### 1 Data

In the following, some details about the dataset.

The description of the main columns in the Table 1.

# 2 Embedding

Some basic information of our final dataset to remark is certainly the number of triples  $1\,558\,700$ , that depends on the number of single instances reported in Tables  $2,\,3,\,4$ .

# 3 KG prediction data

Table 5 reports all value for, all the 9 selected clusters of health services, among the initial 13 clusters.

Field-Name	Type	Explanation
booked-date	date	date of the booked appointment
reservation-date	date	date of the first contact with the booking staff, is also
		the date of the insertion of the record in the database.
last-reservation-	date	last update of the reservation, which usually matches
change-date		the reservation-date
encrypted-nin-id	str	encrypted national insurance number. Used as a non-decriptable numeric ID of the patient, special value $-1$ represents undefined patients
gender	long	1 for male, 2 for female, $-1$ undefined (for anonymous patients)
patient-age	long	age of the patient at the time of the issue of the referral, special value $-1$ is for anonymous patients
nuts-istat-code	long	Italian nuts code, it identifies local administrative areas, it can be linked to postal codes
booking-agent-id	long	anonimized numeric ID of the booking agent
medical-branch-id	str	alphanumeric string that contains a code of the med-
		ical branch
health-service-id	str	alphanumeric ID of the health service
practitioner-id	long	anonimized numerical identifier of the prescriber, spe-
		cial value $-1$ is for undefined practitioners
referral-centre-id	str	identification of the unit that delivers the appointment. It is the concatenation of the <i>dispenser</i> and the <i>ambulatory</i> , separated by the hyphen
appointment-encoding	str	concatenation of local-health-department-id and the appointment codification
booking-type	str	Numeric value: 1 is for direct check-in (e.g. from a hospital during a recovery), 0 is for the conventional booking reservation
referral-id	long	anonimized numeric ID of the referral
referral-date	date	the date of the issue of the referral from the practi-
		tioner to the patient
priority-code	str	the code of the priority of the referral
exemption-code	str	the code of the exemption with respect to the patient
		and the health service
number-of-health-	long	number of needed health-service-ids, rarely
services		greater than 1
status	str	status of the appointment: P: booked; A: canceled
local-health-	long	sub-regional local health department. In our data set
department-id		there are three departments, identified with ${\tt A},{\tt B}$ and
		C

Table 1: Data set features. The table contains the description of the main columns of the local health department booking center  $\frac{1}{2}$ 

@has-relations	Number of instances
@has-booked-date	149198
@has-reservation-date	122744
@has-number-of-health-services	122744
@has-appointment-encoding	122744
@has-booking-type	122744
@has-referral-id	31679
@has-referral-modified-id	31679
@has-patient-age	31679
@has-referral-date	30630
@has-exemption-code	21545
@has-priority-code	10958
@has-nuts-istat-code	3584
@has-local-health-department-id	2907
@has-practitioner-id	1991
@has-referral-centre-id	1837
@has-encrypted-nin-id	1747
@has-gender	1747
@has-refined-medical-branch-id	1337
@has-health-service-id	1316
@has-booking-agent-id	1070
@has-health-service-description	1023
@has-refined-health-service-id	1023
@has-official-branch-description	131
@has-medical-branch-id	131
@has-branch-description	131

Table 2: Number of instances in the @has type relations,, those a re the ones that express a property of either an entity or a relation (i.e. hyper-relation)

relation-entity links	Number of instances
reserved-health-service	122744
updating-agent	122744
booked-referral	122744
booking-agent	122744
referring-centre	84673
referrer	31679
prescribed-health-service	31679
referred-medical-branch	31679
referred-patient	31679
cure-provider	9537
cured-patient	9537
provided-health-service	9471
health-service-provider	9471

Table 3: Number of instances of relation kind.

entities and meta-relations	Number of instances
reservation	122744
referral	31679
health-care	9537
provision	9471
practitioner	1991
appointment-provider	1837
patient	1747
booking-staff	1070
medical-branch	1023

Table 4: Number of instances of entity kind.

#### lccccccc

Nearest Neighbors Linear SVM RBF SVM Gaussian Process Random Forest Neural Network Naive Bayes QDA XGBoost

#### Cluster

- $0.59 \pm 0.024$  **0.67**  $\pm$  **0.027**  $0.58 \pm 0.025$  **0.67**  $\pm$  **0.03**  $0.62 \pm 0.024$   $0.64 \pm 0.028$   $0.65 \pm 0.027$   $0.63 \pm 0.02$   $0.65 \pm 0.022$

- $0.51 \pm 0.029$   $0.54 \pm 0.028$   $0.52 \pm 0.036$   $0.56 \pm 0.037$   $0.53 \pm 0.05$  **0.59**  $\pm$  **0.031**  $0.56 \pm 0.036$   $0.49 \pm 0.048$   $0.57 \pm 0.031$
- $0.54 \pm 0.031$   $0.6 \pm 0.044$   $0.6 \pm 0.034$   $0.59 \pm 0.041$   $0.6 \pm 0.037$  **0.62**  $\pm$  **0.044**  $0.61 \pm 0.036$   $0.5 \pm 0.055$  **0.62**  $\pm$  **0.033**
- $0.59 \pm 0.022$  **0.67**  $\pm$  **0.021**  $0.57 \pm 0.021$   $0.66 \pm 0.025$   $0.62 \pm 0.021$   $0.62 \pm 0.024$   $0.65 \pm 0.022$   $0.58 \pm 0.022$   $0.62 \pm 0.021$
- $0.57 \pm 0.031$   $0.69 \pm 0.025$   $0.59 \pm 0.028$   $0.71 \pm 0.028$   $0.69 \pm 0.027$   $0.67 \pm 0.022$  **0.72**  $\pm$  **0.024**  $0.54 \pm 0.026$   $0.71 \pm 0.026$
- $0.52 \pm 0.04$   $0.65 \pm 0.049$   $0.62 \pm 0.038$   $0.68 \pm 0.068$   $0.68 \pm 0.046$   $0.69 \pm 0.055$  **0.73**  $\pm$  **0.052**  $0.52 \pm 0.044$   $0.69 \pm 0.052$
- $0.59 \pm 0.02$  **0.65**  $\pm$  **0.026**  $0.57 \pm 0.025$   $0.64 \pm 0.041$   $0.62 \pm 0.027$   $0.64 \pm 0.028$   $0.64 \pm 0.025$   $0.62 \pm 0.022$   $0.64 \pm 0.021$
- MEAN  $0.55 \pm 0.034$   $0.63 \pm 0.052$   $0.57 \pm 0.031$   $0.64 \pm 0.048$   $0.61 \pm 0.051$   $0.63 \pm 0.04$  **0.65**  $\pm$  **0.052**  $0.55 \pm 0.052$   $0.62 \pm 0.065$

Table 5: AUC values of every classification techniques, repeated 30 times, for every selected cluster written in the form of (mean  $\pm$  std). In the last row the means values of every classification techniques. Bolded values are the best values for every row.