

**Q No 4. [Local Search]****[5 Points]**

In this question we are going to pose the subset sum problem of described in first question as an optimization problem and then use Hill climbing strategy (i.e. a local search algorithm) to solve it.

Once again assume that for a set having  $n$  elements, a solution is coded using a bit string of length  $n$  with a bit being set to 1 if the element is part of the subset and 0 otherwise. Further, assume that the optimality of a solution is computed using  $1 / (|S - \sum| + 1)$  where  $S$  is the required value of sum and  $\sum$  is sum of the subset and  $|x|$  represents absolute value of  $x$ .

A simple operator to generate a new solution from an existing solution can be defined as follows

**NEW\_SOLUTION(X) = FLIP A BIT IN THE SOLUTION X**

This is equivalent to including an element in the subset or excluding an already chosen element from the subset. It is obvious that for a set of size  $n$  we can generate  $n$  new solutions from an existing solution.

Use the above operator for generating new solutions along with the hill climbing search strategy (also known as local search) to find a solution for the following subset sum problem.

Find a subset of the set  $\{2, 3, 4, 8, 16\}$  having sum **17**. Take the solution **00000** as the starting solution in your local search.

You must show all intermediate steps in the form of the following table. For each iteration show all intermediate solutions considered/generated and the solution selected at that iteration.

Iteration No	Intermediate Solutions	Selected Solution
1		
2		
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