

# Index

## A

Absolute space, 18  
 Accelerated expansion, 321  
 Accelerated frame, 108, 109, 112  
 Accelerated frame hyperbolically, 108  
 Accelerated reference frame, 89, 112  
 4-acceleration, 272  
 Acceleration in a rotating reference frame, 142  
 Acceleration of gravity, 14, 16, 135, 192, 194, 271, 283  
 Acceleration of particle in non-rotating frame, 142  
 Acceleration of particle in rotating frame, 142  
 Acceleration scalar, 272  
 Action, 127  
 Adiabatic, 327  
 Age-density relation, 384, 496  
 Age of the universe, 311, 315, 383, 489  
 Age-redshift relationship, 329, 341  
 Ampere's circuit law, 54  
 Angular acceleration, 95  
 Angular momentum, 228  
 Anisotropic universe models, 351  
 Anisotropy parameter, 352  
 Antisymmetric tensor, 78, 86, 119, 426  
 Antisymmetrization, 80  
 Archimedean spiral, 99  
 Atmospheric mesons, 421

## B

Basis forms, 178  
 Basis vector, 71, 147  
 Bergmann, 393  
 Bianchi

1<sup>st</sup> identity, 185, 186  
 component form, 185  
 2<sup>nd</sup> identity, 186, 201

Bianchi type-I, 351  
 Big Bang, 275  
 Big Bang cosmology, 361  
 Big Rip, 351  
 Binary system, 265, 266  
 Black body radiation, 44  
 Black hole, 221, 222, 263, 271, 273, 476  
 horizon, 271  
 radiation, 273  
 temperature, 273  
 Blueshift, 56  
 Boltzmann's constant, 273, 363  
 Boost, 35  
 Born-rigid motion, 108  
 Born-stiff motion, 108  
 Boyer-Lindquist coordinates, 276, 280, 299  
 Boyer-Lindquist coordinate system, 277, 281, 480, 482  
 Brill, 19, 377

## C

Canonical momentum, 128  
 Cartan  
 surface curvature, 183  
 Cartan connection, 147, 150  
 Cartan formalism, 183, 211  
 Cartan's structure equations, 178, 395  
 Cartan structure equations 1<sup>st</sup>, 148, 149, 178, 185, 212, 395, 456  
 Cartan structure equations 2<sup>nd</sup>, 178, 179, 185, 186, 212, 397, 457  
 Cartesian basis, 169

Cartesian coordinates, 47, 73, 75, 155, 164, 169  
 Cartesian coordinate system, 23, 34, 49, 61, 66, 67, 115, 116, 123, 140, 152, 177, 198, 444  
 Causal, 76  
 Causal mass, 378, 380  
 $\Lambda$ CDM universe, 380  
 Centrifugal acceleration, 143  
 Centrifugal barrier, 230  
 Centrifugal force, 19, 95  
 Centripetal acceleration, 99, 105  
 Chaotic inflation, 375  
 Cherenkov radiation, 57, 422  
 Chirp, 260, 267  
 Chirp mass, 263, 264  
 Christoffel, 122  
 Christoffel symbols, 122, 130, 135, 141, 142, 146, 155, 171, 177, 189, 190, 192, 195, 215, 244, 272, 282, 402, 449, 459, 475  
 Christoffel symbols in coordinate basis, 123  
 Christoffel symbols physical interpretation, 215  
 Christoffel symbols rotating reference frame, 141  
 Classical electron radius, 300  
 Clock, 78, 98  
 Codifferential, 157, 166  
 Cohen, 19, 377  
 Coincidence problem, 348  
 Commutator, 68, 143, 149, 155  
 Co-moving coordinate system, 64, 311  
 Conformally flat, 295, 296  
 Conformal time, 331, 383, 489  
 Connection coefficients, 123, 140, 142, 144, 145, 148, 176, 188  
 Connection coefficients in coordinate basis, 123  
 Connection coefficients rotating reference frame, 140  
 Connection forms, 147, 177, 183, 212, 457  
 Connections coefficients, 177  
 Conservation energy-momentum, 197  
 Conservation of mass-energy, 198  
 Constants of motion, 128, 156, 171, 453  
 Continuity equation, 197, 198, 366  
 Contraction, 69, 86, 149, 168, 177  
 Contractions of tensors, 427  
 Contravariant components, 74  
 Contravariant tensor, 70  
 Convective derivative, 151, 152  
 Coordinate basis, 120, 143, 150

Coordinate basis connection coefficients, 123  
 Coordinate basis forms, 161  
 Coordinate basis vector, 64, 66, 67, 141, 161, 179  
 Coordinate clocks, 24, 94, 109, 141, 216  
 Coordinate cyclic, 128, 129  
 Coordinate Gaussian, 123  
 Coordinate singularity, 239  
 Coordinate system, 23, 64  
 Coordinate time, 24, 98, 109, 112  
 Coordinate transformation, 65, 87, 91, 93  
 Coordinate vector, 62  
 Coriolis acceleration, 143, 193  
 Cosmic fluids, 317  
 Cosmic Microwave Background (CMB), 372  
 Cosmic microwave background radiation, 372  
 Cosmic red-shift, 323, 326  
 Cosmic time, 311  
 Cosmological constant, 204, 242, 318, 367, 462, 471, 484  
 Cosmological horizon, 359  
 Cosmological red-shift, 315–317  
 Cosmology, 311  
 Covariance principle, 17, 122  
 Covariant, 18  
 Covariant components, 86  
 Covariant derivative, 119, 122, 144–146, 153, 189  
 Covariant differentiation, 119  
 Covariant directional derivative, 124, 140, 144, 145, 153, 173, 188, 453  
 Covariant equation, 72  
 Covariant Euler-Lagrange equations, 127, 128  
 Covariant tensor, 70  
 Critical density, 345  
 Curl, 157, 160–162, 445  
 Current form, 166  
 Curvature, 173, 195, 456  
 forms  
 of surface, 183  
 Gaussian, 183, 184  
 geodesic, 181  
 normal, 181  
 principal, 182  
 Ricci, 177  
 Riemann tensor, 175  
 surface (Cartan formalism), 183  
 Curvature coordinates, 211, 216, 220, 222, 226

Curvature forms, 177, 212, 457  
 Curvature of space, 196  
 Curvature scalar, 457  
 Cyclic coordinate, 128, 228, 250  
 Cylinder conditions, 394  
 Cylinder coordinates, 93, 225  
 Cylinder dimension, 404

**D**  
 D'Alembertian wave operator, 162, 164  
 D'Alembert's wave operator, 157, 244  
 Deceleration parameter, 324, 342, 385, 494, 498  
 Deflection of light, 211, 236  
 Density parameter, 322, 345, 386, 499  
 de Sitter spacetime, 241, 321, 387, 471  
 de Sitter universe, 505  
 de Sitter universe models, 386, 501  
 Determinant, 81  
 Differential forms, 211  
   curvature  
     of surface, 183  
 Differential forms connection, 212  
 Differential forms curvature, 212  
 Differential forms, directional derivatives of, 145  
 Differential geometry, 179  
 Differential operator, 66, 140, 169, 444  
 Differentiation covariant, 124  
 Differentiation of forms, 119  
 Dimension, 59  
 Dirac delta function, 6  
 Directional derivative, 66, 140, 153, 156, 179  
 Distance coordinate, 211  
 Distance physical, 211  
 Divergence, 157, 162, 167, 170, 198, 445  
 D'Lambertian wave operator, 159  
 Domain wall, 309, 485  
 Doppler effect, 26, 311, 326, 418, 477  
 Dragging angular velocity, 251, 278  
 Dual, 82, 83, 160, 161, 167  
 Dual forms, 84, 169, 442  
 Dust, 200, 205, 317, 321, 328, 348  
 Dust dominated universe, 331  
 Dust-dominated universe model, 331, 333

**E**  
 Earth, 12, 20, 33, 34, 117, 226, 227, 232, 253, 264, 412, 413  
 Earth-Moon system, 21, 413, 414  
 Eccentricity, 266  
 Eddington, 255

Eddington-Finkelstein coordinates, 216, 219  
 Eddington-Finkelstein coordinate system, 220  
 Effective potential, 230  
 Ehrenfest's paradox, 89  
 Einstein, 15, 17, 19, 23, 31, 44, 45, 52, 99, 197, 201, 393  
 Einstein-de Sitter, 333  
 Einstein-de Sitter model, 342  
 Einstein-de Sitter universe, 378, 379, 490  
 Einstein field equations, 202, 241  
 Einstein's constant of gravity, 202  
 Einstein's curvature tensor, 201, 211, 285, 484  
 Einstein's field equations, 197, 201, 202, 206-208, 238, 243, 244-247, 255, 275, 284, 285, 295, 326, 462, 497  
 Einstein spaces, 204  
 Einstein's theory, 211  
 Einstein synchronization, 92, 101  
 Einstein synchronized, 25  
 Einstein tensor, 202, 211, 213, 284, 469  
 Electrical field, 53  
 Electric field, 209  
 Electric field strength, 163  
 Electricity, 51  
 Electric scalar potential, 163  
 Electromagnetic current form, 165  
 Electromagnetic field, 51, 167, 168, 201, 207  
 Electromagnetic field form, 163, 166  
 Electromagnetic field tensor, 207  
 Electromagnetic potential form, 162  
 Electromagnetic vector potential, 163, 207  
 Electromagnetic waves, 33, 167  
 Electromagnetism, 162  
 Ellipse, 266  
 Embedding, 225  
 Embedding of the Schwarzschild metric, 225  
 Emission point of time, 329  
 Empty space, 204  
 Energy, 44, 47  
 Energy conservation, 168  
 Energy-momentum conservation, 197, 208, 326  
 Energy-momentum tensor, 197-200, 205, 207, 209, 210, 238, 246, 247, 460  
 Eötvös, 15  
 Equation of continuity, 167, 210, 460  
 Equation of geodesic deviation, 189, 196  
 Equation of state, 462  
 Equatorial plane, 229  
 Euclidean geometry, 94

Euclidean plane, 87, 155, 428  
 Euclidean space, 169, 442  
 Euclidean 3-space, 82, 161  
 Euclidean spatial geometry, 323, 361  
 Euler equation, 240  
 Euler equation of motion, 198, 199, 210, 460  
 Euler-Lagrange equation, 119, 128, 131, 135  
 Event, 23, 77  
 Event horizons, 386, 501  
 Expansion, 153  
 Exterior derivative, 119-121, 147, 150, 157-161, 163, 165, 166, 178  
 Exterior differentiation, 150  
 Exterior Schwarzschild metric, 215  
 Extrinsic curvature tensor, 298

**F**  
 Fabry-Pérot cavities, 260  
 False vacuum, 362  
 Fermi gamma ray space telescope, 269  
 Field equations Einstein, 202  
 Field equations vacuum, 204  
 First order phase transition, 363  
 Flamm paraboloid, 226  
 Flatness problem, 360, 365  
 Flat spacetime, 76  
 Flat universe model, 319  
 Force, 47-49  
 Form-components, 80  
 Form-invariant, 18  
 Forms, 59, 78, 119  
 Four-acceleration, 62  
 Four momentum, 61  
 Four-vectors, 85, 424  
 Four-velocity, 60, 65, 76  
 Four-velocity identity, 76  
 Free fall, 15, 217  
 Freely falling reference frame, 15  
 Free particle, 130, 135  
 Frequency, 116  
 Friedman-Lemaître Eq., 328  
 Friedmann-Lemaître, 338  
 Friedmann-Lemaître model, 342, 348  
 Friedmann-Lemaître universe model, 347  
 Friedmann equation, 366, 488  
 Friedmann-Lemaître equations, 319, 331, 332  
 Friedmann metric, 488  
 Friedmann models, 360, 362, 365  
 Friedmann's 1<sup>st</sup> equation, 500

**G**  
 Galilean kinematics, 23  
 Galilei, 14  
 Galilei transformation, 18, 35  
 Galileo, 1  
 Gamma ray burst, 269  
 Gauge transformation, 164, 394  
 Gauss  
   curvature, 183  
   theorem egregium, 184  
 Gauss' equation, 180  
 Gaussian coordinates, 123  
 Gaussian curvature, 183, 184, 457  
 Gauss integral theorem, 6  
 Gauss' law, 410  
 Gauss's integral theorem, 246  
 General principle of relativity, 17  
 General theory of relativity, 1, 16, 19, 62, 95, 119, 122, 123, 215, 232, 233, 243, 266, 290, 305  
 Geodesic  
   curvature, 181  
 Geodesic curve, 78, 125, 130, 156, 181, 206, 448  
 Geodesic deviation, 188, 257  
 Geodesic equation, 125, 171, 312, 453  
 Geodesic normal coordinates, 189  
 Geodesic postulate, 204  
 Geodesic world lines, 133  
 Geometrical optics, 118, 439  
 GPS, 242, 473  
 GPS-satellite, 474  
 Gradient, 157, 159, 161, 170, 444  
 Gravitation, 18  
 Gravitational acceleration, 214  
   Tolman-Whittaker expression, 284  
 Gravitational antenna, 258  
 Gravitational collapse, 382, 486  
 Gravitational field, 4, 16, 95, 112, 118, 138, 192, 243, 438  
 Gravitational force, 412  
 Gravitational frequency shift, 211  
 Gravitational mass, 283  
 Gravitational mass-density, 321  
 Gravitational potential, 193, 246, 411  
 Gravitational radiation emission, 266  
 Gravitational redshift, 140  
 Gravitational self energy, 295  
 Gravitational shift of wavelength, 326  
 Gravitational time dilation, 89, 98, 99, 112, 134  
 Gravitational wave detector, 264

Gravitational waves, 243, 245, 253–257, 260, 263, 266  
 Gravitoelectric field, 252  
 Gravitoelectromagnetic fields, 253  
 Gravitoelectromagnetism, 251  
 Gravitomagnetic clock effect, 281, 483  
 Gravitomagnetic field, 252  
 Gravitomagnetic vector potential, 251  
 Gravitomagnetism, 243  
 Gravity, 119  
 Gravity probe B, 253  
 Guth, Alan, 363

## H

Hafele-Keating experiment, 232  
 Hamiltons principle, 127  
 Harrison-Zel'dovich spectrum, 373  
 Hawking, 273  
 Hawking radiation, 271, 273  
 Heat capacity of black hole, 274  
 Heisenberg uncertainty relationships, 200  
 Higgs field, 361, 362  
 Higgs mechanism, 361  
 Hilbert, 204, 206  
 Hilbert's variational principle, 206  
 Hodge Laplacian, 158  
 Horizon, 113, 220, 222, 271, 277, 380, 471  
 Horizon problem, 358, 364  
 Horizon radius, 379  
 Hubble age, 315, 334, 340, 342, 359, 360, 379, 490, 494  
 Hubble constant, 314, 320, 322, 339  
 Hubble flow, 305, 308, 315  
 Hubble-Lemaître expansion law, 311  
 Hubble-Lemaître law, 314, 315  
 Hubble length, 315, 323  
 Hubble parameter, 314, 320, 322, 342, 348, 350, 367, 368, 383, 489, 494  
 Hubble slow roll parameters, 368  
 Hydrostatic equilibrium, 8  
 Hyperbolically accelerated frame, 107  
 Hyperbolic motion, 41–43

## I

Incompressible star, 7, 288  
 Inertial dragging, 243, 250, 253, 271, 277, 377, 378, 405  
 Inertial dragging angular velocity, 377  
 Inertial effects, 193  
 Inertial forces, 19  
 Inertial frame, 16, 47, 93, 108, 123, 198, 250

Inertial reference frame, 16, 40, 41, 64, 123, 133, 140  
 Inertial rest frame, 116  
 Infalling coordinates, 382  
 Inflation, 363  
 Inflationary era, 364, 366, 372, 377  
 Inflationary model, 363  
 Inflationary universe models, 361  
 Inflaton field, 366, 367, 375  
 Inflaton potential, 368  
 Inhomogeneous universe models, 355  
 Instantaneous rest frame, 92  
 INTEGRAL telescope, 269  
 Interference, 99  
 Interference fringes, 99  
 Interferometer, 260, 264  
 Internal coordinate transformation, 91  
 Internal Schwarzschild solution, 283  
 Internal Schwarzschild space-time, 289  
 Interval, 37, 40, 77, 78  
 Invariant, 72, 73  
 Invariant basis, 155, 156  
 Invariant equation, 72  
 Invariant interval, 116  
 Isotropic coordinates, 241, 468  
 Israel formalism, 283, 290, 291, 309, 485

## J

Jupiter, 21

## K

Kaluza-Klein theory, 206, 393, 400, 404  
 Kasner universe, 353  
 Kepler motion, 240, 463, 465  
 Kepler's 2<sup>nd</sup> law, 235  
 Kepler's 3<sup>rd</sup> law, 236, 263, 484  
 Kerr, 275  
 Kerr black hole, 278, 280  
 Kerr metric, 275, 278  
 Kerr-Newman spacetime, 299, 302, 304  
 Kerr solution, 276  
 Kerr spacetime, 271, 275, 277, 280, 281, 283, 479, 481, 483  
 Killing equation, 154–156  
 Killing vectors, 154–157  
 Kinetic energy, 46  
 Klein, 404  
 Koszul connection coefficient, 140  
 Kretschmann curvature scalar, 216, 297  
 Kruskal-Szekeres, 216, 222, 224  
 Kruskal-Szekeres line element, 224

## L

LAGEOS satellites, 253  
 Lagrange density, 204  
 Lagrange dynamics, 463  
 Lagrange equation, 128, 129, 228, 464  
 Lagrange equations free particle, 129  
 Lagrange function, 127–129, 131, 171, 206, 250, 276, 403, 463, 476  
 Lagrange function free particles, 129  
 Lagrange multiplier, 181  
 Lagrangian, 206, 306  
 Lagrangian function, 217, 447  
 Lambda-Cold-Dark-Matter, 338  
 Laplace-Beltrami operator, 158, 167  
 Laplace equation, 5  
 Laplacian, 157, 158, 162, 170  
 LCDM-universe, 357, 358  
 Leads to an Einstein-de Sitter universe, 333  
 Leibowitz, 401  
 Leibowitz-Rosen tensor, 401  
 Lemaître, 200, 321  
 Lemaître-Friedmann-Robertson-Walker universe models, 311  
 Lemaître-Tolman-Bondi, 355  
 Length, 35  
 Length contraction, 33  
 Lense, 19  
 Lense-Thirring effect, 19, 250  
 Lever paradox, 49  
 Levi-Civita, 124, 295  
 Levi-Civita Bertotti-Robinson metric, 283  
 Levi-Civita Bertotti Robinson solution, 295  
 Levi-Civita Bertotti Robinson spacetime, 297  
 Levi-Civita connection, 123  
 Levi-Civita symbol, 80, 251  
 LFRW cosmological models, 330  
 LFRW universe, 500  
 LFRW universe models, 325, 348, 384, 493  
 Lie derivative, 155, 156  
 Light, 33  
 Light cone, 24, 218  
 Light cone coordinates, 223  
 Light deceleration of, 226  
 Light deflection of, 236  
 Light-like, 37, 39, 78  
 LIGO, 243, 260, 263, 269  
 Linear combination, 59  
 Linear field approximation, 243, 252  
 Linearized field equations, 246  
 Linearly independent, 59  
 Line element, 40, 75, 83, 93, 94, 98, 101, 104, 161

Line element free particle, 129  
 LIVE, 200, 210, 242, 285, 306, 311, 318, 321, 328, 336, 338, 339, 344, 345, 348, 353, 354, 357, 358, 366, 374, 386, 460, 462, 492, 497, 502  
 LIVE-Cold-Dark-Matter, 338  
 Local derivative, 151  
 Local inertial frame, 215  
 Local inertial reference frame, 135  
 Locally Cartesian coordinates, 192  
 Locally Cartesian coordinate system, 186  
 Lookback time, 329, 335, 383, 489  
 Lopez, 300  
 Lopez's source of the Kerr-Newman metric, 303  
 Lorentz contracted, 95  
 Lorentz contraction, 33, 35, 56, 95, 96, 108, 420  
 Lorentz factor, 30  
 Lorentz force, 252  
 Lorentz invariance, 200  
 Lorentz invariant, 37, 47, 75, 460  
 Lorentz invariant vacuum energy, 200, 311, 318, 338  
 Lorentz's force law, 52  
 Lorentz transformation, 34–37, 47, 58, 92, 95, 109, 423, 425, 460  
 Lorenz condition, 164  
 Lorenz gauge, 164  
 Lorenz gauge condition, 252, 254  
 Lowering an index, 74  
 Luminosity distance, 385  
 Lyth bound, 371

## M

Mach, 19  
 Mach's principle, 18  
 Magnetic flux density, 163  
 Magnetism, 51  
 Manifestly covariant, 18  
 Mass, 44, 45  
 Material derivative, 151  
 Matrix, 81  
 Matter-dominated universe, 385  
 Mattig's formula, 385, 496  
 Maximally linearly independent, 59  
 Maximally symmetric, 155  
 Maxwell, 33  
 Maxwell's equations, 18, 51, 162, 252, 424  
 Maxwell source equations, 166  
 Maxwell's source free equations, 165, 208  
 Measuring rods, 97

Mechanical energy, 266  
 Mercury, 227, 241, 471  
 Mercury's orbit, 236  
 Mercury's perihelion precession, 233  
 Meson, 56  
 Metric, 72  
   Kerr (rotating), 275  
 Metric covariant differentiation, 146  
 Metric perturbations, 257  
 Metric static, stationary, 129  
 Metric tensor, 72, 74, 81, 82, 94, 146, 200, 216, 232  
 Michelson and Morley, 33  
 Michelson interferometers, 260  
 Michelson–Morley experiment, 33  
 Milky Way, 107, 108  
 Milne universe, 353, 383, 388, 490, 507  
 Milne universe model, 319  
 Mini-black hole, 275  
 Minkowski diagram, 23, 24, 30, 42, 102, 106, 133, 388, 433  
 Minkowski-force, 62  
 Minkowski force form, 168  
 Minkowski line-element, 76  
 Minkowski metric, 76, 86, 148, 210, 243, 317, 433, 459  
 Minkowski space, 116  
 Minkowski spacetime, 75, 78, 133, 166, 214, 223, 244, 277, 295, 296, 300, 319, 320, 377, 460  
 Minkowski space-time from Schwarzschild solution, 214  
 Minkowski universe, 353  
 Mixed components, 86  
 Mixed metric tensor, 74  
 Mixed tensor, 70, 71  
 Møller coordinates, 108  
 Momentum, 47, 48  
 Momentum-energy tensor, 198  
 Moon, 12, 21, 413  
 Multilinear function, 70  
 Multi messenger astronomy., 269

## N

Natural Inflation, 389, 508  
 Newton, 1, 18  
 Newton fluid, 198  
 Newtonian 3-velocity, 151  
 Newtonian approximation, 190, 210, 215, 459, 497  
 Newtonian fluid, 197, 198  
 Newtonian force, 16

Newtonian gravitational potential, 190, 251  
 Newtonian gravity, 230, 289  
 Newtonian hydrodynamics, 151, 198  
 Newtonian law of gravitation, 203  
 Newtonian limit, 135, 191, 203, 214, 325, 459, 470  
 Newtonian physics, 190  
 Newtonian potential, 20, 21, 203, 230, 410  
 Newtonian theory, 265  
 Newtonian tidal tensor, 191  
 Newton's 1<sup>st</sup> law, 16, 64, 135, 192  
 Newton's 2<sup>nd</sup> law, 14, 57, 412, 423  
 Newton's law of gravitation, 1, 4, 201, 409  
 Newton's law of gravity, 411  
 Newton's theory, 16, 95, 119, 193, 230  
 Newton's theory of gravitation, 1, 192  
 Non-Euclidean, 94  
 Non-tidal gravitational field, 195  
 Normal curvature, 181  
 Null-geodesic curve, 17, 359  
 Number of e-folds, 370

## O

One-form basis, 69  
 Orbit equation, 231  
 Orthogonal basis, 82  
 Orthonormal basis, 64, 67, 76, 102, 104, 109, 142, 150, 160, 211, 212, 239  
 Orthonormal basis field, 148, 150  
 Outer product, 120

## P

Parallel transport, 124, 174, 195, 453  
 Partial derivative, 122, 144  
 Particle horizon, 359, 379, 380, 494, 495  
 Particle trajectories, 228  
 Particle trajectory Schwarzschild 3-space, 228  
 Past light cone, 378  
 Peculiar velocity, 315  
 Perfect dragging, 378  
 Perfect fluid, 199, 210, 317, 459, 493  
 Perfect inertial dragging, 341, 379  
 Perihelion precession, 471  
 Perihelion precession of Mercury, 242  
 Perihelion shift of Mercury, 211  
 Permeability of empty space, 166, 207  
 Permeability of vacuum, 54  
 Permittivity of empty space, 166  
 P-form, 78  
 Phantom energy, 348, 350  
 Photon, 99

Photon clock, 28  
 Photon sphere, 242, 474  
 Physical components, 160  
 Physical laws, 18  
 Physical singularity, 216  
 Planck length, 240  
 Planck mass, 274, 375  
 Planck spectrum, 273  
 Planck time, 275  
 Plane polar coordinates, 66, 69, 73, 75, 123, 140, 150  
 Poincaré's lemma, 121, 158, 160, 162, 164, 165, 167, 178, 185, 395  
 Poisson equation, 7, 385  
 Polarization, 256, 257, 372  
 Polynomial inflation, 375  
 Pound-Rebka experiment, 140  
 Power spectra, 373  
 Precession, 235  
 Precession of Mercury's perihelion, 233  
 Pressure, 44  
 Pressure forces, 8  
 Primordial black hole, 275  
 Principal curvatures, 182  
 Principle of equivalence, 1, 15, 16, 95, 192, 215  
 Principle of general relativity, 136  
 Principle of relativity, 1, 17, 18, 41, 95, 380  
 Projectile motion, 171  
 Projection, 89, 153  
 Projection tensor, 113, 114, 153  
 Proper acceleration, 105, 107, 114  
 Proper distance, 92  
 Proper time, 30, 38, 78, 98, 112, 116, 127, 134, 216  
 Proper time-interval, 40, 106, 232  
 Proxima Centauri, 137

## Q

Quasars, 417

## R

Radar method, 25  
 Radially moving photons, 219  
 Radiation, 45, 200, 317, 321, 328  
 Radiation dominated universe, 330, 361, 384, 496  
 Radiation-dominated universe model, 330  
 Radiation pressure, 44  
 Rank, 70, 71  
 Rapidity, 36, 109, 110  
 Redshift, 56

Kerr spacetime, 276  
 Redshift cosmological, 315  
 Redshift–luminosity relation, 385, 496  
 Reduced mass, 263  
 Reference frame, 16, 17, 64  
 Reference frame inertial, 123  
 Reference particle, 94  
 Reinterpretation principle, 50  
 Reissner–Nordström solution, 211, 239, 406  
 Reissner–Nordström spacetime, 238  
 Relativistic Doppler effect, 67, 421  
 Relativistic Doppler shift, 56  
 Relativistic gravitational potential, 325  
 Relativistic gravity, 230  
 Relativistic rotating disc, 115, 429  
 Relativity of simultaneity, 30, 32, 50, 92, 93, 96  
 Repulsive gravitation, 285, 321  
 Rest acceleration, 42, 43  
 Rest frame, 61  
 Rest length, 33  
 Ricci  
   curvature, 177  
   identity, 184  
   component form, 184  
 Ricci curvature scalar, 177, 179, 207, 213, 243  
 Ricci curvature tensor, 177, 179, 213, 243, 457  
 Ricci curvature tensor, divergence, 201  
 Ricci identity, 184  
 Ricci scalar, 244  
 Ricci tensor, 201  
 Riemann curvature forms, 179  
 Riemann curvature tensor, 173, 175–178, 184, 186, 190, 195, 213, 243, 457  
 Riemannian space, 188  
 Riemann tensor, 175–177, 179, 184, 189, 255  
 Rigid rotation, 104  
 Rindler coordinates, 108  
 River model of space, 283  
 River of space, 306  
 Robb, 54  
 Robb's formula, 417  
 Robertson–Walker line element, 314  
 Robertson–Walker metric, 312, 359  
 Robertson–Walker universe, 383  
 Roche limit, 21, 416, 417  
 Rosen, 401  
 Rosser, 47  
 Rotating black hole, 275  
 Rotating frame, 94–96, 101, 102, 141

Rotating frame of reference, 170, 447  
 Rotating motion, 95  
 Rotating reference frame, 92, 99, 101, 195, 447, 456  
 Rotating reference frame connection coefficients, 140  
 Rotating spherical shell, 247  
 Rotation, 152, 153  
 Rotational motion, 380  
 Running of the spectral indices, 373

## S

Sagnac effect, 99, 280  
 Sagnac experiment, 89  
 Scalar field, 318, 444  
 Scalar perturbation, 372  
 Scalar product, 72  
 Scalar quantity, 70  
 Scale factor, 311, 317, 379  
 Scale invariant, 373  
 Schwarzschild spacetime, 223, 272  
 Schwarzschild 3-space, 228  
 Schwarzschild 3-space energy, 228  
 Schwarzschild 3-space momentum, 228  
 Schwarzschild black hole, 273, 279, 476  
 Schwarzschild-de Sitter metric, 241, 309, 469, 484  
 Schwarzschild-de Sitter spacetime, 306, 485  
 Schwarzschild horizon, 241, 308  
 Schwarzschild light cones, 218  
 Schwarzschild line-element, 223, 475, 487  
 Schwarzschild metric, 215, 216, 225, 239, 241, 293  
 Schwarzschild metric embedding, 225  
 Schwarzschild radius, 3, 19, 216, 218, 222, 226, 227, 236, 238, 243, 264, 268, 271, 278, 279, 293, 299, 378–382, 469, 474, 486, 488  
 Schwarzschild's exterior solution, 211  
 Schwarzschild's interior solution, 287  
 Schwarzschild solution, 211, 241, 468, 469  
 Schwarzschild space, 241  
 Schwarzschild spacetime, 211, 216–218, 225, 238, 247, 250, 272, 468, 479, 481, 487  
 Semi-latus rectum, 266  
 Shapiro, 226  
 Shapiro experiment, 226  
 Shear, 152, 153  
 Shoemaker-Levy, 21  
 Shoemaker-Levy 9, 417  
 Simultaneity, 101

Simultaneity space, 91, 102, 104, 115, 153  
 Simultaneous events, 93  
 Singularity coordinate, 216  
 Singularity physical, 216  
 Singular mass shells, 290  
 Slow roll approximation, 367  
 Slow roll era, 374  
 Slow roll parameters, 368, 375  
 Space, 42  
 Space-like, 37, 78  
 Space ship, 117  
 Spacetime, 16, 61, 64, 65, 247  
 Spacetime curvature, 17, 190  
 Spacetime interval, 37  
 Spatial geodesics, 447  
 Spatial geometry, 89, 95  
 Spatial line-element, 90, 94, 114  
 Spatial metric, 102, 114  
 Spatial metric tensor, 89, 91, 94, 114  
 Spatial simultaneity space, 456  
 Special principle of relativity, 17  
 Special theory of relativity, 23, 25, 41, 98, 200  
 Spectral indices, 373  
 Spectral parameters, 509  
 Spectral tilt, 375  
 Spherical coordinates, 161, 169, 214, 247, 444  
 Spherical coordinate system, 82  
 Spherically symmetric spacetime, 209  
 Spontaneous symmetry breaking, 361, 362  
 Standard clock, 98, 112, 116, 134, 217  
 Standard measuring rod, 95, 96  
 Static border, 278  
 Static metric, 129, 275  
 Stationary metric, 129, 275  
 Stefan–Boltzmann law, 274, 330, 364  
 Structure coefficients, 68, 143, 148, 176, 188  
 Sun, 226, 227, 236, 238, 264, 269, 274  
 Surface curvature, 183  
 Surface gravity, 271, 273  
 Synchronization, 25

## T

Tachyons, 50  
 Tachyon telephone paradox, 51  
 Tangent vector, 66  
 Tangent vector field, 62, 64, 125  
 Taylor expansion, 193  
 Tensor, 59, 69, 78, 146  
 contraction of, 177  
 Ricci curvature, 177

Riemann curvature, 175  
 Tensor covariant differentiation of, 146  
 Tensor Einstein, 202  
 Tensor equation, 18, 72  
 Tensor momentum energy, 198  
 Tensor perturbation, 373  
 Tensor product, 70, 86, 426  
 Tensor Riemann curvature, 213  
 Tensor-to-scalar ratio, 373  
 Tetrad, 102  
 The de Sitter universe models, 336  
 The Friedmann–Lemaître model, 337  
 The Hubble parameter, 503  
 Theorema egregium, 184  
 Theory of relativity, 95  
 The river of space, 305  
 The static border, 278  
 The twin paradox, 54, 417  
 Thin dust shell, 291  
 Thirring, 19, 377  
 Tidal acceleration, 190  
 Tidal field, 14  
 Tidal force, 1, 10, 16, 173, 193  
 pendulum  
 relativistic, 196  
 Tidal force pendulum, 19, 196, 409, 410, 458  
 Tidal gravitational field, 194  
 Tidal potential, 14  
 Tilt, 373  
 Time dilation, 28, 30, 38, 39, 56, 98, 134, 420  
 Time-like, 37, 76  
 Tolman–Oppenheimer–Volkoff (TOV) equation, 285, 287, 288  
 Tolman–Whittaker expression, 284  
 Tolman–Whittaker formula, 299  
 Torque, 49  
 Torsion, 187  
 Torsion form, 187  
 Total derivative, 151, 153  
 Transformation matrix, 81  
 Transverse traceless gauge condition, 256  
 Twin paradox, 40, 41, 136, 138

## U

Uniformly accelerated motion, 42, 43, 114  
 Uniformly accelerated reference frame, 43, 89, 105, 107, 112, 116, 131, 139, 171, 449

Uniformly accelerated space ship, 436  
 Uniformly accelerated system of reference, 433  
 Unit vector, 67  
 Universe, 19  
 Universe model dust dominated, 331  
 Universe model inflationary, 363  
 Universe model radiation dominated, 330

## V

Vacuum energy, 200  
 Vacuum field equations, 204  
 Variational principle, 130, 131, 204, 206  
 Vector, 18, 59  
 Vector field, 64  
 Vectorial form, 147  
 Vector perturbation, 372  
 Velocity, 47  
 Velocity addition, 36  
 Velocity field, 151  
 4-velocity identity, 129  
 Velocity of light, 24  
 Venus, 226  
 Vertical free fall, 131  
 Vertical projectile motion, 451  
 Virgo, 263, 269  
 Volume-element, 82  
 Volume expansion, 152  
 Volume form, 80, 82, 83  
 Vorticity, 372

## W

Wave number, 373  
 Weak gravitational field, 216  
 Wedge product, 79, 84  
 Weingarten's equation, 181  
 Wheeler, 204  
 White hole, 221  
 Wien's displacement law, 273  
 World line, 24, 38, 42, 76

## Z

Zel'dovich fluid, 366  
 Zero-Angular-Momentum-Observers (ZAMO), 250, 276, 277, 280, 377, 480