

Parallel and Distributed Computing

CS3006

Lecture 13

Basic Communication Operations-III

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All-Reduce

Basic Communication Operations

(All-Reduce)

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- Precondition: Every process i has a single message M_i of size m words.
- Post condition: All processes have a reduced message M of size m words.

Strategies:

1. Use **all-to-one reduction** followed by **one-to-all** broadcast ($2 * (t_s + mt_w) \log p$)
2. Use **modified All-to-All comm.** algorithm for hypercube $((t_s + mt_w) \log p)$
 - Replace Union with associative operator

Prefix-Sum

Basic Communication Operations (Prefix-Sums)

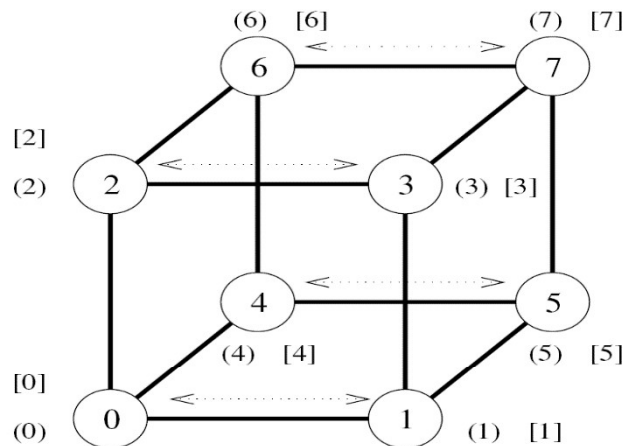
- Prefix-sums are also known as scan operations
- Given p numbers n_0, n_1, \dots, n_{p-1} (one on each node), the problem is to compute the sums such that: -
 - $S_k = \sum_{i=0}^K(n_i)$
 - Here S_k is the prefix-sum computed at k th node after the operation.

Example:

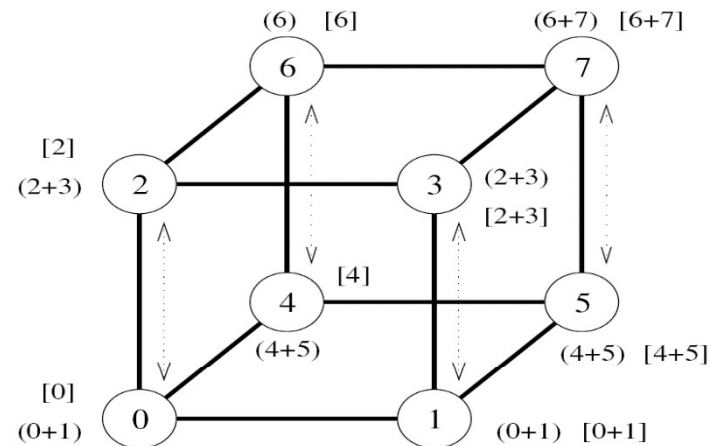
- Original sequence: $\langle 3, 1, 4, 0, 2 \rangle$
- Sequence of prefix sums: $\langle 3, 4, 8, 8, 10 \rangle$

Basic Communication Operations (Prefix-Sums)

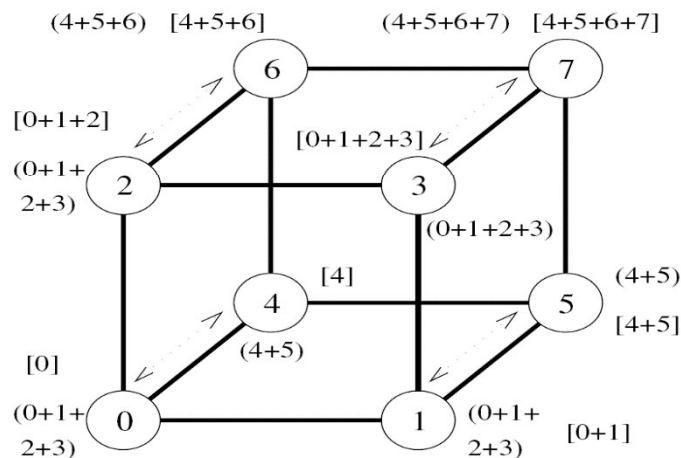
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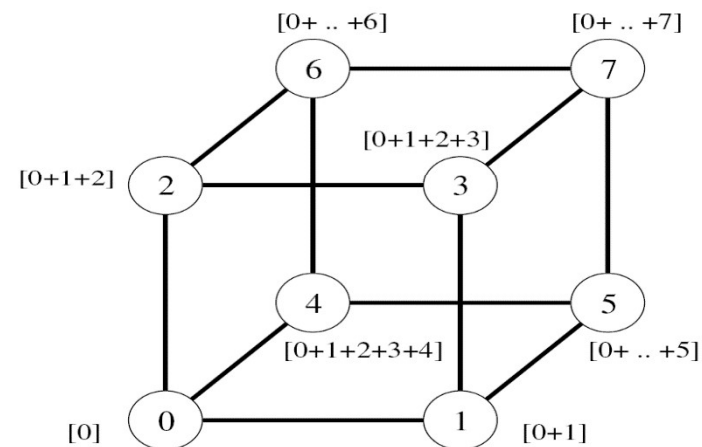
(a) Initial distribution of values



(b) Distribution of sums before second step



(c) Distribution of sums before third step



(d) Final distribution of prefix sums

Basic Communication Operations

(Prefix-Sums)

```
1.  procedure PREFIX_SUMS_HCUBE(my_id, my_number, d, result)
2.  begin
3.      result := my_number;
4.      msg := result;
5.      for i := 0 to d - 1 do
6.          partner := my_id XOR  $2^i$ ;
7.          send msg to partner;
8.          receive number from partner;
9.          msg := msg + number;
10.         if (partner < my_id) then result := result + number;
11.     endfor;
12. end PREFIX_SUMS_HCUBE
```

Algorithm 4.9 Prefix sums on a d -dimensional hypercube.

Scatter and Gather

Basic Communication Operations (Scatter and Gather)

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- Gather is different than reduction as it doesn't reduce the results with associative operator

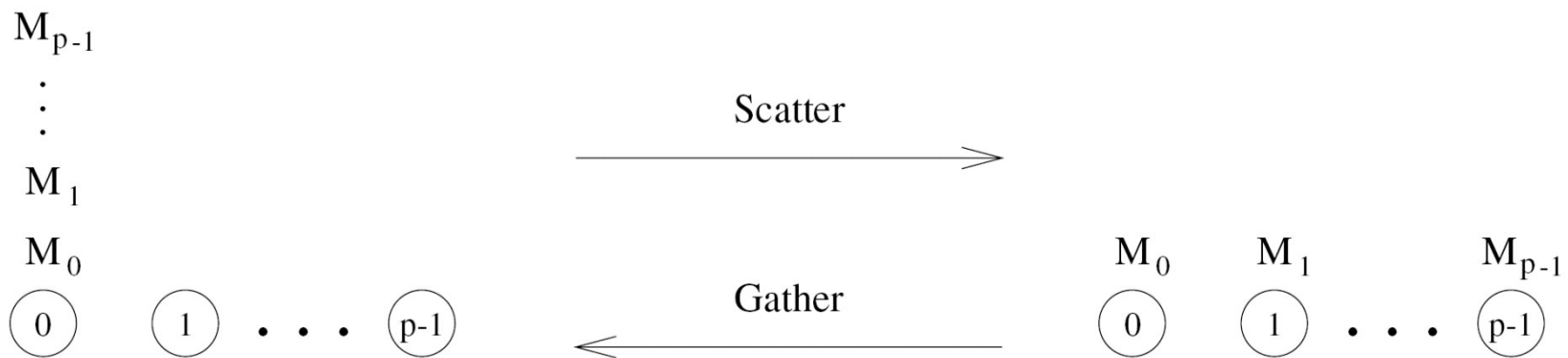
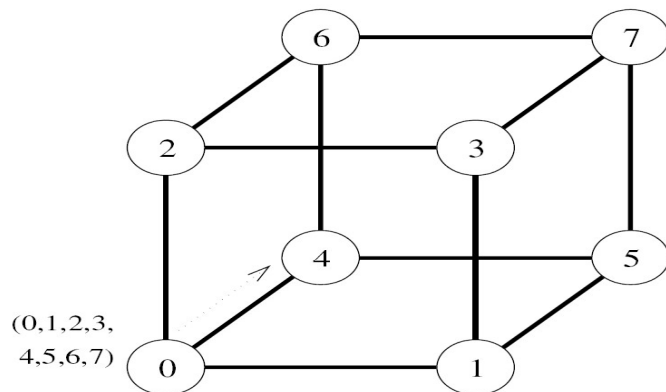


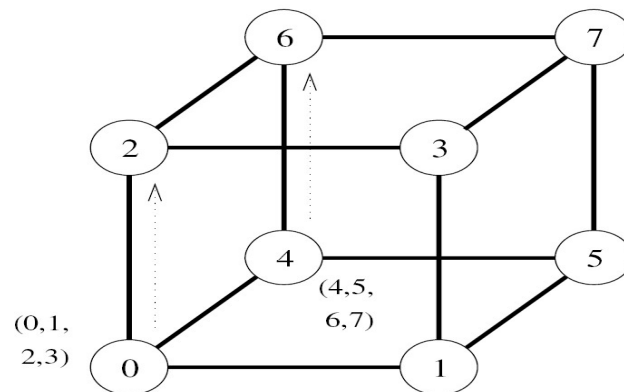
Figure 4.14 Scatter and gather operations.

Basic Communication Operations

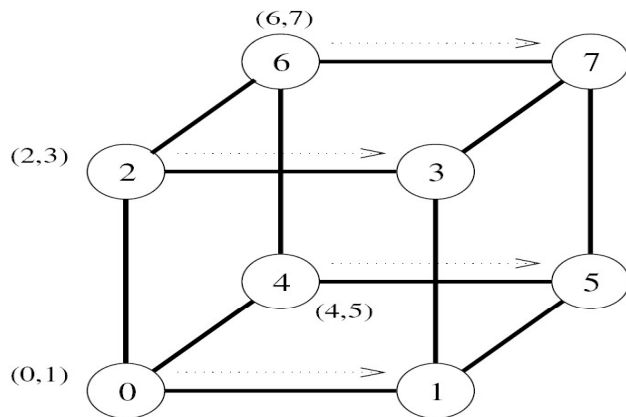
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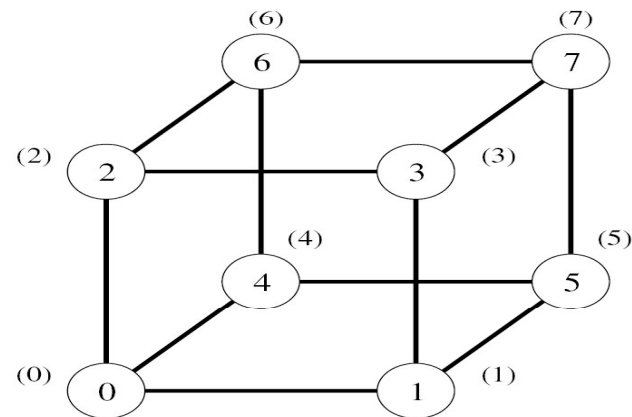
(a) Initial distribution of messages



(b) Distribution before the second step



(c) Distribution before the third step



(d) Final distribution of messages

Figure 4.15 The scatter operation on an eight-node hypercube.

All-to-All personalized Communication

Basic Communication Operations

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(All-to-All personalized)

- Each node sends a distinct message of size ***m*** to every other node.
- Also known **total exchange**

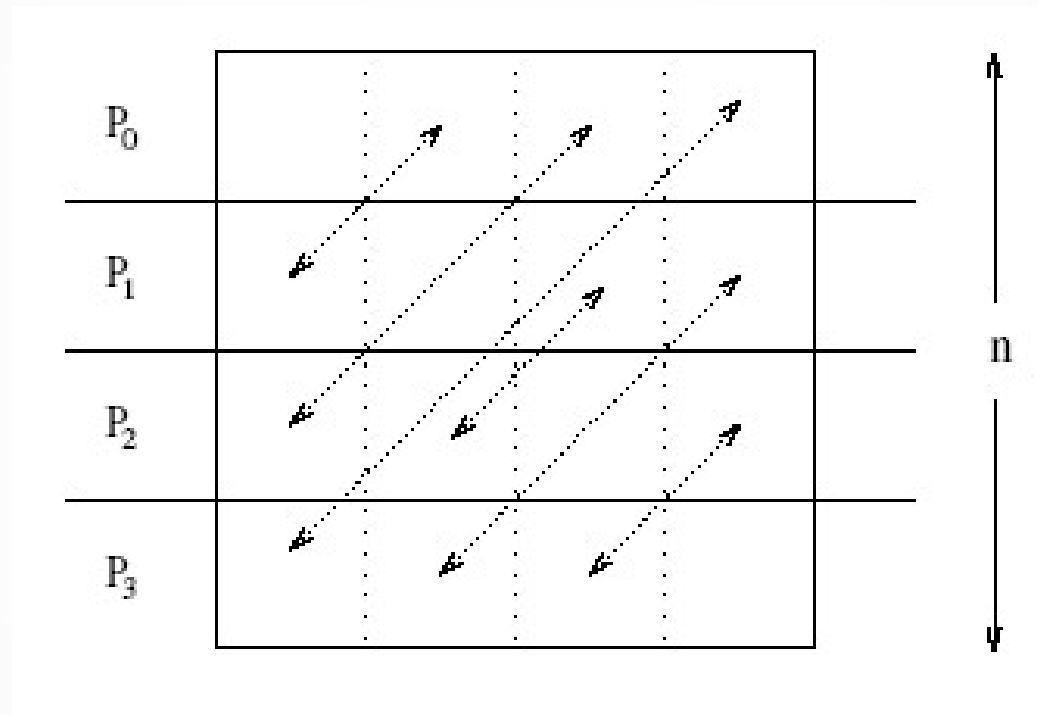


Figure 4.16 All-to-all personalized communication.

Basic Communication Operations

(All-to-All personalized)

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All-to-all personalized communication in transposing a 4×4 matrix using four processes.

Basic Communication Operations

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(All-to-All personalized [Ring])

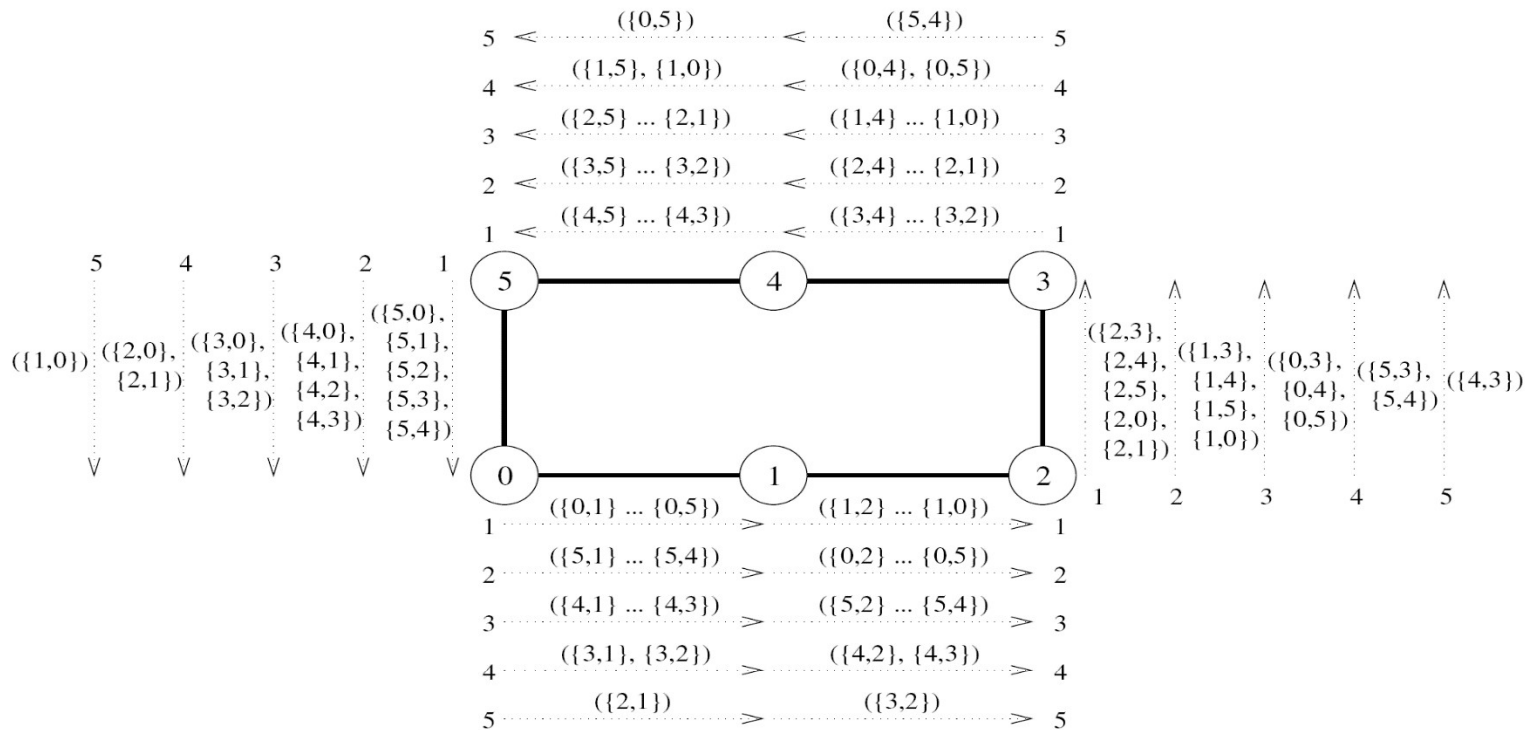


Figure 4.18 All-to-all personalized communication on a six-node ring. The label of each message is of the form $\{x, y\}$, where x is the label of the node that originally owned the message, and y is the label of the node that is the final destination of the message. The label $\{(x_1, y_1), \{x_2, y_2\}, \dots, \{x_n, y_n\}\}$ indicates a message that is formed by concatenating n individual messages.

Basic Communication Operations

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(All-to-All personalized [Ring])

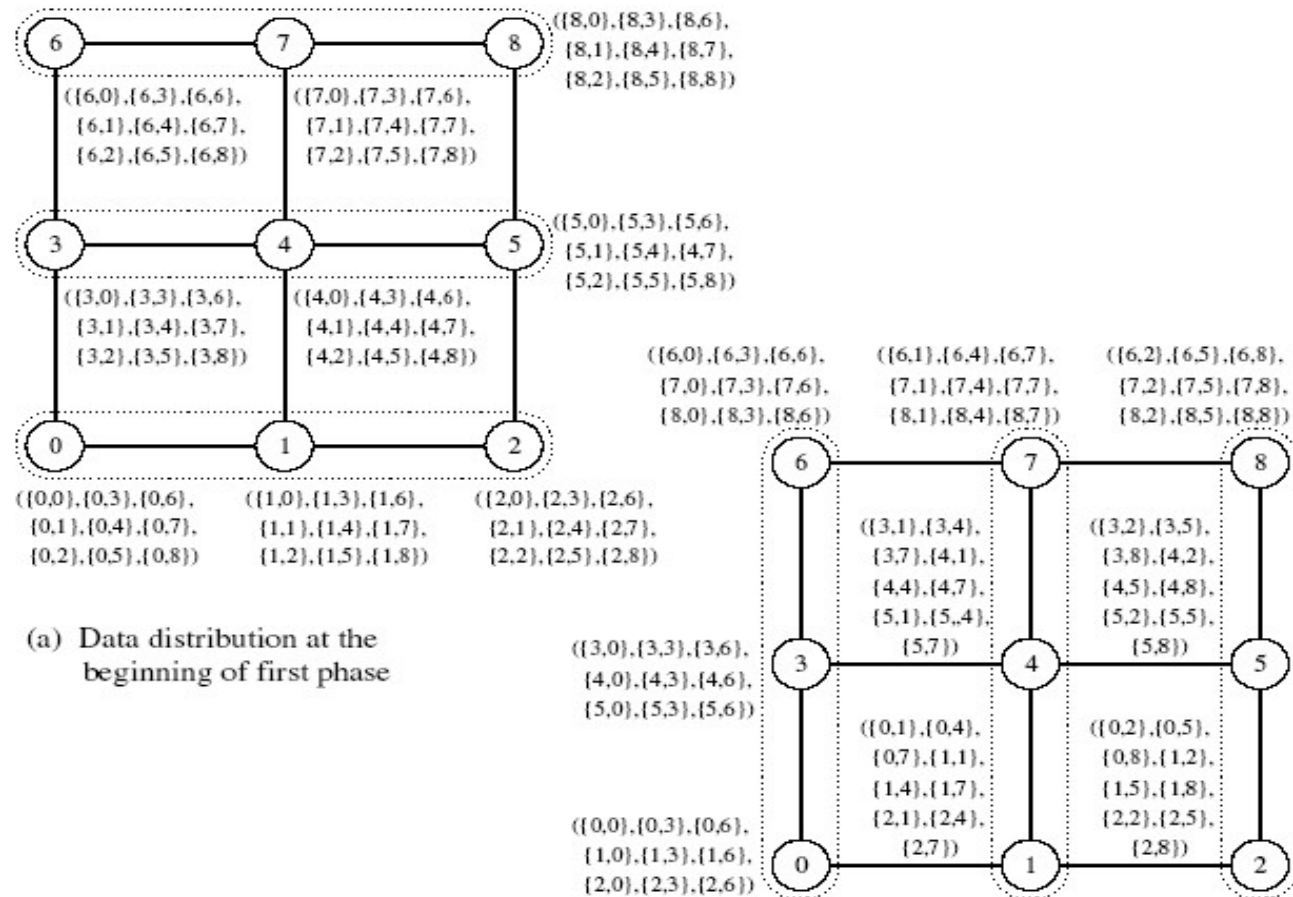
Cost Analysis

$$\begin{aligned} \Rightarrow T &= \sum_{i=1}^{(p-1)} (t_s + (p - i)mt_w) \\ &= \sum_{i=1}^{(p-1)} (t_s) + mt_w \sum_{i=1}^{(p-1)} (p - i) \\ &\rightarrow (p - 1)(t_s) + mt_w \sum_{i=1}^{(p-1)} (i) \\ &\rightarrow \left((t_s + \left(\frac{1}{2}\right) pmt_w) (p - 1) \right) \end{aligned}$$

Basic Communication Operations

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(All-to-All personalized [Mesh])



Basic Communication Operations

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(All-to-All personalized [Mesh])

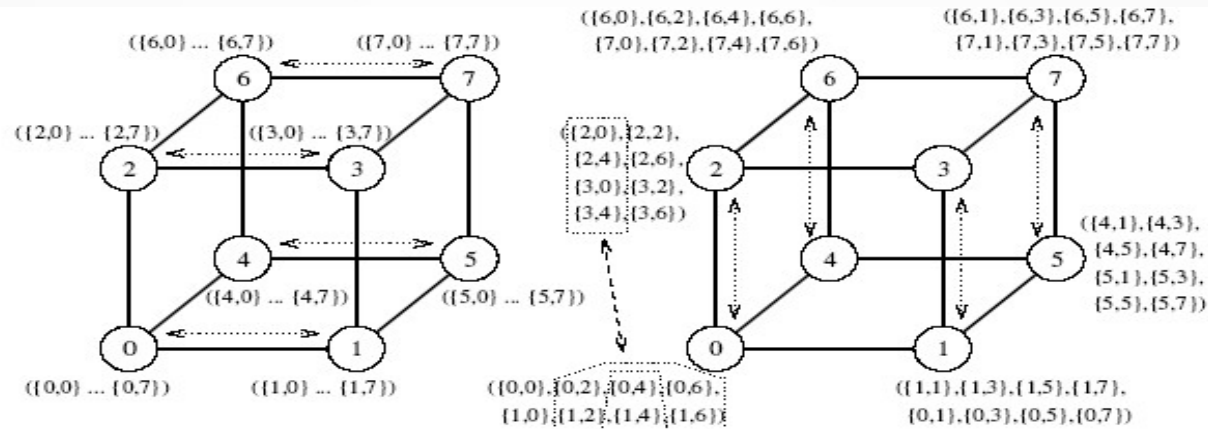
Cost Analysis

- Time for the first phase is identical to that in a ring with \sqrt{p} processors, i.e., $(t_s + t_w mp/2)(\sqrt{p} - 1)$.
 - Here mt_w becomes $\sqrt{p} mt_w$ and P becomes \sqrt{p}
- Time in the second phase is identical to the first phase. Therefore, total time is twice of this time, i.e.,

Basic Communication Operations

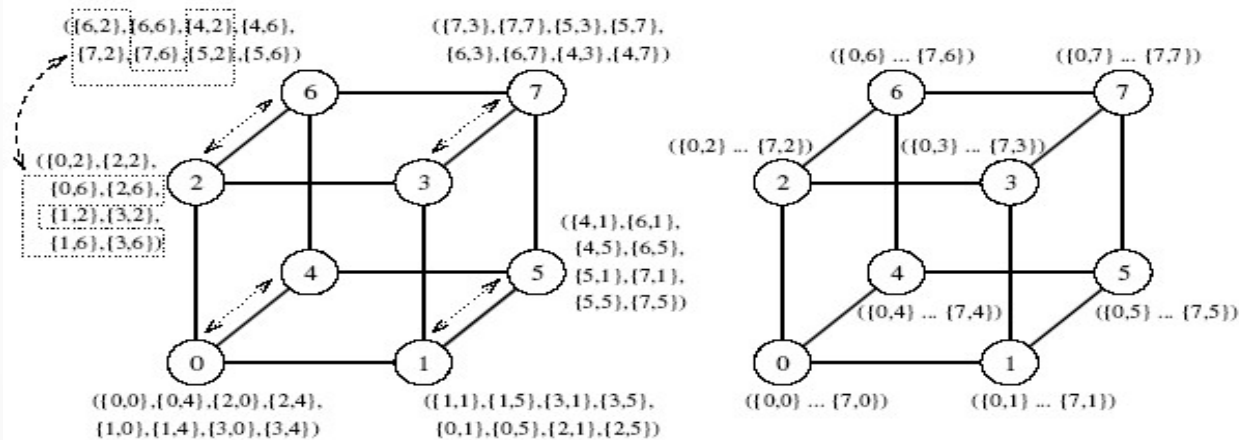
(All-to-All personalized [Hyper Cube])

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(a) Initial distribution of messages

(b) Distribution before the second step



(c) Distribution before the third step

(d) Final distribution of messages

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Questions



References

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1. Kumar, V., Grama, A., Gupta, A., & Karypis, G. (2017). *Introduction to parallel computing*. Redwood City, CA: Benjamin/Cummings.