

Iteration 3 (current);

$$m_2 = 1.26, ; b_2 = 1.9$$

Predictions:

$$\cdot \hat{y}_1 = 3.16, \quad e_1 = -0.16$$

$$\cdot \hat{y}_2 = 5.68, \quad e_2 = 0.32$$

Gradients:

$$\begin{aligned} \sum_{i=1}^n e_i &= 1 \times (-0.16) + 3 \times (0.32) = -0.16 + 0.96 \\ &= 0.80 \end{aligned}$$

$$\text{so } \frac{\partial J}{\partial m} = -1 \times 0.80 = 0.80$$

$$\sum e_i = -0.16 + 0.32 = 0.16$$

$$\text{so } \frac{\partial J}{\partial b} = -1 \times 0.16 = -0.16$$

Update parameters:

$$\therefore m_3 = 1.26 - 0.1 \times (-0.80) = 1.26 + 0.08 = 1.34$$

$$\therefore b_3 = 1.9 - 0.1 \times (-0.16) = 1.9 + 0.016 = 1.916$$

Predictions 3 MSE after update (given $m_3 = 1.34$, $b_3 = 1.916$):

$$\hat{y}_1 = 1.34 \times 1 + 1.916 = 1.34 + 1.916 = 3.256$$

$$\text{Error: } 3 - 3.256 = -0.256$$

$$\hat{y}_2 = 1.34 \times 3 + 1.916 = 4.02 + 1.916 = 5.936$$

$$\text{Error: } 6 - 5.936 = 0.064$$

\therefore MSE after iter 3:

$$\text{MSE}_3 = \frac{(-0.256)^2 + (0.064)^2}{2}$$

$$= \frac{0.065536 + 0.004096}{2}$$

$$= \frac{0.069632}{2} = 0.034816$$