$$\dfrac{X \xrightarrow{f} Y}{(A,X) \xrightarrow{(A,f)} (A,Y)}(A,-) \quad ; \quad \dfrac{A \xrightarrow{\varphi} X}{A \xrightarrow{\varphi} X \xrightarrow{f} Y}(A,f)$$