----------|---|---|
| Element | ш | X | Α | M | <u> բ</u> | L | Е |

Operations

Some of the operations assume there is one element in the list designated as current.

```
first()
                                 getPosition()
last()
                                 addBefore(entry)
                                 addAfter(entry)
next()
prior()
                                 remove()
seek(position)
                                 isElement()
search (target)
                                 isEmpty() , isFull()
                                 size()
get()
set(entry)
                                 clear()
```

List Implementation Using a Linked Structure

- Use a Circularly Doubly Linked List structure with a head pointer
- Each node in the list is an instance of a DNode class that contains the following private fields:
 - element where the node information is stored
 - next which is a forward link pointer
 - prev which is a backward link pointer

prev element next

- Use two external pointers into the list:
 - head points to the first node in the list
 - current points to the current node in the list

List Implementation Using a Linked Structure (cont.)

- Use two integer variables:
 - position stores the position of the current node.
 - size stores the number of nodes currently in the list.
- An empty list is initialized by setting:
 - head = current = null
 position = size = 0.

 The Constructor
- At any time, if the list has position == 0 or current == null, then there is no current item.

List Implementation The DNode Class Structure

- Used as a generic class with a variable data type, E, as the type of information stored in each node
- The link fields are pointers to a DNode object type
- The class has a constructor to initialize its data fields
- Functions for accessing the class fields are also members of the DNode class

```
public class DNode <E>
private E element;
private DNode<E> next;
private DNode<E> prev;
```

List Implementation The DLinkedList Class Structure

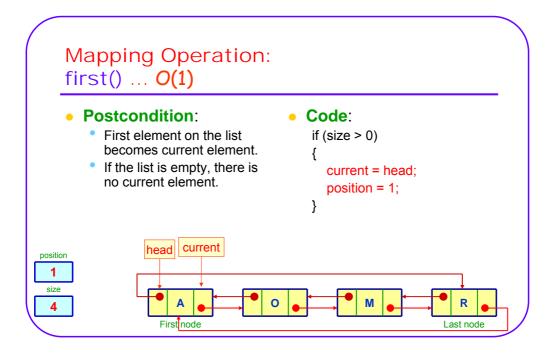
- Used as a generic class with a variable data type, E, as the type of information stored in each node
- The head and current fields are external pointers to the list nodes
- The class has a constructor to initialize its data fields.
- Some functions that implement the List operations are also members of the List class

```
public class DLinkedList<E>
private DNode<E> head;
```

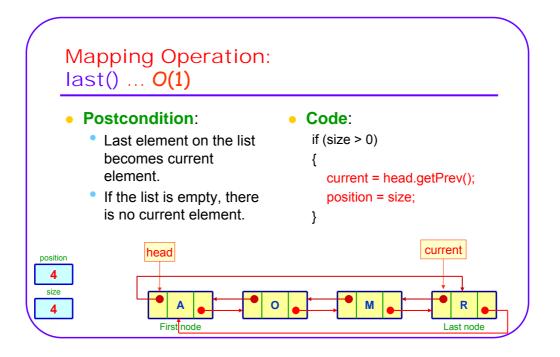
private DNode<E> current; private int position, size;

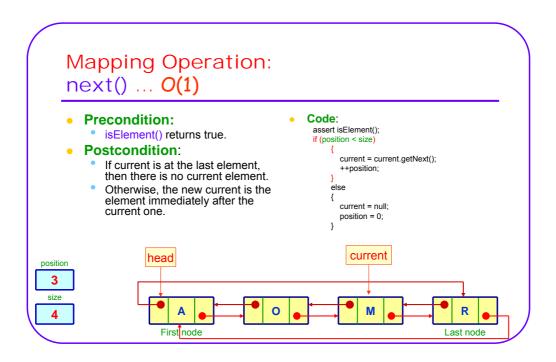
```
public DLinkedList();
public void first(); .....
public void next(); .....
public void search(E target);
public void addBefore(E entry);
public void addAfter(E entry);
public void remove();
public void set(E entry);
public void clear();
public int size(); .....
```

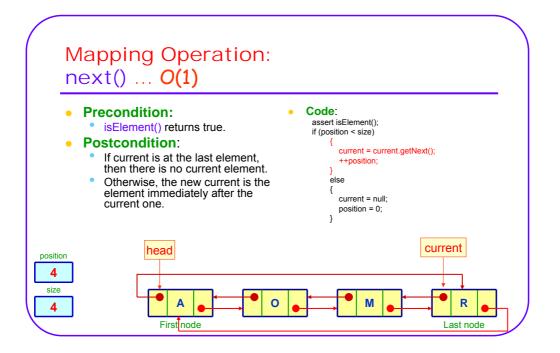
Mapping Operation: first() ... O(1) Postcondition: Code: if (size > 0) First element on the list becomes current element. If the list is empty, there is current = head; no current element. position = 1; current head position 3 size M 4 First node Last node

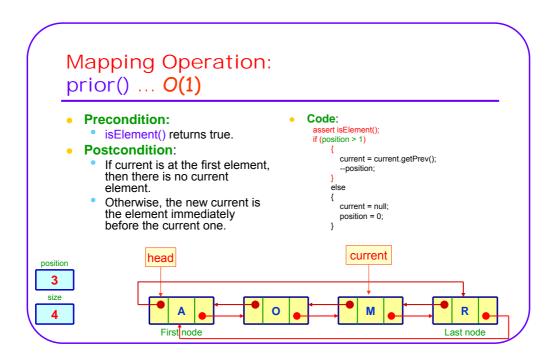


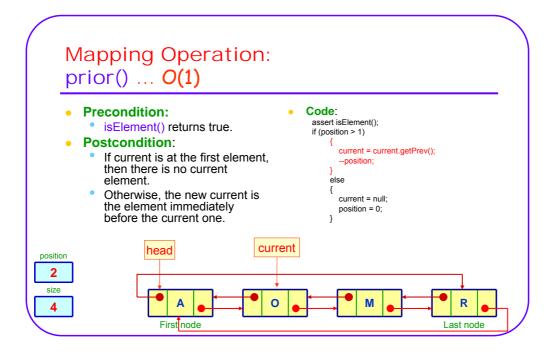
Mapping Operation: last() ... O(1) Postcondition: Code: Last element on the list if (size > 0) becomes current element. current = head.getPrev(); position = size; If the list is empty, there is no current element. current head position 3 4 Firstnode Last node

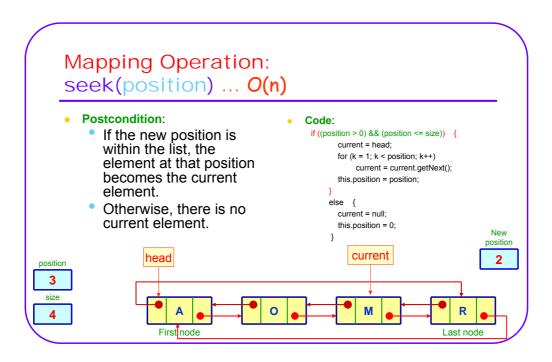


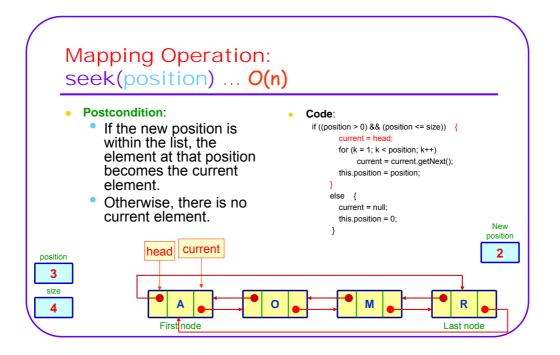


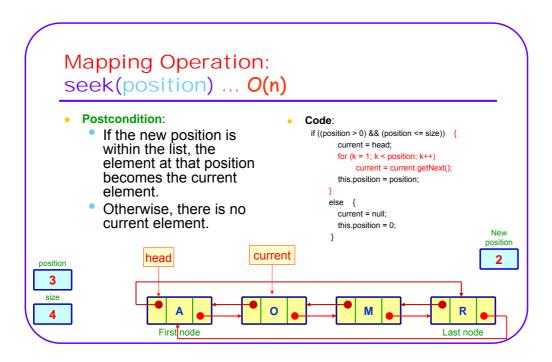


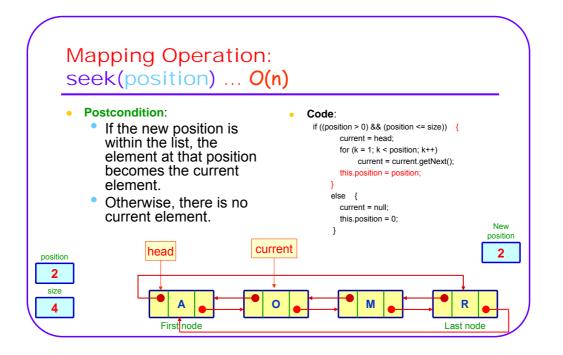


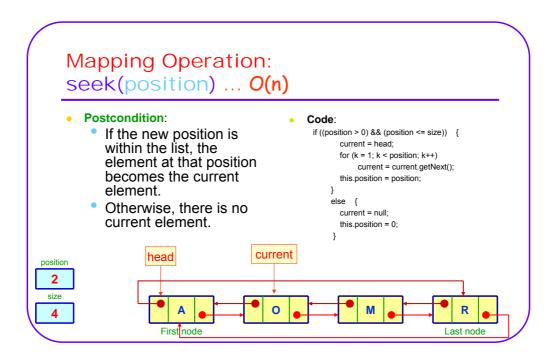


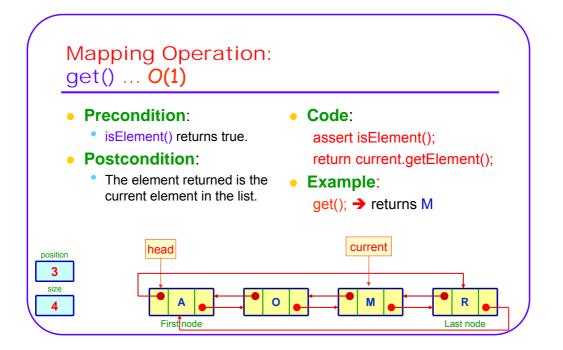


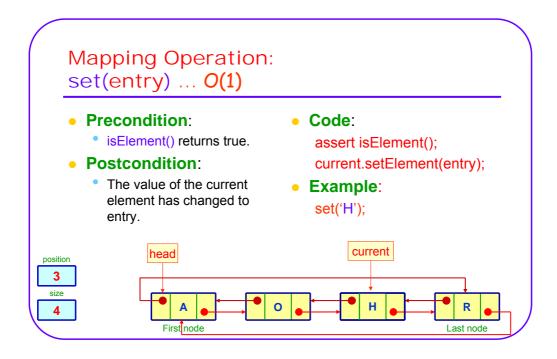


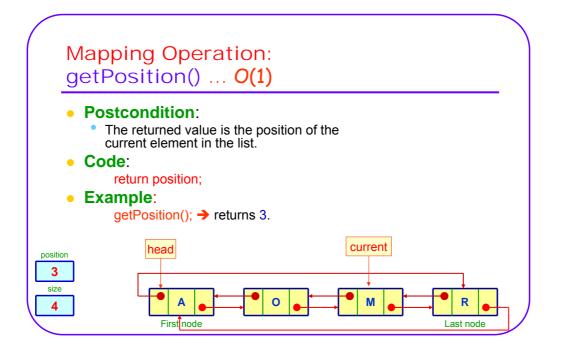


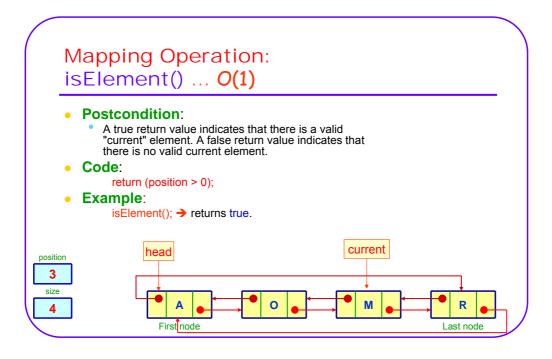


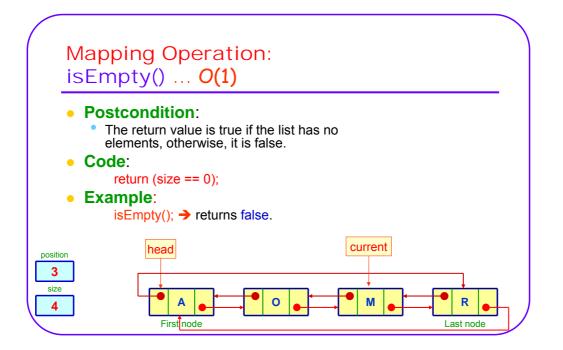


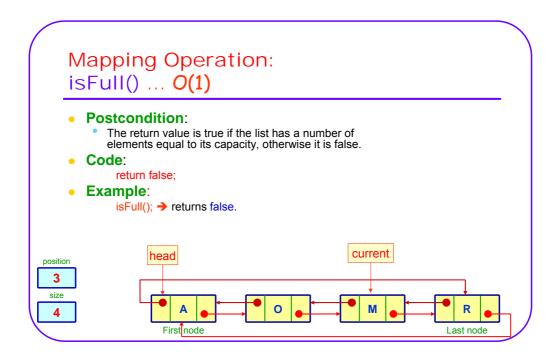


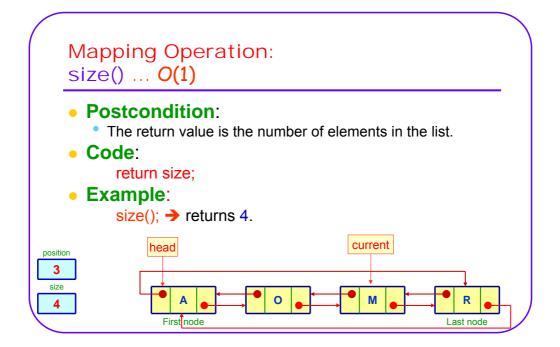


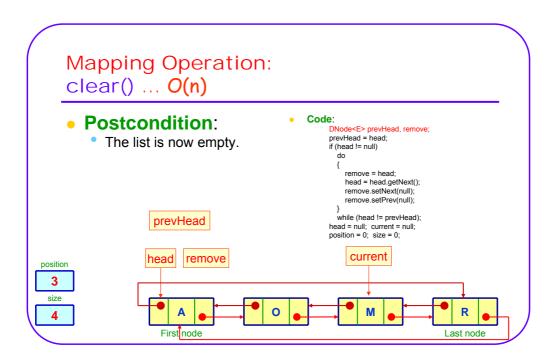


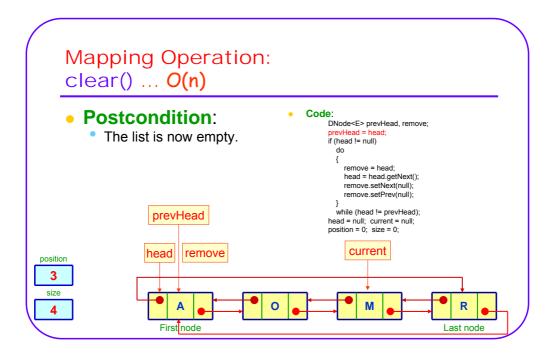


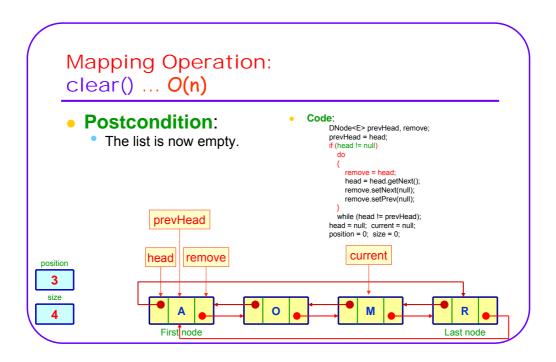


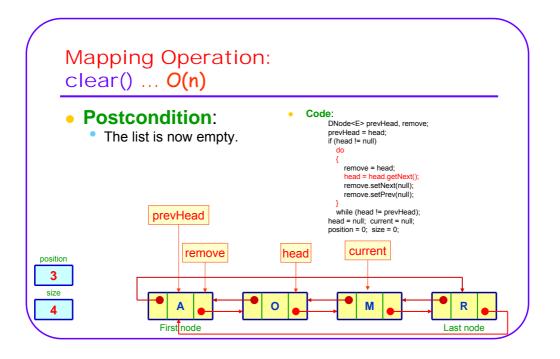


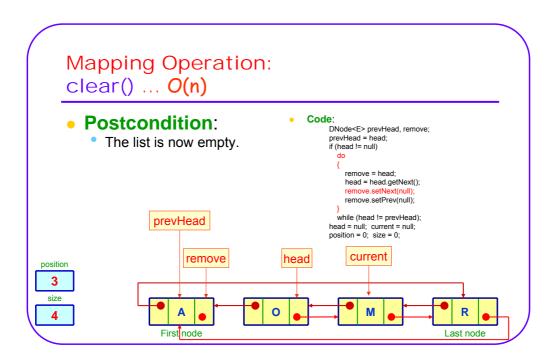


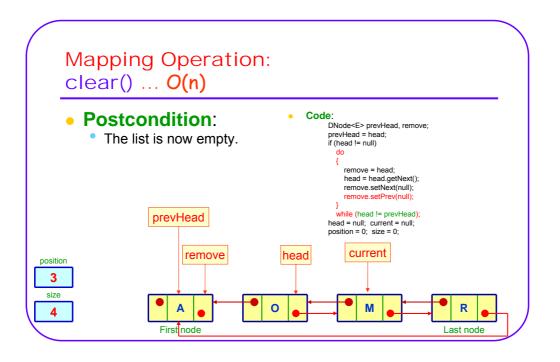


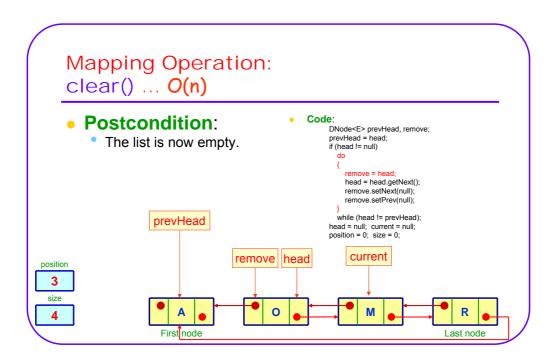


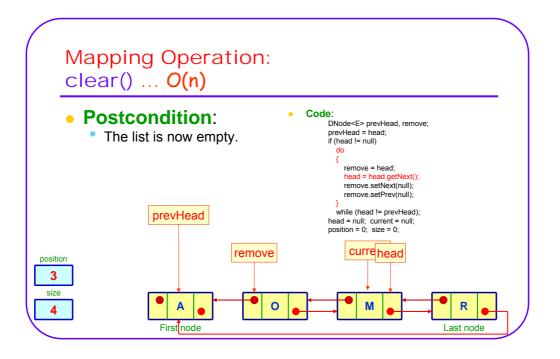


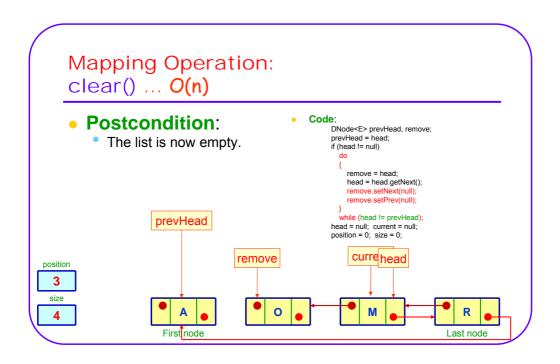


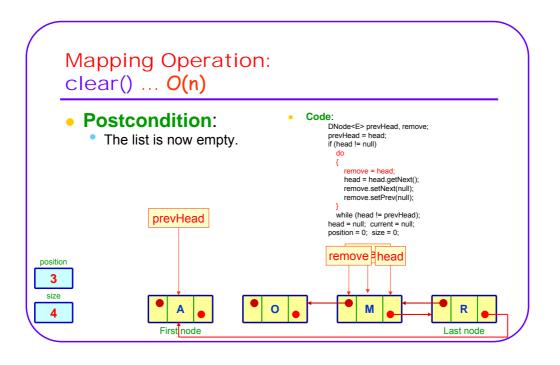


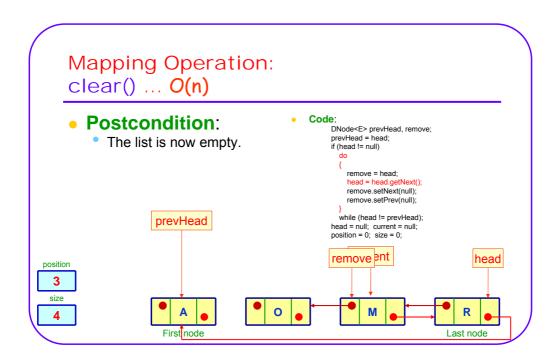


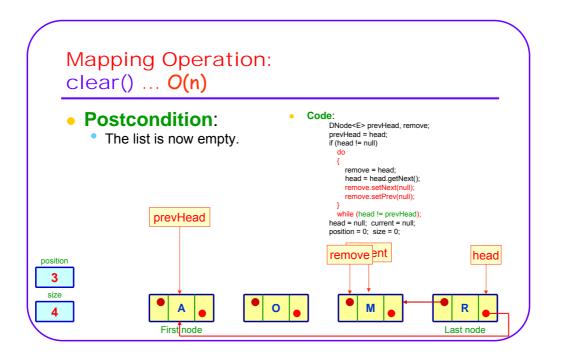


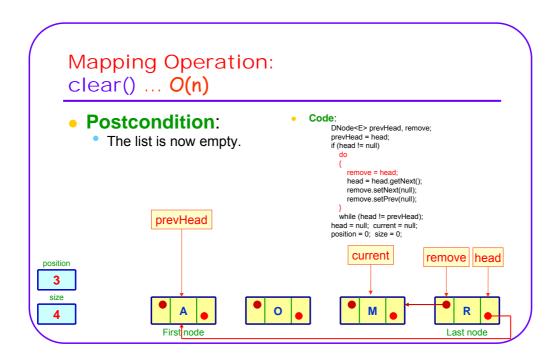


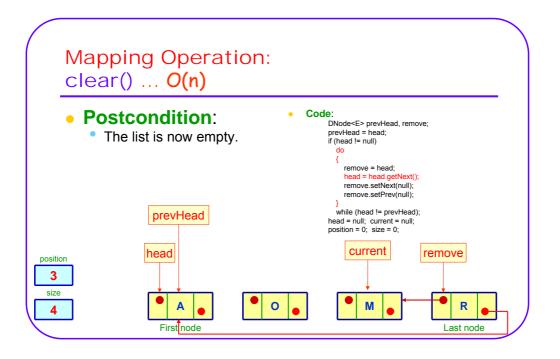


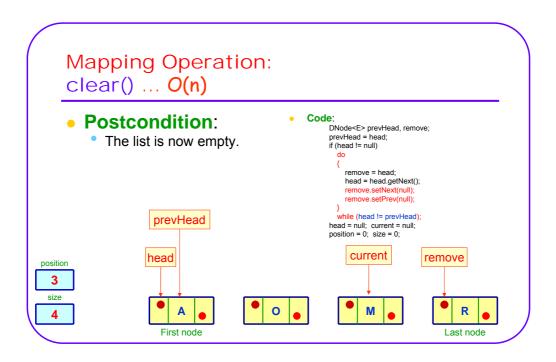


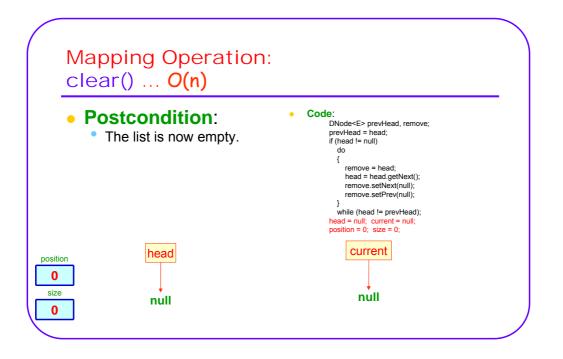












Mapping Operation: search(target) ... O(n)

Postcondition:

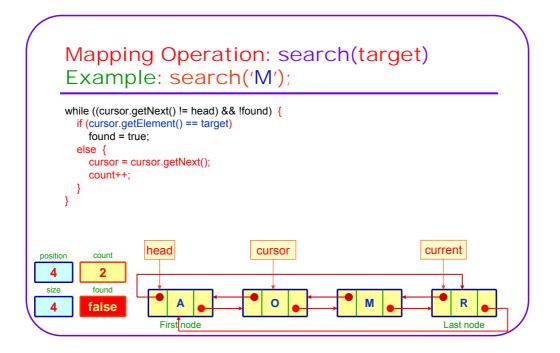
The list has been searched for the target. If the target was present, then the found target is now the current element. Otherwise, there is no current element.

```
code:
    int count = 1;
    boolean found = false;
    DNode<E> cursor = head;

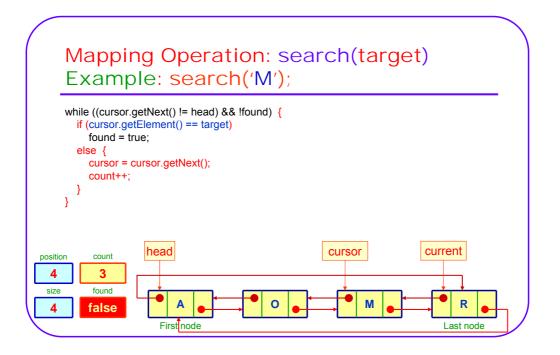
while ((cursor.getNext() != head) && !found) {
    if (cursor.getElement() == target)
        found = true;
    else {
        cursor = cursor.getNext();
        count++;
    }
}
if (found) {
    current = cursor;
    position = count;
}
else {
    current = null;
```

position = 0;

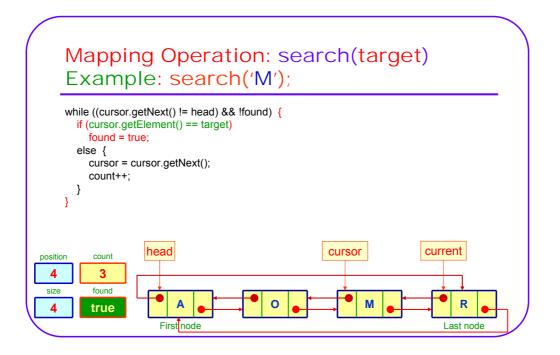
Mapping Operation: search(target) Example: search('M'); while ((cursor.getNext() != head) && !found) { if (cursor.getElement() == target) found = true; else { cursor = cursor.getNext(); count++; } head cursor current 4 found 4 false Firstnode Last node



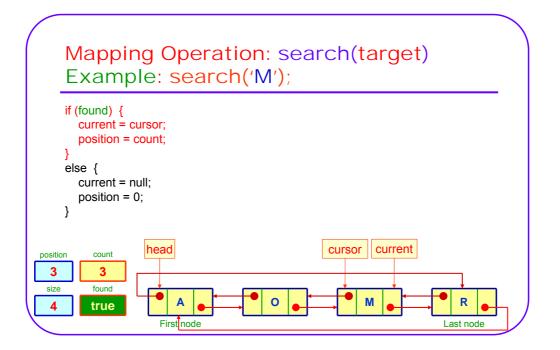
Mapping Operation: search(target) Example: search('M'); while ((cursor.getNext() != head) && !found) { if (cursor.getElement() == target) found = true; else { cursor = cursor.getNext(); count++; } head cursor current 4 found 4 false Firstnode Last node



Mapping Operation: search(target) Example: search('M'); while ((cursor.getNext() != head) && !found) { if (cursor.getElement() == target) found = true; else { cursor = cursor.getNext(); count++; } head cursor current 4 3 found 4 false Firstnode Last node



Mapping Operation: search(target) Example: search('M'); while ((cursor.getNext() != head) && !found) { if (cursor.getElement() == target) found = true; else { cursor = cursor.getNext(); count++; } head cursor current 4 3 4 true Firstnode Last node



Mapping Operation: search(target) Example: search('M'); if (found) { current = cursor; position = count; else { current = null; position = 0; } head current position 3 4 Firstnode Last node

Mapping Operation: addAfter(entry) ... O(1)

- Precondition:
 - size() < CAPACITY.
- Postcondition:
 - A copy of entry has been inserted in the list after the current element. If there was no current element, then the new entry has been attached to the end of the list. In either case, the newly inserted element becomes current.

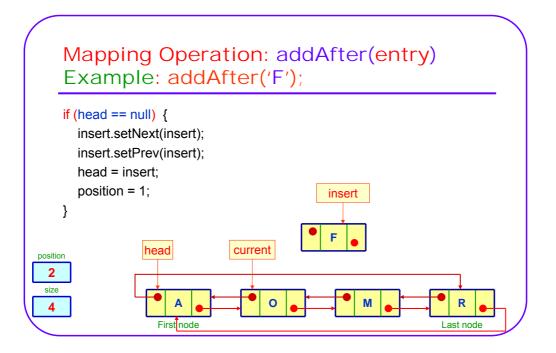
```
Code:
    DNode<E> insert;
    insert = new DNode<E>(entry, null, null);
    if (head == null) {
        insert.setNext(insert);
        insert.setPrev(insert);
        head = insert;
        position = 1;
    }
    else {
        if (position == 0) last();
        insert.setNext(current.getNext());
        insert.setPrev(current);
        current.getNext() setPrev(insert);
        current.setNext(insert);
        ++position;
    }
    current = insert;
    ++size;
```

```
Mapping Operation: addAfter(entry)
Example: addAfter('F');

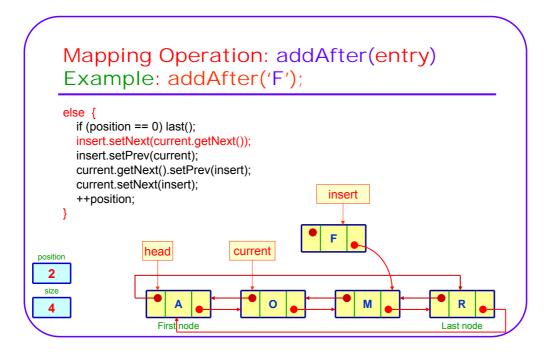
DNode<E> insert;
insert = new DNode<E>('F', null, null);

position

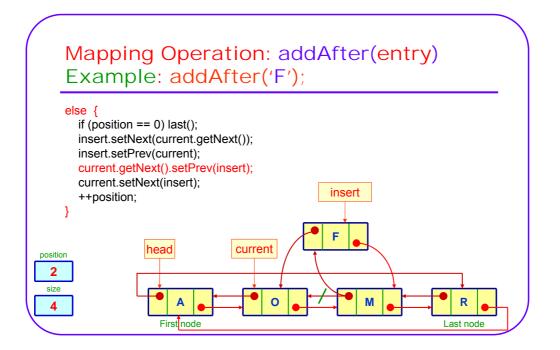
position
```



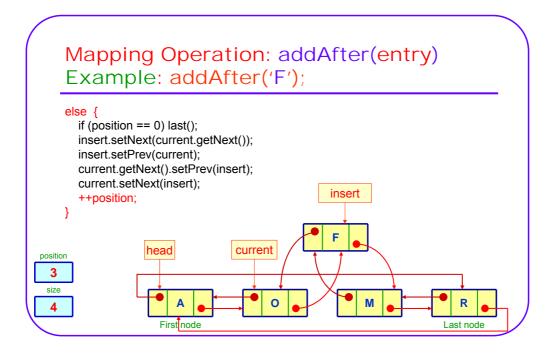
```
Mapping Operation: addAfter(entry)
  Example: addAfter('F');
  else {
    if (position == 0) last();
    insert.setNext(current.getNext());
    insert.setPrev(current);
    current.getNext().setPrev(insert);
    current.setNext(insert);
                                            insert
    ++position;
                             current
               head
2
4
                 Firstnode
                                                               Last node
```



```
Mapping Operation: addAfter(entry)
  Example: addAfter('F');
  else {
    if (position == 0) last();
    insert.setNext(current.getNext());
    insert.setPrev(current);
    current.getNext().setPrev(insert);
    current.setNext(insert);
                                             insert
    ++position;
                             current
               head
2
4
                 Firstnode
                                                               Last node
```



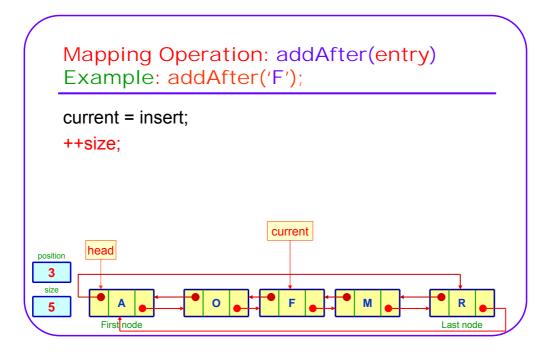
```
Mapping Operation: addAfter(entry)
  Example: addAfter('F');
  else {
    if (position == 0) last();
    insert.setNext(current.getNext());
    insert.setPrev(current);
    current.getNext().setPrev(insert);
    current.setNext(insert);
                                            insert
    ++position;
               head
                             current
2
4
                 Firstnode
                                                               Last node
```



```
Mapping Operation: addAfter(entry)
Example: addAfter('F');

current = insert;
++size;

position
3
size
4
```



Mapping Operation: addBefore(entry) ... O(1)

- Precondition:
 - size() < CAPACITY.
- Postcondition:
 - A copy of entry has been inserted in the list before the current element. If there was no current element, then the new entry has been inserted at the front of the list. In either case, the newly inserted element becomes current.

Code:

```
if ((head != null) &&
     (position != 0)) {
     current = current.getPrev();
     --position;
}
addAfter(entry);
if (current.getNext() == head) {
     head = current;
     position = 1;
}
```

```
Mapping Operation: addBefore(entry)
Example: addBefore('F');

if ((head != null) && (position != 0)) {
    current = current.getPrev();
    --position;
}
```

```
Mapping Operation: addBefore(entry)
Example: addBefore('F');

if ((head != null) && (position != 0)) {
    current = current.getPrev();
    --position;
}
```

```
Mapping Operation: addBefore(entry)

Example: addBefore('F');

if ((head != null) && (position != 0)) {
    current = current.getPrev();
    --position;
}
```

```
Mapping Operation: addBefore(entry)
Example: addBefore('F');

addAfter('F');

if (current.getNext() == head) {
    head = current;
    position = 1;
}

position

incomplete the property of t
```

```
Mapping Operation: addBefore(entry)
Example: addBefore('F');

addAfter('F');

if (current.getNext() == head) {
    head = current;
    position = 1;
}
```

```
Mapping Operation: addBefore(entry)

Example: addBefore('F');

addAfter('F');

if (current.getNext() == head) {
    head = current;
    position = 1;
    }

position

A

First node

Last node
```

```
Mapping Operation: addBefore(entry)
Example: addBefore('F');

addAfter('F');

if (current.getNext() == head) {
    head = current;
    position = 1;
}
```

```
Mapping Operation: addBefore(entry)
Example: addBefore('F');

addAfter('F');

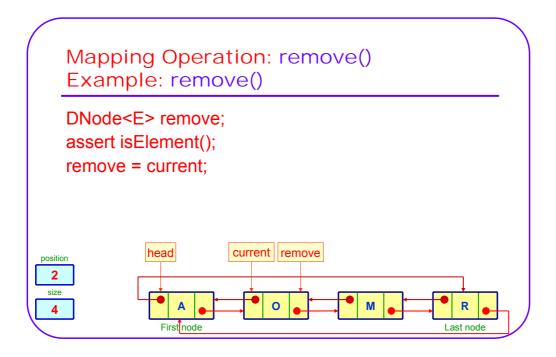
if (current.getNext() == head) {
    head = current;
    position = 1;
}
```

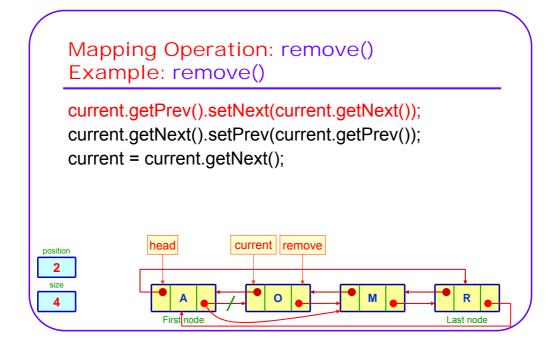
Mapping Operation: remove() ... O(1)

- Precondition:
 - isElement() returns true.
- Postcondition:
 - The current element has been removed from the list, and the one after it (if there is one) becomes current.
- Example:

Remove();

Code: DNode<E> remove; assert isElement(); remove = current: current.getPrev().setNext(current.getNext()); current.getNext().setPrev(current.getPrev()); current = current.getNext(); if (remove.getNext() == head) position = 1; if (size == 1) { head = null; current =null; else if (head == remove) head = current; size--; remove.setNext(null); remove.setPrev(null);

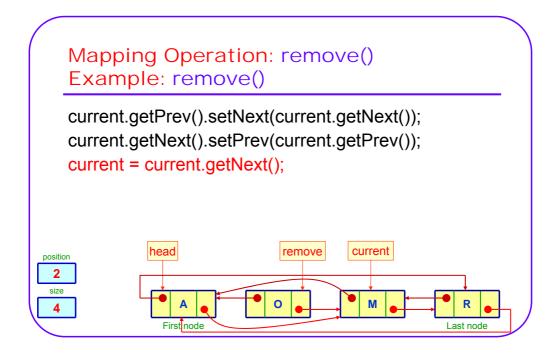




```
Mapping Operation: remove()

Example: remove()

current.getPrev().setNext(current.getNext());
current.getNext().setPrev(current.getPrev());
current = current.getNext();
```



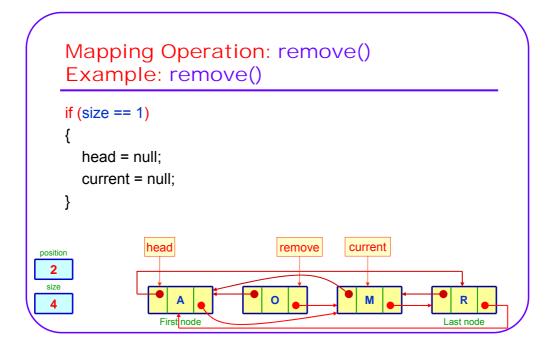
```
Mapping Operation: remove()

Example: remove()

if (remove.getNext() == head)
    position = 1;

position

2
size
4
```



```
Mapping Operation: remove()

Example: remove()

else
    if (head == remove)
    head = current;

position

2
size
4

A Print Index

Last node
```

