

Lab 9

Exercise 9.1

$$D_n = \frac{0.504}{1+j4n}$$

$$x(t) = \sum_{n=-\infty}^{\infty} D_n e^{jn\omega t} \quad \dots \text{Generic Exponential Fourier Series}$$

$$x(t) = 0.504 \sum_{n=-\infty}^{\infty} \frac{1}{1+j4n} e^{j2\pi n t}$$

$$x(t) = 0.504 \left[1 + \frac{1}{1+j4} e^{j2t} + \frac{1}{1+j8} e^{j4t} + \frac{1}{1+j12} e^{j6t} + \dots \right. \\ \left. + \frac{1}{1-j4} e^{-j2t} + \frac{1}{1-j8} e^{-j4t} + \frac{1}{1-j12} e^{-j6t} + \dots \right]$$

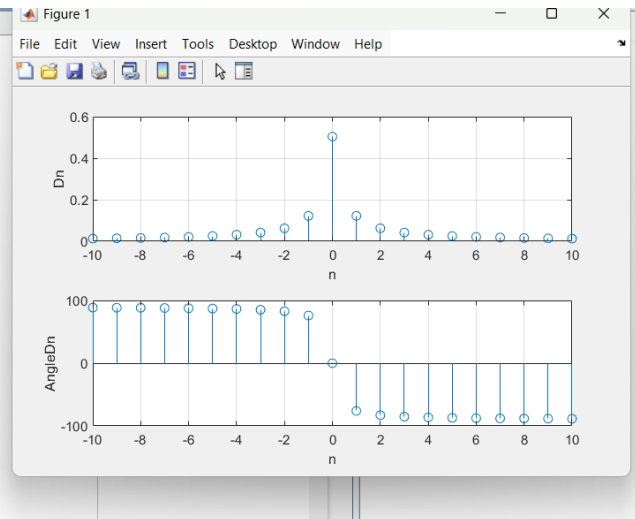
For above series $D_n = 0.504$ * Degree Angle
 $D_1 = \frac{0.504}{1+j4} = 0.122 e^{-j75.96^\circ} \Rightarrow |D_1| = 0.122 \angle D_1 = -75.96^\circ$
 $-D_1 = \frac{0.504}{1-j4} = 0.122 e^{j75.96^\circ} \Rightarrow |D_{-1}| = 0.122 \angle D_{-1} = 75.96^\circ$
 $D_2 = \frac{0.504}{1+j8} = 0.0625 e^{-j82.87^\circ} \Rightarrow |D_2| = 0.0625 \angle D_2 = -82.87^\circ$
 $-D_2 = \frac{0.504}{1-j8} = 0.0625 e^{j82.87^\circ} \Rightarrow |D_{-2}| = 0.0625 \angle D_{-2} = 82.87^\circ$

$\angle D_n$

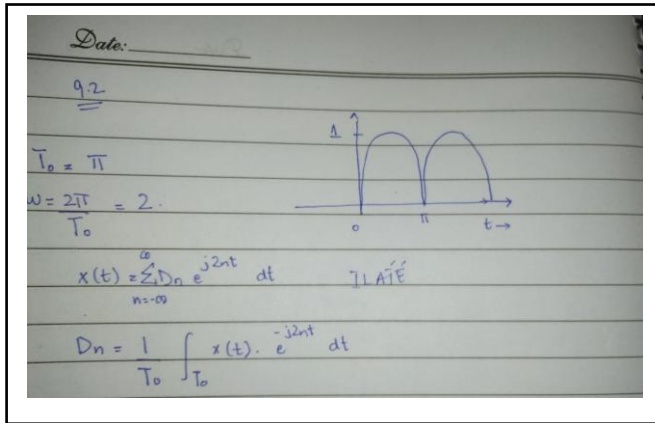
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1
2
3
4     n=-10:1:10;
5     num=0.504;
6     den=1+1j*4*n;
7     Dn=num./den;
8     MagDn=abs(Dn);
9
10    phaseDn=rad2deg(atan2(imag(Dn),real(Dn)));
11    subplot(211),stem(n,MagDn),grid,xlabel('n'),ylabel('Dn');
12    subplot(212),stem(n,phaseDn),grid,xlabel('n'),ylabel('AngleDn')
13

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Exercise 9.2



$$D_n = \frac{1}{\pi} \int_0^{\pi} \sin(t) \cdot e^{-j2nt} dt$$

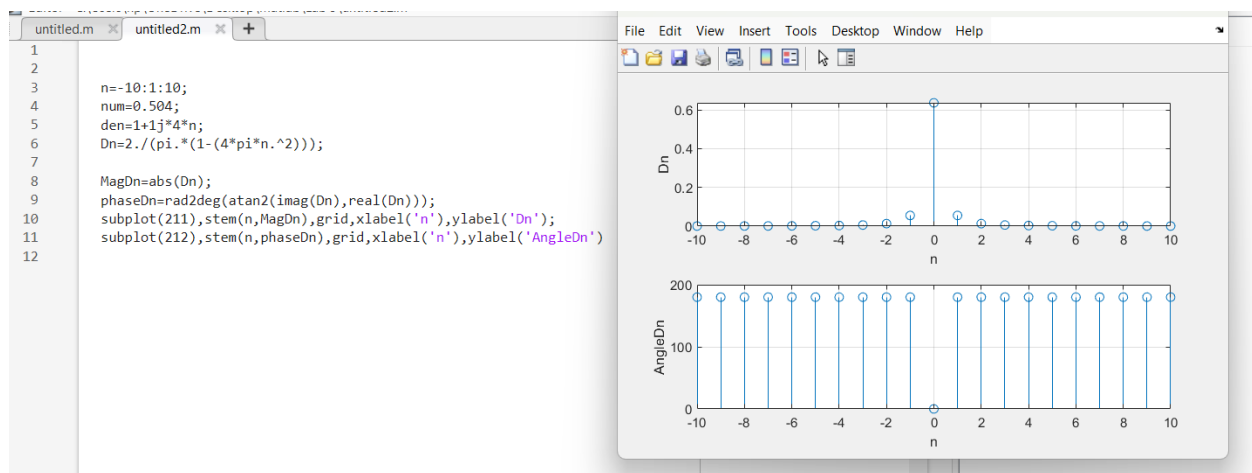
$$\sin(t) = \frac{e^{jt} - e^{-jt}}{2j}$$

$$= \frac{1}{\pi} \int_0^{\pi} \frac{e^{jt} - e^{-jt}}{2j} e^{-j2nt} dt = \frac{1}{\pi} \int_0^{\pi} \frac{e^{j(1-2n)t} - e^{-j(1+2n)t}}{2j} dt$$

$$= \frac{1}{\pi} \left[\frac{e^{j(1-2n)t}}{j(1-2n)} - \frac{e^{-j(1+2n)t}}{-j(1+2n)} \right]_0^{\pi}$$

$$= \frac{1}{2j\pi} \left[\frac{e^{j(1-2n)\pi} - 1}{j(1-2n)} - \frac{e^{-j(1+2n)\pi} - 1}{-j(1+2n)} \right]$$

$$D_n = \frac{2}{\pi(1-4n^2)}$$



Exercise 9.3

