

Date

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Task 1:

We can (split) cut the rod of length 6 in following lengths and get prices:

	length of rod	Price
(i)	6	17
(ii)	1 1 1 1 1 1	$1+1+1+1+1+1=6$
(iii)	1 1 1 1 2	$1+1+1+1+5=9$
(iv)	1 1 2 2	$1+1+5+5=12$
(v)	1 1 1 3	$3+8=11$
(vi)	1 1 4	$1+1+9=11$
(vii)	1 2 3	$1+5+8=14$
(viii)	2 2 2	$5+5+5=15$
(ix)	1 5	$1+10=11$
(x)	2 4	$5+9=14$
(xi)	3 3	$8+8=16$
(xii)	4 2	$9+5=14$

The rest will be same as these like another can be 2 & 4 split but split of 2 and 4 or 4 and 2 gives same price i.e 14.

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Task 2:

Given rod of length 6. We can make dp array ^{using} (with) top down approach.

Given Prices V

1	5	8	9	10	17	17	20	24	30
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12345678910

dp array P

1	5	8	10	13	17
---	---	---	----	----	----

123456

Dry run:

$$dp[1] = 1$$

$$dp[2] = \begin{cases} V_1 + P[1] = 1 + 1 = 2 \\ V_2 = 5 \checkmark \end{cases}$$

$$dp[3] = \begin{cases} V_1 + P[2] = 1 + 5 = 6 \\ V_2 + P[1] = 5 + 1 = 6 \\ V_3 = 8 \checkmark \end{cases}$$

$$dp[4] = \begin{cases} V_1 + P[3] = 1 + 8 = 9 \\ V_2 + P[2] = 5 + 5 = 10 \checkmark \\ V_3 + P[1] = 8 + 1 = 9 \\ V_4 = 9 \end{cases}$$

$$dp[6] = \begin{cases} V_1 + P[5] = 1 + 13 = 14 \\ V_2 + P[4] = 5 + 10 = 15 \\ V_3 + P[3] = 8 + 8 = 16 \\ V_4 + P[2] = 9 + 5 = 14 \\ V_5 + P[1] = 10 + 1 = 11 \\ V_6 = 17 \checkmark \end{cases}$$

$$dp[5] = \begin{cases} V_1 + P[4] = 1 + 10 = 11 \\ V_2 + P[3] = 5 + 8 = 13 \checkmark \\ V_3 + P[2] = 8 + 5 = 13 \checkmark \\ V_4 + P[1] = 9 + 1 = 10 \\ V_5 = 17 \oplus \end{cases}$$

Task 3:

Algorithm for keeping track of cuts of rod. We declare an array of size n and ~~are~~ initialize it with zero and then compare with maximum & then ~~with~~ calculate optimal cuts.

```
Rod Cut (Price[], n) {
    dp[0] = 0;
    Cut_splits[n];
```

```
    for i = 1 to n do
```

```
        q = INT_MIN
```

```
        for j = 1 to i do
```

```
            if max(q,
```

```
                if ( $q < \text{price}[j] + \text{dp}[i-j]$ ) then
```

```
                     $q = \text{price}[j] + \text{dp}[i-j]$ 
```

```
                Cut_splits[i] = j
```

```
            end if
```

```
        end for
```

```
        dp[i] = q
```

```
    Optimal cutting[n]
```

```
    i = 0, ts
```

```
    while n > 0 do
```

```
        ts = Cut_splits[n]
```

```
        Optimal cutting[i] = ts
```

```
        n -= ts
```

```
        i++
```

```
    end while
```

```
end for
```

```
return  
    Optimal cutting;
```