

## Mathematical Induction MCQs - Class 11 Mathematics

*Prepared for Entry Test Preparation*

### Multiple Choice Questions

1. What is the sum of the first  $n$  odd numbers  $1 + 3 + 5 + \cdots + (2n - 1)$ ?
  - (a)  $n^2$
  - (b)  $n(n + 1)$
  - (c)  $\frac{n(2n-1)}{2}$
  - (d)  $2n - 1$
2. The sum  $1 + 2 + 4 + \cdots + 2^{n-1}$  equals:
  - (a)  $2^n - 1$
  - (b)  $2^{n+1} - 1$
  - (c)  $2^n$
  - (d)  $2^{n-1}$
3. For what positive integers  $n$  is  $n^2 + n$  divisible by 2?
  - (a) All  $n$
  - (b) Odd  $n$
  - (c) Even  $n$
  - (d)  $n \geq 2$
4. Prove  $1 + 4 + 7 + \cdots + (3n - 2) = \frac{n(3n-1)}{2}$ . What is the base case value for  $n = 1$ ?
  - (a) 1
  - (b) 2
  - (c) 3
  - (d) 4
5. The sum  $2 + 4 + 6 + \cdots + 2n$  equals:
  - (a)  $n(n + 1)$
  - (b)  $2n^2$
  - (c)  $n(2n + 1)$
  - (d)  $\frac{n(n+1)}{2}$
6. For  $n \geq 3$ , which inequality holds?
  - (a)  $n^2 > n + 3$

(b)  $n^2 < n + 3$

(c)  $n^2 = n + 3$

(d)  $n^2 \leq n + 3$

7. The sum  $1 \times 2 + 2 \times 3 + \cdots + n(n + 1)$  equals:

(a)  $\frac{n(n+1)(n+2)}{3}$

(b)  $\frac{n(n+1)}{2}$

(c)  $\frac{n(n+1)(2n+1)}{6}$

(d)  $n(n + 1)$

8. Prove  $5^n - 1$  is divisible by 4. What is the value for  $n = 1$ ?

(a) 2

(b) 4

(c) 5

(d) 8

9. The sum  $\frac{1}{1 \times 2} + \frac{1}{2 \times 3} + \cdots + \frac{1}{n(n+1)}$  equals:

(a)  $\frac{n}{n+1}$

(b)  $\frac{n+1}{n}$

(c)  $\frac{1}{n+1}$

(d)  $\frac{n}{2n+1}$

10. For  $n \geq 4$ , which holds true?

(a)  $n! > n^2$

(b)  $n! < n^2$

(c)  $n! = n^2$

(d)  $n! \leq n^2$

11. The sum  $1^2 + 3^2 + 5^2 + \cdots + (2n - 1)^2$  equals:

(a)  $\frac{n(4n^2-1)}{3}$

(b)  $n^2(2n^2 - 1)$

(c)  $\frac{n(n+1)(2n+1)}{6}$

(d)  $\frac{n(2n-1)}{2}$

12. Prove  $n^3 - n$  is divisible by 6. What is the value for  $n = 1$ ?

(a) 0

(b) 1

(c) 2

(d) 6

**13.** The sum  $1^3 + 3^3 + 5^3 + \cdots + (2n - 1)^3$  equals:

(a)  $n^2(2n^2 - 1)$

(b)  $\frac{n(4n^2 - 1)}{3}$

(c)  $n(2n - 1)^2$

(d)  $\frac{n(n+1)(2n+1)}{6}$

**14.** For an arithmetic progression, the  $n$ -th term is:

(a)  $a_n = a_1 + (n - 1)d$

(b)  $a_n = a_1 r^{n-1}$

(c)  $a_n = a_1 + nd$

(d)  $a_n = a_1 + (n - 1)d^2$

**15.** The sum  $\frac{1}{3} + \frac{1}{3^2} + \cdots + \frac{1}{3^n}$  equals:

(a)  $\frac{1}{2} \left[ 1 - \frac{1}{3^n} \right]$

(b)  $\frac{1}{3^n}$

(c)  $\frac{1}{2}$

(d)  $1 - \frac{1}{3^n}$

**16.** Prove  $(x + 1)$  is a factor of  $x^{2n} - 1$ . For  $n = 1$ , the expression is:

(a)  $x^2 - 1$

(b)  $x^2 + 1$

(c)  $x - 1$

(d)  $x + 1$

**17.** For  $n > 6$ , which holds?

(a)  $3^n < n!$

(b)  $3^n > n!$

(c)  $3^n = n!$

(d)  $3^n \leq n!$

**18.** The sum  $1 \cdot 1! + 2 \cdot 2! + \cdots + n \cdot n!$  equals:

(a)  $(n + 1)! - 1$

(b)  $n!$

(c)  $(n + 1)!$

(d)  $n(n + 1)!$

**19.** Prove  $\ln x^n = n \ln x$  for  $n \geq 0$ . What is the base case for  $n = 0$ ?

- (a) 0
- (b) 1
- (c)  $\ln x$
- (d)  $x$

20. The sum  $1^2 - 2^2 + 3^2 - 4^2 + \dots + (-1)^{n-1}n^2$  equals:

- (a)  $\frac{(-1)^{n-1}n(n+1)}{2}$
- (b)  $\frac{n(n+1)}{2}$
- (c)  $\frac{n(2n+1)}{6}$
- (d)  $(-1)^n n^2$

## Solutions and Explanations

1. **Answer: a**  $n^2$  *Explanation:* From Q.2, the sum of the first  $n$  odd numbers is  $1 + 3 + \dots + (2n - 1) = n^2$ .
2. **Answer: a**  $2^n - 1$  *Explanation:* From Q.4, the geometric series sum is  $1 + 2 + \dots + 2^{n-1} = 2^n - 1$ .
3. **Answer: a** All  $n$  *Explanation:* From Q.21(i),  $n^2 + n = n(n+1)$ , which is divisible by 2 for all positive integers  $n$ .
4. **Answer: a** 1 *Explanation:* From Q.3, base case:  $n = 1$ ,  $3(1) - 2 = 1$ , and  $\frac{1(3 \cdot 1 - 1)}{2} = \frac{2}{2} = 1$ .
5. **Answer: a**  $n(n+1)$  *Explanation:* From Q.6, the sum of even numbers is  $2 + 4 + \dots + 2n = n(n+1)$ .
6. **Answer: a**  $n^2 > n + 3$  *Explanation:* From Q.33,  $n^2 > n + 3$  holds for  $n \geq 3$ .
7. **Answer: a**  $\frac{n(n+1)(n+2)}{3}$  *Explanation:* From Q.9, the sum is  $1 \times 2 + 2 \times 3 + \dots + n(n+1) = \frac{n(n+1)(n+2)}{3}$ .
8. **Answer: b** 4 *Explanation:* From Q.21(iii), base case:  $n = 1$ ,  $5^1 - 1 = 4$ , which is divisible by 4.
9. **Answer: a**  $\frac{n}{n+1}$  *Explanation:* From Q.11, the sum is  $\frac{1}{1 \times 2} + \dots + \frac{1}{n(n+1)} = \frac{n}{n+1}$ .
10. **Answer: a**  $n! > n^2$  *Explanation:* From Q.36,  $n! > n^2$  for  $n \geq 4$ .
11. **Answer: a**  $\frac{n(4n^2-1)}{3}$  *Explanation:* From Q.19, the sum of squares of odd numbers is  $1^2 + 3^2 + \dots + (2n-1)^2 = \frac{n(4n^2-1)}{3}$ .
12. **Answer: a** 0 *Explanation:* From Q.21(v), base case:  $n = 1$ ,  $1^3 - 1 = 0$ , which is divisible by 6.
13. **Answer: a**  $n^2(2n^2 - 1)$  *Explanation:* From Q.24, the sum of cubes of odd numbers is  $1^3 + 3^3 + \dots + (2n-1)^3 = n^2(2n^2 - 1)$ .

- 14. Answer: a**  $a_n = a_1 + (n - 1)d$  *Explanation:* From Q.17, the  $n$ -th term of an arithmetic progression is  $a_n = a_1 + (n - 1)d$ .
- 15. Answer: a**  $\frac{1}{2} \left[ 1 - \frac{1}{3^n} \right]$  *Explanation:* From Q.22, the geometric series sum is  $\frac{1}{3} + \frac{1}{3^2} + \dots + \frac{1}{3^n} = \frac{1}{2} \left[ 1 - \frac{1}{3^n} \right]$ .
- 16. Answer: a**  $x^2 - 1$  *Explanation:* From Q.25, base case:  $n = 1$ ,  $x^{2 \cdot 1} - 1 = x^2 - 1$ , which has  $x + 1$  as a factor.
- 17. Answer: a**  $3^n < n!$  *Explanation:* From Q.35,  $3^n < n!$  for  $n > 6$ .
- 18. Answer: a**  $(n + 1)! - 1$  *Explanation:* From Q.16, the sum is  $1 \cdot 1! + 2 \cdot 2! + \dots + n \cdot n! = (n + 1)! - 1$ .
- 19. Answer: a**  $0$  *Explanation:* From Q.31, base case:  $n = 0$ ,  $\ln x^0 = \ln 1 = 0 = 0 \cdot \ln x$ .
- 20. Answer: a**  $\frac{(-1)^{n-1}n(n+1)}{2}$  *Explanation:* From Q.23, the alternating sum is  $1^2 - 2^2 + 3^2 - \dots + (-1)^{n-1}n^2 = \frac{(-1)^{n-1}n(n+1)}{2}$ .