CSE472 (Machine Learning Sessional)

Assignment- 2: Logistic Regression with Bagging and Stacking

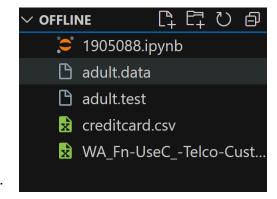
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Process to run the code:

The .ipynb file along with all the unzipped csv files need to be kept in the same directory.

Inside the .ipynb file under 'Workflow' section, by commenting or uncommenting the lines one can get the results for different datasets. After selecting the desired dataset, 'run all' instances gives the necessary evaluations.





Performance Evaluation:

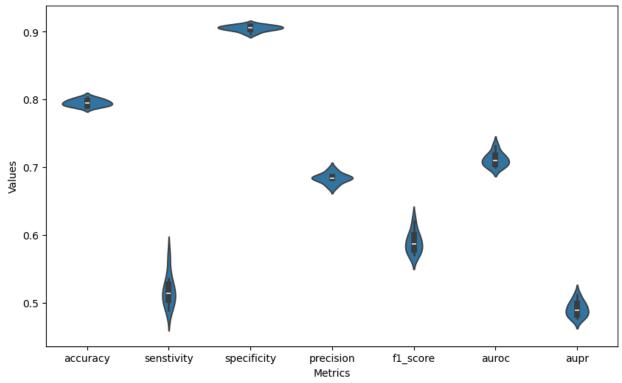
1. Teleco-customer-churn dataset

Performance on Test set

| | Accuracy | Sensitivity | Specificity | Precision | F₁-score | AUROC | AUPR |
|-------------------|-----------------|--------------------|--------------------|-----------------|-----------------|---------------|-------------------|
| LR | 0.8032 ± 0.0024 | 0.5294 ± 0.0140 | 0.8947 ± 0.0056 | 0.6271 ± 0.0081 | 0.5739 ± 0.0072 | 0.712 ± 0.005 | 0.4498 ± 0.005 |
| Voting ensemble | 0.8071 | 0.5341 | 0.8984 | 0.6373 | 0.5811 | 0.7162 | 0.4571 |
| Stacking ensemble | 0.8036 | 0.5483 | 0.8889 | 0.6226 | 0.5831 | 0.7186 | 0.4545 |

The highest performance was observed for standard scaling, no feature selection, decaying learning rate with small initial learning rate & L2 regularization.





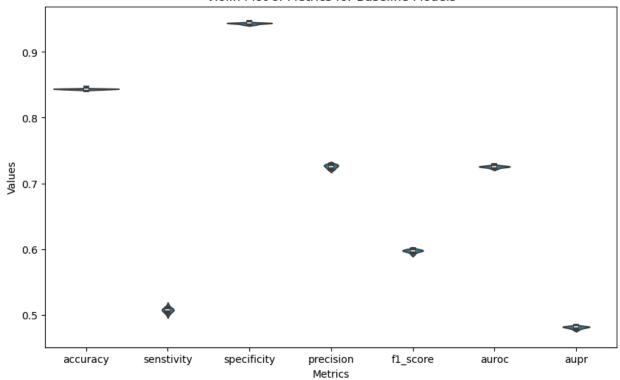
2. Adult dataset

Performance on Test set

| | Accuracy | Sensitivity | Specificity | Precision | F₁-score | AUROC | AUPR |
|-------------------|-----------------|--------------------|--------------------|-----------------|--------------------|--------------------|-------------------|
| LR | 0.8287 ± 0.0009 | 0.4908 ± 0.0032 | 0.9391 ± 0.0013 | 0.7246 ± 0.0037 | 0.5852 ± 0.0023 | 0.7150 ± 0.0014 | 0.481 ± 0.0021 |
| Voting ensemble | 0.8284 | 0.4913 | 0.9386 | 0.7230 | 0.5850 | 0.7149 | 0.4804 |
| Stacking ensemble | 0.8282 | 0.4900 | 0.9387 | 0.7230 | 0.5841 | 0.7143 | 0.4798 |

The highest prediction was observed for standard scaling, no feature selection, decaying learning rate with small initial learning rate & L2 regularization.

Violin Plot of Metrics for Baseline Models



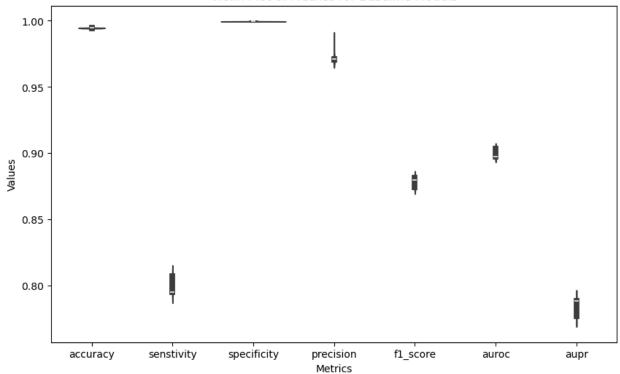
3. Credit-card-fraud dataset

Performance on Test set

| | Accuracy | Sensitivity | Specificity | Precision | F₁-score | AUROC | AUPR |
|-------------------|--------------------|--------------------|--------------------|--------------------|--------------------|--------------------|-----------------|
| LR | 0.9972 ± 0.0002 | 0.8852 ± 0.0055 | 0.9997 ± 0.0002 | 0.9851 ± 0.0074 | 0.9325 ± 0.0038 | 0.9425 ± 0.0027 | 0.8746 ± 0.0070 |
| Voting ensemble | 0.9973 | 0.8901 | 0.9998 | 0.9878 | 0.9364 | 0.9449 | 0.8817 |
| Stacking ensemble | 0.9971 | 0.8901 | 0.9995 | 0.9759 | 0.9310 | 0.9448 | 0.8711 |

The highest prediction is accrued by standard scaling, Feature selection, decaying learning rate with small initial learning rate & L2 regularization.





Observations:

1. Teleco-customer-churn dataset

Output with min-max scaling:

| accuracy | 0.7934 ± 0.0019 | 0.7936 | 0.7900 |
|-------------|-----------------|--------|--------|
| senstivity | 0.5085 ± 0.0148 | 0.5057 | 0.5284 |
| specificity | 0.8886 ± 0.0032 | 0.8898 | 0.8775 |
| precision | 0.6040 ± 0.0031 | 0.6054 | 0.5905 |
| f1_score | 0.5521 ± 0.0091 | 0.5511 | 0.5577 |
| auroc | 0.6985 ± 0.0060 | 0.6978 | 0.7030 |
| aupr | 0.4303 ± 0.0059 | 0.4300 | 0.4302 |

Standard scaling increases accuracy more than min-max scaling.

| accuracy | 0.7954 ± 0.0030 | 0.7936 | 0.7943 |
|-------------|-----------------|--------|--------|
| senstivity | 0.5243 ± 0.0184 | 0.5199 | 0.5483 |
| specificity | 0.8860 ± 0.0042 | 0.8851 | 0.8765 |
| precision | 0.6060 ± 0.0059 | 0.6020 | 0.5975 |
| f1_score | 0.5620 ± 0.0114 | 0.5579 | 0.5719 |
| auroc | 0.7052 ± 0.0077 | 0.7025 | 0.7124 |
| aupr | 0.4369 ± 0.0080 | 0.4332 | 0.4408 |
| | | | |

Training with all the columns increases accuracy.

| accuracy | 0.7974 ± 0.0035 | 0.7936 | 0.7979 |
|-------------|-----------------|--------|--------|
| senstivity | 0.5246 ± 0.0187 | 0.5284 | 0.5682 |
| specificity | 0.8886 ± 0.0069 | 0.8822 | 0.8746 |
| precision | 0.6118 ± 0.0106 | 0.6000 | 0.6024 |
| f1_score | 0.5646 ± 0.0103 | 0.5619 | 0.5848 |
| auroc | 0.7066 ± 0.0071 | 0.7053 | 0.7214 |
| aupr | 0.4400 ± 0.0075 | 0.4352 | 0.4505 |
| | | | |

Large learning rate worsens the performance

| accuracy | 0.7949 ± 0.0042 | 0.7929 | 0.7964 |
|-------------|---------------------|--------|--------|
| senstivity | 0.5205 ± 0.0208 | 0.5227 | 0.5455 |
| specificity | 0.8866 ± 0.0075 | 0.8832 | 0.8803 |
| precision | 0.6056 ± 0.0118 | 0.5993 | 0.6038 |
| f1_score | 0.5596 ± 0.0121 | 0.5584 | 0.5731 |
| auroc | 0.7035 ± 0.0082 | 0.7030 | 0.7129 |
| aupr | 0.4353 ± 0.0088 | 0.4329 | 0.4432 |
| | | | |

Decaying learning rate works better than constant learning rate

| accuracy | 0.8032 ± 0.0025 | 0.8071 | 0.8036 |
|-------------|-----------------|--------|--------|
| senstivity | 0.5297 ± 0.0139 | 0.5341 | 0.5483 |
| specificity | 0.8947 ± 0.0056 | 0.8984 | 0.8889 |
| precision | 0.6273 ± 0.0083 | 0.6373 | 0.6226 |
| f1_score | 0.5742 ± 0.0072 | 0.5811 | 0.5831 |
| auroc | 0.7122 ± 0.0050 | 0.7162 | 0.7186 |
| aupr | 0.4500 ± 0.0051 | 0.4571 | 0.4545 |
| | | | |

L1 regularization worsens the performance:

| accuracy | 0.7975 ± 0.0036 | 0.8021 | 0.7943 |
|-------------|-----------------|--------|--------|
| senstivity | 0.4318 ± 0.0232 | 0.4375 | 0.4659 |
| specificity | 0.9198 ± 0.0052 | 0.9240 | 0.9041 |
| precision | 0.6429 ± 0.0090 | 0.6581 | 0.6189 |
| f1_score | 0.5163 ± 0.0167 | 0.5256 | 0.5316 |
| auroc | 0.6758 ± 0.0097 | 0.6808 | 0.6850 |
| aupr | 0.4200 ± 0.0101 | 0.4289 | 0.4221 |
| | | | |
| | | | |

No regularization improves the performance than L1.

| accuracy | 0.8032 ± 0.0025 | 0.8071 | 0.8036 |
|-------------|-----------------|--------|--------|
| senstivity | 0.5297 ± 0.0139 | 0.5341 | 0.5483 |
| specificity | 0.8947 ± 0.0056 | 0.8984 | 0.8889 |
| precision | 0.6273 ± 0.0083 | 0.6373 | 0.6226 |
| f1_score | 0.5742 ± 0.0072 | 0.5811 | 0.5831 |
| auroc | 0.7122 ± 0.0050 | 0.7162 | 0.7186 |
| aupr | 0.4500 ± 0.0051 | 0.4571 | 0.4545 |
| | | | |

L2 performs the best.

| accuracy | 0.8032 ± 0.0024 | 0.8071 | 0.8036 |
|-------------|-----------------|--------|--------|
| senstivity | 0.5294 ± 0.0140 | 0.5341 | 0.5483 |
| specificity | 0.8947 ± 0.0056 | 0.8984 | 0.8889 |
| precision | 0.6271 ± 0.0081 | 0.6373 | 0.6226 |
| f1_score | 0.5739 ± 0.0072 | 0.5811 | 0.5831 |
| auroc | 0.7120 ± 0.0050 | 0.7162 | 0.7186 |
| aupr | 0.4498 ± 0.0050 | 0.4571 | 0.4545 |
| | | | |

The data seems to be gaussian distributed. Majority voting gives the best result. Stacking adds another layer of learning, which can lead to **overfitting** if the meta-model over-learns the patterns of the base models. Majority voting, being simpler, avoids this risk.

2. Adult dataset:

The adult.test seem to have some values missing than adult.data., hence when the columns are one-hot encoded the no of columns mismatch in case of both datasets

separately preprocessed. Therefore, I first combine the datasets, then preprocess & split it into a train & a test set.

Output with min-max scaling.

| accuracy | 0.7869 ± 0.0013 | 0.7866 | 0.7855 |
|-------------|-----------------|--------|--------|
| senstivity | 0.5519 ± 0.0078 | 0.5515 | 0.5593 |
| specificity | 0.8596 ± 0.0037 | 0.8594 | 0.8554 |
| precision | 0.5488 ± 0.0036 | 0.5482 | 0.5448 |
| f1_score | 0.5503 ± 0.0029 | 0.5498 | 0.5520 |
| auroc | 0.7057 ± 0.0023 | 0.7054 | 0.7074 |
| aupr | 0.4087 ± 0.0018 | 0.4083 | 0.4089 |
| | | | |

Standard-scaling gives better results.

| accuracy | 0.7901 ± 0.0017 | 0.7898 | 0.7897 |
|-------------|---------------------|--------|--------|
| senstivity | 0.3258 ± 0.0145 | 0.3310 | 0.3310 |
| specificity | 0.9417 ± 0.0050 | 0.9396 | 0.9395 |
| precision | 0.6468 ± 0.0128 | 0.6416 | 0.6411 |
| f1_score | 0.4330 ± 0.0114 | 0.4367 | 0.4366 |
| auroc | 0.6338 ± 0.0051 | 0.6353 | 0.6352 |
| aupr | 0.3766 ± 0.0044 | 0.3771 | 0.3769 |
| | | | |

Taking all the input features increases accuracy.

| accuracy | 0.8287 ± 0.0009 | 0.8284 | 0.8282 |
|-------------|---------------------|--------|--------|
| senstivity | 0.4908 ± 0.0032 | 0.4913 | 0.4900 |
| specificity | 0.9391 ± 0.0013 | 0.9386 | 0.9387 |
| precision | 0.7246 ± 0.0037 | 0.7230 | 0.7230 |
| f1_score | 0.5852 ± 0.0023 | 0.5850 | 0.5841 |
| auroc | 0.7150 ± 0.0014 | 0.7149 | 0.7143 |
| aupr | 0.4810 ± 0.0021 | 0.4804 | 0.4798 |
| | | | |

The data seems to be gaussian distributed. Between LR averaging, Majority voting & Stacking LR averaging works the best. LR averaging may perform better as it may not overfit data like stacking and can balance the impact of minority class predictions more effectively than majority voting.

3. Credit-card-fraud dataset

Output of minmax scaling.

| accuracy | 0.9966 ± 0.0000 | 0.9966 | 0.9963 |
|-------------|-----------------|--------|--------|
| senstivity | 0.8571 ± 0.0000 | 0.8571 | 0.8571 |
| specificity | 0.9998 ± 0.0000 | 0.9998 | 0.9995 |
| precision | 0.9873 ± 0.0000 | 0.9873 | 0.9750 |
| f1_score | 0.9176 ± 0.0000 | 0.9176 | 0.9123 |
| auroc | 0.9284 ± 0.0000 | 0.9284 | 0.9283 |
| aupr | 0.8495 ± 0.0000 | 0.8495 | 0.8389 |
| | | | |

Standard scaling works better than min-max scaling. Feature selection of top 20 columns increases accuracy. L2 regularization performs the best. The performance metrics are shown in the performance test data table.

L1 regularization gives the worst results.

| accuracy | 0.9943 ± 0.0007 | 0.9949 | 0.9949 |
|-------------|-----------------|--------|--------|
| senstivity | 0.7436 ± 0.0298 | 0.7692 | 0.7692 |
| specificity | 1.0000 ± 0.0000 | 1.0000 | 1.0000 |
| precision | 1.0000 ± 0.0000 | 1.0000 | 1.0000 |
| f1_score | 0.8526 ± 0.0199 | 0.8696 | 0.8696 |
| auroc | 0.8718 ± 0.0149 | 0.8846 | 0.8846 |
| aupr | 0.7493 ± 0.0291 | 0.7744 | 0.7744 |
| | | | |

No regularization gives a somewhat better prediction than L1.

| accuracy | 0.9966 ± 0.0000 | 0.9966 | 0.9963 |
|-------------|-----------------|--------|--------|
| senstivity | 0.8571 ± 0.0000 | 0.8571 | 0.8571 |
| specificity | 0.9998 ± 0.0000 | 0.9998 | 0.9995 |
| precision | 0.9873 ± 0.0000 | 0.9873 | 0.9750 |
| f1_score | 0.9176 ± 0.0000 | 0.9176 | 0.9123 |
| auroc | 0.9284 ± 0.0000 | 0.9284 | 0.9283 |
| aupr | 0.8495 ± 0.0000 | 0.8495 | 0.8389 |

The performance table above was filled for a short dataset of 20k random negative samples & all positive samples. Taking all instances may increase the accuracy but the dataset gets very skewed. Hence it's best to work with the shorter dataset.

| accuracy | 0.9990 ± 0.0000 | 0.9990 | 0.9990 |
|-------------|---------------------|--------|--------|
| senstivity | 0.4420 ± 0.0304 | 0.4333 | 0.4222 |
| specificity | 0.9999 ± 0.0000 | 0.9999 | 0.9999 |
| precision | 0.8879 ± 0.0066 | 0.8864 | 0.8837 |
| f1_score | 0.5897 ± 0.0283 | 0.5821 | 0.5714 |
| auroc | 0.7209 ± 0.0152 | 0.7166 | 0.7111 |
| aupr | 0.3935 ± 0.0300 | 0.3850 | 0.3740 |
| | | | |

For the larger dataset LR average, Majority voting & Stacking all give the same result, but for the shorter dataset majority voting gives the best result. This may be due to the shorter size of the data, which causes overfitting in case of stacking.