Algorithm 1: MS-EPSO pseudocode

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Input: Objective function f(x), D, LB, UB, NP, NFE, \tau, CP, NR, MLL
      Output: Best solution found P_g = \{x_1, x_2, x_3, ..., x_D\}
      // After each function evaluation:
      /// 1) Increment FEs counter;
// 2) Check for a possible new global best;
      // 3) Check the stopping criteria.
 1 FEs \leftarrow 0
 1 PLS \leftarrow 0
2 MaxV \leftarrow abs(UB - LB)
3 MinV \leftarrow MaxV * -1
 4 for i \leftarrow 0 to to NP do
            Initialize particle (x_i) between [LB, UB]
Initialize velocity (v_i) between [MinV, MaxV]
 6
            Initialize strategic weights (w_{i1}^*, w_{i2}^*, w_{i3}^*, w_{i4}^*) between [0, 1] Initialize local limit (PLL_i) \leftarrow 0
 8
            Initialize exploration mode (EXP_i) \leftarrow 1
 9
10
            x_{i\mu} \leftarrow \mu(x_i)
11
            x_{i\sigma} \leftarrow \sigma(x_i)
            x_{if} \leftarrow f(x_i)
12
13 end
14 Save all local best information (\hat{x}_i, \hat{x}_{if}, \hat{x}_{i\mu}, \hat{x}_{i\sigma})
15 Save global best information (x_g, x_{gf}, x_{g\mu}, x_{g\sigma})
16
     repeat
             \begin{array}{c} \textbf{for} \ i \leftarrow 0 \ to \ \textbf{to} \ NP \ \textbf{do} \\ Rule_1 \leftarrow PLL_i < MLL \land EXP_i \ ? \ 1:0 \\ Rule_2 \leftarrow PLL_i < MLL \land \neg EXP_i \ ? \ 1:0 \\ Rule_3 \leftarrow PLL_i \geq MLL \ ? \ 1:0 \end{array} 
17
18
19
20
                   if Rule_1 then
21
                          x_{new} \leftarrow \text{DrawFromGaussianDistribution}(x_{g\mu}, x_{g\sigma}, D) \text{ // } D \text{ samples}
22
23
                          x_{newf} \leftarrow f(x_{new})
                          best_{replica} \leftarrow \texttt{GenerateReplicas}(NR, w_i^*, \tau) \; \textit{//} \; \texttt{EPSO} \; \; \texttt{strategy}
24
25
                          best_{replicaf} \leftarrow f(best_{replica})
                   end
26
                   if Rule_2 then
                          best_{replica} \leftarrow \text{GenerateReplicas}(NR, w_i^*, \tau) \text{ // EPSO strategy}
                          best_{replicaf} \leftarrow f(best_{replica})
29
                          x_{new} \leftarrow \text{MoveParticle}(x_i, v_i, \hat{x}_i, x_g, CP) \text{// EPSO Movement}
30
                          x_{newf} \leftarrow f(x_{new})
31
                   end
32
                   if Rule<sub>3</sub> then
33
                          x_{new} \leftarrow \text{DrawFromGaussianDistribution}(\hat{x}_{i\mu}, \hat{x}_{i\sigma}, D) // D \text{ samples}
34
35
                          x_{newf} \leftarrow f(x_{new})
                          best_{replica} \leftarrow \texttt{GenerateReplicas}(NR, w_i^*, \tau) \text{ // EPSO strategy}
36
37
                          best_{replicaf} \leftarrow f(best_{replica})
                          PLL_i \leftarrow 0 \\ EXP_i \leftarrow 0
38
39
40
                   x_i, x_{if}, v_i, w_i^* \leftarrow Compare(x_{new}, best_{replica})
41
                   \hat{x}_i, \hat{x}_{if}, NewLocalBest? \leftarrow Compare(x_i, \hat{x}_i)
42
                   \mathbf{if}\ \mathit{NewLocalBest}\ \mathbf{then}
43
44
                          \hat{x}_{i\mu} \leftarrow \mu(\hat{x}_i)
                          \hat{x}_{i\sigma} \leftarrow \sigma(\hat{x}_i)
45
46
                          PLL_i \leftarrow PPL_i + 1
47
                   \mathbf{end}
48
            end
49
50 until FEs == NFE
```