

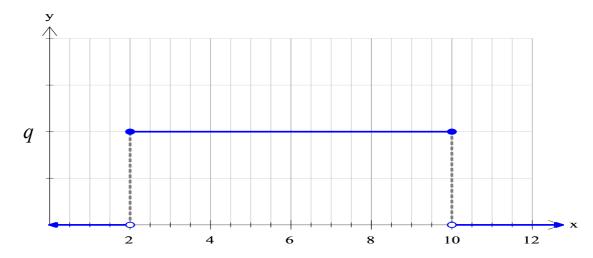
Determine $P(3 < t \le 6)$

d)

| | | ATMAM Mathematics Methods Test 3 Calculator Assumed | | | | | | | |
|-----|--|--|--------------------------------|--|-----------------------------------|--------------------|------------|-----|-----|
| SHE | NTON LEGE | Name: | | | | | | | |
| | | Teacher: | F | riday | Smi | ith | | | |
| | Time | Allowe | ed : 50 |) minu | ites | Ma | arks | /5 | 4 |
| ı | Materials allow | ved: Classpa | d, Formu | la Sheet. | | | | | |
| | All necessary was where appropriate of the series of the s | iate, values s to <u>four</u> deci be awarded ow shows al | should be mal place for untidy | given to <u>ty</u> es. or poorly ible outcor | <u>vo</u> decimal p arranged w | laces, exc ork. | | | |
| | Score (t) | 1 | 2 | 3 | 4 | 5 | 6 | 7 | |
| | Probability | 0.15 | k | 0.05 | 2k + 0.2 | 0.1 | 3 <i>k</i> | 0.2 | |
| a) | Determine the | e value of <i>k</i> . | | | | | | | (1) |
| b) | Determine the | e expected v | alue of T. | | | | | | (1) |
| c) | Determine the | e standard de | eviation o | fT. | | | | | (1) |

(1)

The graph below shows a probability density function for a uniform random variable X, defined over $2 \le x \le 10$.



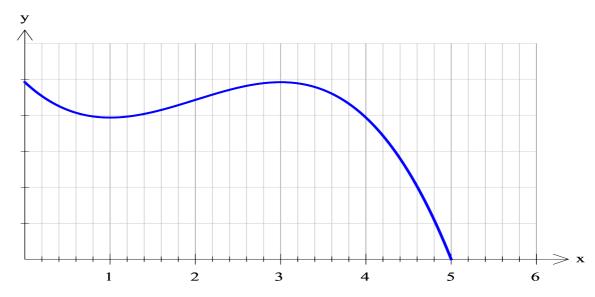
- a) Determine the value of q.
- b) Determine P(3 < x < 9) (1)

(1)

c) Find t such that P(x < t) = 0.4 (2)

d) Determine $P(x > 8 \mid x > 5)$ (2)

The graph below shows a probability density function for a random variable X, defined by the function $f(x) = k(x^3 - 6x^2 + 9x - 20)$.



- a) Find the value of k
- b) Find the expected value of X. (Give your answer as an exact value.) (2)

(2)

A triangular random variable is defined by the function f(x). It has an expected value E(X) = 7 and standard deviation $\sigma_X = 3$. The mode m has a frequency f(m) = k.

If f(x) is transformed into f(3X - 1), determine the new...

- a) expected value (1)
- b) standard deviation (1)
- c) value for the mode in terms of m, and the new frequency in terms of k. (2)

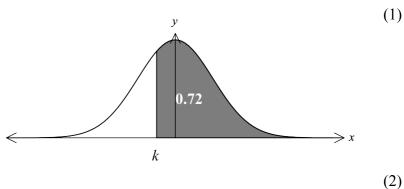
| 5 | | "Fun Size" Ganymede™ bars are sold in bags of 13. There is a 1% chance that any individual Fun Size bar contains a whole rat foot or a rat tooth. | |
|---|----|--|-----|
| | a) | What is the probability that a bag of Fun Size Ganymede TM bars contains at least one bar with a whole rat foot or rat tooth? | (1) |
| | b) | The bags of Fun Size bars are packed together into boxes of 15 for delivery to supermarkets. What is the probability that a box chosen at random contains no more than three bags that contain at least one bar with a whole rat foot or rat tooth? | (2) |
| | c) | Rob, a Ganymede [™] bar addict, regularly eats a whole bag of Fun Size bars as a snack. Given that Rob has already eaten 8 bars that have not had any rat body parts in them, what is the probability that the next bar he eats contains a whole rat foot or rat tooth? | (1) |
| 6 | | A random binomial variable V has the distribution $V \sim Bin(4, p)$. | |
| | a) | What is $P(V = 1)$? | (1) |
| | b) | What is $P(V > 2)$? | (2) |
| 7 | | A random binomial variable G has the distribution $H \sim Bin(n, 0.8)$ | |
| | | Determine the smallest value of <i>n</i> such that the chance of there being more than 4 successes is at least 95%. | (2) |

| 8 | a) | Discuss the following methods of sample selection. In particular, consider the method of selection in terms of any possible introduced bias. A local council is considering increasing the width of a road by removing a footpath and decreasing the size of the verge. They use a systematic sampling technique to get | (2) |
|---|----|---|-----|
| | | feedback from local residents on those streets, selecting every fourth house. | |
| | | | |
| | L. | | (2) |
| | b) | A fast food restaurant that offers dine-in, take-away and drive-thru options has posters in its dining area inviting customers to rate their satisfaction with their meal. They offer a range of social media formats as well as a paper form that customers can fill out. | (2) |
| | | | |
| | | | |
| | c) | A small island, known to be a popular penguin breeding spot, has a perimeter of approximately 4km. To try and determine the number of penguins on the island, a group of volunteers walk along 1km of the coast, carefully counting any penguins they can see. They then multiply this result by 4 to determine the total penguin population. | (2) |
| | | | |

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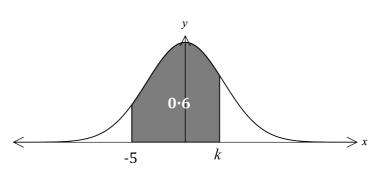
Determine the value of *k* in the normal distributions below.

a) $X \sim N(14, 3^2)$



b)





(4)

A normally distributed random variable R has distribution $R \sim N(12, 2.5^2)$. Determine

a)
$$P(R < 8)$$
 (1)

b)
$$P(10 < R < 14)$$
 (1)

c)
$$P(R > 10 | R < 14)$$
 (1)

d) Find
$$k$$
 if $P(R > k) = 0.15$ (1)

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H is a normally distributed random variable, with 20% of values greater than 70 and 40% of values less than 50. Determine the mean and standard deviation of H, to two decimal places.

- In a game of chance, two coins are tossed at the same time and the player wins if there is at least one Head. After the game has been played 40 times, 21 wins have been recorded.
 - a) Determine the proportion of wins \hat{p} in the sample of 40 games. (1)
 - b) Determine the value of p and use this to find the standard deviation of the sample proportions. (2)
 - C) Calculate the number of standard deviations between p and \hat{p} . Use this information to comment on the results in the sample of 40 games. (3)

out to determine the number of people who have cracked screens on their mobile phones. The results of these surveys are recorded in the table to the right.

| Sample | Number of | Proportion with | | |
|--------|-----------------|-----------------|--|--|
| | people surveyed | cracked screens | | |
| 1 | 20 | 0.55 | | |
| 2 | 14 | 0.5 | | |
| 3 | 16 | 0.625 | | |
| 4 | 10 | 0.6 | | |
| 5 | 25 | 0.56 | | |
| 6 | 36 | 0.75 | | |

- a) Use the complete set of results to determine your best estimate for p, the population proportion. (1)
- b) Use your value of p to determine the standard deviation of samples involving 36 people. (1)
- C) Calculate the number of standard deviations between p and \hat{p} for the sample number 6. (2) Use this information to comment on the results of sample 6.