

Year 12 Specialist TEST 3 2018

TIME: 45 minutes working Classpads allowed! 39 Marks 7 Questions

Name:	()	lan	Cono	Keu	
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Teacher:

Note: All part questions worth more than 2 marks require working to obtain full marks.

Q1 (2 & 2 = 4 marks)

$$x = 3 - 5\lambda$$

Consider a line with parametric equations

$$y = -7 + 2\lambda$$

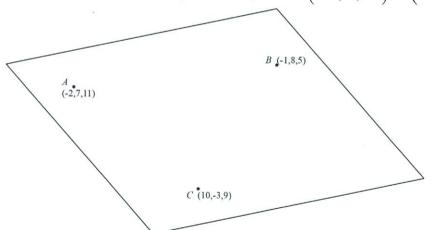
i) Determine a vector equation

L= 
$$\begin{pmatrix} 3 \\ -7 \end{pmatrix} + \lambda \begin{pmatrix} -5 \\ 2 \end{pmatrix}$$
 voltain vector egn

Determine a cartesian equation.

Q2 (3 & 2 = 5 marks)

Consider a plane containing the three points A  $\left(-2,7,11\right)$  , B  $\left(-1,8,5\right)$  & C  $\left(10,-3,9\right)$  .



Determine the vector equation of the plane.

$$\overrightarrow{AB} = \begin{pmatrix} 1 \\ -6 \end{pmatrix}$$

$$\overrightarrow{AC} = \begin{pmatrix} 12 \\ -10 \\ -2 \end{pmatrix}$$

$$\sqrt{31} = \begin{pmatrix} -2 \\ 7 \\ 11 \end{pmatrix}, \begin{pmatrix} 31 \\ 35 \\ 11 \end{pmatrix} = 304$$

$$\overrightarrow{AB} \times \overrightarrow{AC} = \begin{pmatrix} -62 \\ -70 \\ -22 \end{pmatrix} = -2 \begin{pmatrix} 31 \\ 35 \\ 11 \end{pmatrix}$$

I obtain two vectors in plane

Vures cross product to find normal

I finds vector ego of plane

Continued-

ii) Determine the cartesian equation of the plane. (simplified)

$$31x + 35y + 11z = 304$$

I was dot product with ( ) V simplified co-efficients

Q3 (4 marks)

Determine the distance of point P 
$$\left(-5,1,3\right)$$
 from the line  $\underline{r} = \begin{pmatrix} -1 \\ 7 \\ 2 \end{pmatrix} + \lambda \begin{pmatrix} 5 \\ -8 \\ 1 \end{pmatrix}$ 

$$d = \overrightarrow{PA} + \lambda \cdot \frac{1}{4}$$

$$= \left(-\frac{1}{72}\right) - \left(-\frac{5}{3}\right) + \lambda \left(\frac{5}{9}\right)$$

$$= \left(\frac{1}{72}\right) - \left(-\frac{1}{3}\right) + \lambda \left(\frac{5}{9}\right)$$

$$= \left(\frac{4+5\lambda}{6-8\lambda}\right)$$

$$= \left(\frac{4+5\lambda}{1+\lambda}\right)$$

$$\frac{d}{d} \cdot \left(\frac{5}{8}\right) = 0$$

$$\begin{pmatrix} 4+51 \\ 6-81 \\ 1+1 \end{pmatrix} \cdot \begin{pmatrix} 5 \\ -8 \\ 1 \end{pmatrix} = 5(4+51) - 8(6-81) - 1+1 = 0$$

$$\lambda = \frac{29}{90}$$

$$\left|\frac{1}{4}\right| = \sqrt{39290}$$
 or  $= 6.607$ 
using classpace.

OR I determines 1-08 Volatain appression for magnitude variantes distance, using calculus

I sets up a displacement vector of wes dot product equated to zero

I solver for parameter 1 determines d

## Q4 (4 marks)

Consider two particles A and B whose position at t=0 is recorded as below moving with constant velocities  $v_A \& v_B$ . Determine the distance of closest approach and the time that this occurs.

velocities 
$$v_A$$
 &  $v_B$ . Determine the distance of closest approach and the time that this occurs.

$$r_A = \begin{pmatrix} 2 \\ -5 \\ 9 \end{pmatrix} \qquad v_A = \begin{pmatrix} 11 \\ -5 \\ 7 \end{pmatrix}$$

$$r_B = \begin{pmatrix} 1 \\ -1 \\ 9 \end{pmatrix} \qquad v_B = \begin{pmatrix} 12 \\ -10 \\ 2 \end{pmatrix} = \begin{pmatrix} 5 \\ -5 \\ 9 \end{pmatrix} - \begin{pmatrix} -1 \\ -1 \\ 9 \end{pmatrix} + \begin{pmatrix} -1 \\ 5 \\ 5 \end{pmatrix}$$

$$d = \begin{pmatrix} 1 \\ -1 \\ 5 \\ 5 \end{pmatrix} + \begin{pmatrix} -1 \\ 5 \\ 5 \end{pmatrix} = \begin{pmatrix} -2 \\ -5 \\ 9 \\ 7 \end{pmatrix} - \begin{pmatrix} -1 \\ -1 \\ 9 \end{pmatrix} + \begin{pmatrix} -1 \\ 5 \\ 5 \end{pmatrix}$$

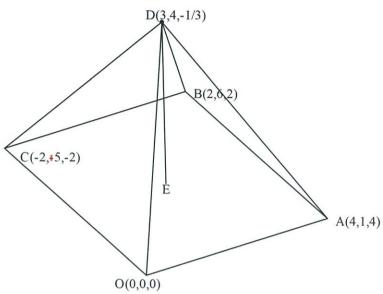
$$d = \begin{pmatrix} 1 \\ -4 \\ 5 \end{pmatrix} + \begin{pmatrix} -1 \\ 5 \\ 5 \end{pmatrix} = \begin{pmatrix} -1 \\ -4 \\ 5 \end{pmatrix} + \begin{pmatrix} -1 \\ 5 \\ 5 \end{pmatrix} = \begin{pmatrix} -1 \\ -4 \\ 5 \end{pmatrix} + \begin{pmatrix} -1 \\ 5 \\ 5 \end{pmatrix}$$

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minimises distance expression a solver for time

obtains distance (minimum)

OABCD is a pyramid. The height of the pyramid is the length of DE, where E is the point on the base OABC such that DE is perpendicular to the base.



i) Show that the base OABC is a rhombus. 
$$\overrightarrow{OZ} = \overrightarrow{AB}$$

$$LHS = \begin{pmatrix} -2 \\ +5 \\ -2 \end{pmatrix} - \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$$

$$RHS = \begin{pmatrix} 2 \\ 6 \\ 2 \end{pmatrix} - \begin{pmatrix} 4 \\ 1 \\ 4 \end{pmatrix} = \begin{pmatrix} -2 \\ 5 \\ -2 \end{pmatrix}$$

The unit vector  $p_{\tilde{L}}+q_{\tilde{L}}+r_{\tilde{k}}$  is perpendicular to both  $\overrightarrow{OA}$  and  $\overrightarrow{OC}$  .

ii) Show that q=0 and determine the exact values of p & r.

Show that 
$$q=0$$
 and determine the exact values of  $p\&r$ .

(a)  $\begin{pmatrix} -2 \\ 5 \\ -2 \end{pmatrix} = 0$ 

(b)  $\begin{pmatrix} -2 \\ 5 \\ -2 \end{pmatrix} = 0$ 

(c)  $\begin{pmatrix} 4 \\ 2 \\ 5 \end{pmatrix} = 0$ 

(d)  $\begin{pmatrix} 4 \\ 4 \\ 5 \end{pmatrix} = 0$ 

(e)  $\begin{pmatrix} 4 \\ 4 \\ 5 \end{pmatrix} = 0$ 

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$$\left| \begin{pmatrix} \rho \\ -\rho \end{pmatrix} \right| = 1$$

$$\rho^{2} + \rho^{2} = 1$$
 $2\rho^{2} = 1$ 
 $\rho = \pm \sqrt{2}$ 

iii) height = 
$$\left| \overrightarrow{OD} \cdot \begin{pmatrix} \overrightarrow{t_2} \\ 0 \\ -1 \\ v_2 \end{pmatrix} \right|$$
were det

Vexpresser

height = 
$$|\overrightarrow{OD} \cdot (\frac{12}{0})|$$
 =  $|(\frac{3}{4}) \cdot (\frac{1}{12})|$  =  $\frac{3}{1/2} + \frac{1}{3\sqrt{2}}$   
det  $|(\frac{3}{12})|$  =  $|(\frac{3}{12})|$ 

Q6 (5 marks)

Consider a sphere of centre (-3,2,7) and radius of a units , where a is a constant.

The line 
$$r = \begin{pmatrix} 2 \\ 1 \\ -8 \end{pmatrix} + \lambda \begin{pmatrix} 4 \\ 1 \\ -3 \end{pmatrix}$$
 is a tangent to the above sphere.

Determine the possible value(s) of  $\alpha$ 

Solution to value (s) of 
$$a$$

$$\begin{vmatrix}
x - \begin{pmatrix} -3 \\ 2 \\ 7
\end{vmatrix} = a$$

$$\begin{vmatrix}
x + 4 \\ 4 - 3\lambda
\end{vmatrix} = a$$

$$\begin{vmatrix}
x + 4 \\ 4 - 3\lambda
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Q7(2, 3 & 3 = 8 marks)

Consider the function  $f(x) = ax^4 + bx^3 + cx^2 + dx$  where a, b, c & d are constants.

The graph has a stationary point ( f'=0 ) at  $\left(1,1\right)$  and passes through the point  $\left(-1,4\right)$  .

i) Write down three linear equations satisfied by  $a,b,c\ \&\ d$  .

$$1 = a + b + c + d - - 0$$

$$4 = a - b + c - d - 0$$

$$f'(x) = \frac{1}{4}x^{2} + \frac{3}{5}b^{2} + \frac{2}{5}cx + d$$

$$0 = \frac{1}{4}a + \frac{3}{5}b + \frac{2}{5}c + \frac{1}{5}c + d - 0$$

ii) Express a, b & c in terms of d.

iii) Determine the value of d for which the graph has a stationary point where x=4

$$f'(z) = 4ax^{2} + 3bx^{2} + 2cx + d$$
 $0 = 256a + 48b + 8c + d$ 
 $0 = 256(-\frac{1}{4}+d) + 48(-\frac{3}{2}-d) + 8(\frac{11}{4}-d) + d$ 

Solve on classfed

 $d = \frac{38}{67}$  or  $a = 0.567$ 

Solve of description

 $d = \frac{38}{67}$  or  $a = 0.567$ 

Solves for  $d = 0.567$ 

Solves for  $d = 0.567$