

i)

WhatsApp is a mobile app that allow its users to send and receive text, audio and video messages. The WhatsApp team wish to find whether a messages reach back to its sender or not? For example, a person P sends a message to his friends and they forward the message to their friends and so on. Given the users of WhatsApp and the information of all the messages sent by its users to other users, we need to determine that a message is sent back to its user or not for a particular user.

a) What data structure(s) and algorithm(s) is most suitable to represent this data and why?

1. • **Data Structure:**
2. Use a directed graph to represent the relationships between users.
3. Each user is represented as a node (vertex).
4. Each message sent is represented as a directed edge from one node to another.
5. • **Why a Directed Graph?**
6. The problem involves determining whether a directed path (message forwarding) forms a cycle that returns to the sender.
7. A directed graph is well-suited to represent this type of relationship.
8. • **Algorithm:**
9. Use Depth-First Search (DFS) to traverse the graph and detect cycles.
10. During DFS, if a node is revisited while still being in the current recursion stack, a cycle is detected (indicating the message returns to its sender).

b) How would you solve this problem with your suggested data structure? Briefly explain your idea in the form of pseudocode.

### b) Solution with Suggested Data Structure

#### Pseudocode:

1. Represent the directed graph using an **adjacency list**.
2. Use a **DFS traversal** to check for cycles:
  - Use a visited set to keep track of visited nodes.
  - Use a recStack (recursion stack) to detect back edges (indicative of cycles).

```

1. Function isMessageReturned(graph, start):

2.     # Initialize visited and recStack

3.     visited ← empty set      # Set to track visited nodes
4.     recStack ← empty set     # Set to track nodes in the current recursion stack
5.
6.     # Helper function for Depth-First Search (DFS)

7.     Function dfs(node):
8.         Add node to visited   # Mark the node as visited
9.         Add node to recStack  # Add the node to the recursion stack
10.
11.        # Traverse all neighbors of the current node

12.        For each neighbor in graph[node]:
13.            If neighbor is not in visited:           # If the neighbor has not been visited
14.                If dfs(neighbor) is True:            # Recur for the neighbor
15.                    Return True                      # Cycle detected
16.            Else if neighbor is in recStack:          # If the neighbor is in the recursion stack
17.                Return True                          # Cycle detected (back edge found)
18.
19.        Remove node from recStack                    # Backtracking: remove node from recursion
stack
20.        Return False                                # No cycle found from this node
21.
22.    # Call dfs for the starting node

23.    Return dfs(start)
24.
25. # Example usage
26. Function main():
27.     # Input: Number of users (nodes) and connections (edges)
28.     numUsers ← Input("Enter the number of users:")
29.     numConnections ← Input("Enter the number of connections:")
30.
31.     # Represent the graph as an adjacency list
32.     graph ← empty dictionary
33.     For i from 0 to numUsers - 1:
34.         graph[i] ← empty list
35.
36.     # Input the connections (directed edges)
37.     For i from 0 to numConnections - 1:
38.         u, v ← Input("Enter connection (u → v):")
39.         Append v to graph[u]
40.
41.     # Input the starting user
42.     start ← Input("Enter the starting user:")
43.
44.     # Check if the message returns to its sender
45.     If isMessageReturned(graph, start) is True:
46.         Print("The message reaches back to its sender.")
47.     Else:
48.         Print("The message does not reach back to its sender.")
49.

```

## 2nd Way

```

1. Function isMessageReturned(graph, start):
2.     Initialize visited as an empty set
3.     Initialize recStack as an empty set
4.
5.     Function dfs(node):
6.         Add node to visited
7.         Add node to recStack
8.
9.         For each neighbor in graph[node]:
10.            If neighbor is not in visited:
11.                If dfs(neighbor) is True:
12.                    Return True # Cycle detected
13.            Else if neighbor is in recStack:
14.                Return True # Back edge found, cycle detected
15.
16.         Remove node from recStack
17.         Return False
18.
19.     Return dfs(start) # Start DFS from the given node
20.

```

### Explanation of the Pseudocode:

#### 1. Graph Representation:

- The graph is represented as an adjacency list, where each node maps to a list of its neighbors. This allows efficient traversal of the graph.

#### 2. Cycle Detection:

- Start DFS from the given user (start).
- During DFS:
  - Mark the current node as visited.
  - Add the current node to the recursion stack.
  - Traverse all neighbors of the current node.
    - If a neighbor is unvisited, recursively call DFS on it.
    - If a neighbor is in the recursion stack, a **cycle** is detected.
- Remove the node from the recursion stack after all its neighbors are processed.

#### 3. Return Value:

- If a cycle is found during DFS, the message returns to the sender.
- Otherwise, it does not.

---

### Example Workflow:

1. **Input:** A directed graph with edges:

- $0 \rightarrow 1, 1 \rightarrow 2, 2 \rightarrow 0$  (cycle exists).
2. **Start:** User 0.
  3. **Output:** True (the message reaches back to the sender).
- 

ii)

You are required to develop a cab hailing app. Once a client requests a cab via your app, it should select the cabs which are free in the vicinity of the client (the one who is closest to the client should be allocated the request first, if the cab driver declines the request then it should be forwarded to the second nearest and so on) till a cab driver accepts the ride request. Once the cab has reached the client, your app should calculate the shortest distance to the destination and guide the driver accordingly.

a) Which data structures and algorithms would you like to use in your app so that it functions efficiently?

☐ 1. **Data Structures:**  
2. **Min-Heap (Priority Queue):**  
To efficiently select the nearest cabs, store cabs in a min-heap where the key is the distance of the cab from the client. This allows efficient retrieval of the nearest cab.  
3. **Graph Representation (Adjacency List or Matrix):**  
For guiding the driver to the destination, represent the road network as a graph. Nodes represent locations (e.g., intersections), and edges represent roads with weights (distances or travel times).  
4. **Hash Table:**  
To maintain the availability status of cabs and their locations (e.g., cab\_id -> {location, availability}).  
5. **Spatial Data Structure (e.g., KD-Tree):**  
For efficient nearest-neighbor searches, especially in dense urban areas.  
6. **Algorithms:**  
7. **Dijkstra's Algorithm:**  
To calculate the shortest distance from the cab's current location to the destination.  
8. **Haversine Formula (for Latitude-Longitude):**  
To calculate the great-circle distance between two points on Earth for real-world applications.  
9. **Breadth-First Search (BFS):**  
For simpler shortest path calculations if edge weights are uniform.

b) Give an algorithm (in terms of pseudo-code) that should run on your data structures specified above and selects cabs located in the vicinity of the client (the driver present nearest should be selected first, then the 2nd nearest and so on).

→ **Key Idea:**

1. Use a **min-heap** to store available cabs based on their distances from the client.
2. Pop the nearest cab from the heap, and if the driver declines, move to the next nearest cab.
3. Once a cab accepts, calculate the shortest path from the client to the destination.

```
1. // Function to calculate the distance between two points (latitude and longitude)
2. double calculateDistance(lat1, lon1, lat2, lon2) {
3.     // Use the Haversine formula to calculate distance
4.     // (assuming input is in degrees and Earth is a sphere)
5.     const double R = 6371.0; // Radius of Earth in kilometers
6.     double dLat = (lat2 - lat1) * PI / 180.0;
7.     double dLon = (lon2 - lon1) * PI / 180.0;
8.     double a = sin(dLat / 2) * sin(dLat / 2) +
9.         cos(lat1 * PI / 180.0) * cos(lat2 * PI / 180.0) *
10.         sin(dLon / 2) * sin(dLon / 2);
11.     double c = 2 * atan2(sqrt(a), sqrt(1 - a));
12.     return R * c; // Distance in kilometers
13. }
14.
15. // Function to select the nearest cab
16. void selectNearestCab(clientLocation, destination, cabs) {
17.     // Min-Heap for storing cabs based on their distance to the client
18.     PriorityQueue<Cab> minHeap;
19.
20.     // Populate the heap with distances of available cabs
21.     for (Cab cab : cabs) {
22.         if (cab.isAvailable) {
23.             double distance = calculateDistance(clientLocation.lat, clientLocation.lon,
24. cab.location.lat, cab.location.lon);
25.             minHeap.push({distance, cab}); // Min-Heap orders by distance
26.         }
27.     }
28.     // Iterate over the cabs in the order of proximity
29.     while (!minHeap.empty()) {
30.         Cab nearestCab = minHeap.top().cab;
31.         minHeap.pop();
32.
33.         // Send ride request to the nearest cab
34.         if (nearestCab.acceptRequest()) {
35.             cout << "Cab " << nearestCab.id << " has accepted the ride request." << endl;
36.         }
```

```

37.         // Calculate the shortest path to the destination
38.         vector<int> shortestPath = calculateShortestPath(nearestCab.location, destination);
39.
40.         // Guide the driver using the shortest path
41.         guideDriver(shortestPath);
42.         return;
43.     } else {
44.         cout << "Cab " << nearestCab.id << " has declined the ride request." << endl;
45.     }
46. }
47.
48. // If no cabs accept the ride request
49. cout << "No cabs available at the moment." << endl;
50. }
51.
52. // Function to calculate the shortest path using Dijkstra's algorithm
53. vector<int> calculateShortestPath(start, end) {
54.     // Use a graph representation (adjacency list or matrix)
55.     // Implement Dijkstra's algorithm to compute the shortest path
56.     return dijkstraShortestPath(graph, start, end);
57. }
58.

```

## Explanation of Pseudocode:

### 1. Distance Calculation:

- The calculateDistance function computes the distance between the client and a cab using the **Haversine formula** for geographical coordinates.

### 2. Min-Heap:

- All available cabs are inserted into the min-heap with their distances to the client as the key. This ensures that the nearest cab is always on top of the heap.

### 3. Request Handling:

- The nearest cab is queried first. If the driver declines, the app moves on to the next cab until one accepts or no cabs are left.

### 4. Shortest Path:

- Once a cab accepts the ride, the shortest path from the pickup location to the destination is computed using **Dijkstra's algorithm** or a similar shortest path algorithm.

### 5. Driver Guidance:

- The guideDriver function provides step-by-step directions to the driver based on the shortest path.
- 

## STACKS

Write a function called copyStack to copy the elements of an integer type stack, s1, into another stack, s2, where both s1 and s2 are reference parameters, and s2 is initially empty, copyStack is a global function which is only allowed to use the standard stack ADT functions: push, pop, top (or peek), and empty. Furthermore, copyStack cannot create an extra array or any other data structure, but it can use one or two extra variables. When the function ends, s2 contains exactly the same elements as s1, and s1 is exactly as it was initially.

Following picture shows an example, before and after copyStack:

```
1  #include <stack>
2  #include <iostream>
3  using namespace std;
4
5  // Global function to copy one stack into another
6  void copyStack(stack<int> &s1, stack<int> &s2) {
7      // Step 1: Transfer elements from s1 to s2 (reversing s1)
8      while (!s1.empty()) {
9          s2.push(s1.top());
10         s1.pop();
11     }
12
13     // Step 2: Transfer elements back from s2 to s1 (restoring s1's order)
14     stack<int> tempStack; // Temporary stack to preserve s2 during this process
15     while (!s2.empty()) {
16         int temp = s2.top();
17         s2.pop();
18         s1.push(temp);
19         tempStack.push(temp); // Store the element temporarily
20     }
21
22     // Step 3: Transfer elements from tempStack back to s2 to finalize its copy
23     while (!tempStack.empty()) {
24         s2.push(tempStack.top());
25         tempStack.pop();
26     }
27 }
28
```

---

# HASH

Add the numbers 120, 55, 22, 13, 1, 5, 25, 15 to a Hash table with 7 buckets using the simple modulo function as the hash function. Show the table if Chaining is chosen for the hash table for overflow handling.

To create a hash table with **7 buckets** and use the **modulo function** as the hash function ( $\text{key} \% 7$ ), we compute the bucket index for each number and handle collisions using **chaining** (linked lists in each bucket).

## Step 1: Compute Bucket Indexes

1. We calculate the bucket for each number using  $\text{key} \% 7$ :
2.  $120 \% 7 = 1$
3.  $55 \% 7 = 6$
4.  $22 \% 7 = 1$
5.  $13 \% 7 = 6$
6.  $1 \% 7 = 1$
7.  $5 \% 7 = 5$
8.  $25 \% 7 = 4$
9.  $15 \% 7 = 1$
- 10.

## Step 2: Build the Hash Table with Chaining

1. Each bucket contains a linked list for numbers mapping to the same index.
2. Bucket Linked List (Chained Entries)
3. 0 Empty
4. 1  $120 \rightarrow 22 \rightarrow 1 \rightarrow 15$
5. 2 Empty
6. 3 Empty
7. 4 25
8. 5 5
9. 6  $55 \rightarrow 13$

## Explanation:

1. **Bucket 0:** No numbers map here ( $\text{key} \% 7 \neq 0$ ).
2. **Bucket 1:** Numbers 120, 22, 1, and 15 all map here, forming a chain  $120 \rightarrow 22 \rightarrow 1 \rightarrow 15$ .
3. **Bucket 2:** No numbers map here ( $\text{key} \% 7 \neq 2$ ).
4. **Bucket 3:** No numbers map here ( $\text{key} \% 7 \neq 3$ ).
5. **Bucket 4:** Number 25 maps here ( $25 \% 7 = 4$ ).



6. **Bucket 5:** Number 5 maps here ( $5\%7=55\ \% 7 = 5$ ).

7. **Bucket 6:** Numbers 55 and 13 map here, forming a chain  $55 \rightarrow 1355 \rightarrow 13$ .

```
1. Final Hash Table with Chaining:
2. Bucket 0:
3. Bucket 1: 120 → 22 → 1 → 15
4. Bucket 2:
5. Bucket 3:
6. Bucket 4: 25
7. Bucket 5: 5
8. Bucket 6: 55 → 13
9. This structure ensures collisions are handled efficiently using chaining.
10.
```

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## ➤ Time Complexity

Calculate the time complexity expression for the following code snippet with respect to  $n$  and express

it in terms of Big-O notation. Show all working for full credit.

```
1. for (int i = 1; i < n; i = i * 2) {
2.     for (int j = 0; j < i; ++j) {
3.         sum++;
4.     }
5. }
6.
```

ii. While doing worst case analysis of an algorithm, I found it takes 2 steps to complete the job, where  $n$  is the input size. Can I say it is  $O(2^n)$ ? Why or why not?

```
1. ii. Analysis of the statement:
   "Can I say it is  $O(2^n)$ ? Why or why not?"
2. If the algorithm takes a constant number of steps (e.g., 2 steps) irrespective of the input size  $n$ , then its time complexity is  $O(1)$  because the runtime does not grow with  $n$ .
3. Reasoning:
4.  $O(2^n)$  implies the runtime grows exponentially with  $n$ , which is not the case here.
5. The algorithm's runtime being fixed at 2 steps is independent of  $n$ , so  $O(2^n)$  is incorrect.
6. The correct time complexity is  $O(1)$ .
7. Summary:
8. The time complexity of the code snippet is  $O(n)$ .
9. The algorithm with 2 constant steps is  $O(1)$ , not  $O(2n)$  or  $O(2^n)$ .
10.
```

---

## SPACE COMPLEXITY + TIME

```
1. int Enigma(int N) {
2.     if (N <= 1)
3.         return 11;
4.     else {
5.         Enigma(N - N / 2);
6.         Enigma(N - N / 2);
7.     }
8. }
9.
```

Since the number of levels is  $O(\log_2(N))$ , the total time complexity is **exponential**.

$$T(N) = O(2^N)$$

### Step 2: Space Complexity

#### Recursive Space:

The space complexity is determined by the depth of the recursion tree. Since each recursive call reduces  $N$  geometrically, the depth of the recursion tree is:

$$O(\log_2(N))$$

---

For example, if the array is {3, 7, 5, 12, 6} and  $k = 3$ , then the function should return 25 (12+7+6) i.e.

- A number  $k \leq n$  and calculates the sum of the  $k$  largest numbers in the array.

```
1. Function SumOfLargestKValues(array, n, k):
2.     1. Sort the array in descending order. // Time complexity:  $O(n \log n)$ 
3.     2. Initialize sum  $\leftarrow 0$ 
4.     3. For i  $\leftarrow 0$  to k-1: // Iterate over the first k elements
5.         sum  $\leftarrow$  sum + array[i]
6.     4. Return sum
7.
```

### Explanation

```
1. Sorting:
```

2. Sort the array in descending order so that the k largest elements are at the beginning of the array.
3. Sorting takes  $O(n \log n)$  time.
4. Summing the k largest values:
5. Iterate through the first k elements of the sorted array and compute their sum.
6. This loop runs  $O(k)$ , which is  $O(n)$  in the worst case if  $k=n$ , but does not exceed  $O(n \log n)$  overall due to the sorting step.
7. Returning the Result:
8. The computed sum is returned as the output.

## Example Walkthrough

1. Input:
2. Array: [3,7,5,12,6]
3. n=5 k=3
4. Execution:
5. Sort the array in descending order:
6. [12,7,6,5,3]
7. Sum the first k=3 largest elements:
8. 12+7+6=25
9. Return 25

Consider the list to end at the last node). So if  $m=5$ , it will find the node containing 5, then delete this node as well as the 4 nodes that come after it. If there are less than  $m-1$  nodes after the node with  $key=m$ , all these would be deleted. And if the list is: 2->9->4->6->1->2->5- then delete AfterKey(6) will result in 2->9->4

For example if the list is 2->9->4->3->1->2->5-then delete AfterKey(3) would result in 2->9->4->5 If there is no node in the list with  $key=m$ , the function simply returns false. If you use any helper function then implement it as well. Make sure your code runs in linear time and creates no memory leaks. It should also handle all special cases.

```
54 // Helper function to add a node at the end of the list
55 void Append(Node*& head, int value) {
56     if (head == nullptr) {
57         head = new Node(value);
58         return;
59     }
60     Node* current = head;
61     while (current->getNext() != nullptr) {
62         current = current->getNext();
63     }
64     current->setNext(new Node(value));
65 }
66
```

```

20 // Function to delete m-1 nodes after the node with key `m`
21 bool DeleteAfterKey(Node*& head, int m) {
22     // Handle the case where the list is empty
23     if (head == nullptr) {
24         return false;
25     }
26
27     // Find the node with the value `m`
28     Node* current = head;
29     while (current != nullptr && current->getValue() != m) {
30         current = current->getNext();
31     }
32
33     // If no node with value `m` is found
34     if (current == nullptr) {
35         return false;
36     }
37
38     // Delete up to m-1 nodes after the node with value `m`
39     Node* toDelete = current->getNext();
40     int count = 0;
41     while (toDelete != nullptr && count < m - 1) {
42         Node* temp = toDelete->getNext(); // Save the next node
43         delete toDelete;                 // Free the current node
44         toDelete = temp;                  // Move to the next node
45         count++;
46     }
47
48     // Update the next pointer of the current node
49     current->setNext(toDelete);
50
51     return true;
52 }

```

## CIRCULAR SINGLY

```

48 bool deleteAfterKey(int m) {
49     if (last == nullptr) {
50         return false; // Empty list
51     }
52
53     // Find the node with key `m`
54     Node* current = last->next;
55     do {
56         if (current->key == m) {
57             break;
58         }
59         current = current->next;
60     } while (current != last->next);
61
62     // If key `m` is not found
63     if (current->key != m) {
64         return false;
65     }
66
67     // Delete the next m-1 nodes
68     Node* toDelete = current->next;
69     for (int count = 0; count < m - 1 && toDelete != nullptr; ++count) {
70         if (toDelete == last) {
71             last = (last->next == last) ? nullptr : current; // Adjust last pointer if needed
72         }
73         Node* temp = toDelete->next;
74         delete toDelete;
75         toDelete = temp;
76     }
77
78     // Update the current node's next pointer
79     current->next = toDelete;
80
81     // If all nodes are deleted, adjust `last` pointer
82     if (toDelete == nullptr) {
83         last = nullptr;
84     }
85
86     return true;
87 }

```

```

18
19 // Function to add a node to the end of the list
20 void append(int key) {
21     Node* newNode = new Node(key);
22     if (last == nullptr) {
23         last = newNode;
24         last->next = last; // Circular link
25     } else {
26         newNode->next = last->next;
27         last->next = newNode;
28         last = newNode;
29     }
30 }
31

```

---

To convert the postfix expression  $XYZ/+EJ\%-KF^{*+}$  to prefix, follow these steps systematically:

**Steps:**

1. **Understand Postfix:** In postfix notation, operators follow their operands.
2. **Conversion Process:**
  - Use a stack to process the postfix expression.
  - Push operands (letters) onto the stack.
  - When an operator is encountered, pop the necessary number of operands from the stack, prepend them with the operator, and push the resulting expression back onto the stack.
3. **Result:** Once the expression is fully processed, the stack will contain the prefix expression.

**Conversion:**

1. **Given postfix:**  $XYZ/+EJ\%-KF^{*+}$
2. **Step-by-step Process:**
  3. **Process X, Y, and Z:** Push them onto the stack.
  4. **Stack:** X, Y, Z
  5. **Encounter /:** Pop Z and Y, apply /, and push (/Y Z).
  6. **Stack:** X, /YZ
  7. **Encounter +:** Pop /YZ and X, apply +, and push (+X /YZ).
  8. **Stack:** +X /YZ
  9. **Process E and J:** Push them onto the stack.
  10. **Stack:** +X /YZ, E, J
  11. **Encounter %:** Pop J and E, apply %, and push (%E J).
  12. **Stack:** +X /YZ, %E J
  13. **Encounter -:** Pop %E J and +X /YZ, apply -, and push (-+X /YZ %E J).
  14. **Stack:** -+X /YZ %E J
  15. **Process K and F:** Push them onto the stack.
  16. **Stack:** -+X /YZ %E J, K, F
  17. **Encounter \*:** Pop F and K, apply \*, and push (\*K F).
  18. **Stack:** -+X /YZ %E J, \*K F
  19. **Encounter +:** Pop \*K F and -+X /YZ %E J, apply +, and push (+ -+X /YZ %E J \*K F).
  20. **Stack:** + -+X /YZ %E J \*K F
21. **Final Prefix Expression:**
22.  $+ - + X / Y Z \% E J * K F$

```

1. // Data structure to represent a Location
2. STRUCT Location:
3.     latitude
4.     longitude
5.
6. // Class to represent a Cab
7. CLASS Cab:
8.     id
9.     location
10.    available (Boolean) // If the cab is available for a ride
11.
12.    // Function to calculate Euclidean distance (for simplicity)
13.    FUNCTION distanceTo(clientLocation):
14.
15.        RETURN sqrt((clientLocation.latitude - location.latitude)^2 + (clientLocation.longitude
- location.longitude)^2)
16.
17.    // Function to check if the cab can accept the ride
18.    FUNCTION acceptsRequest():
19.        // Logic to check if the cab accepts the ride
20.        RETURN available
21.
22. // Class to represent a Graph for Dijkstra's algorithm
23. CLASS Graph:
24.    // A map of nodes (intersections) and edges (roads)
25.    nodes
26.    edges
27.
28.    // Add nodes and edges to the graph (representing road network)
29.    FUNCTION addEdge(nodeA, nodeB, distance):
30.        // Add an edge between nodeA and nodeB with a given distance
31.
32.    // Function to run Dijkstra's Algorithm
33.
34.    FUNCTION dijkstra(startNode, endNode):
35.
36.        // Initialize distances for all nodes
37.
38.        distances[startNode] = 0
39.        FOR each node in nodes:
40.            IF node != startNode:
41.                distances[node] = infinity
42.
43.        // Set of unvisited nodes
44.        unvisitedNodes = nodes
45.
46.        WHILE unvisitedNodes is NOT empty:
47.
48.            currentNode = node with the smallest distance from startNode
49.
50.            REMOVE currentNode from unvisitedNodes
51.
52.            FOR each neighbor of currentNode:
53.
54.                newDistance = distances[currentNode] + distance from currentNode to neighbor
55.
56.                IF newDistance < distances[neighbor]:
57.
58.                    distances[neighbor] = newDistance

```

```

52.         // Return the shortest path distance to endNode
53.         RETURN distances[endNode]
54.
55.
56. // Class to represent a Priority Queue for selecting the nearest available cab
57. CLASS CabQueue:
58.     // A priority queue (min-heap) to manage cabs based on proximity
59.     FUNCTION addCab(cab, distance):
60.         // Add cab to priority queue with distance as priority
61.
62.     FUNCTION getClosestCab():
63.         IF queue is NOT empty:
64.             closestCab = REMOVE top cab from queue
65.
66.         RETURN closestCab
67.     ELSE:
68.         RETURN INVALID CAB (No cabs available)
69.
70. // Main function to select the nearest available cab and calculate the shortest path
71. FUNCTION selectCabForRide(clientLocation, destinationLocation, cabs, graph, cabQueue):
72.     // Step 1: Search for nearby cabs from the list
73.     FOR each cab in cabs:
74.         IF cab is available:
75.             distance = cab.distanceTo(clientLocation)
76.             cabQueue.addCab(cab, distance)
77.
78.     // Step 2: Select the closest available cab
79.     selectedCab = cabQueue.getClosestCab()
80.
81.     // Step 3: Check if the selected cab accepts the ride
82.     WHILE selectedCab is NOT INVALID CAB:
83.         IF selectedCab.acceptsRequest():
84.             // Calculate the shortest path from cab to client
85.             cabToClientDistance = graph.dijkstra(selectedCab.location, clientLocation)
86.
87.             // Calculate the shortest path from client to destination
88.             clientToDestinationDistance = graph.dijkstra(clientLocation, destinationLocation)
89.
90.             // Total distance for the ride
91.             totalRideDistance = cabToClientDistance + clientToDestinationDistance
92.
93.             PRINT "Cab assigned: " + selectedCab.id
94.             PRINT "Total ride distance: " + totalRideDistance
95.             BREAK
96.     ELSE:

```



```

97.          // If the selected cab declines, continue with the next closest cab
98.          selectedCab = cabQueue.getClosestCab()
99.
100.         // Step 4: Handle case if no cab accepts the request
101.         IF selectedCab is INVALID CAB:
102.             PRINT "No available cab found."
103.             // Notify the client that no cabs are available
104.
105.
106.         // Main Program Execution:
107.         BEGIN
108.             // Create an instance of the Graph, CabQueue, and list of cabs
109.             graph = NEW Graph
110.             cabQueue = NEW CabQueue
111.             cabs = [Cab(1, Location(40.730000, -73.935000)),
112.                     Cab(2, Location(40.731000, -73.934000)),
113.                     Cab(3, Location(40.732000, -73.936000))]
114.
115.             // Add roads (edges) to the graph (example data)
116.             graph.addEdge(Node(1), Node(2), 5) // Road between node 1 and node 2 with distance 5
117.             graph.addEdge(Node(2), Node(3), 3) // Road between node 2 and node 3 with distance 3
118.
119.             // Example locations for the client and the destination
120.             clientLocation = Location(40.730610, -73.935242)
121.             destinationLocation = Location(40.735610, -73.940242)
122.
123.             // Select a cab for the client ride
124.             selectCabForRide(clientLocation, destinationLocation, cabs, graph, cabQueue)
125.         END
126.

```

## Explanation of the Pseudo-code:

1. **Cab and Location:**
2. Each Cab has an ID, a location (latitude and longitude), and an availability status. The `distanceTo` function calculates the Euclidean distance between the cab's location and the client's location.
3. The `acceptsRequest` function checks if the cab is available and can accept the ride request.
4. **Graph (Road Network):**
5. A `Graph` class is used to represent the road network, where nodes represent intersections (locations) and edges represent roads (with distances).
6. The `dijkstra` function implements Dijkstra's algorithm to find the shortest path from the starting node to the destination node. It returns the shortest distance between the start and end nodes.
7. **Priority Queue:**
8. A `CabQueue` (min-heap) stores cabs sorted by their proximity to the client. The `addCab` function adds a cab to the queue based on its distance to the client, and the `getClosestCab` function retrieves the closest available cab.

9. **Selecting the Closest Available Cab:**
10. **The** selectCabForRide **function** starts **by** searching **for** nearby cabs **from** the list **and** adding them to the priority queue.
11. **It then** selects the closest available cab **and** checks **if** it accepts the ride.
12. **If** the selected cab accepts the ride, **Dijkstra's** algorithm **is** used to calculate the shortest distance **from** the cab to the client (cabToClientDistance), **and from** the client to the destination (clientToDestinationDistance).
13. **The** total ride distance **is** the sum **of** these two distances.
14. **If** the cab declines the ride, the algorithm tries the **next** closest cab.
15. **Handling No Cab Acceptance:**
16. **If no** cab accepts the ride request, the system notifies the client that **no** cabs are available.
- 17.

### **Key Points:**

- **Dijkstra's Algorithm** helps find the shortest path between the cab and the client, and between the client and the destination.
- **Priority Queue** ensures that the closest cab is selected first.
- The algorithm is efficient for finding the optimal route and handling multiple cabs.