

# Intro to AI 2021 B Ex. 3

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A:

Logic syntax

a. let a be Jane in town and b be John in town

and let c be we will play tennis then

the sentence will be  $\boxed{\neg(a \vee b) \rightarrow c}$

b. let a be it will rain today and b be

it will be dry today then the sentence

will be  $\boxed{a \vee b}$ , not that if the intention

was for  $a = \neg b$  then the sentence was  $a \vee \neg a$ .

c. let a be you will pass this course

and b be you study then the sentence

will be  $\boxed{\neg b \rightarrow \neg a}$ .

B:

a. ~~action(x)  $\wedge$  reaction(y)  $\wedge$  equals(x,y)  $\wedge$  opposite(x,y)~~

$\forall x \exists y \text{ action}(x) \wedge \text{reaction}(y) \wedge \text{equals}(x,y) \wedge \text{opposite}(x,y)$

b.

~~$\forall x \exists y \text{ loves}(x,y) \wedge \text{loves}(y,x)$~~

$\forall x \exists y \forall z \text{ loves}(x,y) \rightarrow \text{loves}(y,z)$ .

c.

$\forall x \exists y \text{ we}(x) \wedge \text{earth}(y) \wedge \text{green}(y) \wedge \text{living-in}(x,y)$ .

C:

a.

can't live with or without you.

b. you own Earth or you can for each color of the

wind you can point with this color and you own the Earth.

## Most general unifier

②

- MGU:  $\{y \setminus \text{postman}, x \setminus \text{Blue}\}$
- MGU:  $\{y \setminus F(A), x \setminus F(F(A)), v \setminus F(A)\}$
- MGU:  $\{x \setminus y\}$

## Resolution

① goal state  $\alpha = \exists x (M(x) \wedge MC(x) \wedge \neg S(x))$

where M stands for member, MC mountain climber

for convince  $\alpha = \exists x (MC(x) \wedge \neg S(x))$  and more

generally we will assume that any  $x$  is such that  $M(x)$ . also will mark likes in L

knowledge Base

0.  $S(x) \vee MC(x)$
1.  $\neg MC(x) \vee \neg L(x, \text{rain})$
2.  $\neg S(x) \vee L(x, \text{snow})$
3.  $\neg L(\text{Porthos}, x) \vee \neg L(\text{Athos}, x)$
4.  $L(\text{Porthos}, x) \vee L(\text{Athos}, x)$
5.  $L(\text{Athos}, \text{rain})$
6.  $L(\text{Athos}, \text{snow})$
7.  $\neg M(\text{Athos})$
8.  $M(\text{Porthos})$
9.  $M(\text{Aramis})$
10.  $\neg MC(x) \vee S(x)$

we will use shortest clause heuristic, however we will skip 7, 8, 9



(Resolution)

~~for 3, 6, 2, 1, 4~~

$$\{3, 6\} \vdash \neg L(\text{Porthos}, \text{show}) \quad a.$$

$$\{a, 2\} \rightarrow \neg S(\text{Porthos}) \quad b.$$

$$\{b, 1, \alpha\} \rightarrow \neg MC(\text{Porthos}) \quad c.$$

$$\{c, 0\} \rightarrow S(\text{Porthos}) \quad d.$$

but then b, d. contradict, thus  $\alpha$  is true.

(2)

a. "Horses are animals" will translate  $\forall x \text{Horse}(x) \rightarrow \text{animal}(x)$   
from we'll mark  $H(x), A(x)$ . also let HeadOf be  $H_o$   
then "The head of a Horse is the Head of an animal"

be 
$$\forall x \forall y (H(x) \wedge H_o(y, x) \rightarrow \exists z (A(z) \wedge H_o(y, z)))$$

b. ~~and~~ converting the premise will result in

$$\boxed{\neg(H(x) \vee A(x))} \quad *$$

Negate the conclusion

$$\neg(\forall x \forall y (H(x) \wedge H_o(y, x) \rightarrow \exists z (A(z) \wedge H_o(y, z))))$$

$$= \neg(\forall x \forall y (\neg(H(x) \wedge H_o(y, x)) \vee \exists z (A(z) \wedge H_o(y, z))))$$

$$= \exists x \exists y (H(x) \wedge H_o(y, x) \wedge \forall z (\neg A(z) \vee \neg H_o(y, z)))$$

mark  $x = a, y = b$  constant

$$= \boxed{H(a) \wedge H_o(b, a) \wedge (\neg A(z) \vee \neg H_o(b, z))} \quad **$$

(Resolution 2)

C.  $\neg A(a) + \neg H(b/a) \Rightarrow A(a)$

substitute  $z/a$  and we get  $(\neg A(a) \vee \neg H(b/a))$

$= (\neg(\text{true}) \vee \neg(\text{true})) = \text{False} \vee \text{False} = \text{False}$  in contradiction

thus the conclusion is following the premise.  $\square$