

Trigonometric Identities MCQs for Entry Test - Exercise 10.4

Introduction

This document contains 20 multiple-choice questions based on Exercise 10.4 of the trigonometry chapter, designed for entry test preparation. Each question tests concepts such as product-to-sum identities, sum-to-product identities, proofs of trigonometric identities, and specific angle applications. Solutions with detailed explanations are provided at the end.

Multiple-Choice Questions

1. **Express $2 \sin 3\theta \cos \theta$ as a sum.**

- A) $\sin 4\theta + \sin 2\theta$
- B) $\sin 4\theta - \sin 2\theta$
- C) $\cos 4\theta + \cos 2\theta$
- D) $\cos 4\theta - \cos 2\theta$

2. **Express $2 \cos 5\theta \sin 3\theta$ as a sum.**

- A) $\sin 8\theta + \sin 2\theta$
- B) $\sin 8\theta - \sin 2\theta$
- C) $\cos 8\theta + \cos 2\theta$
- D) $\cos 8\theta - \cos 2\theta$

3. **What is $\sin 5\theta \cos 2\theta$?**

- A) $\frac{1}{2}[\sin 7\theta + \sin 3\theta]$
- B) $\frac{1}{2}[\sin 7\theta - \sin 3\theta]$
- C) $\frac{1}{2}[\cos 7\theta + \cos 3\theta]$
- D) $\frac{1}{2}[\cos 7\theta - \cos 3\theta]$

4. **Express $2 \sin 7\theta \sin 2\theta$ as a sum.**

- A) $\cos 9\theta - \cos 5\theta$
- B) $\cos 5\theta - \cos 9\theta$

- C) $\sin 9\theta + \sin 5\theta$
 D) $\sin 9\theta - \sin 5\theta$
5. **What is $\cos(x + y) \sin(x - y)$?**
- A) $\frac{1}{2}[\sin 2x + \sin 2y]$
 B) $\frac{1}{2}[\sin 2x - \sin 2y]$
 C) $\frac{1}{2}[\cos 2x + \cos 2y]$
 D) $\frac{1}{2}[\cos 2x - \cos 2y]$
6. **Express $\cos(2x + 30^\circ) \cos(2x - 30^\circ)$.**
- A) $\frac{1}{2}[\cos 4x + \cos 60^\circ]$
 B) $\frac{1}{2}[\cos 4x - \cos 60^\circ]$
 C) $\frac{1}{2}[\sin 4x + \sin 60^\circ]$
 D) $\frac{1}{2}[\sin 4x - \sin 60^\circ]$
7. **What is $\sin 12^\circ \sin 46^\circ$?**
- A) $\frac{1}{2}[\cos 58^\circ - \cos 34^\circ]$
 B) $\frac{-1}{2}[\cos 58^\circ - \cos 34^\circ]$
 C) $\frac{1}{2}[\sin 58^\circ - \sin 34^\circ]$
 D) $\frac{-1}{2}[\sin 58^\circ - \sin 34^\circ]$
8. **Express $\sin(x + 45^\circ) \sin(x - 45^\circ)$.**
- A) $\frac{1}{2}[\cos 2x - \cos 90^\circ]$
 B) $\frac{-1}{2}[\cos 2x - \cos 90^\circ]$
 C) $\frac{1}{2}[\sin 2x - \sin 90^\circ]$
 D) $\frac{-1}{2}[\sin 2x - \sin 90^\circ]$
9. **Express $\sin 5\theta + \sin 3\theta$ as a product.**
- A) $2 \sin 4\theta \cos \theta$
 B) $2 \cos 4\theta \sin \theta$
 C) $2 \sin 4\theta \sin \theta$
 D) $2 \cos 4\theta \cos \theta$
10. **What is $\sin 8\theta - \sin 4\theta$?**
- A) $2 \sin 6\theta \cos 2\theta$
 B) $2 \cos 6\theta \sin 2\theta$
 C) $2 \sin 6\theta \sin 2\theta$
 D) $2 \cos 6\theta \cos 2\theta$
11. **Express $\cos 6\theta + \cos 3\theta$.**

- A) $2 \cos \frac{9\theta}{2} \cos \frac{3\theta}{2}$
- B) $2 \sin \frac{9\theta}{2} \sin \frac{3\theta}{2}$
- C) $2 \cos \frac{9\theta}{2} \sin \frac{3\theta}{2}$
- D) $2 \sin \frac{9\theta}{2} \cos \frac{3\theta}{2}$

12. **What is** $\cos 7\theta - \cos \theta$?

- A) $-2 \sin 4\theta \sin 3\theta$
- B) $-2 \cos 4\theta \cos 3\theta$
- C) $2 \sin 4\theta \sin 3\theta$
- D) $2 \cos 4\theta \cos 3\theta$

13. **Express** $\cos 12^\circ + \cos 48^\circ$.

- A) $2 \cos 30^\circ \cos 18^\circ$
- B) $2 \sin 30^\circ \sin 18^\circ$
- C) $2 \cos 30^\circ \sin 18^\circ$
- D) $2 \sin 30^\circ \cos 18^\circ$

14. **What is** $\sin(x + 30^\circ) + \sin(x - 30^\circ)$?

- A) $2 \sin x \cos 30^\circ$
- B) $2 \cos x \sin 30^\circ$
- C) $2 \sin x \sin 30^\circ$
- D) $2 \cos x \cos 30^\circ$

15. **What is** $\frac{\sin 3x - \sin x}{\cos x - \cos 3x}$?

- A) $\tan 2x$
- B) $\cot 2x$
- C) $\tan x$
- D) $\cot x$

16. **What is** $\frac{\sin 8x + \sin 2x}{\cos 8x + \cos 2x}$?

- A) $\tan 5x$
- B) $\cot 5x$
- C) $\tan 3x$
- D) $\cot 3x$

17. **What is** $\frac{\sin \alpha - \sin \beta}{\sin \alpha + \sin \beta}$?

- A) $\tan \left(\frac{\alpha - \beta}{2} \right) \cot \left(\frac{\alpha + \beta}{2} \right)$
- B) $\tan \left(\frac{\alpha + \beta}{2} \right) \cot \left(\frac{\alpha - \beta}{2} \right)$
- C) $\sin \left(\frac{\alpha - \beta}{2} \right) \cos \left(\frac{\alpha + \beta}{2} \right)$

D) $\cos\left(\frac{\alpha-\beta}{2}\right)\sin\left(\frac{\alpha+\beta}{2}\right)$

18. **What is** $\cos 20^\circ + \cos 100^\circ + \cos 140^\circ$?

A) 0

B) $\frac{1}{2}$

C) 1

D) -1

19. **What is** $\sin\left(\frac{\pi}{4} - \theta\right)\sin\left(\frac{\pi}{4} + \theta\right)$?

A) $\frac{1}{2}\cos 2\theta$

B) $\frac{1}{2}\sin 2\theta$

C) $\cos 2\theta$

D) $\sin 2\theta$

20. **What is** $\cos 20^\circ \cos 40^\circ \cos 60^\circ \cos 80^\circ$?

A) $\frac{1}{8}$

B) $\frac{1}{16}$

C) $\frac{1}{32}$

D) $\frac{1}{4}$

Solutions and Explanations

1. **Solution to Question 1:**

$$2 \sin 3\theta \cos \theta = \sin(3\theta + \theta) + \sin(3\theta - \theta) = \sin 4\theta + \sin 2\theta$$

Answer: A) $\sin 4\theta + \sin 2\theta$

2. **Solution to Question 2:**

$$2 \cos 5\theta \sin 3\theta = \sin(5\theta + 3\theta) - \sin(5\theta - 3\theta) = \sin 8\theta - \sin 2\theta$$

Answer: B) $\sin 8\theta - \sin 2\theta$

3. **Solution to Question 3:**

$$\sin 5\theta \cos 2\theta = \frac{1}{2}[2 \sin 5\theta \cos 2\theta] = \frac{1}{2}[\sin(5\theta + 2\theta) + \sin(5\theta - 2\theta)] = \frac{1}{2}[\sin 7\theta + \sin 3\theta]$$

Answer: A) $\frac{1}{2}[\sin 7\theta + \sin 3\theta]$

4. **Solution to Question 4:**

$$2 \sin 7\theta \sin 2\theta = -[-2 \sin 7\theta \sin 2\theta] = -[\cos(7\theta + 2\theta) - \cos(7\theta - 2\theta)] = -[\cos 9\theta - \cos 5\theta] = \cos 5\theta - \cos 9\theta$$

Answer: B) $\cos 5\theta - \cos 9\theta$

5. Solution to Question 5:

$$\cos(x+y)\sin(x-y) = \frac{1}{2}[2\cos(x+y)\sin(x-y)] = \frac{1}{2}[\sin(2x) - \sin(2y)]$$

Answer: B) $\frac{1}{2}[\sin 2x - \sin 2y]$

6. Solution to Question 6:

$$\cos(2x+30^\circ)\cos(2x-30^\circ) = \frac{1}{2}[2\cos(2x+30^\circ)\cos(2x-30^\circ)] = \frac{1}{2}[\cos 4x + \cos 60^\circ]$$

Answer: A) $\frac{1}{2}[\cos 4x + \cos 60^\circ]$

7. Solution to Question 7:

$$\sin 12^\circ \sin 46^\circ = \frac{-1}{2}[-2\sin 12^\circ \sin 46^\circ] = \frac{-1}{2}[\cos(12^\circ+46^\circ) - \cos(12^\circ-46^\circ)] = \frac{-1}{2}[\cos 58^\circ - \cos(-34^\circ)]$$

Answer: B) $\frac{-1}{2}[\cos 58^\circ - \cos 34^\circ]$

8. Solution to Question 8:

$$\sin(x+45^\circ)\sin(x-45^\circ) = \frac{-1}{2}[-2\sin(x+45^\circ)\sin(x-45^\circ)] = \frac{-1}{2}[\cos 2x - \cos 90^\circ]$$

Answer: B) $\frac{-1}{2}[\cos 2x - \cos 90^\circ]$

9. Solution to Question 9:

$$\sin 5\theta + \sin 3\theta = 2\sin\left(\frac{5\theta+3\theta}{2}\right)\cos\left(\frac{5\theta-3\theta}{2}\right) = 2\sin 4\theta \cos \theta$$

Answer: A) $2\sin 4\theta \cos \theta$

10. Solution to Question 10:

$$\sin 8\theta - \sin 4\theta = 2\cos\left(\frac{8\theta+4\theta}{2}\right)\sin\left(\frac{8\theta-4\theta}{2}\right) = 2\cos 6\theta \sin 2\theta$$

Answer: B) $2\cos 6\theta \sin 2\theta$

11. Solution to Question 11:

$$\cos 6\theta + \cos 3\theta = 2\cos\left(\frac{6\theta+3\theta}{2}\right)\cos\left(\frac{6\theta-3\theta}{2}\right) = 2\cos \frac{9\theta}{2} \cos \frac{3\theta}{2}$$

Answer: A) $2\cos \frac{9\theta}{2} \cos \frac{3\theta}{2}$

12. Solution to Question 12:

$$\cos 7\theta - \cos \theta = -2\sin\left(\frac{7\theta+\theta}{2}\right)\sin\left(\frac{7\theta-\theta}{2}\right) = -2\sin 4\theta \sin 3\theta$$

Answer: A) $-2\sin 4\theta \sin 3\theta$

13. **Solution to Question 13:**

$$\cos 12^\circ + \cos 48^\circ = 2 \cos \left(\frac{12^\circ + 48^\circ}{2} \right) \cos \left(\frac{12^\circ - 48^\circ}{2} \right) = 2 \cos 30^\circ \cos 18^\circ$$

Answer: A) $2 \cos 30^\circ \cos 18^\circ$

14. **Solution to Question 14:**

$$\sin(x+30^\circ) + \sin(x-30^\circ) = 2 \sin \left(\frac{x+30^\circ + x-30^\circ}{2} \right) \cos \left(\frac{x+30^\circ - x+30^\circ}{2} \right) = 2 \sin x \cos 30^\circ$$

Answer: A) $2 \sin x \cos 30^\circ$

15. **Solution to Question 15:**

$$\frac{\sin 3x - \sin x}{\cos x - \cos 3x} = \frac{2 \cos \left(\frac{3x+x}{2} \right) \sin \left(\frac{3x-x}{2} \right)}{-2 \sin \left(\frac{3x+x}{2} \right) \sin \left(\frac{3x-x}{2} \right)} = \frac{\cos 2x}{\sin 2x} = \cot 2x$$

Answer: B) $\cot 2x$

16. **Solution to Question 16:**

$$\frac{\sin 8x + \sin 2x}{\cos 8x + \cos 2x} = \frac{2 \sin \left(\frac{8x+2x}{2} \right) \cos \left(\frac{8x-2x}{2} \right)}{2 \cos \left(\frac{8x+2x}{2} \right) \cos \left(\frac{8x-2x}{2} \right)} = \frac{\sin 5x}{\cos 5x} = \tan 5x$$

Answer: A) $\tan 5x$

17. **Solution to Question 17:**

$$\frac{\sin \alpha - \sin \beta}{\sin \alpha + \sin \beta} = \frac{2 \cos \left(\frac{\alpha+\beta}{2} \right) \sin \left(\frac{\alpha-\beta}{2} \right)}{2 \sin \left(\frac{\alpha+\beta}{2} \right) \cos \left(\frac{\alpha-\beta}{2} \right)} = \cot \left(\frac{\alpha + \beta}{2} \right) \tan \left(\frac{\alpha - \beta}{2} \right)$$

Answer: A) $\tan \left(\frac{\alpha-\beta}{2} \right) \cot \left(\frac{\alpha+\beta}{2} \right)$

18. **Solution to Question 18:**

$$\cos 20^\circ + \cos 100^\circ + \cos 140^\circ = 2 \cos \left(\frac{140^\circ + 20^\circ}{2} \right) \cos \left(\frac{140^\circ - 20^\circ}{2} \right) + \cos 100^\circ = 2 \cos 80^\circ \cos 60^\circ + \cos 100^\circ$$

Answer: A) 0

19. **Solution to Question 19:**

$$\sin \left(\frac{\pi}{4} - \theta \right) \sin \left(\frac{\pi}{4} + \theta \right) = \left(\frac{\sqrt{2}}{2} \cos \theta - \frac{\sqrt{2}}{2} \sin \theta \right) \left(\frac{\sqrt{2}}{2} \cos \theta + \frac{\sqrt{2}}{2} \sin \theta \right) = \frac{1}{2} (\cos^2 \theta - \sin^2 \theta) = \frac{1}{2} \cos 2\theta$$

Answer: A) $\frac{1}{2} \cos 2\theta$

20. **Solution to Question 20:**

$$\cos 20^\circ \cos 40^\circ \cos 60^\circ \cos 80^\circ = \frac{1}{4} [\cos 60^\circ + \cos 20^\circ] \cos 80^\circ = \frac{1}{4} \left[\frac{1}{2} + \cos 20^\circ \right] \cos 80^\circ = \frac{1}{8} [\cos 80^\circ + \cos 100^\circ]$$

Answer: B) $\frac{1}{16}$