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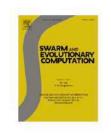


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Survey Paper

Induction of decision trees as classification models through metaheuristics



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ABSTRACT

The induction of decision trees is a widely-used approach to build classification models that guarantee high performance and expressiveness. Since a recursive-partitioning strategy guided for some splitting criterion is commonly used to induce these classifiers, overfitting, attribute selection bias, and instability to small training set changes are well-known problems in them. Other approaches, such as incremental induction, classifier ensembles, and the global search in the decision-tree-space, have been implemented to overcome these problems. In particular, metaheuristics such as simulated annealing, genetic algorithms, genetic programming, and ant colony optimization have been used to induce compact and accurate decision trees. This paper presents a state-of-the-art review of the use of single-solution-based metaheuristics and swarm and evolutionary computation algorithms to build decision trees as classification models. We outline the decision-tree-induction process components and detail the existing literature studies on metaheuristic-based approaches to building these classifiers. Several timelines showing the chronological order in which these approaches were introduced in the literature are included. A summary analysis of these studies is also conducted, focusing on their internal components and experimental studies. This work provides a useful reference point for future research in this field.

1. Introduction

Machine learning is an exciting artificial intelligence area whose objective is that an artificial entity becomes able to improve its performance (it learns) from the previously obtained results (its experience). Machine learning techniques have gained importance over the past few decades due to the growing demand for data analysis in diverse disciplines such as data science, business intelligence, and big data. The most representative machine learning approaches are supervised learning (a model is learned from labeled data) and unsupervised learning (a model is obtained from unlabeled data). The main supervised techniques are

classification and regression, while clustering is the most used unsupervised technique.

Han et al. [1] point out that data classification is a two-step process (Fig. 1) where a classification model is first built (learning step) and then is used to predict the class membership of new unclassified instances (classification step). The learning step uses a *training set* with several pre-classified instances. Each instance is composed of a collection of attribute values and one label identifying its class membership. In the classification step, the model performance is typically evaluated with its predictive accuracy, which is computed using the *test set*. Other criteria such as size, speed, robustness, scalability, and others can also be applied [2].

Abbreviations: AF, Aggregating fitness function; AP, Axis-parallel; B&B, Branch-and-bound; BNF, Backus-Naur form; CART, Classification and Regression Trees; CV, Cross-validation; DT, Decision tree; DTI, Decision tree induction; EA, Evolutionary algorithm; FF, Fitness function; GS, Global search; HH, Hyper-heuristic; LDA, Lineal discriminant analysis; MEP, Multi-expression programming; MF, Multi-objective fitness function; MH, Metaheuristic; MO, Multi-objective; MSMT, Multisurface method-tree; NL, Non-linear; OB, Oblique; PGM, Probabilistic graphical model; RH&R, Ramped half-and-half; RP, Recursive partitioning; RPART, Recursive and partition trees; S-Expressions; SF, Soft; SI, Swarm intelligence; SO, Subsequent optimization; SPV, Smallest-position-value; SS, Single-solution; UCI, University of California in Irving; UF, Single-objective fitness function.

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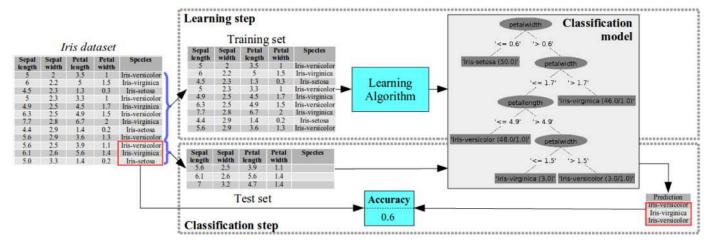


Fig. 1. The learning and classification steps in a classification process.

Among the most widely used classification methods are Bayesian classifiers, decision trees, artificial neural networks, and kernel-based algorithms. In particular, decision trees (DTs) are characterized by their simplicity in construction and interpretability, making them one of the most used classification methods. However, the vast majority of decision-tree-induction (DTI) procedures described in the existing literature implement a recursive-partitioning strategy through a greedy heuristic that fails to achieve desirable performance for some problems [3].

An effective strategy to search in large and complex solution spaces involves applying some swarm or evolutionary computation method. In particular, since genetic programming is an evolutionary algorithm using a tree representation to its candidate solutions, it is commonly used to find near-optimal DTs [4–6]. Furthermore, since genetic algorithms encode candidate solutions as sequences of values, their application for DTI is associated with the challenge of mapping a DT from a linear chromosome [7,8]. However, with the implementation of specialized genetic operators, they can use a tree encoding scheme [9,10]. Alternatively, there are few swarm-intelligence-based methods and other metaheuristics (MHs) for DTI. Among them, the use of simulated annealing [11], and ant-colony-optimization-based algorithms [12,13] stands out.

This paper presents a state-of-the-art review and a summary analysis of MH-based approaches for DTI. This review describes the studies concerning the construction of DTs using MHs and provides several timelines showing the chronological order in which these studies were published. Furthermore, the comparative analysis is conducted with a focus on their internal components and experimental studies. The rest of this document is organized as follows: Section 2 outlines the elements commonly considered when a DTI method is implemented and describes the main drawbacks of greedy heuristics for DTI. Furthermore, an overview of single-solution-based MHs and swarm and evolutionary computation methods is presented in Section 3, along with a description of (1) their implementation strategies, (2) their algorithm components (fitness function types, encoding schemes of candidates solutions, variation operators, and initialization procedures), and (3) their experimental studies elements (performance measures, sampling methods, and statistical tests). The state-of-the-art review of the use of single-solutionbased MHs and swarm and evolutionary computation algorithms to build DTs is presented in Sections 4, 5, and 6, respectively, and the use of hyper-heuristic-based approaches to make DTI methods is depicted in Section 7. Section 8 develops a comparative analysis of the algorithms components and the elements considered in their experimental studies. A general summary of the classification of the methods described in this review is also presented. Finally, Section 9 holds the open questions and conclusions of this review.

2. Decision tree induction

A DT is a white-box classification model representing its decisions through a tree-like structure composed of a set of nodes containing *test conditions* (internal nodes) and *class labels* (leaf nodes). Nodes are joined by arcs, symbolizing the possible outcomes of each test condition. DTs stand out for their simplicity and high interpretability level. Since the DTI process determines the importance of the attribute when builds test conditions, it provides a built-in feature selection mechanism [14]. These characteristics, along with its predictive power, allow placing DT as one of the most widely used classifiers.

The DTI procedure quality affects both the performance and expressiveness of induced DTs. This procedure involves (1) the splitting criterion measuring test condition quality, (2) the scheme to deal with numerical and categorical attributes, and (3) the mechanism to handle missing values. Furthermore, tree pruning techniques are also used to remove overfitting tree branches, trying to improve the induced tree's predictive power. Several studies have been conducted describing, analyzing, categorizing, and comparing DTI techniques such as those of Mingers [15], Safavian & Landgrebe [16], Brodley & Utgoff [17], Esposito et al. [18], Breslow & Aha [19], Murthy [20], Rokach & Maimon [21], Kotsiantis [22], Lomax & Vadera [23], Loh [24], Barros et al. [25], and Krętowski [26], among others.

2.1. Types of decision trees

According to the number of attributes evaluated in each test condition, two DT types can be induced: univariate and multivariate DTs. In a univariate DT, each test condition evaluates a single attribute to split the training set. Two advantages of univariate DTs are their comprehensibility and the simplicity of their induction algorithms. However, when the training instance distribution is complex, induced DTs include many internal nodes. Alternatively, a combination of attributes is used in each multivariate DT test condition. These classifiers commonly show better performance, and they are smaller than univariate DTs. Nevertheless, they are less expressive and require more computational effort to induce them.

Univariate DTs are also known as axis-parallel-DTs since their test conditions represent axis-parallel (AP) hyperplanes dividing the instance-space, similar to those shown in Fig. 2(a). If the test condition includes a numerical attribute, a hyperplane is defined as Eqn. (1).

$$x_i \le c, \tag{1}$$

where x_i is the *i*-th attribute value, and c is a threshold value used to define the partition.

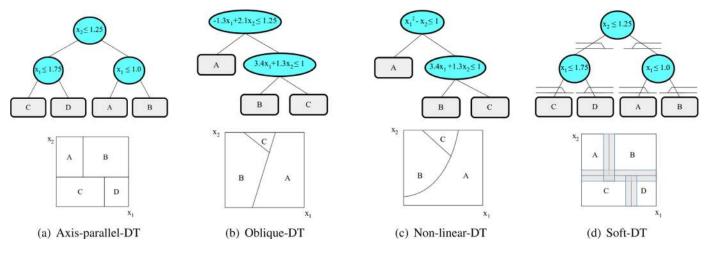


Fig. 2. Decision tree types (Adapted from [27] and [28]).

When a categorical attribute is evaluated, the following criteria are applied:

- Multi-branching: as many branches are created as values exist in the attribute domain,
- Binary-branching: the values of the attribute are grouped into two subsets,
- Numerical mapping: each categorical value is mapped as an integer value, and the attribute is treated as a numerical one, and
- Binary mapping: The categorical attribute is transformed into as many binary attributes as values exist in the attribute domain.

In the case of a linear combination of attributes, DTs are named oblique-DTs as their test conditions represent hyperplanes having an oblique (OB) orientation relative to the instance-space axes. An oblique hyperplane is defined as Eqn. (2).

$$\sum_{i=1}^{d} w_i x_i \le \theta \tag{2}$$

where w_i is a real-valued coefficient corresponding to the i-th attribute value x_i of a training set with d attributes, and θ is the independent term. Fig. 2(b) shows an example of one oblique-DT. Similarly, nonlinear-DTs produce curved hypersurfaces as they use a non-linear (NL) combination of attributes. For example, the test condition used in the DT's root-node shown in Fig. 2(c) represents a quadratic curve.

Moreover, *Wang* et al. [29] argue that uncertainty such as fuzziness and ambiguity should be incorporated into the DTI process. Soft-DTs implement a soft (SF) test at each internal node representing the probability that a branch of the node is selected based on the evaluation of its test condition. The soft-DT in Fig. 2(d) depicts a fuzzy-DT.

2.2. Splitting criteria

The splitting criterion applied to measure test condition quality is perhaps the element having the most significant impact on one classifier's effectiveness and expressiveness. These criteria can measure the partition impurity, estimate some other discriminant value or evaluate some cost value. Besides, considering the presence of uncertainty and ambiguity in the information, a soft measure should be included in a splitting criterion.

A typical way of grouping the vast number of splitting criteria found in the existing literature is as information-theory-based, distance-based, and other splitting criteria. Table 1 shows a representative set of these criteria.

Details of these splitting criteria are discussed in several surveys such as those of Safavian & Landgrebe [16], Murthy [20], Rokach & Maimon

[21], Lomax & Vadera [23], Lee et al. [40], and Barros et al. [25], among others.

2.3. Tree-pruning approaches

Kotsiantis [22] indicates that tree pruning permits to generalize the previously induced DTs by removing nodes and subtrees, avoiding overfitting, and improving the DT comprehensibility level. Cost-complexity pruning [34], reduced-error pruning [41], pessimistic-error pruning [41], and error-based pruning [30], are considered the most typical pruning methods. Detailed studies on tree-pruning have been carried out by Mingers [15], Reed [42], Esposito et al. [18], and Breslow & Aha [19], among others.

2.4. Recursive-partitioning problems

Most DTI methods described in the existing literature apply a recursive-partitioning strategy implementing some splitting criterion to separate the training instances. This plan is typically complemented by a pruning procedure, trying to improve the classifier performance. CART (Classification and Regression Trees) [34] and C4.5 [30] are the most common DTI algorithms implementing this induction strategy. However, several studies point out that recursive partitioning has three fundamental problems: overfitting, selection bias toward multi-valued attributes, and instability to small changes in the training set.

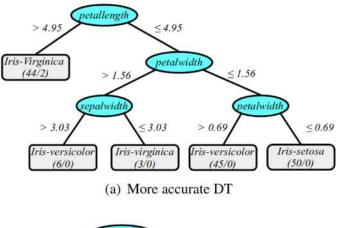
A DT suffers overfitting when its classification performance is lower than its learning performance and is more complex than necessary. *Mitra & Acharya* [43] indicate that this problem occurs when data contain noise or irrelevant attributes or a small training set exists. Additionally, several studies have shown that some splitting criteria are biased in choosing an attribute type over others, even though this selection affects DT performance [44,45]. For example, the information gain criterion and the Gini index are biased in favor of multi-valued attributes [46]. Finally, *Strobl* et al. [47] argued that the main problem of DTI methods is their instability to small changes in the training set. They remark that in recursive-partitioning, the exact position of the cutpoints and selection of the splitting attribute strongly depends on the particular training instances distribution.

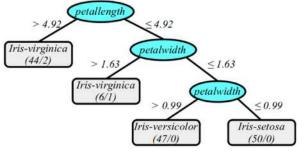
The incremental induction of trees [48], using classifier ensembles such as bagging, boosting, and random forest [49], as well as applying modern mixed-integer optimization techniques [50] are alternatives to avoiding these problems. Also, algorithms implementing a global-search strategy can ensure efficient solution-space exploration, although it is known that building optimal DTs is NP-Hard [51]. In particular, MH-based approaches for DTI allow creating more accurate DTs than those induced with traditional methods. MHs use intelligent search procedures

 Table 1

 Splitting criteria used for inducing decision trees.

Acronym	Description
Information	-theory-based splitting criteria:
GR	Gain ratio [30]
IG	Information gain [31]
Distance-ba	sed splitting criteria:
ClusterS	Cluster separation measure [32]
Dipolar	Mixed and pure dipoles (A dipole is a pair of training instances represented as vectors) [33]
Gini	Gini index [34]
LinearS	Degree of linear separability [35]
MarginS	Margin of separation [36]
Twoing	Twoing rule [34]
Other splitti	ing criteria:
MaxM	Max minority [37]
MDL	Minimum description length [38]
SSRE	Sum of square-root error [39]
SumM	Sum minority [37]
SumV	Sum of variances [37]





(b) More simple DT

Fig. 3. Two DTs induced by the DE-ADT^{SPV} method [8].

combining their exploration and exploitation skills, thus providing a better way of discovering relationships between training set attributes. Fig. 3 shows two DTs induced from the well-known iris dataset with an MH-based approach for DTI [8]. The first is more accurate, and the second is more compact than the DT induced by the J48 algorithm [52].

3. Metaheuristics for DTI

MHs are algorithmic templates simulating intelligent processes and behavior observed in both nature and other disciplines. They can be easily adapted to solve any complex problem [53,54]. MHs are characterized by combining the exploration of the solution space to identify promising areas with the exploitation of these areas to improve the known solution or solutions. They might provide or not provide optimal

Table 2
MHs used to induce decision trees.

Acronym	Description
Single-soluti	ion-based MHs:
GRASP	Greedy Randomized Adaptive Search Procedure [57]
SA	Simulated Annealing [58]
SLS	Stochastic Local Search [59]
TS	Tabu Search [60]
VNS	Variable Neighborhood Search [61]
Evolutionar	y Algorithms:
CEA	Co-Evolutionary Algorithms [62,63]
DE	Differential Evolution [64]
EDA	Estimation of Distribution Algorithm [65]
ES	Evolution Strategies [66,67]
GA	Genetic Algorithms [68]
GE	Grammatical Evolution [69]
GEP	Gene Expression Programming [70]
GGP	Grammar-based Genetic Programming [71]
GP	Genetic Programming [72]
TGP	Strongly-typed Genetic Programming [73]
Swarm Inte	lligence Methods:
ACO	Ant Colony Optimization [74]
BA	Bat Algorithm [75]
PSO	Particle Swarm Optimization [76]

solutions. However, MHs are typically largely satisfactory, in contrast to other techniques failing to solve the problem or spending excessive time finding the best solution.

Talbi [55] classifies these procedures as single-solution-based (SS-based) and population-based MHs. SS-based MHs conduct an intelligent search that iteratively replaces a solution with a neighboring one to reach a near-optimal solution. In contrast, population-based MHs use a group of candidate solutions in each step of their iterative process. Some generate new solutions by recombining information from the current population, and others update the solution properties. The most commonly used population-based MHs are related to evolutionary and swarm intelligence algorithms. Table 2 enumerates the MHs used to induce DTs.

Evolutionary algorithms (EAs) are inspired by theories synthesizing Darwinian evolution with Mendelian genetic inheritance. In each iteration of its evolutionary process (known as a generation), a group of candidate solutions (individuals) evolves by applying selection, recombination, and mutation operators. New populations are created until a stop condition is reached, then the best solution in the last population is returned. Commonly, two individuals (parents) are selected from the current population, and their values (genes) are recombined and typically mutated, creating new solutions (offsprings). Offsprings are considered part of the new generation.

Swarm intelligence (SI) methods are inspired by the collective behavior of some groups of animals such as ants, bees, or birds. *Vicsek & Zafeiris* [56] indicate that the main feature of collective behavior is that others' influence dominates the individual action. In SI methods, a group of candidate solutions (particles, agents) is moved in the solution-space by updating their properties, combining the local and global information of swarm transmitted by some communication type.

Finally, Du et al. [54] point out that a hyper-heuristic (HH) is a search procedure implemented to build algorithms that efficiently solve complex search problems. HHs explore one algorithm set to solve a problem instead of searching in the solution space.

Several surveys and reviews describing the implementation of MHbased approaches for DTI have been previously published. Galea et al. [77] analyze different EA-based strategies to automated fuzzy knowledge acquisition through DTs and classification rules. Espejo et al. [78] survey the existing literature on genetic-programming-based approaches generating DTs, classification rules, and discriminant functions. Jabeen & Baig [79] review several genetic-programming-based classification algorithms using decision trees, neural networks, and other rule induction methods. Kokol et al. [80] describe several EA-based approaches for DTI with a focus on their application in medical domains. Barros et al. [28] provide a detailed description of EAs inducing classification and regression trees. Also, they describe EAs implementing pruning methods and handling cost-sensitive mechanisms. Kolçe & Frasheri [81] summarize some approaches using genetic-algorithms, simulated annealing, and tabu search to inducing DTs. Finally, Krętowski [26] describes several EA-based DTI approaches, grouping them in evolutionary split searching, evolutionary meta-learning, and global evolution, Kozak [82] conducts a review of ant-colony-optimization-based algorithms with emphasis on decision rules, clustering, and decision trees, and Bida & Aouat [83] provide a brief analysis of the existing swarmbased DTI methods.

Unlike them, in this work:

- The three types of MHs and the HH-based methods to build DTI algorithms are included, not just EA-based approaches for DTI.
- Three types of implementation strategies are introduced, according to the place where an MH is used in the DTI process.
- The differences in the solution representation are highlighted, as they impact the MH-based implementation.
- The principal components of each method are detailed, such as fitness measures and variation operators.
- An analysis of the experimental studies conducted in these methods is provided.

Although DTs are used in other strategies such as classifier ensembles [49], multi-trees [84], multi-test tree [85], and regression trees [86], these models are excluded in this review. The first three determine the class membership of a new instance using different schemes than those defined for a DT, and regression trees use continuous class values.

In this review, each study is associated with some of the following implementation strategies:

- Recursive partitioning (RP): A DT is created like any traditional induction method, but an MH replaces the standard splitting criterion to obtain a better training instances separation. A candidate solution is a test condition, and, in this case, the MH is invoked as many times as internal nodes are required when inducing a DT.
- Global search (GS): One MH performs a global search in the decisiontree-space to find near-optimal DTs. Here, a candidate solution is a DT represented as a hierarchical structure or one sequence of values.
- Subsequent optimization (SO): Taking a DT previously induced by another classification method, the MH optimizes either the tree structure or some of its elements. Here, the MH conducts a postprocessing task since it does not induce one DT.

Fig. 4 shows a graphical scheme of these strategies. MH-based approaches for data preprocessing are not considered in this review. Al-

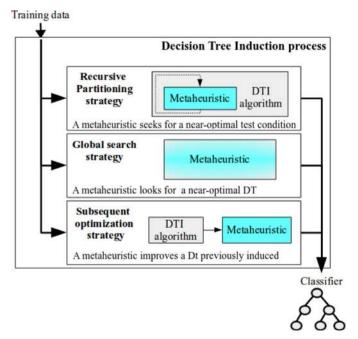


Fig. 4. Strategies implemented by the MH-based approaches for DTI.

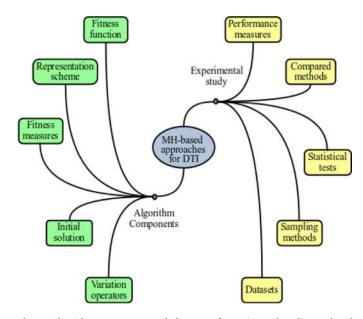


Fig. 5. Algorithm components and elements of experimental studies analyzed in this review.

though some MH-based techniques to manipulate the data involve creating a classifier (such as the wrapper schemes for feature subset selection), the MH is not applied on the DT but the data.

This work is organized according to the type of MH used and the type of DT induced. In each study, the implemented strategy, its main components, and the elements of its experimental studies are described (Fig. 5). In particular, two types of studies can be distinguished: those providing only a general description of their implementations [87–89] and others conducting several experiments to compare the method performance [8,10,11]. For the last case, the results obtained are compared with those of other methods such as C4.5 or CART. Table 3 shows the methods commonly used in the experimental studies reported in the existing literature.

Table 3Main methods used in the experimental studies of MH-based approaches for DTI.

Methods to build univariate DTs: C4.5 Quinlan [30] C5.0 Quinlan CHAID Chi-square automatic interaction detection [90] ID3 Quinlan [31] J48 Witten & Frank [52] REPTree Reduced-error pruning tree [52] RTree Random tree [52] Methods to build multivariate DTs: CART Classification and regression trees [34] CRUISE Classification rule with unbiased interaction selection and estimation method [91] QUEST Quick, unbiased, efficient, statistical tree [92] Other methods: CN2 Clark-Niblett method [93] kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49] SVM Support Vector Machines [98]	Method	Description
C5.0 Quinlan CHAID Chi-square automatic interaction detection [90] ID3 Quinlan [31] J48 Witten & Frank [52] REPTree Reduced-error pruning tree [52] RTree Random tree [52] Methods to build multivariate DTs: CART Classification and regression trees [34] CRUISE Classification rule with unbiased interaction selection and estimation method [91] QUEST Quick, unbiased, efficient, statistical tree [92] Other methods: CN2 Clark-Niblett method [93] kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	Methods to	build univariate DTs:
CHAID Chi-square automatic interaction detection [90] ID3 Quinlan [31] J48 Witten & Frank [52] REPTree Reduced-error pruning tree [52] RTree Random tree [52] Methods to build multivariate DTs: CART Classification and regression trees [34] CRUISE Classification rule with unbiased interaction selection and estimation method [91] QUEST Quick, unbiased, efficient, statistical tree [92] Other methods: CN2 Clark-Niblett method [93] kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	C4.5	Quinlan [30]
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REPTree Reduced-error pruning tree [52] RTree Random tree [52] Methods to build multivariate DTs: CART Classification and regression trees [34] CRUISE Classification rule with unbiased interaction selection and estimation method [91] QUEST Quick, unbiased, efficient, statistical tree [92] Other methods: CN2 Clark-Niblett method [93] kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	ID3	Quinlan [31]
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CART Classification and regression trees [34] CRUISE Classification rule with unbiased interaction selection and estimation method [91] QUEST Quick, unbiased, efficient, statistical tree [92] Other methods: CN2 Clark-Niblett method [93] kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	RTree	Random tree [52]
CRUISE Classification rule with unbiased interaction selection and estimation method [91] QUEST Quick, unbiased, efficient, statistical tree [92] Other methods: CN2 Clark-Niblett method [93] kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	Methods to	build multivariate DTs:
QUEST Quick, unbiased, efficient, statistical tree [92] Other methods: CN2 Clark-Niblett method [93] kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	CART	Classification and regression trees [34]
Other methods: CN2 Clark-Niblett method [93] kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	CRUISE	Classification rule with unbiased interaction selection and estimation method [91]
CN2 Clark-Niblett method [93] kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	QUEST	Quick, unbiased, efficient, statistical tree [92]
kNN k-nearest neighbors [94] LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	Other meth	ods:
LR Logistic regression [95] MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	CN2	Clark-Niblett method [93]
MLP Multi-layer perceptron [96] NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	kNN	k-nearest neighbors [94]
NB Naïve Bayes RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	LR	Logistic regression [95]
RBF-NN Radial-basis-function neural network [97] RF Random Forest [49]	MLP	Multi-layer perceptron [96]
RF Random Forest [49]	NB	Naïve Bayes
	RBF-NN	Radial-basis-function neural network [97]
SVM Support Vector Machines [98]	RF	Random Forest [49]
	SVM	Support Vector Machines [98]

Table 4Performances measures used in the summary analysis.

Name	Description					
Confusion-matrix-based performance measures:						
Accuracy	Accuracy					
Error	Error Rate or Misclassification Rate					
Miss-rate	Miss rate or False Negative Rate					
F-Score	F-Score, F-Measure or F ₁ Score					
Fall-out	Fall out or False Positive Rate					
Precision	Precision or Positive Predictive Value					
Sensitivity	Sensitivity, Recall or True Positive Rate					
Specificity	Specificity or True Negative Rate					
Other perform	nance measures:					
AUC	Area under cuve of ROC curve [108]					
Fidelity	Fidelity [109]					
HV	Hypervolume [110]					
J-Measure	J-Measure [111]					
MC	Misclassification cost					
ROC	ROC curve [112]					
Size	Complexity					
Stability	Stability [113]					
Time	Running Time					
Speedup	Speedup-ratio [114]					

3.1. Components of the MH-based approaches for DTI

Fitness function (FF): This function defines the quality measure used to guide the search for a near-optimal solution. Several splitting criteria (Table 1) and different performance measures (Table 4) have been used as quality measures. Both single-objective and multi-objective fitness functions have been used with these approaches. Only one quality measure is applied with a single-objective fitness function (UF), and two or more measures are assessed with a multi-objective fitness function.

Following the existing multi-objective (MO) optimization literature [99,100], two evaluation schemes are described in this review: On the one hand, an aggregating fitness function (AF) defines a weighted combination of measures to compute the fitness value. Weighting coefficients represent the relative importance of each measure in the combination. Alternatively, a multi-objective fitness function (MF) first evaluates each measure separately and then applies (1) a lexicographic-ordering criterion to rank the measures in order of importance, or (2) a Pareto-based fitness assignment strategy to find a set of non-dominated solutions. A solution is non-dominate if another solution does not exist with

better quality measure than the current one without worsening another quality measure [99].

Representation schemes: Candidate solutions have been encoded either with sequences of values or tree structures. Sequences of values are commonly used by several EAs such as genetic algorithms, grammatical evolution, and differential evolution, but genetic programming uses tree structures.

Variation operators: They are used to create new solutions through two strategies: (1) by altering the current solution values and (2) merging the information on several solutions. Each MH-based approach defines its variation operators based on the representation scheme adopted.

Initialization procedure: The random generation of initial solutions is the strategy most commonly implemented with these approaches. However, other MH-based methods for DTI reported in the existing literature start their search process either with a fixed initial solution [101] or create several variants of a DT induced by C4.5 as their initial population [102,103].

3.2. Elements of experimental studies

If the performance of one proposed method is evaluated in some studies, an experimental test is conducted using one or several datasets. When this performance is compared with those of similar procedures, one sampling method is used. Also, in some cases, statistical tests are conducted.

Datasets: Two types of datasets have been used for performance comparison. The University of California, Irvine (UCI) machine learning repository [104] provides the datasets collection most commonly employed to compare classifiers. Also, several studies evaluate datasets from diverse sources (artificial or private) in their experiments.

Performance measures: A performance measure such as accuracy, complexity, and running time is used to compare and evaluate the predictive power of a classifier [105–107]. Table 4 shows a list of performance measures.

Sampling methods: Sampling methods are accepted as validation schemes to determine the classifier generalization power [107]. Both cross-validation (CV) and hold-out are the most commonly used sampling methods [115,116]. Several CV variants such as k-fold CV [117] and 5×2 -CV [118] have been applied in these induction methods. Furthermore, bootstrap [119] is another method where a dataset is randomly sampled with replacement, generating small subsets of data. Although DTI using the complete dataset is not suitable to validate classi-

Table 5Statistical tests used to compare the performance of the MH-based approaches for DTI.

Name	Description
ANOVA	Analysis of variance [120]
Avg	Average result
Avg-R	Average ranks
Bergmann	Bergmann-Hommel test [123]
Bonferroni	Bonferroni-Dunn test [124]
Friedman	Friedman test [121]
Holm	Holm test [125]
Hommel	Hommel test [126]
Iman-D	Iman-Davenport test [127]
Kruskall	Kruskall-Wallis test [128]
Mann-W	Mann-Whitney U test [129]
Nemenyi	Nemenyi test [130]
t-test	Paired t-test
Tukey	Tukey test [131]
Shaffer	Shaffer test [132]
Wilcoxon	Wilcoxon test [133]
WTL	Counts of wins, ties and losses

Table 6
Acronyms used to identify several SS-based MH for DTI.

Acronym	Description
Stochastic L	ocal Search:
OC1	Oblique Classifier 1 [134]
OC1-AP	OC1 for axis-parallel DTs [135]
Simulated A	nnealing:
SACS	SA Classifier System [136]
SADT	SA of Decision Trees [37]
OC1-SA	OC1-based SA [137]
Tabu search	r.
EPTS	Extreme Point TS [138]
$LDSDT_{TS}$	Linear discrete support vector DT method [36]
LDTS	Linear Discriminant and TS [139]

fier performance, it has been applied in early-proposed methods, mainly to demonstrate its implementation feasibility.

Statistical tests: Table 5 describes the statistical tests employed to compare the performance of MH-based approaches. ANOVA [120] and Friedman test [121] are the statistical tests most commonly used to examine differences between experimental results. Luengo et al. [122] indicate that exist numerous post-hoc tests to determine whether an algorithm has statistical differences concerning other methods.

4. Single-solution-based metaheuristics for DTI

Table 6 lists the acronyms used to name SS-based MHs for DTIs, as defined by their authors. Others do not provide a name for their algorithms, and in this review, these last are identified with the authors reference. The timeline of these methods is shown in Fig. 6.

4.1. Axis-Parallel-DTs

Simulated Annealing: Three SA-based methods implement a subsequent-optimization strategy to improve a previously induced DT:

- Bucy & Diesposti [101,140] reconfigure a fixed-length binary DT created at random, either (1) exchanging two test conditions, (2) replacing a branch with a new set of test conditions, or (3) creating a new DT. After each modification, a pruning process is used to eliminate unfeasible subtrees.
- 2. Sutton [141] alters a DT induced by CART by shifting its partition boundaries.
- 3. Lutsko & Kuijpers [136] optimize a binary DT produced by ID3 in their SA Classifier System (SACS). SACS randomly selects one test

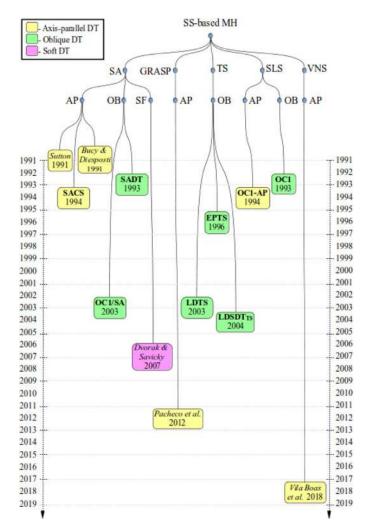


Fig. 6. Timeline of the SS-based MHs for DTI.

condition using a previously defined weighted distribution and replaces its attribute with an unused one.

In these methods, reconfigured DT is accepted as a new solution through the Boltzmann criterion.

GRASP: Pacheco et al. [142] implement one recursive-partitioning strategy using GRASP to build a binary DT. In each iteration, instead of choosing the attribute with the maximum information gain, GRASP randomly selects one from a set of attributes with the highest information gain values. A user-specified parameter defines the set size.

Variable Neighborhood Search: Vilas Boas et al. [143] apply VNS to improve the performance of a DT induced by C4.5. This method implements a subsequent-optimization strategy where an attribute is randomly changed in a test condition also selected at random, with leaf nodes' re-optimization.

4.2. Oblique-DTs

Several SS-based MHs have been used to build an oblique-DT in one recursive-partitioning strategy, as shown in Fig. 7. In this figure, $\mathbf{w}^T\mathbf{x} = \theta$ represents the hyperplane, \mathbf{w} is the vector of hyperplane coefficients, \mathbf{x} is the vector of attribute values, and θ is the independent term. Also, \mathbf{w}^s and \mathbf{x}^s are subsets of coefficients and attribute values, respectively, and \mathbf{w}' is the new vector of coefficients produced by the algorithm.

Stochastic Local Search: Murthy et al. [134] introduce the Oblique Classifier 1 (OC1) applying a two-step process to find a near-optimal hyperplane. First, by using a deterministic rule, OC1 adjusts the hyperplane

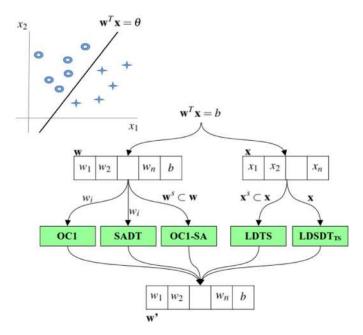


Fig. 7. Methods to build a new hyperplane using SS-based MHs.

coefficients, taking one by one and looking for its optimal value. Next, it applies SLS to jump out of a locally optimal solution. Also, an OC1 variant to induce an axis-parallel-DT, known as OC1-AP, is described in *Murthy* et al. [135].

Simulated Annealing: Heath et al. [37] describe the SA of Decision Trees (SADT) method that, starting with a fixed initial hyperplane, applies SA to improve its fitness value. In each iteration, SA modifies a single hyperplane coefficient that is chosen at random to adjust the hyperplane orientation. Furthermore, Cantú-Paz & Kamath [137] implement an OC1 variant known as OC1-SA, where SA simultaneously modifies several hyperplane coefficients. OC1-SA starts with the best axis-parallel hyperplane found by OC1-AP.

Tabu search: The Linear Discriminant and TS (LDTS) method of Li et al. [139] first selects at random a subset of attributes from the dataset. Then, one hyperplane is created using this subset through a Linear Discriminant Analysis (LDA). Finally, LDTS iteratively replaces an attribute in this subset with another one outside it. The new attribute is included in the subset while improving the hyperplane quality. The replaced attribute is added to the tabu list. Also, Orsenigo & Vercellis [36] use TS in the discrete support vector DT method (LDSDT $_{TS}$), implementing a linear discrete SVM (LDSVM) as its splitting criterion. A hyperplane is modeled as a mixed-integer linear program, which is solved using both

On the other hand, *Bennet & Blue* [138] describe the Extreme Point TS (EPTS) algorithm modifying a DT previously induced by the Multisurface Method-Tree (MSMT) [144]. DT is represented as a system of disjunctive linear inequalities, and TS is applied in the pivoting procedure of the Simplex method used to solve this system. An attribute is inserted into the tabu list when it leaves the basis of the system. The neighbors used by TS are the nonbasic attributes of the linear constraints. The best neighbor is one that, when it is considered one basic attribute, improves the fitness hyperplane value.

4.3. Soft-DTs

Simulated Annealing: Dvořák & Savický [145] implement a subsequent-optimization strategy to find the soft threshold values of the test conditions of an axis-parallel-DT induced by CART. Here, SA perturbs a subset of these values in each step of its iterative process.

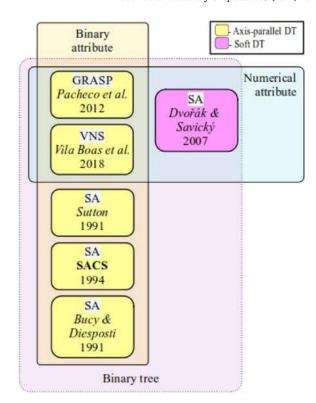


Fig. 8. DTs and attribute types used with SS-based MHs inducing axis-parallel-DTs

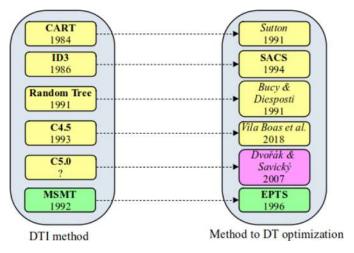


Fig. 9. Scheme used to subsequent-optimization with SS-based MHs.

4.4. Discussion

All methods described in this section induce binary DTs only. Fig. 8 shows the attribute and branch types of axis parallel DTs generated using these methods. In particular, the GRASP-based algorithm described by *Pacheco* et al. transforms categorical attributes into several binary attributes. Finally, Fig. 9 shows the scheme used for the methods implementing a subsequent-optimization strategy.

The components of these methods are described in Table 7, and the experimental analysis reported is summarized in Table 8. Two studies use an aggregating fitness function, and the remaining apply single-objective fitness functions. Six methods use a splitting criterion such as information gain and twoing rule as fitness measures. Several algorithms use performance measures such as error-rate and size. Furthermore, this table shows that the linear representation of candidate solu-

Stra- tegy	DT	FF	MH	Studies	Year	Repr. scheme	Fitness measures	Initial solution
RP	AP	UF	GRASP	Pacheco et al. [142]	2012	Tree	IG	•
	OB	UF	SLS	OC1 [134,135]	1993	Linear	IG, MaxM, SumM, SumV, Gini, Twoing	The best axis-parallel hyperplane found by OC1-AP
			SA	SADT [37]	1993	Linear	SumM	A fixed hyperplane
				OC1-SA [137]	2003	Linear	Twoing	The best axis-parallel hyperplane found by OC1-AP
			TS	LDTS [139]	2003	Linear	IG	A hyperplane constructed using LDA with a subset of attributes randomly selected from the dataset
		AF	TS	LDSDT _{TS} [36]	2004	Linear	Error+MarginS	A feasible hyperplane modeled as a linear mixed integer problem and solved using a truncated B&B
SO	AP	UF	SA	Sutton [141]	1991	Tree	Gini	A DT induced by CART
				SACS [136]	1994	Tree	MDL	A DT induced by ID3
		AF	SA	Bucy & Diesposti [101,140]	1991	Tree	Error+Size	A fixed-length DT randomly created
			VNS	Vila Boas et al. [143]	2018	Tree	Accuracy+Size	A DT induced by C4.5
	OB	UF	TS	EPTS [138]	1996	Tree	Error	A DT induced by MSMT
	SF	UF	SA	Dvořák & Savický [145]	2007	Tree	Error	A DT induced by C5.0

 Table 8

 Experimental analysis reported by SS-based MHs for DTI.

Stra-	DT	MH		Studies	Datas	ets	Sampling	Performance	Statistical	Compared methods
tegy	type				UCI	other	method	measures	tests	
RP	AP	GRASP		Pacheco et al. [142]	17	-	10-f CV	Accuracy, Size	Avg, WTL, t-test	Traditional DTI method
	OB	SLS		OC1 [134,135]	2	2	10-f CV	Accuracy, Size	-	ID3, SADT, kNN, MLP
		SA		SADT [37]	2	2	10-f CV	Accuracy, Size	-	ID3
				OC1-SA [137]	10	-	5-f CV	Accuracy, Size, Time	t-test	CART, OC1, OC1-ES, OC1-GA
		TS		LDTS [139]	13	-	10-f CV	Error, Size, Time	Avg, Tukey, ANOVA	C4.5, CART, OC1, QUEST, Linear tree [146]
				LDSDT _{TS} [36]	6	2	10-f CV	Accuracy, Size, Time	-	C4.5, OC1, SVM, QUEST, LDSDT _{B&B} [36] \mathbb{E}
SO	AP	SA		Bucy & Diesposti [101,140]	-	3	Complete dataset	Error, Size	-	Huffman algorithm [147]
				Sutton [141]	-	-		-	-	-
				SACS [136]	-	10	Hold-out	Error, Size	-	Gelfand-Ravishankar-Delp method [148]
		VNS		Vila Boas et al. [143]	-	308	10f-CV	Accuracy, Size, Time	-	Locally weighted learning [149], Sequential Minimal Optimization [150], Random Committee [52]
	OB	TS		EPTS [138]	5	3	5-f CV	Error	-	MSMT, Frank-Wolfe method [151]
	SF	SA	•	Dvořák & Savický [145]	-	1	Hold-out	Error	-	C5.0, CART

tions has only been used to build oblique-DTs. Finally, several strategies have been implemented to generate the first candidate solution: two studies create it randomly, and others start their search procedure with a previously induced DT.

K-fold CV is the sampling method most used in these studies, and only two apply the hold-out scheme. Furthermore, accuracy, error-rate, and size are the performance measures most commonly adopted in these methods. Finally, three studies use a statistical test to analyze their experimental results, and only one of them conducts one post-hoc analysis.

The use of only five SS-based MHs has been explored for DTI. Except for the GRASP-based method, they try improving an initial solution (internal node or decision tree) by applying an iterative strategy. All these approaches can suffer the same problems of traditional DTI procedures since they use one recursive-partitioning strategy or, in the subsequent-optimization case, start with a previously induced DT, limiting the search for solutions to that tree's neighborhood.

5. Evolutionary algorithms for DTI

EAs are the most widely used population-based MHs to induce DTs. Numerous EA-based approaches conduct a global search to find near-optimal DTs. However, recursive-partitioning and subsequent-optimization strategies have also been implemented with these MHs. Genetic algorithms and genetic programming methods are the EAs most commonly used for DTI.

Following the definitions and interpretations provided in the existing literature, two types of GAs-based approaches are described in this review: Genetic algorithms with linear chromosomes (LGA) and tree-based genetic algorithms (TGA), although there exists disagreement about whether to consider TGAs as genetic algorithms or genetic programming methods. Since one TGA disturbs the tree population in its evolutionary process, it can be regarded as a GP algorithm. Nevertheless, Koza [152] points out that GP individuals are generated by combining elements taken from function and terminal sets, and TGAs do not define any set to represent candidate solutions. In contrast, some authors point out that they implement a GP-based approach but build their trees without using the previously referred sets. In this review, analyzed studies are classified according to the definition provided in them. Table 9 illustrates the acronyms used to identify various GA-based MHs for DTIs, as defined by their authors. The timeline of GA-based approaches for DTI is shown in Fig. 10. Furthermore, the genetic operators used by these studies are described in Table 10.

5.1. Genetic algorithms with linear chromosomes

LGA can use binary, integer, or real-valued chromosomes. Since these chromosomes represent DTs, the next mapping is commonly applied (Fig. 11): First, the initial chromosome element is used as the tree root-node. Next, remaining elements are inserted in the tree as successor nodes of those previously added so that each new tree-level is completed before placing new nodes at the next one, similar to a breadth-first-search strategy. In univariate DTs, the number of successors of an internal node is calculated based on the attribute domain used in its test condition. For a multivariate DT, each internal node has two successor nodes.

5.1.1. Axis-Parallel-DTs

Kennedy et al. [7] introduce the Caltrop method, a global-search strategy evolving a population of DTs represented as sets of sub-trees. Each sub-tree with three nodes (a caltrop) is encoded with an integer-valued vector referring to binary attributes used as test conditions.

Chromosomes used in other approaches encode (1) nodes of a complete DT or (2) tree nodes' internal elements (attributes, class labels, and threshold values). In the first case:

1. Cha & Tappert [175,176] encode test conditions and leaf nodes with an integer-valued vector. One test condition is identified with the

- relative location of the binary attribute in a list of ordered attributes. Similarly, one leaf node is encoded with the location of its class label in its corresponding list.
- Bandar et al. [87] represent one internal node with an index identifying the evaluated attribute. Here, threshold values and leaf nodes are determined by evaluating the training set.
- 3. Evolutionary Classifier with Cost Optimization (ECCO) of *Omielan & Vadera* [155] use a binary chromosome to represent the test conditions of a complete DT by indexes identifying them. ECCO is used to induce cost-sensitive multi-branch DTs.

In the other case, the works of *Smith* [177] and *Ersoy* et al. [178], as well as the Evolutionary Algorithm for DTI (EVO-Tree) of *Jankowski* & *Jackowski* [157] implement similar approaches. They use two arrays to store the internal elements of nodes making up a binary DT: the one identifies attributes and class labels, and the other threshold values. Also, in the Bi-level GA (BiLeGA), *Adibi* [153] encodes only attributes indexes and threshold values in a numeric-valued chromosome.

Finally, *Grubinger* et al. [3] introduce the evtree (Evolutionary Tree) package using a variable-length numerical chromosome with attributes and splitting rules of a binary DT. Attributes are identified by an index of its dataset relative position, and splitting-rules contain threshold values.

Fig. 12 shows an example of these encoding schemes. A complete DT with three test conditions and four leaf-nodes is depicted. This tree is induced from a hypothetical training set with three binary attributes and two class labels.

András & Dumitrescu [171] apply an alternative encoding scheme named Multi-Expression Programming (MEP) 1 in the MEP-based DTI (MEPDTI) method where test conditions are encoded as functional symbols, and leaf nodes as terminals.

5.1.2. Oblique-DTs

LGA-based approaches commonly use a linear chromosome representing the hyperplane coefficients of one oblique-DT induced through a recursive-partitioning strategy. *Chai* et al. [154] implement the Binary Tree-Genetic Algorithm (BTGA) encoding these coefficients in a binary sequence. Furthermore, four studies use real-valued chromosomes: an OC1 variant (OC1-GA) of *CantA-Paz & Kamath* [11,137], the methods proposed by *Krętowski* [33] and *Pangilinan & Janssens* [180], and the Real-Coded GA-based Linear DT Algorithm with k-D Trees (RCGA-kDT) of *Ng & Leung* [173].

In particular, *Struharik* et al. [169] apply a GA variant² in the Here-Boy for DT (HBDT) method using a single fixed-length binary chromosome. *Vukobratovic & Struharik* [156] apply the same GA variant in the Evolutionary Full Tree Induction (EFTI) method with a single variable-length linear chromosome. EFTI grows the DT structure during its evolutionary process, starting with a one-node DT randomly created.

Alternatively, global search is conducted with the Generalized DT Inducer (GDTI) of *Dumitrescu & András* [167] that uses MEP to represent oblique-DTs.

5.1.3. Non-linear-DTs

Llorà & Garrell [162] and Llorà & Wilson [182] implement the Genetic and Artificial Life Environment (GALE), a parallel global-search strategy evolving a population of DTs placed in a two-dimensional grid. DTs can be axis-parallel, oblique, or non-linear DTs. In particular, non-linear-DTs use hyper-spheres as test conditions.

Alternatively, two studies implement a recursive-partitioning strategy to build one non-linear DT:

¹ MEP [179] defines a linear chromosome composed of variable-length genes. Each gene encodes a terminal or a functional symbol. Functional symbols contain functions taking as arguments the indices of other elements.

² The HereBoy algorithm (HBA) [181] is a particular GA evolving a unique binary chromosome using a mutation operator only.

Table 9Acronyms used to identify several GA-based MH for DTI.

Acronym	Description
BiLeGA	Bi-level GA [153]
BTGA	Binary Tree-GA [154]
Caltrop	Caltrop algorithm [7]
ECCO	Evolutionary Classifier with Cost Optimization [155]
EFTI	Evolutionary Full Tree Induction [156]
EVO-Tree	Evolutionary Algorithm for DTI [157]
evtree	Evolutionary Tree [3]
FVBDT	Fuzzy Variable-Branch DT [158]
G-DT	Genetically optimized fuzzy-DT [159]
GA-FID3	GA for Fuzzy ID3 [160]
GA-QDT	GA-based Quadratic DT method [161]
GAIT	GA inducing trees [102]
GALE	Genetic and Artificial Life Environment [162]
GATree	Genetically Evolved DTs [163]
GC-SDT	Genetically optimized Cluster oriented Soft DTs [39]
GDT	Global EA for DTI [9]
GDT-MA	GDT with local-search [164]
GDT-MC	GDT for cost-sensitive classification [165]
GDT-Mix	Global Induction of Mixed DTs [166]
GDTI	Generalized DT Inducer [167]
GEA-ODT	Global EA for oblique DTI [166]
genTrees	Genetic decision trees [168]
HBDT	HereBoy for DT method [169]
IIVFDT	Ignorance functions based Interval-Valued Fuzzy DT with genetic tuning [170]
LEGAL-Tree	Lexicographic GA for Learning DTs [10]
MEPDTI	MEP-based DTI method [171]
MS	Meta-Silvae [113]
NLDT	Non-linear DT method [172]
OC1-GA	OC1-based Genetic Algorithm [11]
RCGA-kDT	Real-Coded GA-based linear DT algorithm with k-D Trees [173]
TARGET	Tree Analysis with Randomly Generated and Evolved Trees [174]

Table 10Genetic operators used by EA-based approaches of DTI.

Acronym	Description
Selection operators:	
Tournament	Tournament-based selection
Roulette	Roulette-wheel-based selection
Exponential ranking	Exponential-ranking-based selection
Linear ranking	Linear-ranking-based selection
Truncate	Truncate-based selection
Assortative	Assortative mating
Crossover operators:	
Double-point	Double-point crossover
Uniform	Uniform crossover
Arithmetic	Arithmetic crossover
Single-point	Single-point crossover
Binomial	Binomial crossover
Mutation operators:	
Bit-string	Bit-string mutation
Flip-bit	Flip-bit mutation
Uniform	Uniform mutation
Non-uniform	Non-uniform mutation

 Ng & Leung [161,183] introduce the GA-QDT (GA-based Quadratic DT) method to find a near-optimal hypersurface used as test condition. Each hypersurface is modeled as Eqn. (3)

$$\mathbf{x}^T \mathbf{A} \mathbf{x} + \mathbf{b}^T \mathbf{x} > \theta \tag{3}$$

where ${\bf x}$ is a vector of attribute values, ${\bf A}$ is a symmetric matrix, ${\bf b}$ is a vector, and θ is the independent term in the inequality. Each GA-QDT chromosome encodes the values of ${\bf A}$, ${\bf b}$, and θ .

2. *Dhebar* & *Deb* [172] use a bilevel GA in their NLDT method. A population of linear combinations of power-law rules containing the dataset attributes evolve to find a near-optimal test condition. A power-law rule B is defined as Eqn. (4).

$$\mathbf{B} = \prod_{i=1}^{d} x_i^{b_i} \tag{4}$$

where x is an attribute value, d is the number of attributes, and $b = \{-3, -2, \dots, 2, 3\}$.

5.1.4. Soft-DTs

Janikow [184] and Chang et al. [160] implement similar recursive-partitioning strategies encoding the membership-functions used by one soft-DT test condition in a real-valued chromosome: The first uses the corners of trapezoidal functions, and the others represent the mean and variance of Gaussian functions in their GA for Fuzzy ID3 (GA-FID3).

The subsequent-optimization strategy is also used to create soft-DTs. Here, an LGA evolves chromosomes encoding fuzzy regions associated with all soft-DT test conditions. *Crockett* et al. [185] and *Sanz* et al. [170] use real-valued chromosomes: the first by optimizing piecewise-linear functions of a DT induced by ID3, and the second, in the IIVFDT (Ignorance functions based Interval-Valued Fuzzy DT with genetic tuning) method, improving the ignorance-degree³ associated with triangular functions of a DT induced by Fuzzy-ID3 [187]. Furthermore, in the Genetically optimized fuzzy-DT (G-DT) method, *Pedrycz & Sosnowski* [159] use a binary chromosome encoding membership-functions (piecewise-linear or Gaussian) of a DT induced by C4.5.

Alternatively, *Kim & Ryu* [188] implement a global-search strategy to create fuzzy-DTs, using a real-valued vector representing triangular functions.

DTI by clustering is also used to build soft-DTs in two approaches implementing a recursive-partitioning strategy, as shown in Fig. 13. The GC-SDT (Genetically optimized Cluster oriented Soft DTs) inducer of *Shukla & Tiwari* [39] encodes the centroids of instances groups, and the FVBDT (Fuzzy Variable-Branch DT) method of *Yang* [158] computes the number of branches outgoing from one internal node.

 $^{^3}$ Ignorance degree quantifies the uncertainty to assign membership values in fuzzy sets when a classifier is being trained [186].

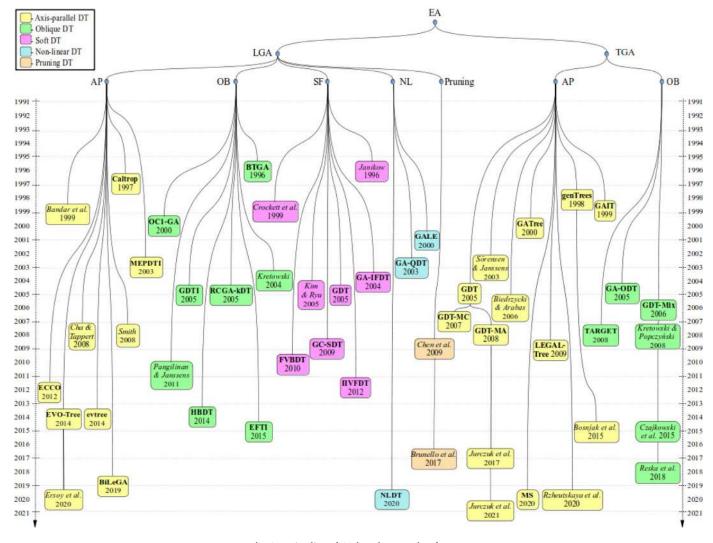


Fig. 10. Timeline of GA-based approaches for DTI.

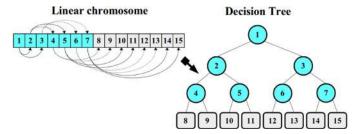


Fig. 11. Mapping strategy to build a DT from a linear chromosome.

5.1.5. DT Pruning

Two studies using binary-valued vectors have been conducted for DT pruning: *Chen* et al. [189] encode the edges, and *Brunello* et al. [190] represent the test conditions, of a DT induced by ID3 and J48, respectively. In these chromosomes, value 1 indicates that the element is removed from the DT, and its associated sub-tree is pruned.

5.1.6. Discussion

Most of the methods that build axis-parallel DTs use a breadth-first strategy to map a DT from a chromosome. However, two algorithms first apply a depth-first strategy to place internal nodes in a DT and then insert leaf nodes evaluating the training set [3,178].

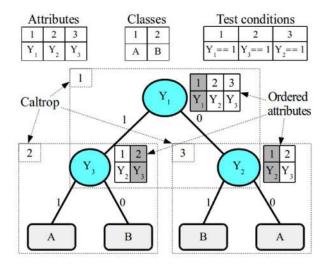
Criteria used to handle categorical attributes with LGA-based methods.

Criteria	Study
Multi-branching	ECCO [155], MEPDTI [171]
Binary-branching	evtree [3]
Numerical mapping	Ersoy et al. [178], EVO-Tree [157]

Fig. 14 shows the attribute and branch types of axis parallel DTs induced by previous studies, and Table 11 lists the criteria used to handle categorical attributes.

Fig. 15 shows the methods used in the studies implementing a subsequent-optimization strategy. Finally, since LGA-based methods encoding one axis-parallel DT on a linear chromosome, the chromosome's size is a priori defined (Table 12). However, some studies use a variable-length chromosome ([156,162,171]).

Table 13 summarizes the principal components of LGA-based methods for DTI. The single-objective fitness function is the tree-quality evaluation procedure most used in these studies, but seven works implement an aggregating fitness function, and only one uses a multi-objective fitness function. Ten studies evaluate some splitting criterion as fitness measure, and accuracy and size are most commonly utilized in those implementing global-search or subsequent-optimization strategies.



Caltrop [7]: Sequence of caltrops.

1 3 2 3 0 0 2 0 0

Bandar et al. [87]: Sequence of attributes.

1 3 2

Cha & Tappert [175, 176]: Sequence of ordered atributes.

1 2 1 * * * *

ECCO [155]: Sequence of test conditions.

0 0 1 0 1 0 0 1 1

EVO-Tree [157]: Sequences of attributes and thresholds.

1	3	2	null	null	null	null
1	1	1	1	0	0	1

Fig. 12. Linear chromosome representation of one DT.

Furthermore, some authors describe the genetic operators applying in their works, but others only report using some GA-based library such as GENESIS (Genetic Search Implementation System) [191], GENOCOP [192], and GALib [193]. Tournament and roulette-based selection, single-point and double-point crossover, as well as bit-string and uniform mutation, are the genetic operators most commonly applied by these LGAs, although several authors create ad hoc operators. Finally, the initial population in these works is commonly created at random,

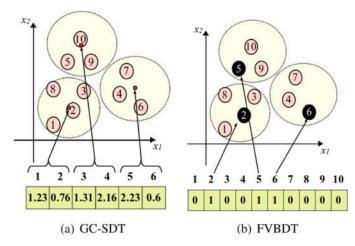


Fig. 13. Linear chromosome representation for clusters-based DTI.

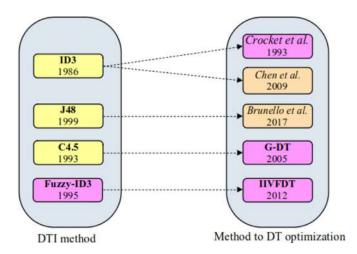


Fig. 15. Scheme used to subsequent-optimization with LGA-based MHs.

but only OC1-GA introduces several copies of the best axis-parallel hyperplane found by OC1-AP in its initial population.⁴

⁴ A bisecting hyperplane is that containing the normal vector to the segment connecting two instances with different class labels. This hyperplane cuts that segment into two equal parts.

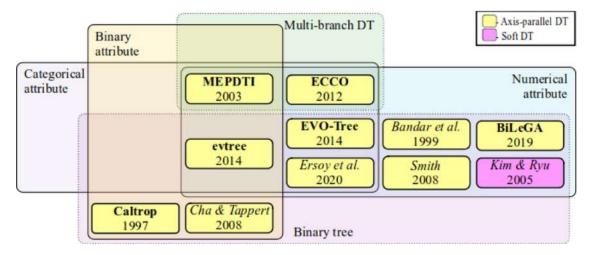


Fig. 14. DTs and attribute types used with LGA-based MHs inducing axis-parallel-DTs.

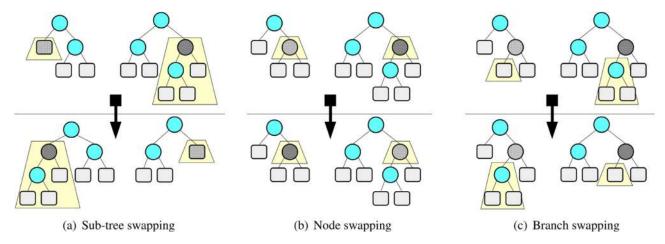


Fig. 16. Crossover operators used by tree-based chromosomes (Adapted from [163], [88], [204], [9], and [205]).

 Table 12

 Size of a linear chromosome encoding axis-parallel DTs.

Study	Number of genes
Caltrop [7]	72
Bandar et al. [87]	63
MEPDTI [171]	Variable
Cha & Tappert [175]	127
Smith [177]	$2^{h+1} - 1 \mid h$ is the number of attributes
ECCO [155]	$2^h - 1 \mid h \in [5, 11] \text{ or } 50,000$
evtree [3]	Variable
EVO-Tree [157]	$2^h - 1 \mid h$ is a user-specific value
BiLeGA [153]	$2(2^h - 1) \mid h$ is the number of attributes
Ersoy et al. [178]	$2(2^h - 1) \mid h \in [2, 5]$

Table 14 summarizes the experimental studies of these approaches. K-fold CV and hold-out are the sampling methods most commonly applied in these works. Test accuracy and the tree size are computed to determine the method performance in most of these studies. Finally, only eleven studies report applying a statistical test to compare their experimental results, and three of them apply a post-hoc analysis after finding statistical differences.

LGA-based approaches for DTI are competitive methods to build precise classifiers. However, some only induce DTs with a particular attribute type (binary or numerical attributes, for example). In particular, LGA is the MH most used to induce soft-DTs. A drawback for some LGA-based methods is that the chromosome size is defined without considering the dataset characteristics, affecting the model performance.

5.2. Tree-based genetic algorithms (TGA)

When GAs use tree-like chromosomes, several specialized genetic operators to build valid offsprings have been implemented in the studies found in the existing literature. Table 15 details these operators, and Figs. 16 and 17 show a graphical scheme for each one.

5.2.1. Axis-Parallel DTs

Several approaches implementing a global search of DTs with numerical and categorical attributes have been developed, such as:

- The GATree (Genetically Evolved DTs) method of Papagelis & Kalles [163,206].
- Global EA for DTI (GDT) and its variants for cost-sensitive classification (GDT-MC), and with local-search (GDT-MA) of *Krętowski & Grześ* [9,164,165], as well as its parallel versions of *Jurczuk* et al. [207–209].
- 3. The genetic decision trees (genTrees) induction method of *Podgorelec* & *Kokol* [168].

In particular, to reduce processing time: (a) all possible thresholds are pre-calculated in GDT [9], (b) the reuse of fitness values is applied in the GATree latest version [206], and (c) the implementation of diverse parallel approaches are conducted [207–209].

Furthermore, *Basgalupp* et al. [10] propose LEGAL-Tree (Lexicographic GA for Learning DTs), a multi-objective GA inducing DTs encoded as a collection of decision stumps⁵ A lexicographic scheme using tolerance thresholds is used to select either accuracy or size as the fitness value. They improve LEGAL-Tree by including a beam-search-procedure to create the initial population and applying a statistical test in the selection operator [205]. Finally, to prevent premature algorithm convergence, *Bosnjak* et al. [210] introduce diversity in the population through a modified selection operator: One DT is selected based on its fitness value, and the other according to its similarity level.

Alternatively, some studies induce DTs with specific attribute types:

- Fu [102], Fu & Mae [211] and Fu et al. [204,212-214] implement several variants of GAIT, a method to evolve binary DTs with numerical attributes.
- 2. Ranzato & Zanella [113] also evolve DTs with numerical attributes in their Meta-Silvae (MS) method.
- 3. Sörensen & Janssens [88] evolve DTs with binary attributes.
- 4. Biedrzycki & Arabas [215] use categorical attributes, only.

Different from previous methods, *Rzheutskaya* et al. [216] implement a recursive-partitioning strategy to build a DT by selecting the best split criterion (information gain, Gini, and others) for each test condition.

5.2.2. Oblique DTs

In Global EA for oblique DTI (GEA-ODT) of *Krętowski & Grześ* [217,218] a population of oblique DTs is evolved. GEA-ODT implements a global-search strategy to find the DT structure and the hyperplane coefficients used as test conditions. Furthermore, they implement the GDT-Mix (Global Induction of Mixed DTs) method to build DTs with univariate and oblique test conditions [166]. GDT-Mix has been used to build three parallel versions by *Krętowski & Popczyński* [219], *Czajkowski* et al. [114], and *Reska* et al. [220]. Finally, *Gray & Fan* [174] modify their regression tree induction approach, known as TARGET (Tree Analysis with Randomly Generated and Evolved Trees), to induce nearoptimal oblique DTs. The hyperplanes can be constructed using up to three attributes.

5.2.3. Discussion

Fig. 18 shows the attribute and branch types of the axis-parallel DTs induced with the studies described previously. Table 16 lists the criteria used to handle categorical attributes.

⁵ A decision stump is a DT with one internal and two leaf nodes.

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Table 13Components of LGA-based approaches for DTI.

Stra-	DT	FF	Studies	Year	Fitness	Genetic operato	rs		Initial population
tegy					measure	Selection	Crossover	Mutation	_
RP	ОВ	UF	· BTGA [154]	1996	Gini	Roulette	Double-point	Bit-string	Bisecting hyperplanes ⁴ randomly created
			· OC1-GA [11,137]	2000	Twoing	Tournament	Uniform	N/A	Hyperplanes randomly created with several copies of the best axis-parallel hyperplane found by OC1-AP
			· Krętowski [33]	2004	Dipolar	Roulette	Double-point	Special	Bisecting hyperplanes randomly created
			· RCGA-kDT [173]	2005	IG	Roulette	Arithmetic	Special	Bisecting hyperplanes randomly created
			· Pangilinan & Janssens [180]	2011	Twoing	Tournament	Arithmetic	Non-uniform	Hyperplanes randomly created with one axis-parallel hyperplane randomly created
			· HBDT [169]	2014	IG	N/A	N/A	Bit-string	One bisecting hyperplane passing through the centre point of a set of training instances
	NL	UF	· GA-QDT [161,183]	2003	Gini	Roulette	Double-point	Non-uniform	Quadric hypersurfaces randomly created
			· NLDT [172]	2020	Gini	Tournament	Special	Special	Linear combinations of power-law functions with one attribute randomly created
	SF	UF	· Janikow [184]	1996	IG	G	ENOCOP genetic op	erators	Numerical chromosomes randomly creared
			· GC-SDT [39]	2009	SSRE	Tournament	Double-point	Bit-string	Binary chromosomes randomly created
		AF	· GA-FID3 [160]	2004	Accuracy+Size	-	-	-	Numerical chromosomes randomly created
			· FVBDT [158]	2010	Error+Size	Roulette	Double-point	Bit-string	Binary chromosomes randomly created

(continued on next page)

Table 13 (continued)

Stra-	DT	FF	Studies	Year	Fitness	Genetic operato	ors		Initial population
tegy					measure	Selection	Crossover	Mutation	
GS	AP	UF	· Caltrop [7]	1997	Size	Assortative	Single-point	Uniform	Integer chromosomes randomly created
			· Bandar et al. [87]	1999	Accuracy	-	-	-	Integer chromosomes randomly created
			· MEPDTI [171]	2003	Accuracy	Tournament	Double-point	Special	Integer chromosomes randomly created
			· Cha & Tappert [175,176]	2008	Size	-	Single-point	Uniform	Integer chromosomes randomly created
			· ECCO [155]	2012	MC	(GENESIS genetic ope	erators	Binary chromosomes randomly created
			· evtree [3]	2014	Error	Special	Special	Special	Numerical chromosomes with one test condition
			· BiLeGA [153]	2019	Accuracy	Roulette	Double-point	Special	Numerical chromosomes randomly created
			• Ersoy et al. [178]	2020	Accuracy	Roulette	Single-point, Double-point	Uniform	Numerical chromosomes randomly created, CART-based DTs
		AF	· Smith [177]	2008	Error+Time	-			Integer chromosomes randomly created
			· EVO-Tree [157	2014	Error+Size	Roulette	Single-point	Uniform	Numerical chromosomes randomly created
	OB	UF	· GDTI [167]	2005	Accuracy	Tournament	Special	Special	Integer chromosomes randomly created
		AF	· EFTI [156]	2015	Accuracy+Size	N/A	N/A	Special	A hyperplane of a one-node DT
	NL	UF	· GALE [162,182	2] 2001	Accuracy	Special	Single-point	Uniform	Integer chromosomes randomly created
	SF	AF	· Kym & Ryu [188]	2005	Accuracy+Size	Roulette	Special	Special	Numerical chromosomes randomly created
SO	AP	AF	· Chen et al. [18	9] 2009	Error+Size	Roulette	Single-point	Flip-bit	Binary chromosomes randomly created
		MF	· Brunello et al.	2017	Accuracy,Size	Tournament	Special	Flip-bit	Binary chromosomes randomly created
	SF	UF	· Crockett et al.	1999	Accuracy	(GENESIS genetic ope	erators	Numerical chromosomes randomly created
			· G-DT [159]	2005	Error		GALib genetic oper	ators	Numerical chromosomes randomly created
			· IIVFDT [170]	2012	Accuracy	Tournament	Uniform	Uniform	Numerical chromosomes randomly created

Table 14Experimental analysis reported by LGA-based approaches for DTI.

tegy								
			UCI	other	method	measures	tests	
RP	OB	· BTGA [154]	1	3	3-f CV	Error, Size	-	C4.5 variant, Principal
								component analysis [194],
								Fisher's linear-ratio method
								[195]
		· OC1-GA [11,137]	10	-	5-f CV	Accuracy, Size,	t-test	CART, OC1, OC1-ES, OC1-S
		W	4	4	10 f CV	Time		0.01 0.01 0.4
		· Krętowski [33]	4	4	10-f CV	Accuracy, Size, Time	-	OC1, OC1-GA
		· RCGA-kDT [173]		4	2-f CV	Accuracy, Time	-	C4.5, OC1, OC1-GA, OC1-E
		· RCGA-RD1 [1/3]	•	7	2-1 GV	Accuracy, Time	-	BTGA, Linear tree [146]
		· Pangilinan & Janssens [180]	6	1	5-f CV	Accuracy, Size,	_	C4.5 variant, OC1
		Talganara a balasela [100]	Ü	-	51 GV	HV		ono variant, our
		· HBDT [169]	26	-	10-f CV	Accuracy, Size	ANOVA, Tukey	CART, OC1, OC1-AP,
						**	, ,	OC1-SA, OC1-GA, OC1-ES,
								GALE, GATree
	NL	· GA-QDT [161,183]	2	2	10-f CV	Accuracy, Time	t-test	C4.5, C5.0, OC1, OC1-GA,
								OC1-ES, BTGA, Linear
								machine DT [196],
								Non-linear DT [197]
		· NLDT [172]	2	7	Hold-out	Accuracy, Size	Wilcoxon	CART, SVM
	SF	· Jakinow [184]	-	1	Hold-out	Accuracy	-	-
		· GA-FID3 [160]	5	-	-	Accuracy, Size	-	C4.5, Rank-based ID3 [198
		· GC-SDT [39]	6	-	5-f CV	Error, Size	t-test	C4.5, Clustered-oriented
								fuzzy DT (C-fuzzy DT) method [199]
		· FVBDT [158]	8	2	10-f-CV	Accuracy		ID3, C-fuzzy DT, Merging
		· IVBDI [136]	8	2	10-1-CV	Accuracy	-	branches method[200],
								Yeung et al. [201]
GS	AP	· Caltrop [7]		1	Complete	Size	-	ID3
		omer's to 1		_	dataset			
		· Bandar et al. [87]	2	-	Hold-out	Accuracy	-	-
		· MEPDTI [171]	11	-	Hold-out	Accuracy	-	C4.5, CN2, BGP
		· Cha & Tappert [175,176]	-	1	Complete	Size	-	-
					dataset			
		· Smith [177]	-	3	Hold-out	Time	-	-
		· ECCO [155]	4	-	Hold-out	MC	-	Inexpensive classification
								with expensive tests method
			_					[202]
		EVO-Tree [157]	7	-	5 × 2-CV	Accuracy, Size	Avg-R	C4.5, RTree, NB, MLP, SVN
		· evtree [3]	14	3	Bootstrap	Accuracy, Size	-	CART, Conditional inference
		· BiLeGA [153]	12		Hold-out	Accuracy	t toet	trees [45] C5.0, CART, SVM, ANN, LR
		• Ersoy et al. [178]	6	-	5-f CV	Accuracy, time	t-test	CART
	ОВ	· GDTI [167]	11	-	Hold-out	Accuracy		C4.5, CN2, BGP
	OB	· EFTI [156]	26	_	10-f CV	Accuracy, Size	ANOVA, Tukey	CART, OC1, OC1-AP,
		211 [100]	20		10101	ricearacy, oide	invovin, runcy	OC1-SA, OC1-GA, OC1-ES,
								GALE, GATree, HDBT
	NL	· GALE [162,182]	11	-	10-f CV	Accuracy	Avg, t-test	C4.5, CART, OC1
	SF	· Kym & Ryu [188]	7	-	-	Accuracy, Size	Avg	Yeung et al. [201], Abonyi
						-		et al. [203].
SO	AP	· Chen et al. [189]	4	-	Hold-out	Accuracy, Size	-	ID3
		· Brunello et al. [190]	12	-	Hold-out	Accuracy, Size	-	J48, C5.0
	SF	· Crockett et al. [185]	-	2	Hold-out	Accuracy	-	ID3
		· G-DT [159]	5	-	5-f CV	Error	-	C4.5
		· IIVFDT [170]	17	3	5-f CV	Accuracy	Avg, Holm,	C4.5, GA-FID3, Kym & Ryu
							Friedman, Wilcoxon	[188]

Table 15Genetic operators used by tree-based chromosomes.

Acronym	Description
Crossover operators:	
Swap sub-trees	Swaps sub-trees randomly chosen from two DTs.
Swap nodes	Swaps nodes chosen at random from two DTs. Sub-trees of these nodes remain unchanged.
Swap branches	Swaps branches randomly selected from two DTs.
Mutation operators:	
Disturb node	Modifies some internal element of one node chosen at random.
Switch nodes	Swaps two nodes randomly chosen in the same DT. Sub-trees of these nodes remain unchanged.
Switch sub-trees	Swaps two sub-trees selected at random from the same DT.
Insert node	Adds a new node randomly created in the DT.
Replace node	Replaces one node randomly chosen in the DT. Sub-tree can be replaced with a leaf node, or a leaf node can be changed with a new sub-tree.
Replace sub-tree	Replaces one sub-tree randomly chosen in a DT with a new sub-tree.

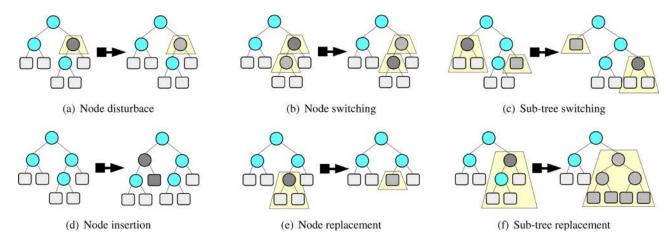
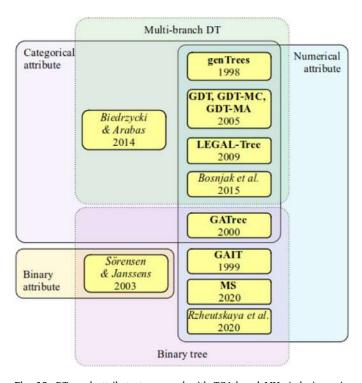


Fig. 17. Mutation operators used by tree-based chromosomes (Adapted from [163], [88], [204], [9], and [205]).

Table 16
Criteria used to handle categorical attributes with TGA-based methods.

Criteria	Study
Multi-branching Binary-branching	GDT [9], GDT-MC [165], GDT-MA [164], genTrees [168], LEGAL-Tree [10], Bosnjak et al. [210], Biedrzycki & Arabas [215] GATree [163]



 $\label{eq:Fig. 18. DTs} \textbf{ and attribute types used with TGA-based MHs inducing axis-parallel-DTs.}$

Components of TGA-based approaches for DTI are shown in Table 17. Single-objective and aggregating fitness functions are the evaluation schemes most used in these studies, and only one applies a multi-objective fitness function. Accuracy and size are the fitness measures most used in these works.

Tournament-based selection is used in three studies, and roulettewheel and linear-ranking-based selection operators have each been implemented in four studies. All studies apply sub-tree-swapping-based crossover, but node-swapping and branch-swapping have also been used. However, *Biedrzycki & Arabas* do not apply one crossover operator. They only use a node-insertion-based mutation to configure initial DTs. Furthermore, DTs' random creation is the most common scheme to build the initial population. However, GAIT uses C4.5 to inducing DTs with instance subsets chosen at random. LEGAL-tree uses a random combination of several decision stumps previously created.

Table 18 shows the experimental studies reported in the existing literature. K-fold CV and hold-out and test accuracy and size are the sampling strategies and the performance measures most used in these methods, respectively. *Bosnjak* et al. and *Basgalupp* et al. adopt F-score as their performance measure, and only GDT-MC implements a cost-sensitive classification approach. Finally, eight studies describe applying a statistical test, and only LEGAL-Tree applies one post-hoc analysis.

The use of tree-like chromosomes is an option to deal with the variable size of DTs. It is guaranteed that there is no loss of information since no mapping scheme is necessary to convert a chromosome into a DT. However, their use in GAs implies the definition of several variation operators to generate feasible solutions. Furthermore, it is necessary to apply two or more genetic operators to avoid the evolutionary process's stagnation.

5.3. Genetic programming (GP)

Fig. 19 shows the timeline of GP-based approaches for DTI. Table 19 illustrates the acronyms used to identify various GP-based MHs for DTIs, as defined by their authors. Standard genetic programming has been applied in many studies, but two GP variants have also been used: Grammar-based genetic programming (GGP) and Strongly-typed genetic programming (TGP). In GGP, a Backus-Naur form (BNF) grammar allows formally defining GP structures and ensuring that the typing and syntax are maintained while manipulating the syntactic tree [71]. In the other case, TGP is an enhanced GP version applying data type constraints [73].

5.3.1. Axis-Parallel DTs

Koza [4] proposes encoding DTs with Lisp S-Expressions (S-Exps), where internal nodes are built with a function set and leaf nodes with a terminal set. S-Exps are used by *Iba* et al. [247] and *Tür & Güvenir* [89]. Function and terminal sets are also used in other studies (Table 20), such as:

Table 17Components of TGA-based approaches for DTI.

Stra-	DT	FF		Studies	Year	Fitness	Genetic operator	s		Initial population
tegy						measure	Selection	Crossover	Mutation	
RP	AP	UF		Rzheutskaya et al. [216]	2020	Accuracy	Special	Swap sub-trees	Disturb node	DTs randomly created
SS	AP	UF		GAIT [102]	1999	Accuracy	-	Swap sub-trees	Switch nodes	DTs induced by C4. with a subset of training instances randomly chosen
				GAIT [204,211–214]	2000	Accuracy	Roulette	Swap sub-trees	Switch sub-trees	DTs induced by C4 with a subset of training instances randomly chosen
			•	Sörensen & Janssens [88]	2003	Accuracy	Roulette	Swap sub-trees, Swap nodes	Switch nodes, Switch sub-trees	Binary DTs randomly created
			•	Bosnjak et al. [210]	2015	Accuracy, Size, F-Score	Tournament	Swap sub-trees	Disturb node	DTs randomly created
		AF	•	genTrees [168]	1998	Error+Size	Exponential ranking	Swap sub-trees	Disturb node	DTs randomly created
			•	GATree [163,206]	2000	Accuracy+Size	-	Swap sub-trees	Disturb node	Decision stumps randomly created
				GDT [9] <i>Jurczuk</i> et al. [207–209]	2005 2017 2021	Accuracy+Size	Linear ranking	Swap sub-trees, Swap nodes, Swap branches	Disturb node, Switch nodes, Replace node, Switch sub-trees	DTs randomly created
			•	Biedrzycki & Arabas [215]	2006	Error+Size	Tournament	N/A	Insert node	Empty DTs
			•	GDT-MC [165]	2007	MC+Size	Linear ranking	Swap sub-trees, Swap nodes, Swap branches	Disturb node, Switch nodes, Replace node, Switch sub-trees	DTs randomly created
			٠	GDT-MA [164]	2008	Accuracy+Size	Linear ranking	Swap sub-trees, Swap nodes, Swap branches	Disturb node, Switch nodes, Replace node, Switch sub-trees	DTs induced with 10% of training set using several splitting criteria (I GR, Gini, and Dipolar)
			•	MS [113]	2020	Accuracy+Stability	Roulette	Swap sub-trees	Replace node	DTs with a single leaf only
		MF	٠	LEGAL-Tree [10,205]	2009	Accuracy, Size	Tournament	Swap sub-trees	Replace node	DTs created with a random combinati of several decision stumps previously induced with 10% training set
	OB	UF		TARGET [174]	2008	Error	Roulette	Swap sub-trees, Swap nodes	Disturb node, Switch nodes	DTs randomly created
		AF	•	GEA-ODT [217,218]	2005	Accuracy+Size	Linear ranking	Swap sub-trees, Swap nodes, Swap branches	Disturb node, Switch nodes, Replace node, Switch sub-trees	DTs randomly created
				GDT-Mix [166] Krętowski & Popczyński [219] Czajkowski et al. [114] Reska et al. [220]	2006 2008 2015 2018	Accuracy+Size	Linear ranking	Swap sub-trees, Swap nodes	Disturb node, Switch nodes, Replace node, Switch sub-trees	DTs randomly created

- 1. The Evolutionary Dynamic Data Investment Evaluator (EDDIE) system of *Tsang* et al. [230] where leaf nodes are encoded as terminals with indicators of financial forecasting.
- The Evolutionary Multi-objective Optimization (EMO) of Kim [232,248].
- 3. The GPDTI method of Estrada-Gil et al. [239].
- 4. The work of *Niimi & Tazaki* [249,250] where the initial population is created using the Apriori algorithm [251].

Other GP-based methods for DTI build their trees without using the function set and the terminal set. *Shirasaka* et al. [263] define a DT as a list of nodes, each one with references to one predecessor node and two successor nodes. Each node is a 6-tuple $\{t, l, p, l, r, c\}$ where t is the node id, l is the class label, p, l and r are pointers to one parent

and two children, and c is a counter set defining internal nodes. This representation scheme is used in the following studies:

- Zhao & Shirasaka [264] evaluate several alternatives for inducing more compact DTs, such as controlling DT size in the selection process and deleting redundant elements.
- 2. Oka & Zhao [103] apply C4.5 with segments of the training set to build the initial population.
- 3. *Tanigawa & Zhao* [265] use GP to induce small subtrees, which are combined to build a complete DT.
- 4. *Haruyama & Zhao* [266] implement three multi-objective GA-based methods for DTI.

Furthermore, a simple DT encoding scheme is applied in the Evolutionary Programming Tree (EPTree) of *DeLisle & Dixon* [233], as well as by *Buontempo* et al. [267] and *Wang* et al. [268].

Table 18Experimental analysis reported by TGA-based approaches for DTI.

Stra-	DT		Studies	Datase	ts	Sampling	Performance	Statistical	Compared methods	
tegy				UCI other		method	measures	tests		
RP	AP	•	Rzheutskaya et al. [216]	10	-	ē	Accuracy	-	-	
GS	AP		genTrees [168]	-	1	Hold-out	Accuracy, Size	-	Traditional DTI metho	
			GAIT [102]	-	1	Hold-out	Accuracy, Time	-	C4.5 variant [102]	
		•	GATree [163]	13	5	5-f CV	Accuracy, Size	Avg	C4.5, One-rule method [221]	
			GAIT [211,212]	-	1	Hold-out	Accuracy, Time	-	C4.5	
			Sörensen & Janssens [88]	-	1	-	Accuracy	-	-	
			GAIT [213]	-	1	Hold-out	Accuracy, Time	t-test	LR	
			GAIT [204]	1	2	Hold-out	Accuracy, Size, Time	t-test	C4.5	
			GDT [9]	8	3	10-f CV	Accuracy, Size	-	C4.5	
			Jurczuk et al. [207,208]	2	1	Complete dataset	Speedup	-	-	
			Jurczuk et al. [209]	2	1	Complete dataset	Time	-	J48, GDT	
			GAIT [214]	3	2	Hold-out	Accuracy, Size	t-test	C4.5	
			Biedrzycki & Arabas [215]	4	2	10-f CV	Error, Size	-	ID3, J48	
		•	GDT-MC [165]	13	-	10-f CV	MC, Size	Avg	C5.0, Cost-sensitive J4 [52], MetaCost [222]	
			GDT-MA [164]	15	-	10-f CV	Accuracy, Size	-	C4.5, GDT	
			LEGAL-Tree [10]	6	-	10-f CV	Accuracy, Size	t-test	J48	
			GATree [206]	12	-	5-f CV	Accuracy, Size, Time	-	J48	
			LEGAL-Tree [205]	16	-	10-f CV	Accuracy, F-Score, Size, Time	Friedman, Nemenyi	J48, CART, GALE	
			Bosnjak et al. [210]	20	-	Hold-out	Accuracy, Size, F-Score	Kruskall	GATree	
			MS [113]	4	6	Hold-out	Accuracy, Stability	-	RF	
	OB		GEA-ODT [217,218]	10	5	10-f CV	Accuracy, Size	-	C4.5, OC1	
			GDT-Mix [166]	10	15	10-f CV	Accuracy, Size	-	C4.5, OC1, GEA-ODT, GDT	
			Krętowski & Popczyński [219]	10	10	10-f CV	Accuracy, Size	-	C4.5, OC1, GDT-Mix	
			Czajkowski et al. [114]	-	4	Complete dataset	Speedup	-	-	
		•	Reska et al. [220]	2	1	Complete dataset	Speedup	-	-	
			TARGET [174]	3	2	10-f CV	Error, Size		CART, QUEST, CRUIS RF, Bayesian CART [223], Bootstrap bumping [224]	

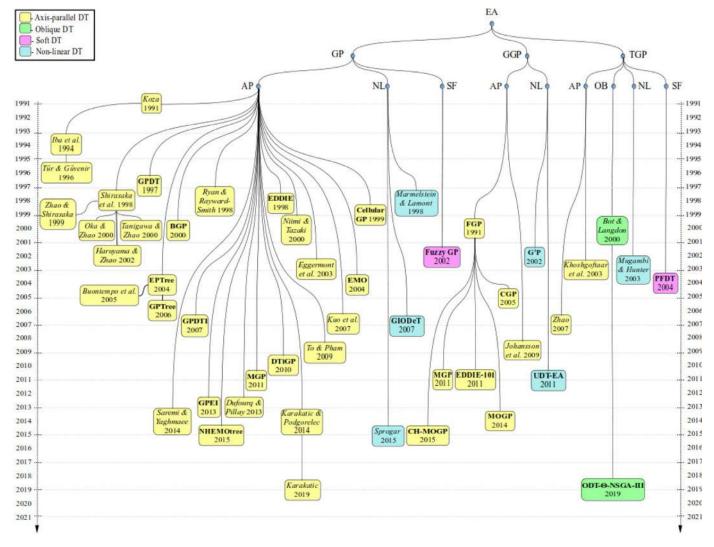


Fig. 19. Timeline of GP-based approaches for DTI.

Table 19Acronyms used to identify several GP-based MH for DTI.

Acronym	Description
BGP	Building Block approach for GP [225]
Cellular GP	Cellular GP algorithm [226]
CGP	Constrained GP [227]
CH-MOGP	Convex-Hull-based MOGP [228]
DTiGP	DT Injection GP [229]
EDDIE	Evolutionary Dynamic Data Investment Evaluator [230]
EDDIE-101	EDDIE-101 [231]
EMO	Evolutionary Multi-objective Optimization [232]
EPTree	Evolutionary Programming Tree [233]
FGP	Financial GP [234]
fuzzy-GP	Fuzzy GP [235]
G^3P	Grammar-guided GP [236]
GIODeT	GP for Induction of Oblique DTs [237]
GPDT	GP for DT [238]
GPDTI	GP for DTI [239]
GPEI	GP Evolved Intervals [240]
M-GP	Memetic GP [241]
MGP	Multiage GP [242]
MOGP	Multi-objective GP [243]
NHEMOtree	Nonhierarchical Evolutionary MO tree learner [244]
ODT-Θ-NSGA-III	ODT-based-Θ-Nondominated Sorting GA-III [245]
PFDT	Polynomial-Fuzzy DTs [246]
UDT-EA	Unconstrained DT-EA [231]

Rouwhorst & Engelbrecht [225] and Engelbrecht et al. [269] implement the Building Block approach for GP (BGP) to encode DTs with test conditions as building blocks as Eqn. (5).

$$\left(x, op, \{x|t\}\right) \tag{5}$$

where x is an attribute, t is a threshold value, and op can be $\{=, \neq, <, \leq, >, \geq\}$. By starting with a population of decision stumps, BGP adds new nodes in its evolutionary process. BGP also applies one pruning operator.

A similar encoding scheme called *full atomic representation* is described by *Eggermont* et al. [270,271] where DTs evolve through a multilayered fitness function of two ranked fitness measures. They first use an information-theory-based splitting criterion [270] and then develop a refined atomic representation using bounded values for numerical attributes [271]

Some GP-based methods introduce specialized operators to build feasible and more accurate offspring.

- 1. GP for DT (GPDT) method of *Nikolaev & Slavov* [238] implement a depth-first search strategy for its mutation operator.
- Ryan & Rayward-Smith [252] use the training set to refine the offspring generated in the crossover stage.
- 3. *Kuo* et al. [257] introduce operators to eliminate redundant sub-trees and to remove subsumed sub-trees.

Table 20
Structure of internal and leaf nodes used in GP-based approaches for DTI

	:		
Study	dy	Function set	Terminal set
Axi	Axis-parallel DT:		
	Koza [4]	Attributes as functions with arguments	Class labels
	Iba et al. [247], Tür & Güvenir[89], Ryan & Rayward-Smith [252]	Attributes as boolean functions	Class labels
	GPDT [238], Cellular GP [226,253], To & Pham [254]	Attributes	Class labels
	EDDIE [230], FGP [5,234]	$\{if$ -then-else, \land , \lor , \rightarrow , $<$ $\}$	Attributes, class labels, real-valued values
	EMO [232,248]	A comparison operator for an attribute and its threshold	Class labels
	GPDTI [239]	Functions with arguments	Class labels
	Niimi & Tazaki [250]	$\{if$ -less-than, if -equals, $*$, $/$, $+$, $ \}$	Attributes, class labels
	Khoshgoftaar et al. [255,256]	$\{if,<\}$, class labels	Attributes, real-valued values
	Kuo et al. [257]	$\{if$ -then, if -then-else, $\land, \lor, \lor, \gt, \lt, \gt, \lt\}$.	Attributes, class labels
	Zhao [258]	A empty node.	Attributes, class labels, real-valued values
	Johansson et al. [259,260], DTiGP [229]	$\{ij, >, <, =\}$	Attributes, class labels, real-valued values
	MGP [241], EDDIE-101 [231], MOGP [243]	$\{if$ -then-else, \land , \lor , \lor , \gt , $<$, $=$ $\}$	{0, 1}
	Oblique DT:		
	Bot & Langdom [6,261]	A label indicating the number of attributes in the linear combination (1, 2, 3).	Attributes, class labels, real-valued values
	Non-linear DTs:		
	Marmelstein & Lamont [237]	$\{+, -, \times, \div, \leq\}$.	Attributes, a random value generator
	UDT-EA [231]	$\{if$ -then-else, $+, -, *, \wedge, \vee, \neg, >, <, \geq, \leq, =, \leq\}$.	Attributes, class labels, real-valued constants
	Šprogar [262]	$\{if, +, -, *, /, 0, eph\}$, attributes.	{modus}

4. *Dufourq & Pillay* [272] use an encapsulation operator to preserve promising sub-trees.

Also, a migration operator is periodically used to swap DTs placed in a bi-dimensional grid with the Cellular GP proposed by *Folino* et al. [226,253]. *To & Pham* [254] use a similar operator to exchange chromosomes between sub-populations evolving in an island-based parallel GP.

More recently, two methods improve the crossing point determination of the recombination operator:

- 1. *Karakatič & Podgorelec* [273] select individuals based on the accuracy and usage of the internal node. The usage of one node is a percentage of training instances processed in it.
- 2. The Nonhierarchical Evolutionary Multi-Objective tree learner (NHEMOtree) of *Casjens* et al. [244] use the importance of an attribute. They argue that an attribute is more important than the others if it is near the root node and is more likely to be selected as a crossover point.

Several GP-based approaches for DTI have been implemented to avoid premature convergence and improve the model performance. In the DT Injection GP (DTiGP), König et al. [229] use an adaptive fitness function to include diversity in the population and control the size model. First, the fitness value of a DT induced using a subset of instances randomly chosen is designated as a reference value. Next, the evolutionary process starts. At even intervals, the fitness value of the best DT is compared with the reference value. If the first is less than the second, the fitness function is modified to create larger DTs. Furthermore, Yi & Wanli [242] implement the multiage GP (MGP) to evolve groups of DTs according to their number of leaf nodes (ages). MGP first divides the population using their ages and then evolves each group independently. These evolved groups are combined to build a new population. This grouping scheme reduces the selection pressure in a particular area (group) and tries preventing genetic operators destroy the evolutionary process continuity. Finally, Karakatič et al. [274] introduce a Lazy Evaluation Model of the fitness value considering only DTs used in the selection procedure to reduce the processing time. They also define a strategy to assign weights to the instances to be used in the DT evaluation.

Additionally, the discretization of real-valued attributes has been implemented in the following methods: The GP Evolved Intervals (GPEI) approach of *Dufourq & Pillay* [240] including an adaptive discretization with fixed and varying number of intervals. The work of *Saremi & Yaghmaee* [275,276] introduce specialized operators to modify threshold values.

Alternatively, GGP has been implemented in the following DTI approaches:

- 1. The Financial GP (FGP) described by Li [234] and Tsang & Li [5].
- 2. The Constrained GP (CGP) of Li et al. [227] for cost-sensitive classification.
- 3. The Memetic GP (MGP) and the EDDIE-101 system of Wang et al. [231,241] where class labels are replaced by instance counters. EDDIE-101 also uses a local search to improve the threshold values of each test condition.
- The multi-objective GP (MOGP) [243] and the Convex-Hull-based MOGP (CH-MOGP) [228] where the ROC curve is used in the evolutionary process.
- The methods of Johansson & Niklasson [259], and Johansson et al. [260] where one oracle data⁶ is used to improve the DT performance.

Finally, TGP has been used: (1) by *Khoshgoftaar* et al. [255] and *Khoshgoftaar & Liu* [256] in a multi-objective method, and (2) by *Zhao*

⁶ An oracle data is a set of test instances together with their predictions (class labels) obtained using another classifier method (ANN or RF).

Table 21
Criteria used to handle categorical attributes with GP-based methods.

Criteria	Study
Multi-branching Binary mapping	Koza [4] Niimi & Tazaki [249], BGP [225], Johansson et al. [260], MOGP [243], Ryan & Rayward-Smith [252], Eggermont et al. [270], Kuo et al. [257]

[258] in a MOGA-based application to select partial preferences on conflicting objectives.

5.3.2. Oblique DTs

Bot & Langdon [6,261] apply TGP to encode the hyperplanes of an oblique DT in a global-search strategy. The function set allows creating test conditions using either one attribute or a linear combination of two or three attributes. This representation is used in the ODT-Θ-NSGA-III (ODT-based-Θ-Nondominated Sorting GA-III) of *Chabbouth* et al. [245].

5.3.3. Non-linear DTs

Two similar GP-based approaches implementing a recursive-partitioning strategy to find a near-optimal hypersurface in each test condition of a non-linear DT are described by *Shali* et al. [277] in the GP for Induction of Oblique DTs (GIODeT) method, and by *Marmelstein & Lamont* [237].

Alternatively, a global search of non-linear DTs also has been implemented in four methods:

- The Unconstrained DT-EA (UDT-EA) implemented by Wang et al.
 [231] uses hypersurfaces in test conditions, and that described by
 Šprogar [262] using the node information-gain-value in its prudentcrossover operator.
- 2. The Grammar-guided GP (G³P) method of *Tsakonas* [236,278].
- 3. Mugambi & Hunter [279] implement TGP in a multi-objective approach evolving a population of DTs to find Pareto optimum values.

5.3.4. Soft DTs

Eggermont [235] applies his full atomic representation in the fuzzy-GP method to evolve a population of soft DTs with triangular membership functions. Moreover, Mugambi et al. [246] use TGP in the Polynomial-Fuzzy DTs (PFDT) method to find near-optimal hypersurfaces of a nonlinear DT. PFDT evolves both polynomials representing the hypersurfaces and sigmoid and bell-shaped membership functions associated with numerical attributes.

5.3.5. Discussion

Fig. 20 shows the attribute and branch types of the axis-parallel DTs induced with the studies described previously. Two criteria have been used to handle categorical attributes: multi-branching and binary mapping (Table 21). In particular, although several methods manipulate numeric attributes, they are first discretized to be used as categorical attributes in GPDT, Cellular GP, and GPEI, and that of *Saremi & Yaghmaee*.

Table 22 shows the components of GP-based approaches for DTI. Twenty studies implement a single-objective fitness function, 17 use an aggregating fitness function, and the remaining studies evaluate a multi-objective fitness function. Accuracy and tree size are the fitness measure most commonly applied to these methods.

Furthermore, sub-tree-swapping crossover and sub-tree-replacement mutation operators are typically applied in these algorithms, although the node-perturbation is also used. The random creation of the initial population and the ramped half-and-half (RH&H) criterion [152] are used to generate the majority's initial candidate solutions of these studies. However, some apply alternative strategies, such as using C4.5 with a collection of instances randomly chosen from the training set, creating decision stumps, and mapping DTs from rules previously created.

Table 23 shows the experimental studies' elements conducted by these approaches. K-fold CV and hold-out sampling methods are used

in 23 studies each. Three works evaluate the complete datasets to compute the algorithm performance.

Accuracy, size, and error-rate are adopted as performance measures in most of these methods. Misclassification cost, sensitivity, specificity, fidelity, AUC, and ROC curve analysis have been used as performance measures in several methods. Furthermore, 14 studies conducted a statistical test to compare their experimental results with those obtained from other methods, Finally, two studies implement some post-hoc analysis only.

Genetic programming is the EA most used to induce DTs since it can evolve DTs directly, and a mapping scheme to build a DT from a chromosome is not needed. In the previous paragraphs, diverse directions to improve genetic programming capacities to induce near-optimal DTs have been described, such as avoiding premature convergence, improving diversity, and reducing the bloat problem. The first two problems are common to all EAs. However, bloat is a particular GP problem, occurring when the evolved trees grow without improving the model performance.

5.4. Other EA-based approaches for DTI

Although genetic algorithms and genetic programming are the most used MHs to create DTI methods, other EAs such as coevolutionary algorithms, estimation of distribution algorithms, grammatical evolution, gene expression programming, differential evolution, and the evolution strategies have also been used for the same purpose. The first two encode their chromosomes as trees, and the others use linear chromosomes. Fig. 21 shows a timeline of the other EA-based approaches applied to induce DTs. Table 24 illustrates the acronyms used to identify various EA-based MHs for DTIs, as defined by their authors.

5.4.1. Axis-parallel-DTs

Coevolutionary algorithms: Podgorelec & Kokol [286,298], Babič et al. [299], and Zorman et al. [300] describe several versions of the Selfadapting Evolutionary DT (SEADT) method, a competitive-CEA-based approach to build DTs. SAEDT uses a tree-based chromosome with three independent populations competing to find a near-optimal DT (Fig. 22). One population contains only one DT induced by C4.5, and the others evolve DT populations. The best chromosome from the main population competes with the best one from the others. When it becomes dominant over the others, the fitness functions are adjusted in each population. A global fitness value is used to determine the dominance of one population over the others.

Furthermore, *Aitkenhead* [301] implements competition between one DT and the training set. This algorithm mutates the tree nodes while updating the training set size and the DT-depth. In the beginning, the training set contains only two sets randomly chosen from the dataset. Once DT evolves and its fitness value becomes higher than a threshold value, the sets are increased. This process continues until the entire dataset is used to evaluate the DT.

Alternatively, the multi-population GA for DTI (MPGA) of *Podgorelec & Karakatic* [284] and the multi-population genTrees (MPGT) method of *Podgorelec* et al. [285] are cooperative CEA using two DTs sub-populations. After a predefined number of generations, one DTs exchange between populations occurs according to one migration rate. The first sub-population uses accuracy, and the other applies one balanced single-class accuracy as their fitness values.

Differential Evolution: Rivera-López & Canul-Reich introduce the DE-based approach to build axis-parallel-DTs using the smallest-position-

Table 22Components of GP-based approaches for DTI.

Stra-	- DT FF MF		MH	Studies	Year	Fitness	Genetic operators			Initial population
tegy						measure	Selection	Crossover	Mutation	•
RP	NL	AF	GP	Marmelstein & Lamont [237]	1998	Error+Size	Tournament	Swap sub-trees	Replace sub-tree	S-Exps randomly created
				GIODeT [277]	2007	GR+Size	Tournament	Swap sub-trees	Replace sub-tree	ExpTs randomly created
GS	AP	UF	GP	Koza [4]	1991	Accuracy	Tournament	Swap sub-trees	Replace sub-tree	-
				<i>Iba</i> et al. [247]	1994	MDL	Tournament	Swap sub-trees	Replace node, Replace sub-tree	S-Exps randomly created
				GPDT [238]	1997	MDL	Roulette	Swap sub-trees	Special	DTs randomly created
				EDDIE [230]	1998	Accuracy	Tournament	Swap branches	Replace sub-tree	-
				Shirasaka et al. [263]	1998	Accuracy	Truncate	Swap sub-trees	Disturb node	-
				Cellular GP [226,253]	1999	J-Measure	Special	Swap sub-trees	Replace sub-tree	DTs randomly created
				Zhao & Shirasaka [264]	1999	Accuracy	Truncate	Swap sub-trees	Disturb node	DTs randomly created
				Oka & Zhao [103]	2000	Accuracy	Truncate	Swap sub-trees	Disturb node	DTs created using C4.5
				Tanigawa & Zhao [265]	2000	Accuracy	Truncate	Swap sub-trees	Disturb node	DTs randomly created
				BGP [225,269]	2000	Accuracy	Tournament	Swap sub-trees	Disturb node	Decision stumps randomly created
				Niimi & Tazaki [250]	2000	Accuracy	Tournament	Swap sub-trees	Replace sub-tree	DTs created using Apriori
				EPTree [233]	2004	MDL	Tournament	Swap sub-trees	Disturb node, Replace sub-tree	DTs randomly created
				GPTree [267,268]	2005	Accuracy	Tournament	Swap sub-trees	Disturb node, Replace sub-tree	DTs randomly created
				To & Pham [254]	2009	Accuracy	Truncate	Swap sub-trees	N/A	DTs randomly created
				GPEI [240,272]	2013	Accuracy	Tournament	Swap sub-trees	Replace sub-tree	RH&H criterion
				Karakatič & Podgorelec [273]	2014	Accuracy	Tournament	Special	Special	DTs randomly created
										(continued on next page)

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Table 23Experimental evaluation reported by GP-based approaches for DTI.

Stra-	DT	MH	Studies	Datasets		Sampling	Performance	Statistical	Compared methods
tegy				UCI other		method	measures	tests	
RP	NL	GP	· Marmelstein & Lamont [237]	2	1	Hold-out	Error	-	RBF-NN, MLP, GP
			· GIODeT [277]	19	-	5-f CV	Accuracy, Size	Avg	C4.5
GS	AP	GP	· Koza [4]	-	-	-	-	-	-
			· Iba et al. [247]	-	2	Hold-out	Accuracy	-	ANN
			· Tür & Güvenir [89]	-	1	Hold-out	Accuracy, Time	-	-
			· GPDT [238]	1	11	Hold-out	Accuracy, Size	-	C4.5
			· EDDIE [230]	-	2	Hold-out	Accuracy	-	-
			· Shirasaka et al. [263]	-	1	Complete dataset	Accuracy, Size	-	-
			· Ryan & Rayward-Smith [252]	6	-	Hold-out	Error, Size	-	C4.5
			· Cellular GP [226,253]	5	-	Hold-out	Error	-	C4.5
			· Zhao & Shirasaka [264]	-	1	Hold-out	Accuracy, Size	-	-
			· Oka & Zhao [103]	-	1	Hold-out	Accuracy, Size	-	C4.5, Shirasaka et al. [263]
			· Tanigawa & Zhao [265]	-	1	Hold-out	Accuracy, Size	-	-
			· BGP [225,269]	4	-	Hold-out	Accuracy	t-test	C4.5, CN2
			· Niimi & Tazaki [249]	1	1	Hold-out	Accuracy, Size	-	C4.5
			· Niimi & Tazaki [250]	1	-	Hold-out	Accuracy, Size	-	Niimi & Tazaki [249]
			· Haruyama & Zhao [266]	3	1	Hold-out	Accuracy, Size	-	Shirasaka et al. [263]
			 Eggermont et al. [270,271] 	6	-	10-f CV	Error	-	C4.5
			· EPTree [233]	-	2	10-f CV	Accuracy, Size	-	CART
			· EMO [232,248]	8	1	10-f CV	Error	-	C4.5
			· GPTree [267,268]	-	2	Hold-out	Accuracy, Size	-	C5.0
			· GPDTI [239]	-	4	10f-CV	Error	-	GP-based neural network [280]
			· Kuo et al. [257]	-	1	Hold-out	Accuracy	-	C5.0
			· To & Pham [254]	-	1	Complete dataset	Sensitivity, Specificity	-	SVM, LR, LDA
			· DTiGP [229]	18	-	4-f CV	Accuracy	Avg, WTL	J48, GP
			· MGP [242]	12	-	10-f CV	Accuracy, Time		C4.5, DTiGP, GP
			· GPEI [240,272]	5	-	10-f CV	Accuracy	-	C4.5, ID3-S [281]
			· Saremi & Yaghmaee [275]	6	-	Hold-out	Accuracy, Size	-	C4.5
			· Karakatič & Podgorelec [273]	6	-	10f-CV	Accuracy	Mann-W	GP with sub-tree switching
			· NHEMOtree [244]	-	301	5-f CV	Error, MC	Friedman, Wilcoxon	CART, NHEMOtree with sub-tree switching
			· Saremi & Yaghmaee [276]	6	-	5-f CV	Accuracy, Size, Time	-	CHAID, evtree
			· Karakatič et al. [274]	10	-	5-f CV	Accuracy, F-Score, Time	Kruskall, Wilcoxon	GP with standard fitness evaluati

(continued on next page)

Table 23 (continued)

Stra-	DT	MH	Studies	Datasets		Sampling	Performance	Statistical	Compared methods
tegy				UCI	other	method	measures	tests	
		GGP	· FGP [5,234]	-	2	3-f CV	Accuracy	-	C4.5
			· CGP [227]	3	-	10-f CV	MC	-	C4.5, kNN, NB, PART [282]
			Johansson et al. [259,260]	26	-	4-f CV	Accuracy, Fidelity	Friedman, Bonferroni, Nemenyi	J48
			· MGP [241]	10	-	5-f CV	AUC	WTL, Wilcoxon	C4.5, FGP, GGP, EGP
			· EDDIE-101 [231]	5	3	Hold-out	Accuracy	Wilcoxon	J48, REPTree, RF, UDT-EA
			· MOGP [243]	27	-	5-f CV	AUC	WTL, Wilcoxon	C4.5, NB, FGP, GGP, EGP, PRIE [283], 4 MO-based EAs
			· CH-MOGP [228]	27	-	5-fCV	AUC, Time	Wilcoxon	C4.5, NB, PRIE [283], 4 MO-based EAs
		TGP	· Khoshgoftaar et al. [255,256]	-	1	Hold-out	Error	-	GP
			· Zhao [258]	13	-	Complete dataset	AUC	-	C4.5, MLP, SVM
	OB	TGP	 Bot & Langdon [6,261] 	4	-	10-f CV	Accuracy, Size	-	C5.0, OC1, M5' [282]
			· ODT-O-NSGA-III [245]	10	-	5-f CV	F-Score	Friedman, Iman-D, Shaffer	OC1-GA, C4.5, ten methods to create classification rules, and five ensemble methods
	NL	GP	· G ³ P [236,278]	6	-	10-f CV, Hold-out	Error, Size	-	C4.5, ID3, NB
			· Šprogar [262]	21	-	5-f CV	Accuracy	Wilcoxon	GP with several crossover operators
		GGP	· UDT-EA [231]	5	3	Hold-out	Accuracy	Wilcoxon	J48, REPTree, RF
		TGP	· Mugambi & Hunter [279]	-	1	Hold-out	ROC	-	RBF-NN
	SF	GP	· Fuzzy-GP [235]	5	-	10-f CV	Error	-	C4.5, and two methods to create classification rules
		TGP	PFDT [246]	-	2	Hold-out	ROC	-	C4.5

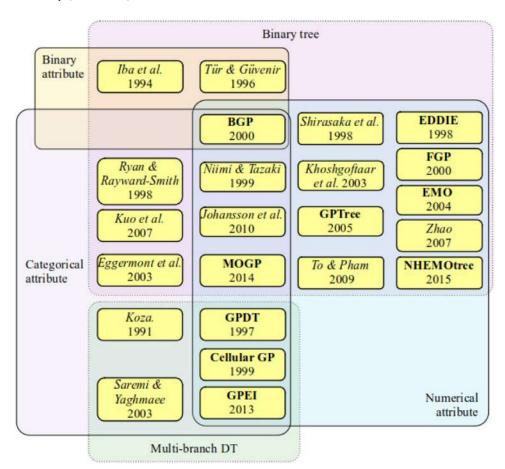


Fig. 20. DTs and attribute types used with GP-based MHs inducing axis-parallel-DTs.

Table 24
Acronyms used to identify several other EA-based MH for DTI.

Acronym	Description
Coevolutionary	algorithms:
MPGA	Multi-population GA for DTI [284]
MPGT	Multi-population genTrees [285]
SEADT	Self-adapting Evolutionary DT [286]
Differential Evo	olution:
AJADE-MDT	Adapted JADE with Multivariate DT [287]
DE-ADT ^{SPV}	DE-based method to build axis-parallel-DTs using SPV rule [8]
DE-ODT	DE algorithm to build oblique-DTs [288]
OC1-DE	OC1-based DE [289]
PA-DE	Parallel-Coordinates-based DE [290]
PDT	Perceptron DT [291]
Evolution strate	egies:
MESODT	Multi-membered ES Oblique DT [292]
OC1-ES	OC1-based ES [11]
Estimation of D	Distributions Algorithm:
Ardennes	Ardennes [293]
Gene Expression	n Programming:
GEPDT	GEP decision tree [294]
Grammatical E	volution:
MGEDT	MO approach to evolving DT using GE [295]
Hybrid approac	ches:
CGP/SA	The Cellular-GP coupled with SA [296]
GP-MM	GP hybridized with Margin Maximisation [297]

value rule (DE-ADT^{SPV}) [8]. This method evolves real-valued parameters encoding the internal nodes (attributes and threshold values) of a DT in a global search strategy. A binary-DT depth, whose number of internal nodes is not less than the number of attributes (*d*) in the training set, is used to define the vector size (*n*), as Eqn. (6).

$$n = 2^{\max\{\lceil \log_2(d+1)+1 \rceil, \lceil \log_2(s)+1 \rceil\}} - 1 + n_z, \tag{6}$$

where s is the number of class labels in the dataset, and n_z is the number of threshold values associated with the numerical attributes used in the internal nodes. Also, a three-stage procedure to map one DT from this real-valued vector is defined (Fig. 23). On the other hand, *Dolotov & Zolotykh* [302] describe a similar approach. However, their coding scheme allows each attribute to be used only once as an internal node. Finally, *Mitrofanov & Semenkin* [303] describe a recursive-partitioning strategy to build an axis-parallel-DT. Here, the population evolves to find a near-optimal univariate test condition.

Estimation of Distributions Algorithm: The Ardennes method of Cagnini et al. [293] implement a global-search strategy to find axis-parallel-DTs with numerical attributes. Ardennes first constructs a Probabilistic Graphical Model (PGM) resembling a complete binary tree. Then, DTs' initial population is created using (1) PGM to place attributes and (2) information gain to compute the threshold values. Next, the evolutionary process is conducted, updating the PGM and replacing the worst individuals with new trees. Finally, the best DT in the last population is returned as the algorithm solution.

Evolution Strategies: Dolotov & Zolotykh [302] uses (1+1)-ES in a global-search strategy where one real-valued chromosome encodes the internal nodes of an axis-parallel-DT. They use the SPV rule to determine how the attributes are used to build a DT. In (1+1)-ES, a single offspring is created from one parent.

Grammatical Evolution: Motsinger-Reif et al. [304] define an appropriate grammar to map axis-parallel-DTs from binary strings used to model one gene-gene interaction [305]. The binary string is decoded into an integer string, and then grammar is used to construct a DT. Furthermore, Ono & Kushida [306] try controlling the search bias present on the evolutionary process by estimating the solution landscape using rank correlation. Finally, the MO approach to evolving DT using GE (MGEDT) of Pereira et al. [295] is used to induce binary DTs.

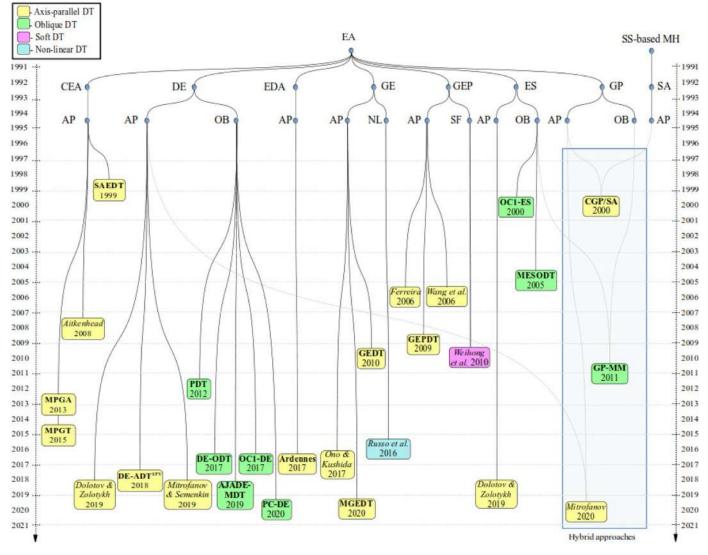


Fig. 21. Timeline of the other EA-based approaches for DTI.

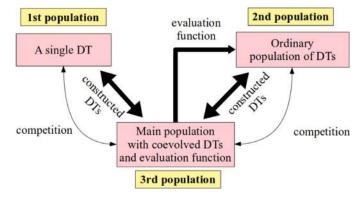


Fig. 22. Population competing to find a near-optimal DT (adapted to [286]).

Gene Expression Programming: Ferreira [307] and Wang et al. [308] conduct a global-search of near-optimal axis-parallel-DTs. A linear chromosome is composed of one or more genes, each one structurally divided into a head and a tail. The head encodes the dataset attributes, and the tail works as a buffer of class labels. An additional vector represents the threshold-values used with numerical attributes. Furthermore,

the GEP decision tree (GEPDT) method of *Qu* et al. [294] considers the values-range of each numerical attribute to compute the threshold-values used in test conditions.

Hybrid approaches: Two studies combine GP with other MHs to implement a global-search strategy to find a near-optimal DT. The Cellular-GP coupled with SA (CGP/SA) of Folino et al. [296] uses a cellular automaton to evolve DTs placed in a grid. In each evolutionary step, the best neighbor of each DT is selected to be recombined and generate two offsprings. The best offspring replace the current DT applying the Boltzmann criterion. Furthermore, Mitrofanov [309] use DE to optimize the threshold-values of all internal nodes of the trees evolving in a GP-based DTI method.

5.4.2. Oblique-DTs

Differential Evolution: Both recursive-partitioning and global-search strategies to induce oblique-DTs have been implemented using DE-based approaches. In the first case, the following methods evolve a population of real-valued individuals to find near-optimal hyperplanes:

- 1. The OC1-DE algorithm of Rivera-López et al. [289].
- 2. The Adapted JADE with Multivariate DT (AJADE-MDT) method of *Jariyavajee* et al. [287].
- The Parallel-Coordinates (PA-DE) algorithm of Estivil-Castro et al. [290].

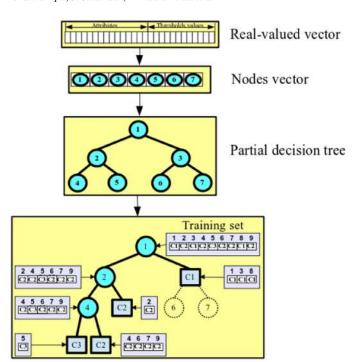


Fig. 23. Mapping scheme used in the DE-ADT^{SPV} method.

Final decision tree

OC1-DE and PA-DE apply the standard DE algorithm. AJADE-MDT uses a self-adaptive version adjusting the DE control-parameters into its evolutionary process.

On the other case, two methods implement a global search strategy to find a near-optimal oblique-DT:

- 1. The Perceptron DT (PDT) method of *Lopes* et al. [291] and *Freitas* et al. [310], where (1) the hyperplane coefficients of one DT are encoded with a real-valued individual, (2) the hyperplane independent terms, and the class label of leaf nodes, are stored in two additional vectors. In each DE iteration, mutation parameters are randomly altered. A group of new DTs randomly created replaces the worst individuals in the population.
- The DE algorithm to build oblique-DTs (DE-ODT) of Rivera-López & Canul-Reich [288], where the size of the real-valued vector is computed as a factor of the number of internal nodes of an oblique-DT estimated using the number of dataset attributes.

Evolution strategies: Two ES-based methods for DTI use a recursive-partitioning scheme to create oblique-DTs:

- 1. The OC1-ES of Cantú-Paz & Kamath [11,137] implements a (1+1)-ES.
- 2. The Multi-membered ES Oblique DT (MESODT) induction method of *Zhang* et al. [292] applies (μ, λ) -ES using μ parents to create λ offsprings.

Hybrid approaches: The GP hybridized with Margin Maximisation (GP-MM) of *Agapitos* et al. [297] is a GGP-based method used to induce oblique-DTs. GP-MM implements a (1+1)-ES as a local search strategy to maximize the margins associated with each hyperplane.

5.4.3. Non-linear-DTs

Grammatical Evolution: Russo et al. [311] apply C4.5 and RTree to create DTs of the initial population of a GE-based approach to induce non-linear-DTs.

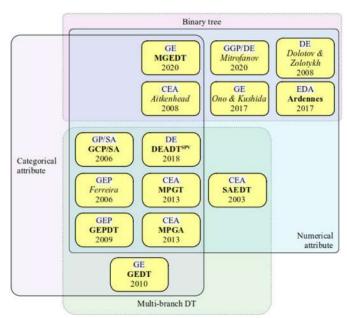


Fig. 24. DTs and attribute types used with other EA-based MHs inducing axis-parallel-DTs.

5.4.4. Soft-DTs

Gene expression programming: Weihong et al. [312] implement a GEP-based method including a fuzzification process of numerical attributes. Several symmetrical triangular membership functions are associated with each test condition of an axis-parallel DT previously induced with the GEPDT method.

5.4.5. Discussion

Fig. 24 shows the attribute and branch types of axis parallel DTs generated using these EA-based methods, and Table 25 lists the criteria used to handle categorical attributes. In particular, the discretization of numerical values is applied in SAEDT and GCP/SA.

Table 26 shows the components of these approaches. Most of these studies use a single-objective fitness function. However, four apply an aggregating fitness function, and only one uses a multi-objective fitness function in its evolutionary process. Furthermore, accuracy is the fitness measure most commonly used by these methods. Tournament-based selection is the prominent operator implemented in these studies, but linear-ranking and roulette-wheel-based selection have also been used. The sub-tree-swapping crossover and the node-disturbance mutation are applied in eight studies, although several studies implement specialized operators to evolve their candidate solutions. Finally, a random generation of candidate solutions to create the initial population is conducted with most of these approaches. In particular, MESODT creates a set of hyperplanes through an ANN-based approach. In the work of *Aitkenhead*, a randomly generated decision stump is used as the first candidate solution in his CEA-based method.

Table 27 resumes the experimental studies reported in the existing literature implementing other EA-based approaches for DTI. K-fold CV and hold-out and test accuracy and size are the sampling methods and the performance measures most used in these studies. Eight studies implement a statistical test of their experimental results. One post-hoc analysis is conducted in four methods.

Fig. 21 shows that more than half of these EA-based studies have been proposed in recent years, highlighting DE and GE-based approaches to induce DTs. In the first case, a mapping scheme to build DT from candidate solutions is needed, and in the second one, this scheme is avoided since grammar is used to build DTs. However, the number of studies using these EAs is far fewer than those using GA or GP, even

Table 25Criteria used to handle categorical attributes with other EA-based methods.

Criteria	Study
Multi-branching Binary mapping	MPGA [284], MPGT [285], DE-ADT ^{SPV} [8], GEDT [304], MGEDT [295], Ferreira [307], and GEPDT [294]. Aitkenhead [301].

though they effectively find near-optimum solutions to many complex problems.

6. Swarm-intelligence-based methods for DTI

Only three swarm-intelligence methods have been applied for DTI: ant colony optimization, particle swarm optimization, and bat algorithm. All approaches described in the existing literature induce axis-parallel DTs, only. Table 28 lists the acronyms used to name various SI-based MHs for DTIs, as defined by their authors. A timeline of these methods is shown in Fig. 25.

6.1. Ant colony optimization

Bursa & Lhotska [317,323] describe the ACO-DTree method as a global-search strategy in which each artificial ant construct an axis-parallel DT using a pheromone matrix. This matrix represents a fully connected graph where the nodes are associated with the attributes of the dataset, the edges indicate the transition between two nodes, and the pheromone values indicate the probability of visiting a successor node. First, a root node with one attribute randomly chosen is created, and for each possible successor node, the next attribute is probabilistically selected using the pheromone matrix. This process is repeated until a predefined DT depth is reached. In the ACO-DTree, only ants representing better solutions can deposit pheromone in the matrix. The induced DTs are pruned by applying a penalty value for unused nodes.

Boryczka & Kozak [12,324] describe a similar approach known as ACDT (Ant Colony algorithm for constructing DTs). ACDT uses a combination of splitting criterion and pheromone values to select the attributes used to build a DT. Also, Boryczka & Kozak [318] implement an adaptive discretization of numerical attributes in the continuous ACDT (cACDT) method.

Furthermore, the Ant-Tree-Miner (ATM) method of *Otero* et al. [13] implements an iterative process where each artificial ant creates a new DT based on a combination of splitting criterion and pheromone values. Each element in the pheromone matrix has three values (edge, level, x), where edge represents a univariate test condition, level is the DT level of the edge, and x is a successor attribute.

6.2. Particle swarm optimization

Veenhuis et al. [321] introduce the Tree Swarm Optimization (TSO) method to induce axis-parallel DTs. A DT is a particle moving in the solution space represented as a sequence of nodes (test conditions and leaf nodes). Each node has a vector of symbols grouping all possible test conditions and class labels (Fig. 26). The symbol used in a node is the one with the maximum value in the real-valued vector representing the swarm particle. If a numerical attribute is selected, the value of the vectors first element is taken as its threshold value.

Furthermore, two multi-objective PSO-based methods have been implemented:

- The DT-MPSO method of Santos & Naval [319] encodes the nodes
 of a complete axis-parallel DT with a predefined depth as a particle. This depth is increased in the search procedure if no significant
 improvement exists in the best solution.
- 2. *Fieldsend* [325] uses a real-valued matrix, where each row is a vector of symbols (similar to TSO), and each column represents a tree node.

An additional matrix column is used to store the threshold values of numerical attributes.

Alternatively, *Chan* et al. [326] perform a recursive-partitioning strategy to find the test conditions with numerical attributes used in an axis-parallel DT. Each particle represents one univariate test condition. Additionally, *Cho* et al. [327] implement a subsequent-optimization strategy to improve the threshold values of the test conditions of a DT previously induced by CART. Each particle in the swarm encodes the threshold values of all test conditions used in the induced DT. Finally, *Malik & Khan* [320] uses PSO to prune binary DTs previously induced. Both the single-objective optimized DT pruning (SO-DTP) and MO optimized DT pruning (MO-DTP) approaches are implemented. In these methods, a particle represents the internal nodes to the tree to be pruned.

6.3. Bat algorithm

In the Bat-Tree-Constructor (BTC) of *Bida & Aouat* [322], a bat population explores the DT space to find a near-optimal DT. DTs can use both nominal and numerical attributes.

6.4. Discussion

Fig. 27 shows the attribute and branch types of axis parallel DTs generated using these SI-based methods, and Table 29 lists the criteria used to handle categorical attributes. In particular, the discretization of numerical values is applied in ACDT and ATM. Fig. 28 shows the scheme used for the methods implementing a subsequent-optimization strategy.

In Table 30 are shown the components of the SI-based methods for DTI. Five studies use one single-objective fitness function and four other evaluate an aggregating fitness function. Only three methods apply a multi-objective fitness function. Test accuracy and error-rate have been used as fitness measures in three and four studies, respectively. Furthermore, matrix representation and sequences of values have been used to encode candidate solutions in three and five studies, respectively. Finally, the random generation of candidate solutions to create the initial population is the strategy applied in all studies implementing these MHs.

Table 31 resumes the experimental studies reported in the existing literature implementing SI-based methods for DTI. Six studies implement a hold-out sampling procedure. One k-fold CV is applied in ATM, APSO, and BTC, as well as in the procedure described by *Chan* et al. TSO and MOPSO use the complete datasets to obtain their performance values. Test accuracy, size, and error-rate have been adopted as performance measures in nine, eight, and three studies, respectively. Finally, two methods report the use of statistical tests to compare its results.

Unlike other data mining techniques such as attribute selection [328,329], or for classifier parameter tuning [330] where swarm-based methods are extensively applied, the use of SI-based approaches to induce DT has been poorly studied. Since the most prominent SI-based methods have been created to solve numerical-optimization problems, their use to disturb tree-like structures involves the definition of (1) a mapping scheme between particles and DTs, and (2) a correspondence between swarm operators and DTI elements.

Ant colony optimization can build DTs since it denotes a problem with a graph where artificial ants walk to find a near-optimal solution. This scheme allows expressing a DT using a pheromone matrix. In particular, a challenge for the use of particle swarm optimization and the bat algorithm is the definition of a scheme to map the DT structure from

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Table 26Components of other EA-based approaches for DTI.

Stra-	DT	FF	MH		Studies	Year	Rep.	Fitness	Genetic operator	rs		Initial population
tegy							scheme	measure	Selection	Crossover	Mutation	_
RP	AP	UF	DE		· Mitrofanov & Semenkin [303]	2019	Linear	ClusterS	Tournament	Binomial	DE mutation	Numerical chromosomes randomly created
	ОВ	UF	DE		· OC1-DE [289]	2017	Linear	Twoing	Tournament	Binomial	DE mutation	Hyperplanes randomly created and several copies of the best axis-parallel hyperplane found by OC1-A
					· AJADE-MDT [287]	2019	Linear	IG	Tournament	Binomial	DE mutation	Hyperplanes randomly created
					· PA-DE [290]	2020	Linear	GR	Tournament	Binomial	DE mutation	Hyperplanes randomly created
			ES		· OC1-ES [11,137]	2000	Linear	Twoing	N/A	N/A	Special	Axis-parallel hyperplanes found by OC1-AP
					 MESODT [292] 	2005	Linear	IG, LinearS	Special	Special	Special	Hyperplanes created by AN
GS	AP	UF	CEA		· Aitkenhead [301]	2008	Tree	Accuracy	N/A	N/A	Disturb node	A decision stump randomly created
			DE		· DE-ADT ^{SPV} [8]	2018	Linear	Accuracy	Tournament	Binomial	DE mutation	Numerical chromosomes randomly created
					Dolotov & Zolotykh [302]	2019	Linear	Accuracy	Tournament	Binomial	DE mutation	Numerical chromosomes randomly created
			EDA		· Ardennes [293]	2017	Tree	Accuracy	TruS	N/A	N/A	DT randomly created
			ES		Dolotov & Zolotykh [302]	2019	Linear	Accuracy	N/A	N/A	Special	Numerical chromosomes randomly created
			GE		Ono & Kushida [306]	2017	Linear	Accuracy	Tournament	Single-point	Flip-bit	DTs randomly created
			GEP		Ferreira [307], Wang et al. [308]	2006	Linear	Accuracy	Roulette	Single-point, Double-point, Special	Uniform, Special	String chromosomes randomly created
					· GEPDT [294]	2009	Linear	Accuracy	Roulette	Single-point, Double-point, Special	Uniform, Special	String chromosomes randomly created
				GGP/SA	· GCP/SA [296]	2000	Tree	Error	Special	Swap sub-trees	Replace sub-tree	DTs randomly created
				GGP/DE	· Mitrofanov [309]	2020	Tree	Accuracy	Tournament	Swap sub-trees	Replace sub-tree	DTs randomly created
		AF	CEA		· SAEDT [286,298–300]	1999	Tree	Accuracy+Size	Linear ranking	Swap sub-trees	Disturb node, Replace sub-tree	DTs randomly created
					· MPGA [284]	2013	Tree	Accuracy+Size	Linear ranking	Swap sub-trees	Disturb node, Replace sub-tree	DTs randomly created
					· MPGT [285]	2015	Tree	Accuracy+F- Score	Tournament	Swap sub-trees	Disturb node, Replace sub-tree	DTs randomly created
			GE		· GEDT [304]	2010	Linear	Sensitivity, Specificity	Tournament	Single-point	Flip-bit	DTs randomly created
		MF	GE		· MGEDT [295]	2020	Linear	AUC, Size	Tournament	Swap sub-trees	Replace sub-tree	DTs randomly created
	ОВ	UF	DE		· PDT [291,310]	2012	Linear	Error	Tournament	Binomial	DE mutation	Numerical chromosomes randomly created
					DE-ODT [288]	2017	Linear	Accuracy	Tournament	Binomial	DE mutation	Numerical chromosomes randomly created
		_		GGP/ES	· GP-MM [297]	2011	Tree	Accuracy	Tournament	N/A	Sub-tree replacement	RH&H criterion
	NL	UF	GE		· Russo et al. [311]	2016	Linear	Error	Tournament	Single-point	Flip-bit	DTs created by C4.5
	SF	UF	GEP		• Weihong et al. [312]	2010	Linear	Accuracy	Roulette	Single-point, Double-point, Special	Uniform, Special	String chromosomes randomly created

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Table 27Experimental analysis reported using other EA-based approaches for DTI.

Stra-	DT	MH		Studies	Datasets		Sampling	Performance	Statistical	Compared methods
tegy					UCI	other	method	measures	tests	
RP	AP	DE		Mitrofanov & Semenkin [303]	4	-	10f-CV	Accuracy, Time	t-test	ID3, CART
	ОВ	DE		OC1-DE [289]	16	-	5-fCV, 10f-CV	Accuracy, Size	Friedman, Nemenyi	OC1, OC1-SA, OC1-GA, OC1-ES, HBDT
				AJADE-MDT [287]	5	-	5-fCV	Accuracy, Size	-	OC1, HHCART [313]
				PA-DE [290]	15	-	10-fCV	F-Score, Size	Friedman, Bergmann	C4.5, J48, OC1, OC1-DE
		ES	٠	OC1-ES [11,137]	10	3	5-f CV	Accuracy, Size, Time	t-test	CART, OC1, OC1-GA, OC1-SA
				MESODT [292]	2	2	Hold-out	Accuracy, Size	-	C5.0, OC1, OC1-ES, Alopex Perceptron DT [35]
GS	AP	CEA		SAEDT [286,298]	-	1	Hold-out	Accuracy, Sensitivity, Specificity, Size	-	C4.5, genTrees
				SAEDT [299]	-	1	Hold-out	Accuracy, Sensitivity, Specificity, Size	-	MtDeciT [314], C5.0
				SAEDT [300]	-	1	Hold-out	Accuracy, Sensitivity, Specificity, Size	-	MtDeciT, Neuro generated DT [300], C5.0
				Aitkenhead [301]	2	-	Complete dataset	Accuracy	-	C4.5, GALE, MLP
				MPGA [284]	-	1	5-f CV	Accuracy	-	genTrees, J48, NB, SVM, MLP, AdaBoost [315]
				MPGT [285]	10	-	5-f CV	Accuracy, F-Score, Size	Friedman, Nemenyi	C4.5, CART, genTrees
		DE		DE-ADT ^{SPV} [8]	20	-	10f-CV	Accuracy, Size	Friedman, Bergmann	J48, CART, NB, MLP, RBF-NN, RF
				Dolotov & Zolotykh [302]	20	-	?	Accuracy	-	CART, MLP, ES
		EDA		Ardennes [293]	10	-	10f-CV	Accuracy, Size	Avg-R	J48, LEGAL-Tree
		ES		Dolotov & Zolotykh [302]	20	-	?	Accuracy	-	CART, MLP, DE
		GEP		Ferreira [307]	2	-	Hold-out	Accuracy	-	-
				Wang et al. [308]	2	-	Complete dataset	Accuracy	-	-
				GEPDT [294]	8	-	5-f CV	Accuracy	-	C4.5
		GE		GEDT [304]	-	40	10-f CV	Error	-	C4.5
				Ono & Kushida [306]	5	-	Complete dataset	Accuracy, F-Score, Size	-	C4.5
				MGEDT [295]	-	1	Hold-out	AUC, Size	-	CART, RF, MLP
		GP/SA		GCP/SA [296]	12	-	Hold-out	Error, Size	-	C4.5
		GGP/DE	٠	Mitrofanov [309]	8	-	10-f CV	Accuracy	-	C4.5
	ОВ	DE		PDT [291,310]	8	-	Hold-out	Accuracy	Kruskall	J48, Best-first DT [316], RTree, RBF-NN, MLP, NB, kNN
				DE-ODT [288]	13	-	10f-CV, Hold-out	Accuracy, Size	Friedman, Nemenyi	J48, OC1, PDT, EFTI
		GGP/ES		GP-MM [297]	5	-	10-f CV	Accuracy	-	C4.5, GP, SVM, NB
	NL	GE		Russo et al. [311]	-	1	Hold-out	Error	-	J48, RTree
	SF	GEP		Weihong et al. [312]	2	-	5-f CV	Accuracy	-	GEPDT

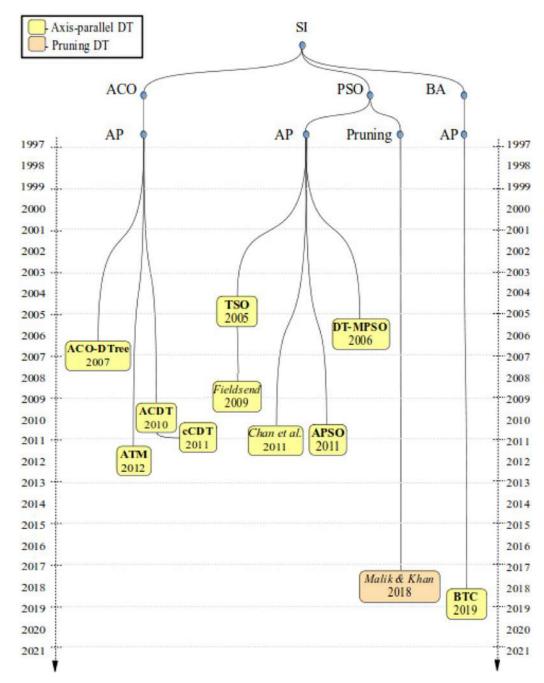


Fig. 25. Timeline of swarm-intelligence-based methods for DTI.

 Table 28

 Acronyms used to identify several SI-based MH for DTI.

•	·								
Acronym	Description								
Ant colony optimization:									
ACDT	Ant Colony algorithm for constructing DTs [12]								
ACO-DTree	ACO-based method for DT [317]								
ATM	Ant-Tree-Miner method [13]								
cACDT	Continuous ACDT method [318]								
Particle swarm	optimization:								
DT-MPSO	DT-based using multi-objective PSO [319]								
MO-DTP	Multi-objective optimized DT pruning [320]								
SO-DTP	Single-objective optimized DT pruning [320]								
TSO	Tree Swarm Optimization method [321]								
Bat algorithm:	-								
BTC	Bat-Tree-Constructor [322]								

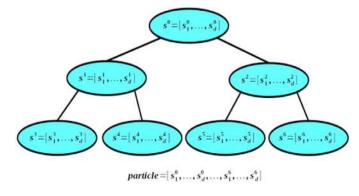


Fig. 26. DTs representation using a TSO particle (Adapted of [321]).

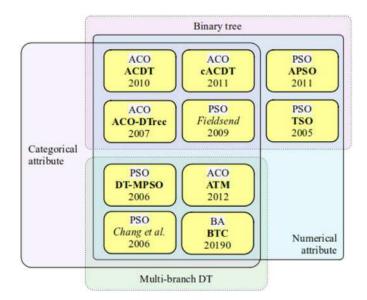


Fig. 27. DTs and attribute types used with other SI-based MHs inducing axisparallel-DTs.

Table 29Criteria used to handle categorical attributes with SI-based methods.

Criteria	Study
Multi-branching	ATM [13], DT-MPSO [319], BTC [322]
Binary mapping	ACDT [12], cACDT [318]
Numerical mapping	ACO-DTree [317], Fieldsend [325]

a real-valued vector representation. The lack of SI-based approaches for DTI can be since they are more recently introduced in the existing literature than EAs.

7. Hyper-heuristic-based approaches to build DTI methods

Hyper-heuristic-based approaches used to create DTI methods described in the existing literature are based on genetic algorithms or grammatical evolution. Table 32 lists the acronyms used to name various HH-based aproaches for DTIs, as defined by their authors. The timeline of these methods is shown in Fig. 29.

7.1. Genetic algorithms with linear chromosomes

Vella et al. [336] describe a GA-based hyper-heuristic to build DTI algorithms (HHDT). An individual represents a list of rules to select the most appropriate splitting criterion based on the entropy degree of

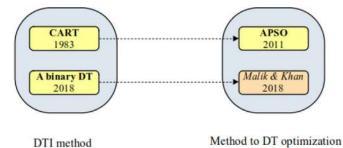


Fig. 28. Scheme used to subsequent-optimization with SI-based MHs.

dataset attributes. Each rule "if (x > high and y < low) then apply criterion h" is codified as a 5-tuple (x, high, y, low, h), where x and y are entropy values, high and low are threshold values, and h identifies one of 5 splitting criteria.

Barros et al. [334,340] describe the hyper-heuristic EA for designing DT algorithms (HEAD-DT). This method encodes four components of a DTI method in a linear chromosome: split criterion, stopping rule, procedure to deal with missing values, and pruning method. Moreover, Basgalupp et al. [337] introduce a multi-objective version of HEAD-DT (MOHEAD-DT) allowing to choose between the Pareto dominance approach and the lexicographic analysis. MOHEAD-DT proposes several modifications in fitness calculation, selection operator, and the procedure to select the best method in the population. Furthermore, Jovanović et al. [341] implement a similar approach encoding five components: split criterion, split evaluation method, stop criterion, pruning approach, and the feature subset selection procedure. These components are obtained from several DTI methods such as ID3, C4.5, CART, and CHAID.

Recently, *Nyath & Pillay* introduce AutoGA [333], a GA-based method to search for a GP configuration to lead optimized classifiers. AutoGA encodes 14 GP parameters: representation, population size, tree generation, initial tree depth, max offspring depth, selection method, selection size, reproduction rates, mutation type, max mutation depth, reproduction sequence, operator pool, fitness type, and number of generations. Finally, *Kumar* et al. implement the Hyper-heuristic Evolutionary Approach with Recursive and Partition Trees (HEARpart). This method uses a GA to evolve a population of chromosomes encoding four parameters of the Recursive and Partition Trees (RPART) package [342]: minimum split, complexity, DT maximum depth, and node-splitting criterion.

7.2. Grammatical evolution

Basgalupp et al. [339] implement a GE-based method known as Evolutionary Split Criteria with Grammatical Evolution (ESC-GE). This method applies a grammar that automatically generates the best split

Table 30Components of SI-based approaches for DTI.

Stra- tegy	DT	FF	MH		Studies	Year	Repr. scheme	Fitness measure	Initial solution		
RP	AP	AF	PSO		Chan et al. [326]	2011	Linear	GR+Accuracy	Particles randomly created		
GS	AP	UF	ACO		ACO-DTree [317,323]	2007	Matrix	Error	A pheromone matrix randomly created		
			PSO		TSO [321]] 2005 Linear Erro		Error	Particles randomly created		
	BA AF ACO			BTC [322]	C [322] 2019 Tree Accuracy		Accuracy	DT randomly created			
			ACO		ACDT [12,324]	2010	Tree	Twoing+Pheromone	A matrix with values based on the number of attributes		
					cACDT [318]	2011	Tree	Twoing+Pheromone	A matrix with values based on the number of attributes		
					ATM [13]	2012	Matrix	GR+Pheromone	A pheromone matrix randomly created		
		MF	PSO		DT-MPSO [319]	2006	Linear	Error, Size	Particles randomly created		
					Fieldsend [325]	2009	Matrix	Error, Size	Particles randomly created		
SO	AP	UF	PSO		APSO [327]	2011	Linear	Accuracy	Particles randomly created (DT from CART)		
	UF,MF		PSO	٠	Malik & Khan [320]	2018	Linear	Sensitivity, Fall-out	Particles randomly created (A binary DT)		

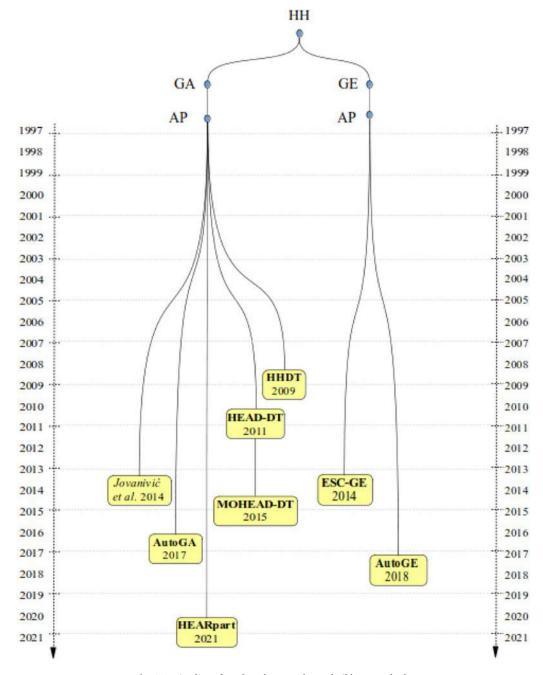
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Table 31Experimental analysis reported using SI-based approaches for DTI.

Stra-	DT	MH		Studies	Datasets Sa		Sampling	Performance	Statistical	Compared methods
tegy					UCI	other	method	measures	tests	
RP	AP	PSO		Chan et al. [326]	4	1	10-f CV	Accuracy, Size	-	C5.0, CART, QUEST, CHAID
GS	AP	ACO	•	ACO-DTree [317,323]	1	2	Hold-out	Error	-	WEKA classifiers [52]
			٠	ATM [13]	22	-	10-f CV	Accuracy, Size	Friedman, Hommel, Wilcoxon	C4.5, CART, aCDT
			٠	ACDT [12]	7	-	Hold-out	Accuracy, Size, Time	-	CART, Ant-Miner [331], cAnt-Miner [332]
				ACDT [324]	30	-	Hold-out, 10f-CV	Accuracy, Size	Friedman	RTree, CART, ATM, C4.5
			•	cACDT [318]	11	-	Hold-out	Accuracy, Size	-	ACDT, Ant-Miner [331], cAnt-Miner [332]
		PSO		TSO [321]	1	-	Complete dataset	Accuracy	-	C4.5, GP
				DT-MPSO [319]	9	-	Hold-out	Error, Size	-	C4.5
				Fieldsend [325]	5	-	Complete dataset	Error	-	C4.5, GP, TSO
		BA		BTC [322]	29	-	10-f CV	Accuracy, Size	-	ATM, C4.5, CART, RTree
SO	AP	PSO		APSO [327]	1	1	5-f CV	Accuracy	-	CART
				Malik & Khan	-	1 Hold-out		Sensitivity, Fall-out,	-	CART, J48, REPTree, and four
				[320]				Accuracy, Precision, Size, Time, MC		NB-based variants

Table 32 Acronyms used to identify several HH-based methods for DTI.

Acronym	Description								
Genetic algorith	Genetic algorithms:								
AutoGA	GA-based method to search a GP configuration [333]								
HEAD-DT	Hyper-heuristic EA for designing DT algorithms [334]								
HEARpart	Hyper-heuristic Evolutionary Approach with Recursive and Partition Trees [335]								
HHDT	Hyper-heuristic GA for DTs [336]								
MOHEAD-DT	Multi-objective HEAD-DT [337]								
Grammatical eve	olution:								
AutoGE	GE-based method to search a GP configuration [338]								
ESC-GE	Evolutionary Split Criteria with Grammatical Evolution [339]								



 $\textbf{Fig. 29.} \ \ \textbf{Timeline of HH-based approaches to build DTI methods}.$

criterion for a DTI method. Each chromosome in the population represents a split criterion that is incorporated into a DTI algorithm. Furthermore, *Nyath & Pillay* introduce AutoGE [338], a version of AutoGA that uses GE to find the near-optimal GP parameters to induce DTI methods.

7.3. Discussion

Except for the method of *Jovanovic* et al. that groups the categorical values in two or more sets, the HH-based methods use the multibranching criterion to manage these attributes. In particular, in the HHDT method, the values of numeric attributes are discretized to be handled as categorical attributes.

In Table 33 are shown the components of the HH-based approaches to building DTI methods. Both HHDT and HEAD-DT methods, and the work of *Jovanovic* et al. evaluate an single-objective fitness functions, the ESC-GE procedure implements an aggregating fitness function, and the MOHEAD-DT method applies a multi-objective fitness function. Test accuracy is the fitness measure most commonly evaluated by these approaches. On the other hand, both the sequence of values as representation scheme and the random generation of candidate solutions for the initial population are the components included in these procedures. Finally, tournament-based selection, single-point crossover, and uniform mutation are the genetic operators commonly used by these methods.

Finally, Table 34 resumes the experimental studies reported in the existing literature in which a hyper-heuristic is implemented to build DTI methods. In this Table is shown that seven methods use UCI datasets, and the ESC-GE method uses another type of dataset. Most of them implement the k-fold CV, and they calculate the test accuracy of DTI method as a performance measure. F-score and size are also evaluated each one in four studies. Six studies implement a statistical test to compare their results with those reported by other approaches.

Hyper-heuristics are novel approaches where classification methods are created to induce DTs. Although these schemes use some MHs, they select the best combination of elements to build a DT. Hyper-heuristics have been applied in two schemes: 1) to build DTI methods combining several components, and 2) to select the best splitting criterion used by one DTI method. However, the model creation process uses a recursive-partitioning strategy. They can have better performance than those models induced using traditional schemes. However, they are created using a greedy scheme, and the problems related to this induction scheme remain.

8. Summary analysis

In the following paragraphs, a summary analysis of the different MH-based approaches for DTI is developed. First, a general classification of the methods described in this paper is presented. Then, a summary analysis of their components and the elements considered in the experimental studies is completed. A histogram based on the published year of these methods is depicted in Fig. 30.

8.1. General classification

SS-based methods: Their classification is detailed in Table 35. These MHs have been implemented only as recursive-partitioning and subsequent-optimization strategies (Fig. 31(a)). They have been used to build oblique and axis-parallel DTs in similar proportion (Fig. 31(b)), and only five types of these MHs have been used for DTI (Fig. 31(c)), highlighting the implementation of those based on SA (50%).

EA-based procedures: Table 36 shows their classification. Global search (78.86%) is the strategy most commonly used to build DTs with these methods (Fig. 32(a)). In particular, EAs implementing a recursive-partitioning strategy are currently used to induce multivariate DTs. Fig. 32(b) shows that they are mainly used to generate either axis-parallel (66.67%) or oblique DTs (17.89%). Also, non-linear and soft DTs are induced to a lesser extent. Table 36 indicates that LGA and GP-based

 Table 33

 Components of HH-based approaches to build DTI methods.

ıtion		Numerical chromosomes randomly created	Numerical chromosomes randomly created	String chromosomes randomly created	Vumerical chromosomes randomly created	Numerical chromosomes randomly created	Numerical chromosomes randomly created	Binary chromosomes randomly created	Integer chromosomes randomly created
Initial population		Numerical ch	Numerical ch		_		Numerical ch	Binary chrom	Integer chron
	Mutation	Uniform	Uniform	Special	Bit-string	Uniform	Uniform	Uniform	Uniform
S.	Crossover	Single-point	Single-point	Uniform	Uniform	Single-point	Single-point	Single-point	Single-point
Genetic operators	Selection	Tournament	Tournament	Roullete	Linear ranking	Tournament	Tournament	Tournament	Tournament
Fitness	measure	Accuracy	Accuracy	Accuracy	Accuracy	Accuracy	Accuracy	Precision+Sensitivity	F-Score, Size
Rep.	scheme	Linear	Linear	Linear	Linear	Linear	Linear	Linear	Linear
Year		2009	2011	2014	2017	2021	2018	2014	2015
Studies		HHDT [336]	HEAD-DT [334,340]	Jovanović et al. [341]	AutoGA [333]	HEARpart [335]	AutoGE [338]	ESC-GE [339]	MOHEAD-DT [337]
		٠							
MH		LGA					GE	GE	LGA
FF		UF						AF	MF
DT		AP							
Stra-	tegy	CS							

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Table 34 Experimental evaluation reported by hyper-heuristics.

Stra-	DT	MH		Studies	Datasets		Sampling	Performance	Statistical	Compared methods
tegy					UCI	other	method	measures	tests	
GS	AP	LGA		HHDT [336]	12	-	9-f CV	Accuracy	-	ID3
			•	HEAD-DT [334,340]	20	-	10-f CV	Accuracy, F-Score, Size	Friedman, Nemenyi	C4.5, CART
				Jovanović et al. [341]	16	-	10-f CV	Accuracy	-	C4.5, REPTree, Alternating DT [343], LR-based DTI method [344]
				MOHEAD-DT [337]	20	-	10-f CV	F-Score, Size	Friedman, Nemenyi	C4.5, CART, HEAD-DT
				AutoGA [333]	11	-	Hold-out	Accuracy	Friedman, Nemenyi	GP, ANN, SVM
			•	HEARpart [335]	30	-	Hold-out	F-Score, Error, Size	Friedman, Nemenyi	J48, CART, ATM
		GE	٠	ESC-GE [339]	-	20	5-f CV	Accuracy, F-Score, Size	Friedman, Nemenyi	J48
			•	AutoGE [338]	22	6	Hold-out	Accuracy,Time	Friedman, Bonferroni	AutoGA, GP-based approaches

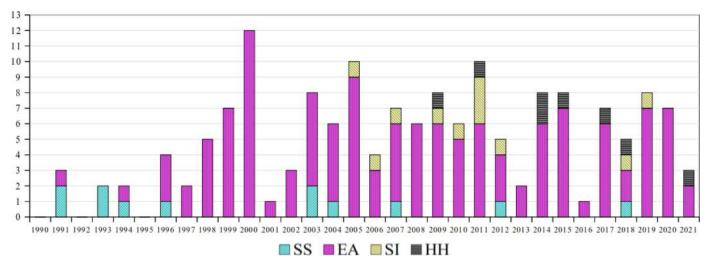


Fig. 30. Number of papers published from 1991 to 2021.

Table 35 SS-based MHs for DTI.

Stra- tegy	DT	MH	Num studies	Studies
RP	AP	GRASP	1	Pacheco et al. [142]
	OB	SLS	1	OC1 [134,135]
		SA	2	SADT [37]; OC1-SA [137]
		TS	2	LDTS [139]; LDSDT _{TS} [36]
SO	AP	SA	3	Sutton [141]; Bucy & Diesposti [101,140]; SACS [136]
		VNS	1	Vila Boas et al. [143]
	OB	TS	1	EPTS [138]
	SF	SA	1	Dvořák & Savický [145]

methods construct non-linear DTs, too. Fig. 32(c) shows that GP is the MH most used to induce DTs (43.09%). Nevertheless, if LGA and TGA are combined, they represent 38.21% of these approaches. In contrast to these MHs, other EAs have been less applied for constructing DTs. They represent 18.7% of all these methods, in comparison with 81.3% of studies using GA or GP for DTI.

SI-based methods: The only DT type induced with SI methods is the axis-parallel DT (Table 37). Fig. 33(a) shows that a global search is typically conducted in these methods (72.73%), and Fig. 33(b) illustrates that PSO is the most used method to build DTs.

Hyper-heuristics: Table 38 shows that LGA is the MH most widely used to implement DTI algorithms. Axis-parallel DTs are the only DT type induced for the classifiers created with these methods.

Summary: Tables 39 and 40 show the classification of MHs-based approaches for DTI by type of strategy implemented and by the sort of induced DT, respectively. Fig. 34(a) shows that the global search is the prominent strategy implemented for MHs (68.18%), and in Fig. 34(b) is shown that axis-parallel DTs are the most common type of induced DT (58.44%). In Fig. 34(c) is observed that GA (34.41%) and GP (34.42%) are the most common types of MHs implemented for DTI.

8.2. Algorithm components

Fitness functions: Single-objective fitness function is the prominent fitness function evaluated in these studies (58.44%). Also, the aggregating fitness function is implemented in 45 studies (29.23%), and only 19 methods (12.54%) evaluate a multi-objective fitness function (Fig. 35 and Table 41).

Representation schemes: Fig. 36 and Table 42 show that the candidate solutions are represented as tree-like structures in 84 studies (54.55%), sequence of values in 67 studies (43.51%), and matrices in only three studies (1.95%).

Fitness measures: Fig. 37 and Table 43 show that accuracy (31.03%) and size (20.26%) are the fitness values more used in these EA-based methods. In the other MH types, the error-rate is more used (1.72% in both classes). Alternatively, information gain, twoing rule, and the Gini index are the most used splitting criteria to conduct the search procedure.

Genetic operators: The kinds of selection, crossover, and mutation operators used for EA-based approaches for DTI are shown in Tables 44, 45, and 46, respectively. Tournament and roulette-wheel-based selection operators are used in 67 and 23 studies, respectively. Single-point crossover in 18 studies and uniform mutation in 15 studies are the most common operators implemented when the chromosomes are sequences of values. Alternatively, sub-tree swapping (65 studies) and sub-tree replacement (40 studies) are most used with tree-like structures. Fig. 38 shows the distribution of the genetic operators implemented in these approaches.

8.3. Experimental studies

Sampling methods: Fig. 39 shows that hold-out (37.58%) and cross-validation (50.30%) are the more popular sampling methods. Table 47 shows that eleven methods use the complete dataset in their experimental analysis.

Performance measures: Fig. 40 shows that accuracy (40.28%) and size (28.82%) are the preferred measures to determine the quality of the induced DTs. Error-rate and the running time have also been used in these experimental studies (Table 48).

Statistical tests: Friedman test (20.93%), t-test (16.27%), Wilcoxon test (12.79%), and Nemenyi post-hoc test (11.63%) are the most adopted statistical tests in the reported studies (Fig. 41). Table 49 shows the complete distribution of each test used in these approaches.

Table 36 EA-based approaches for DTI.

Stra- tegy	DT	MH	Num studies	Studies
RP	AP	TGA	1	Rzheutskaya et al. [216]
		DE	1	Mitrofanov & Semenkin [303]
	OB	LGA	6	BTGA [154]; OC1-GA [11,137]; Krętowski [33]; RCGA-kDT [173]; Pangilinan &
				Janssens [180]; HBDT [169]
		DE	3	OC1-DE [289]; AJADE-MDT [287]; PA-DE
				[290]
		ES	2	OC1-ES [11,137]; MESODT [292]
	NL	LGA	2	GA-QDT [161,183]; NLDT [172]
		GP	2	Marmelstein & Lamont [237]; GIODeT [277]
	SF	LGA	4	Janikow [184]; GC-SDT [39]; GA-FID3 [160]; FVBDT [158]
GS	AP	LGA	10	Caltrop [7]; Bandar et al. [87]; MEPDTI [171]; Cha & Tappert [175,176]; ECCO
				[155]; evtree [3]; BiLeGA [153]; Ersoy
				et al. [178]; Smith [177]; EVO-Tree [157]
		TGA	15	GAIT [102]; GAIT [204,211–214];
				Sorensen & Janssens [88]; Bosnjak et al.
				[210]; genTrees [168]; GATree
				[163,206]; GDT [9]; Biedrzycki & Arabas
				[215]; GDT-MC [165]; Jurczuk et al.
				[207–209]; GDT-MA [164]; MS [113];
				LEGAL-Tree [10,205]
		GP	42	Koza [4]; Iba et al. [247]; GPDT [238];
				EDDIE [230]; Shirasaka et al. [263];
				Cellular GP [226,253]; Zhao & Shirasaka
				[264]; Oka & Zhao [103]; Tanigawa &
				Zhao [265]; BGP [225,269]; Niimi &
				Tazaki [250]; EPTree [233]; GPTree
				[267,268]; To & Pham [254]; GPEI
				[240,272]; Karakatič & Podgorelec [273];
				FGP [5,234]; Johansson et al. [260]; Tur 8
				Guvenir [89]; Ryan & Rayward-Smith
				[252]; Niimi & Tazaki [249]; GPDTI
				[239]; Kuo et al. [257]; DTiGP [229];
				MGP [242]; Saremi & Yaghmaee
				[275,276]; Karakatič et al. [274]; CGP
				[227]; Johansson et al. [259]; MGP [241]
				EDDIE-101 [231]; Haruyama & Zhao
				[266]; Eggermont et al. [270,271]; EMO
				[232,248]; NHEMOtree [244]; MOGP
				[243]; CH-MOGP [228]; Khoshgoftaar
				et al. [255,256]; Zhao [258]; GCP/SA
			_	[296]; Mitrofanov [309]
		DE	2	DE-ADT ^{SPV} [8]; Dolotov & Zolotykh [302]
		ES	1	Dolotov & Zolotykh [302]
		CEA	4	Aitkenhead [301]; SAEDT [286,298–300];
		GEP	2	MPGA [284]; MPGT [285] Ferreira [307]; Wang et al. [308]; GEPDT
				[294]
		GE	3	Ono & Kushida [306]; GEDT [304]; MGEDT [295]
		EDA	1	Ardennes [293]
	OB	LGA	2	GDTI [167]; EFTI [156]
		TGA	6	TARGET [174]; GEA-ODT [217,218];
				GDT-Mix [166]; Krętowski & Popczyński
				[219]; Czajkowski et al. [114]; Reska et al
				[220]
	***	DE	2	PDT [291,310]; DE-ODT [288]
	NL	LGA	1	GALE [162,182]
		GP	3	Mugambi & Hunter [279]; G ³ P [236,278]; Š progar [262]
		GE	1	Russo et al. [311]
	SF	LGA	1	Kym & Ryu [188]
		GP	2	Fuzzy-GP [235]; PFDT [246]
		GEP	1	Weihong et al. [312]
SO	AP	LGA	2	Chen et al. [189]; Brunello et al. [190]
	SF	LGA	3	Crockett et al. [185]; G-DT [159]; IIVFDT
				[170]

Table 37 SI-based MHs for DTI.

Stra- tegy	DT	МН	Num studies	Studies
RP GS	AP AP	PSO ACO	1 4	Chan et al. [326] ACDT [12,324]; cACDT [318]; ACO-DTree [317,323]; ATM [13]
		PSO BA	3 1	TSO [321]; DT-MPSO [319]; Fieldsend [325] BTC [322]
SO	AP	PSO	2	APSO [327]; Malik & Khan [320]

Table 38 HH-based approaches to build DTI methods.

DT	МН	Num studies	Studies
AP	LGA GE	6 2	HHDT [336]; HEAD-DT [334,340]; <i>Jovanović</i> et al. [341]; AutoGA [333]; HEARpart [335]; MOHEAD-DT [337] AutoGE [338]; ESC-GE [339]

Table 39MH-based approaches by type of strategy applied.

МН Туре	MH	RP	GS	SO	Total
SS	GRASP	1			1
	SLS	1			1
	SA	2		4	6
	TS	2		1	3
	VNS			1	1
	Subtotal	6	0	6	12
EA	LGA	12	20	5	37
	TGA	1	15		16
	GP	2	51		53
	DE	4	4		8
	ES	2	1		3
	CEA		4		4
	GEP		3		3
	GE		6		6
	EDA		1		1
	Subtotal	21	105	5	131
SI	ACO		4		4
	PSO	1	3	2	6
	BA		1		1
	Subtotal	1	8	2	11
Total		28	113	13	154

DE 4 4 8 DE ES 2 1 3 ES

Table 40 MH-based approaches for type of induced DT.

МН Туре	MH	AP	OB	NL	SF	Total
SS	GRASP	1				1
	SLS		1			1
	SA	3	2		1	6
	TS		3			3
	VNS	1				1
	Subtotal	5	6	0	1	11
EA	LGA	18	8	3	8	37
	TGA	13	3			16
	GP	43	4	4	2	53
	DE	3	5			8
	ES	1	2			3
	CEA	4				4
	GEP	2			1	3
	GE	5		1		6
	EDA	1				1
	Subtotal	90	22	8	11	131
SI	ACO	4				4
	PSO	6				6
	BA	1				1
	Subtotal	11	0	0	0	11
Total		106	28	8	12	154

Table 41 MH-based approaches by fitness function.

МН Туре	MH	UF	AF	MF	Total
SS	GRASP	1			1
	SLS	1			1
	SA	5	1		6
	TS	2	1		3
	VNS		1		1
	Subtotal	9	3	0	12
EA	LGA	28	7	2	37
	TGA	6	9	1	16
	GP	23	17	13	53
	DE	8			8
	ES	3			3
	CEA	1	3		4
	GEP	3			3
	GE	3	2	1	6
	EDA	1			1
	Subtotal	76	38	17	131
SI	ACO	1	3		4
	PSO	3	1	2	6
	BA	1			1
	Subtotal	5	4	2	11
	Total	90	45	19	154

Table 42 MH-based approaches by representation scheme.

МН Туре	MH	Linear	Tree	Matrix	Total
SS	GRASP	0	1		1
	SLS	1			1
	SA	2	4		6
	TS	2	1		3
	VNS		1		1
	Subtotal	5	7	0	12
EA	LGA	37			37
	TGA		16		16
	GP		53		53
	DE	8			8
	ES	3			3
	CEA		4		4
	GEP	3			3
	GE	6			6
	EDA		1		1
	Subtotal	57	74	0	131
SI	ACO		2	2	4
	PSO	5		1	6
	BA	0	1		1
	Subtotal	5	3	3	12
	Total	67	84	3	154

Table 43 MH-based approaches by fitness measure.

MH	MH	Split	ting criteria			Perfo	rmance i	measures		Tota
type		IG	Twoing	Gini	Other	Acc	Size	Error	Other	1 6 7 4 2 20 46 28 88
SS	GRASP	1								1
	SLS	1	1	1	3					6
	SA		1	1	2		1	2		7
	TS	1			1			2		4
	VNS					1	1			2
	Subtotal	3	2	2	6	1	2	4	0	20
EA	LGA	3	2	3	2	17	10	6	3	46
	TGA					12	10	3	3	28
	GP	3			4	29	24	10	18	88
	DE	1	1		2	3		1		8
	ES	1	1		1	1				4
	CEA					4	2		1	7
	GEP					3				3
	GE					2	1	1	5	9
	EDA					1				1
	Subtotal	8	4	3	9	72	47	21	30	194
SI	ACO		2		1			1	3	7
	PSO				1	2	2	3	2	10
	BA					1				1
	Subtotal	0	2	0	2	3	2	4	5	18
	Total	11	8	5	17	76	51	29	35	232

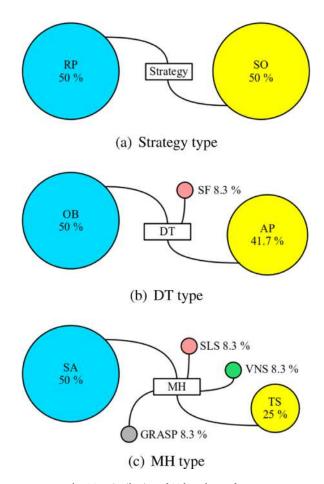


Fig. 31. Distribution of SS-based MHs for DTI.

9. Open questions and conclusions

DTI algorithms stand out from other machine learning techniques since they are simple procedures creating more accurate models with a high interpretability level. An essential aspect of increasing the model

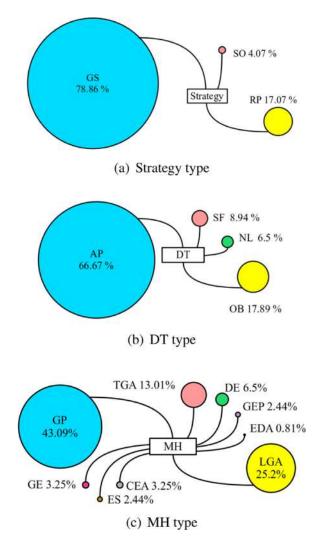


Fig. 32. Distribution of EA-based MHs for DTI.

Table 44 EA-based approaches by selection operator.

МН	Tournament	Roulette	Linear Ranking	Special	Truncate	Other	Total
LGA	12	11	1	2		1	27
TGA	3	4	4	1		1	13
GP	37	5		3	5		50
DE	8						8
ES				1			1
CEA	1		2				3
GEP		3					3
GE	6						6
EDA					1		1
Total	67	23	7	7	6	2	112

Table 45 EA-based approaches by crossover operator.

MH	Linear chromo	osome			Tree-based chromosome				Total
	Single-point	Double-point	Special	Other	Switch sub-trees	Switch nodes	Switch branches	Other	
LGA	10	8	5	6					29
TGA					15	7	4		26
GP					46		1	4	51
DE				8					8
ES			1						1
CEA					3				3
GEP	3	3	3						9
GE	5				1				6
Total	18	11	9	14	65	7	5	4	133

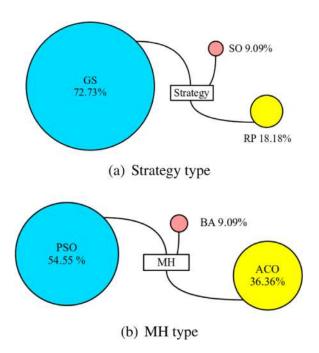


Fig. 33. Distribution of SI-based MHs for DTI.

utility is reducing this complexity level. In DTs, it is associated with its size, then it is critical to generate trees with the least number of nodes.

9.1. Implementation strategies

For avoiding the existing problems of greedy-search-based approaches, several MHs have been used to build DTs. This review identifies three strategies to use MHs as DTI algorithms: recursive partitioning, global search, and subsequent optimization.

Swarm and evolutionary computation methods successfully perform a global search in complex spaces, and EAs have been extensively applied to induce DTs. Although SI methods are remarkably effective in solving numerical optimization problems, their use in this field is limited. In both cases, several challenges must be faced, such as the solution representation, the creation of operators to guarantee the induction of feasible DTs and the issues associated with the particular characteristics of each MH.

Two drawbacks of these approaches are (1) their dependence on the definition and setting of a set of control parameters and (2) the time required for a population of DTs to converge to near-optimal solutions. In particular, GP-based approaches for DTI involve developing strategies to preserve population diversity and avoid the bloat phenomenon.

However, the main challenge in these approaches is to determine the fitness value of each candidate solution. Since each one is evaluated using the training instances, the processing time increases depending on the dataset size. A recently adopted option to deal with this problem is through parallel induction approaches to spread the processing charge into several computing units.

Alternatively, MHs have also been used to replace the traditional splitting criteria in the induction process. They can (1) solve the selection bias problem in axis-parallel DTs by adjusting their fitness function and (2) improve multivariate test conditions used on oblique and non-linear DTs. However, overfitting and instability of small changes in the training set persist since these problems are inherent to a greedy strategy. Here, SS-based MHs are well placed to implement a recursive partitioning strategy, although they can search in any solution space using suitable representation schemes. One advantage of these MHs is that they consume less time in their searching process than that used for population-based methods.

Finally, the use of MHs to improve a DT generated using another technique allows preserving the model's general structure, and by refining its elements, it can improve its predictive power, but always limited to the neighborhood of the original model.

9.2. Types of decision trees

MHs can induce any DT type, but axis-parallel DTs are the most common model built with them. Although multivariate and soft DTs can be more compact and better than the first, their induction through an MH is a little-studied approach. Non-linear DTs with few nodes can be con-

Table 46 EA-based approaches by mutation operator.

МН	Linear chromosome				Tree-based chromosome				
	Bit-String	Uniform	Special	Other	Switch sub-trees	Distub node	Replace Node	Other	
LGA	7	10	10	2					29
TGA						10	7	16	33
GP					36	11	3	9	59
DE				8					8
ES			3						3
CEA					3	4			7
GEP		3	3						6
GE	3	2			1				6
Total	10	15	16	10	40	25	10	25	151

Table 47 MH-based approaches by sampling method.

MH Type	MH	CV	Hold-out	Complete	Other	Total
SS	GRASP	1				1
	SLS	1				1
	SA	2	2	1	1	6
	TS	3				3
	VNS	1				1
	Subtotal	8	2	1	1	12
EA	LGA	13	4		1	18
	TGA	17	17	2	4	40
	GP	25	23	3	1	52
	DE	7	2		1	10
	ES	1	1		1	3
	CEA	2	3	1		6
	GEP	2	1	1		4
	GE	2	3	1		6
	EDA	1				1
	Subtotal	70	54	8	8	140
SI	ACO	2	4			6
	PSO	2	2	2		6
	BA	1				1
	Subtotal	5	6	2	0	13
	Total	83	62	11	9	165

structed using an MH. However, they have a less expressive power than that of axis-parallel DTs. A possible research line is to find a minimal combination of attributes in each internal node providing the same interpretation level as one axis-parallel DT.

9.3. Experimental studies

Similarly to other studies where some DTI method are analyzed, most of the studies detailed in this review focus on describing how an MH is

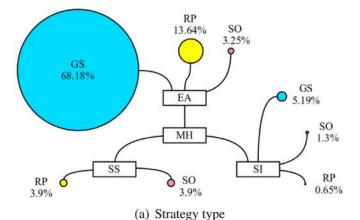
Table 48MH-based approaches by performance measure.

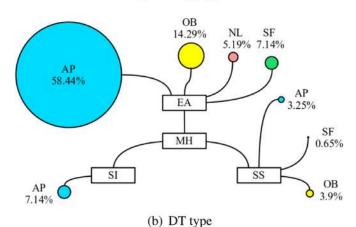
MH								
Type	MH	Accuracy	Size	Error	Time	F-Score	Other	Total
SS	SLS	1	1					2
	SA	2	4	3	1			10
	TS	1	2	2	2			7
	VNS	1	1		1			3
		6	9	5	4	0	0	24
	Subtot	al						
EA	LGA	14	11	3	4	3	1	36
	TGA	32	23	3	8	2	3	71
	GP	31	17	11	5	2	10	76
	DE	7	5		1	1		14
	ES	3	2		1			6
	CEA	6	4			1	6	17
	GEP	4						4
	GE	3	3	2	1	2	1	12
	EDA	1	1					2
		101	66	19	20	11	21	238
	Subtot	al						
SI	ACO	4	4	1	1			10
	PSO	4	3	2	1		4	14
	BA	1	1					2
		9	8	3	2	0	4	26
	Subtot	al						
	Total	116	83	27	26	11	25	288

used to build a DT, and statistical analysis is not conducted. A large percentage only present comparisons of the experimental results and the complexity of the induced DT or use the average results and then apply a paired t-test. Just 13 of the 154 studies in the existing literature use a post-hoc test to compare the performance of their methods with other classifiers.

Table 49MH-based approaches by statistical test.

МН Туре	MH	Friedman	t-test	Wilcoxon	Nemenyi	Avg	WTL	Other	Total
SS	GRASP		1			1	1		3
	SA		1						1
	TS					1		2	3
	Subtotal	0	2	0	0	2	1	2	7
EA	LGA	4	3	1	4			2	14
	TGA	2	6	1	1	5		5	20
	GP	3	1	8	1	2	3	5	23
	DE	4	1		2			3	10
	ES		1						1
	CEA	1			1				2
	GE	2			1			1	4
	EDA							1	1
	Subtotal	16	12	10	10	7	3	17	75
SI	ACO	2		1				1	4
	Subtotal	2	0	1	0	0	0	1	4
	Total	18	14	11	10	9	4	20	86





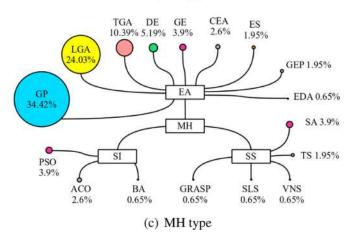


Fig. 34. Distribution of MH-based approaches for DTI.

9.4. Final remarks

This state-of-the-art review is developed to lump together all MH-based methods to build DTs under the same analytical perspective. This work shows the close relationship between machine learning and swarm and evolutionary computation methods, intending to provide better solutions to real problems in science and engineering. DTs are necessary when it is required that a predictive model be sufficiently understandable, and a decision-maker can reproduce a sequence of decisions taken to discriminate one case of study from another. As an extension of the review described in this manuscript, our next step is to conduct a study on the use of MHs to implement other types of DT-based classifiers such as random forests and multi-trees.

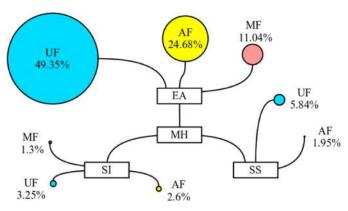


Fig. 35. Distribution of fitness functions.

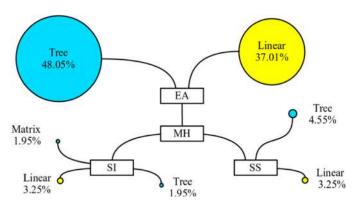


Fig. 36. Distribution of representation schemes.

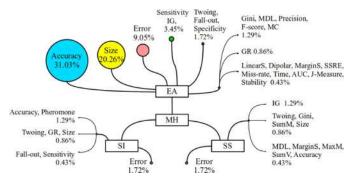
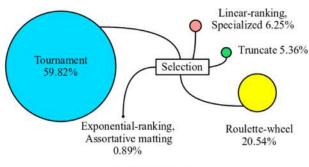


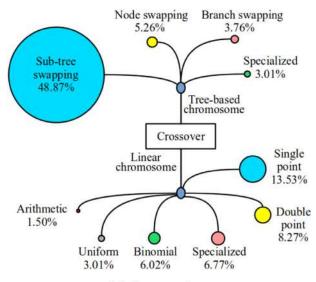
Fig. 37. Distribution of fitness measures.

The use of MH for DTI has provided a new approach to building classifiers with better performance, especially by performing a global search in the solution space. Even though its application to induce DTs began three decades ago, currently presents many opportunities to study and new challenges since there are characteristics of MHs that must be analyzed in the machine learning context.

Since DTs are classifiers distinguished by their simplicity and high level of interpretability, the implementation of new approaches to induce near-optimal DTs is highly important in emerging research areas such as biotechnology, neuroscience, genomics, proteomics, and medical decision making. The use of MH-based approaches for DTI is a promising trend to build classifiers with higher performance. These schemes can combine their exploration and exploitation skills, providing a better way to discover the relationships between the attributes used in the training set. Another potential development area is applying SI-based MHs for DTI by defining schemes allowing an efficient search in the tree space using SI procedures to update the particle position in the swarm. Furthermore, the use of grammar-based MHs can guaran-



(a) Selection type



(b) Crossover type

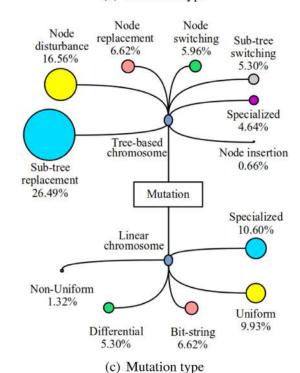


Fig. 38. Distribution of genetic operators.

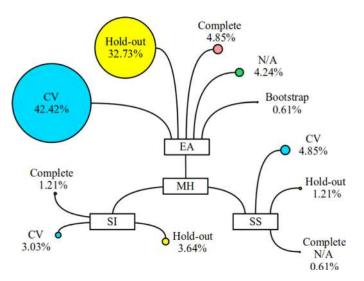


Fig. 39. Distribution of sampling methods.

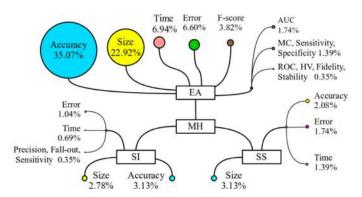


Fig. 40. Distribution of performance measures.

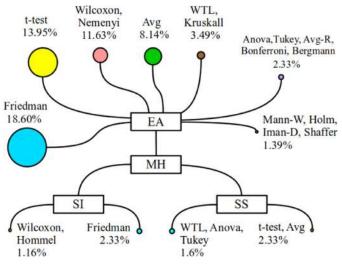


Fig. 41. Distribution of statistical tests.

tee the construction of only feasible candidate solutions. Finally, hyperheuristics to build algorithms that induce DTs are a strategy that has been gaining interest recently.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper

CRediT authorship contribution statement

Rafael Rivera-Lopez: Conceptualization, Methodology, Formal analysis, Investigation, Writing – original draft. Juana Canul-Reich: Conceptualization, Methodology, Formal analysis, Investigation, Supervision, Writing – review & editing. Efrén Mezura-Montes: Methodology, Formal analysis, Writing – review & editing, Supervision. Marco Antonio Cruz-Chávez: Methodology, Formal analysis, Writing – review & editing.

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