## ECE4016 Assignment 2 Report

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## I. Algorithm Analysis

In this project, referring to paper "BOLA: Near-Optimal Bitrate Adaptation for Online Videos", we write a BOLA algorithm. BOLA (Buffer Occupancy based Lyapunov Algorithm) is a buffer-based ABR (Adaptive Bitrate Streaming) algorithm using Lyapunov optimization. While building system model, we need to define some variables:

- 1. The video file is segmented into N segments, each segment represents p seconds in the video.
- 2. Each segment is available in M different bitrates.
- 3. The size of the segment encoded at bitrate index m is  $S_m$  and suppose the utility derived by the user from viewing it is given by

 $v_m$  where  $m \in \{1, 2, ..., M\}$ . Let segment bitrates be non-decreasing in index m then

$$v_1 \leq v_2 \leq \ldots \leq v_m \Leftrightarrow S_1 \leq S_2 \leq \ldots \leq S_m$$
.

- 4. The available bandwidth (in bits/second) is assumed to vary continuously in time according to a stationary random process  $\omega(t)$ .
- 5. The video player have a finite buffer of size  $Q_{max}$  segments.
- 6. The timeline is divided into nonoverlapping consecutive slots of variable length and indexed by  $k \in \{1, 2, ...\}$ . Slot k starts at time  $t_k$  and is  $T_k = t_{k+1} t_k$  seconds long.
- 7. We define

$$a_m(t_k) = \begin{cases} 1, \text{if the player downloads a segment of bitrate index } m \text{ in slot } k \\ 0, \text{otherwise} \end{cases}$$

and denote the buffer level at the start of slot k by  $Q(t_k)$ . Then

$$Q(t_{k+1})=max[Q(t_k)-rac{T_k}{p},0]+a_m(t_k)$$

## II. Implementation

The algorithm we implemented in this assignment is BOLA-FINITE.

```
1: for n in [1, N] do
            t \leftarrow \min[\text{playtime from begin, playtime to end}]
 2:
 3:
            t' \leftarrow \max[t/2, 3p]
           Q_{\text{max}}^{\text{D}} \leftarrow \min[Q_{\text{max}}, t'/p]
V^{\text{D}} \leftarrow (Q_{\text{max}}^{\text{D}} - 1)/(v_M + \gamma p)
m^*[n] \leftarrow \arg\max(V^{\text{D}}v_m + V^{\text{D}}\gamma p - Q)/S_m
 4:
 5:
 6:
           if m^*[n] > m^*[n-1] then
 7:
 8:
                 r \leftarrow bandwidth measured when downloading segment (n-1)
 9:
                 m' \leftarrow \max m such that S_m/p \leq \max[r, S_1/p]
                 if m' \geq m^*[n] then
10:
11:
                      m' \leftarrow m^*[n]
                 else if m' < m^*[n-1] then
12:
13:
                      m' \leftarrow m^*[n-1]
14:
                 else if some utility sacrificed for fewer oscillations then
                      pause until (V^{\mathrm{D}}v_{m'}+V^{\mathrm{D}}\gamma p-Q)/S_{m'}\geq (V^{\mathrm{D}}v_{m'+1}+V^{\mathrm{D}}\gamma p-Q)/S_{m'+1}
                                                                                            ⊳ BOLA-O
15:
16:
                      m' \leftarrow m' + 1
17:
                                                                                            ⊳ BOLA-U
18:
                 end if
                 m^*[n] \leftarrow m'
19:
20:
           pause for \max[p \cdot (Q - Q_{\max}^{D} + 1), 0]
21:
           download segment n at bitrate index m^*[n], possibly abandoning
22:
23: end for
```

Fig 1. Pseudo code of BOLA-FINITE

In actual implementation, codes in line 14,15 (BOLA-O) and line 21 will not be implemented. We set  $v_m$  to  $\ln(S_m/S_1)$ . The buffer level Q is calculated by  $\lceil t/p \rceil$ , where t is the time remain in the buffer. Despite to the arguments we introduce in part I, there is an argument  $\gamma$ , which is an input weight parameter. In actual implementation, we set  $\gamma = 5/p$ .

## III. Evaluation

We run the program by python grader.py. We have the score of given example program and the score of BOLA:

```
testHDmanPQtrace:
Results: Average bitrate: 500000.0buffer time: 91.115switches: 0
Score: 4669.348620686024
testP0:
Results: Average bitrate: 500000.0buffer time: 91.115switches: 0
Score: 4669.348620686024
testALTsoft:
Results:Average bitrate:4100000.0buffer time:5.948000000000001switches:9
Score: 1426836.8172498895
Results: Average bitrate: 4700000.0buffer time: 0.101switches: 1
Score: 4301656.912826439
Your trace file is poorly formed!Results:Average bitrate:2600000.0buffer time:19.751switches:28
Score: 91422, 1523596769
testALThard:
Results: Average bitrate: 2600000.0buffer time: 19.751switches: 28
Score: 91422.1523596769
```

Fig 2. The score of Example Program

```
testHDmanPQtrace:
Results: Average bitrate: 983333.333333334buffer time: 245.21300000000002switches: 1
Score:3.1190835791810283
testPQ:
Results: Average bitrate: 983333.333333334buffer time: 245.21300000000002switches: 1
Score:3.1190835791810283
testALTsoft:
Results:Average bitrate:3833333.33333335buffer time:3.161000000000014switches:8
Score: 1672875.1145839747
testHD:
Results: Average bitrate: 4700000.0buffer time: 0.101switches: 1
Score: 4301656.912826439
Your trace file is poorly formed!Results:Average bitrate:2350000.0buffer time:9.2950000000000002switches:19
Score: 299210.9568638165
testALThard:
Results: Average bitrate: 2350000.0buffer time: 9.295000000000002switches: 19
Score: 299210.9568638165
```

Fig 3. The score of BOLA Algorithm

We found that BOLA Algorithm does more better than algorithm in example program except PQ test. PQ test is a test case with extremely bad network quality. That means BOLA Algorithm does not perform well when bandwidth value is extremely low.

To improve this situation, we add a code block to check if the buffer only remains 1 segment. If it is, set the next bitrate to the lowest.

```
if buffer_info['time']<=p:
    opt = 0</pre>
```

Fig 4. The modification made to improve the algorithm

After this improvement, we have a new score for BOLA, which performs better in PQ test:

```
testHDmanPQtrace:
Results: Average bitrate: 500000.0buffer time: 91.115switches: 0
Score: 4669.348620686024
testPQ:
Results: Average bitrate: 500000.0buffer time: 91.115switches: 0
Score:4669.348620686024
testALTsoft:
Results:Average bitrate:3833333.33333335buffer time:3.161000000000014switches:8
Score: 1672875.1145839747
testHD:
Results:Average bitrate:4700000.0buffer time:0.101switches:1
Score: 4301656.912826439
badtest:
Your trace file is poorly formed!Results:Average bitrate:2350000.0buffer time:9.2950000000000002switches:19
Score: 299210.9568638165
testALThard:
Results: Average bitrate: 2350000.0buffer time: 9.29500000000002switches: 19
Score:299210.9568638165
```

Fig 5. The score of improved BOLA Algorithm