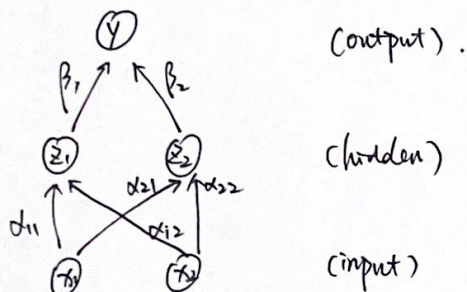


1. Neural Network.

It is like a combination of logistic regression.

But not really. \because no target for hidden units.

Ex #1. NN w/ 1 Hidden Layer and 2 Hidden Units.



$x_i \in \mathbb{R}$.

$z_i \in (0, 1)$ if σ is sigmoid.

$z_i \in \mathbb{R}$ more generally.

增加 Net 的非线性 (增加深度)
激活函数. (Non linear)

σ : activation function.

if σ is sigmoid $\sigma(a) = \frac{1}{1 + \exp(-a)}$.

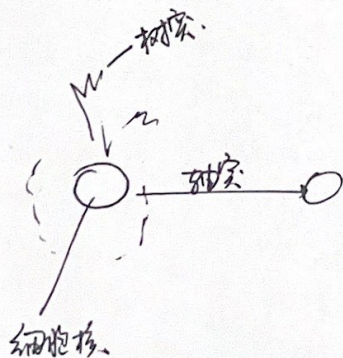
$$z_1 = \sigma(\alpha_{11}x_1 + \alpha_{12}x_2 + \alpha_{10}).$$

$$z_2 = \sigma(\alpha_{21}x_1 + \alpha_{22}x_2 + \alpha_{20}).$$

$$y = \sigma(\beta_1 z_1 + \beta_2 z_2 + \beta_0).$$

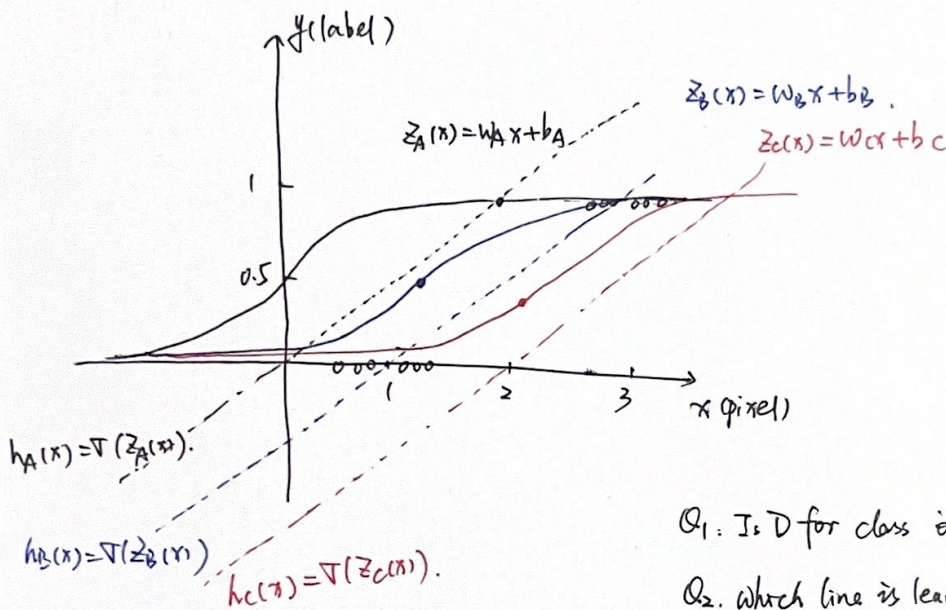
$$= \sigma(\beta_1 \sigma(\alpha_{11}x_1 + \alpha_{12}x_2 + \alpha_{10}) + \beta_2 \sigma(\alpha_{21}x_1 + \alpha_{22}x_2 + \alpha_{20}) + \beta_0).$$

$=$ Don't forget intercepts.



1D Face Recognition

P2

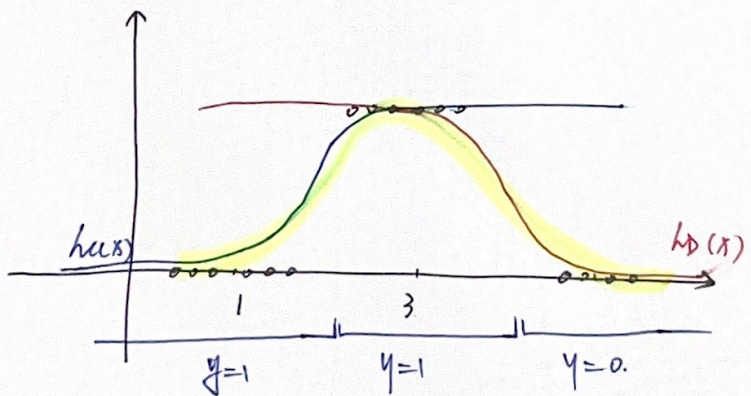


Q1: Is D for class or reg? both

Q2: Which line is learned by linear Reg? $z_A(x)$

Q3: Which sigmoid is learned by (logistic) Reg? $h_C(x)$

Q4: What is the D.B. for $h_C(x)$ point $x=2$



$$h_E(x) = \sigma\left(\frac{h_C(x) + h_D(x)}{2}\right)$$

D.B. is a nonlinear func. of x .

3. Backpropagation 误差反向传播法

R-

(Chain Rule)

Computation graphs

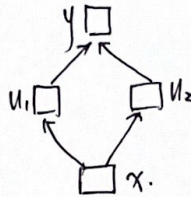
→ Not a NN diagram

Def #1. $y = f(u)$
 $u = g(x)$



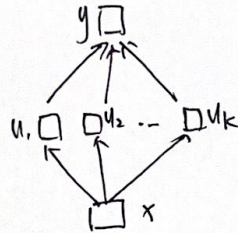
$$\frac{\partial y}{\partial x} = \frac{\partial y}{\partial u} \frac{\partial u}{\partial x}$$

Def #2. $y = f(u_1, u_2)$
 $u_2 = g_2(x)$
 $u_1 = g_1(x)$



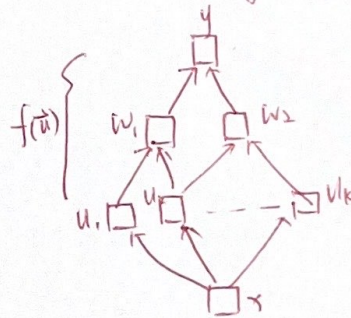
$$\frac{\partial y}{\partial x} = \frac{\partial y}{\partial u_1} \frac{\partial u_1}{\partial x} + \frac{\partial y}{\partial u_2} \frac{\partial u_2}{\partial x}$$

Def #3. $y = f(\vec{u})$
 $\vec{u} = g(x)$



$$\frac{\partial y}{\partial x} = \sum_{k=1}^K \frac{\partial y}{\partial u_k} \frac{\partial u_k}{\partial x}$$

* holds for any intermediate quantities \vec{u}



Derivative of a Sigmoid.

$$s = \frac{1}{1 + \exp(-b)}. \quad \frac{ds}{db} = s(1-s).$$