

Iteration 2

Start with $m_1 = 1.7$, $b_1 = 2.1$

Predictions

$$\hat{y}_1 = 3.8, e_1 = -0.8$$

$$\hat{y}_2 = 7.2, e_2 = -1.2$$

Gradients :

$$\sum x_i e_i = 1 \cdot (-0.8) + 3 \cdot (-1.2) = -0.8 + (-3.6) = -4.4$$

$$\text{So } \frac{\partial J}{\partial m} = -1 \cdot (-4.4) = 4.4$$

$$\sum e_i = -0.8 + (-1.2) = -2.0$$

$$\text{So } \frac{\partial J}{\partial b} = -1 \cdot (-2.0) = 2.0$$

Update parameters:

$$m_2 = m_1 - 0.1 \cdot (4.4) = 1.7 - 0.44 = 1.26$$

(arithmetic: $0.1 \times 4.4 = 0.44$, $1.7 - 0.44 = 1.26$)

$$b_2 = 2.1 - 0.1 \cdot (2.0) = 2.1 - 0.2 = 1.9$$

Predictions & MSE after update (with $m_2 = 1.26$, $b_2 = 1.9$):

$$\hat{y}_1 = 1.26 \cdot 1 + 1.9 = 1.26 + 1.9 = 3.16$$

$$\text{Error: } 3 - 3.16 = -0.16$$

$$\hat{y}_2 = 1.26 \cdot 3 + 1.9 = 3.78 + 1.9 = 5.68$$

$$\text{Error: } 6 - 5.68 = 0.32$$

Date

No.

MSE after iter 2:

$$MSE_2 = \frac{(-0.16)^2}{2} + \frac{(0.32)^2}{2} = \frac{0.0256}{2} + \frac{0.1024}{2} = \frac{0.1280}{2}$$

$$\frac{0.1280}{2} = 0.064$$

$$= 0.064$$