

② Subtraction Operation:-

The direct method of subtraction taught in elementary schools uses the borrow concepts. This method works well when people perform subtraction with paper and pencil.

However, when subtraction is implemented with digital, this method shows less efficiency than the method that uses complements.

Binary Numbers Complements:-

1's Complement: invert the binary representation of the number (1s become 0s and 0s become 1s).

2's Complement: Take 1's complement and add (1) to the result.

Ex:- 1's Complement of 1011000 is 0100111.
2's Complement of 1101100 is 0010100.

Decimal Numbers Complements:-

9's Complement: it is obtained by subtract each digit from 9.

10's Complement: it is obtained by adding (1) to the 9's value.

Ex:-

9's Complement of 546700 is 453299

10's Complement of 246700 is 753300

Note:- Complements are used in digital computers for simplifying the subtraction operation.

Ex: Subtract the following number by use 1's complement?

$$a) (1010100)_2 - (1000011)_2$$

$$b) (1000011)_2 - (1010100)_2$$

Sol.

a) $(1010100)_2 - (1000011)_2$

$$\begin{array}{r}
 1010100 \\
 1000011 - \\
 \hline
 0001000 \\
 1010100 \\
 \hline
 0111100 + \\
 0010000 \\
 \hline
 0010001 \leftarrow \text{the answer}
 \end{array}$$

Is complement
 rotate the carry \rightarrow 1
 and adding

b) $(1000011)_3 - (1010100)_2$

Is complement \rightarrow

$$\begin{array}{r} 1000011 \\ 1010100 - \\ \hline 1000011 \\ 0101011 + \\ \hline 1101110 \end{array}$$

There is no carry therefore the answer is 00

$$= -(\text{1's complement of } 1101110) = -(0010001)_2$$

The answer is:- $-(0010001)_2$

Ex:- Subtract the following binary by use 2's Complement?

a) $(1010100)_2 - (100011)_2$

b) $(1000011)_2 - (1010100)_2$

Sol.)

a) $(1010100)_2 - (1000011)_2$

$$\begin{array}{r} 1010100 \\ 1000011 - \\ \hline 0000000 \\ 1010100 \end{array}$$

2's $\rightarrow 0111101 +$

The carry is $\rightarrow 10010001$
discard

The answer is $\infty (0010001)_2$

b) $(1000011)_2 - (1010100)_2$

$$\begin{array}{r} 1000011 \\ 1010100 - \\ \hline 1000011 \end{array}$$

2's $\rightarrow 0101100 +$

no carry $\rightarrow 1101111$

$$\begin{array}{r} 1010100 \\ 1's \rightarrow 0101011 \\ \hline 1+ \\ 2's \rightarrow 0101100 \end{array}$$

The answer = $-(2's \text{ complement of the result})$

$= -(2's \text{ complement of } 1101111) = -(0010001)_2$

The answer is $\infty - (0010001)_2$

Ex) Using 10's Complement Subtract for $(72532)_{10} - (3250)_{10}$?

Sol.) $(72532)_{10} - (3250)_{10} =$

$$\begin{array}{r} 72532 \\ 03250 - \\ \hline 72532 \\ 10's \rightarrow 96750 + \\ \hline \text{Discard } \boxed{1} \quad 69282 \end{array}$$

$$\begin{array}{r} 99999 \\ 03250 - \\ \hline 96749 \\ 10's \rightarrow 96750 \end{array}$$

The answer is: $(69282)_{10}$

Ex) Using 9's Complement Subtract for $(3250)_{10} - (72532)_{10}$?

Sol.)

$$\begin{array}{r} 03250 \\ 72532 - \\ \hline 03250 \\ 9's \rightarrow 27467 + \\ \hline \text{no carry} \rightarrow 30717 \end{array}$$

$$\begin{array}{r} 99999 \\ 72532 - \\ \hline 27467 \end{array}$$

The answer is: $-(9's \text{ complement of } 30717) = -(69282)_{10}$

Ex) Using 1's Complement to find $(-3)_{10} + (4)_{10}$?

$$\begin{array}{r} -3 + 4 \\ \downarrow \quad \downarrow \\ 011 \quad 100 \end{array}$$

$$\begin{array}{r} -011 \\ 100 + \\ \hline 100 \\ 100 + \\ \hline \boxed{1}000 \\ 01 + \\ \hline 001 \end{array}$$

$$1's \rightarrow \underline{\underline{100}}$$

The answer is $(1)_{10}$

Octal Numbers Complements:-

7's complement:- it is obtained by subtract each digit from 7.

8's complement:- it is obtained by adding (1) to the 7's value.

Ex) Using 8's complement subtract for $(256)_8 - (341)_8$?

Sol.)

$$\begin{array}{r} 256 \\ 341 - \\ \hline \textcircled{1}\textcircled{1} \\ 256 \\ 8's \rightarrow 437 + \\ \hline \text{no carry} \rightarrow 715 \end{array}$$

$$\begin{array}{r} 777 \\ 341 - \\ \hline 7's \rightarrow 436 \\ 1 + \\ \hline 8's \rightarrow 437 \end{array}$$

The answer = $(8's \text{ complement of } 715)$
 $= -(063)_8$

$$\begin{array}{r} 777 \\ 715 - \\ \hline 7's \rightarrow 062 \\ 1 + \\ \hline 8's \rightarrow 063 \end{array}$$

Hexadecimal Numbers Complements:-

15's complement: it is obtained by subtract each digit from 15.

16's complement: it is obtained by adding (1) to the 15's value.

Ex) Find $(592)_{16} - (3A5)_{16}$ using 16's complement?

Sol.)

$$\begin{array}{r} 592 \\ 3A5 - \\ \hline 592 \end{array}$$

$$\begin{array}{r} 16's \rightarrow C5B + \\ \hline \text{discard} \rightarrow \boxed{1} E D \end{array}$$

The answer is:- $(1ED)_{16}$

$$\begin{array}{r} FFF \\ 3A5 - \\ \hline 15's \rightarrow C5A \\ 1 + \\ \hline 16's \rightarrow C5B \end{array}$$

Ex) Find $(3A5)_{16} - (592)_{16}$ by using $15's$ complement?

Sol.

$$\begin{array}{r} 3A5 \\ 592 - \\ \hline \oplus \oplus \\ 3A5 \end{array}$$

$$15's \rightarrow A6D+$$

$$\text{no carry} \rightarrow E12$$

$$\begin{array}{r} FFF \\ 592 - \\ \hline 15's \rightarrow A6D \end{array}$$

The answer is $(1E0)_{16}$

H.w. Find the following:-

- 1) $(1001001)_2 - (101110)_2$ using $1's$ and $2's$ comp.
- 2) $(43C)_{16} - (32B)_{16}$ using $15's$ and $16's$ comp.
- 3) $(316)_8 - (451)_8$ using $7's$ and $8's$ comp.
- 4) Add: $(3F8)_{16}$ and $(5B3)_{16}$
- 5) Find the complement of $(A9B)_{16}$ using $15's$ comp.
- 6) Find the complement of $(346)_8$ using $8's$ comp.