

National University of Computer and Emerging Sciences, Lahore Campus



Course: Probability & Statistics
 Program: BS Computer Science
 Duration: 1 hour
 Paper Date: 3/11/17
 Section: All
 Exam: Mid-2

Course Code: MT206
 Semester: Fall-17
 Total Marks: 30
 Weight: 15%
 Page(s): 02
 Roll No:

Instruction/Notes: Exchange of calculators and stationary is strictly prohibited. Attempt parts of same question together. If you think some information is missing or wrong make assumptions and clearly state them.

Question 1: (4 marks) If x is a continuous random variable with the density

$$f(x) = \begin{cases} x/8, & 0 \leq x \leq 4 \\ 0, & \text{otherwise} \end{cases}$$

- i) Find the distribution function $F(x)$
- ii) Find $P(2 < x < 3)$ using the distribution function

$$\sum_{i=1}^n f(x)$$

Question 2: (10 marks) Let X and Y be two discrete random variables with the following joint probability function

x \ y	1	2	3
1	0.03	0.04	0.03
2	0.15	0.20	0.15
3	0.12	0.16	0.12

Find the following

- i) $E(XY)$
- ii) $\text{Var}(3X - Y)$
- iii) $P(Y=y / X=2)$

$$\frac{f(x, y)}{g(x)}$$

$$g(x) = \sum_y f(x, y)$$

$$E[g(x)] = \sum_x x$$

Question 3: (5 marks) Suppose the HRD manager randomly selects 3 individuals from a group of 10 employees for a special assignment. Assuming that 4 of the employees were assigned to a similar assignment previously, determine the probability that exactly two of the three employees have had previous experience. What is the expected number of employees have had previous experience in a sample of size 5? What is the variance of the number of employees in the sample of size 5?

$$E(X^2) - [E(X)]^2$$