

# ELEC2208 Power Electronics and Drives

## Power Electronics - Introduction -

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59/4219

# Part 1: Power Electronics

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Dr Yoshi Tsuchiya

1. Introduction

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2. Diode

3. Thyristor

4. Transistor

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Individual devices

5. Heating and Cooling

Thermal management

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6. Phase-Controlled Thyristor

    Converter and Diode Rectifier

7. Cycloconverter

8. Inverter

9. DC-to-DC Converter

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Convertors



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# Part 1: Timetable 2022/23

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W/C	Tuesday 3pm	Wednesday 11am	Thursday 3pm
30 <sup>th</sup> Jan	Introduction	Diode	Diode/Thyristor
6 <sup>th</sup> Feb	Thyristor	Tutorial 1	Transistor
13 <sup>th</sup> Feb	Cooling	Tutorial 2	Phase-Controlled Converter
20 <sup>th</sup> Feb	Rectifier	Cycloconverter	Tutorial3
27 <sup>th</sup> Feb	Inverter	DC-DC converter	DC-DC converter
6 <sup>th</sup> Mar	Tutorial 4	Drive Systems (Fred & Zehor)	...
Room	46/2003	02A/2065	58/1007

12 lectures and 4 tutorials



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# Part 1: Power Electronics

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## Tutorials

Tutors will work out the questions in a tutorial sheet to be delivered in advance to tutorials

## Revision sessions

Example questions to be worked out: 10 & 11 May 2023

## Lecture recording

All the sessions will be recorded.

## Further textbook

Daniel W. Hart, “[Power Electronics](#)” 201, McGraw-Hill Companies, Inc

# What is Power Electronics?

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## Definition

Branch of **electrical engineering** devoted to **conversion and control of electric power** using electronic converters based on **semiconductor power switches**.



The input and output may be **alternating current (AC)** or **direct current (DC)** and may differ in magnitude and frequency.

# Elements of Power Converters

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## Passive components

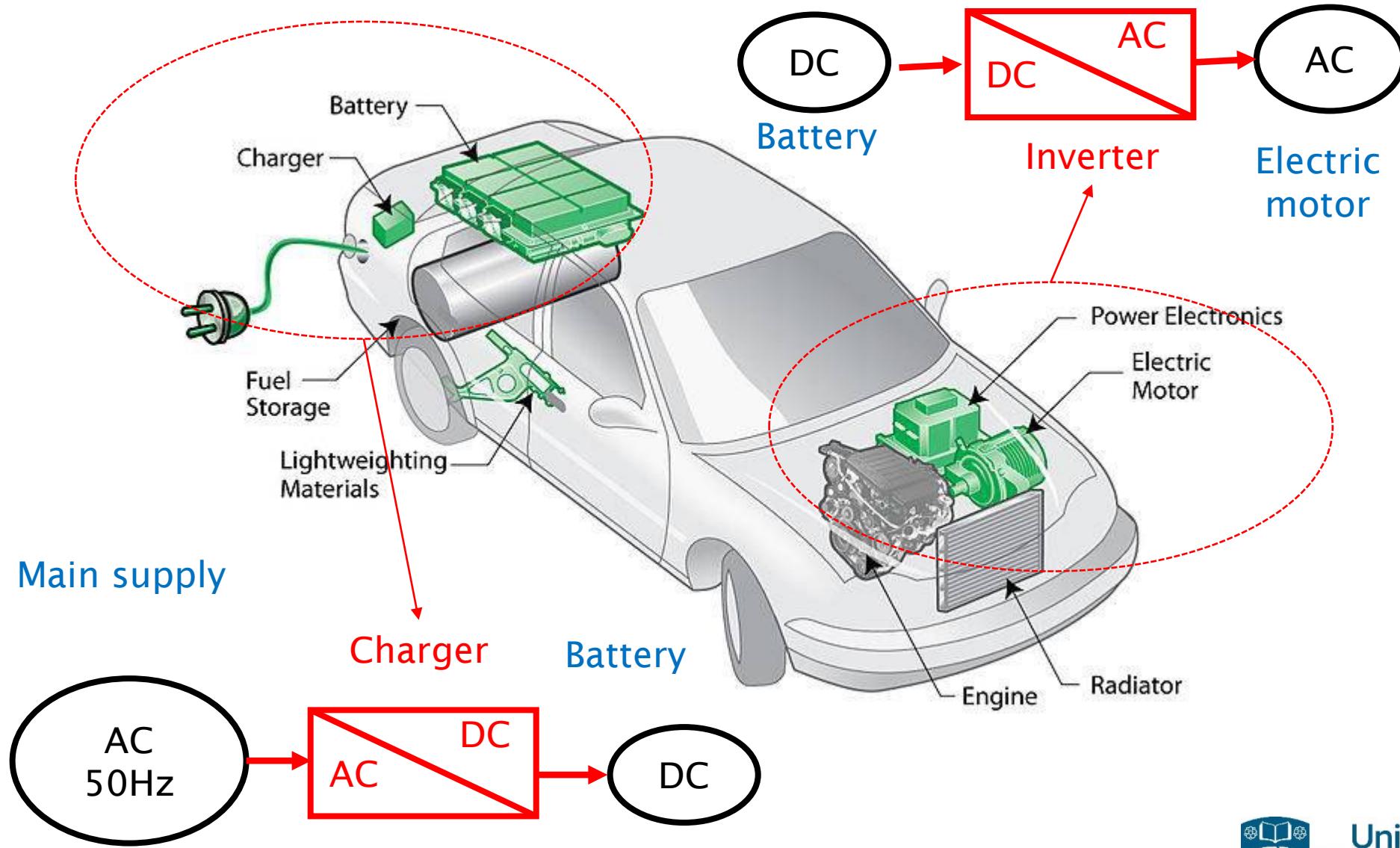
- Capacitors
- Inductors
- Transformers

## Power switches

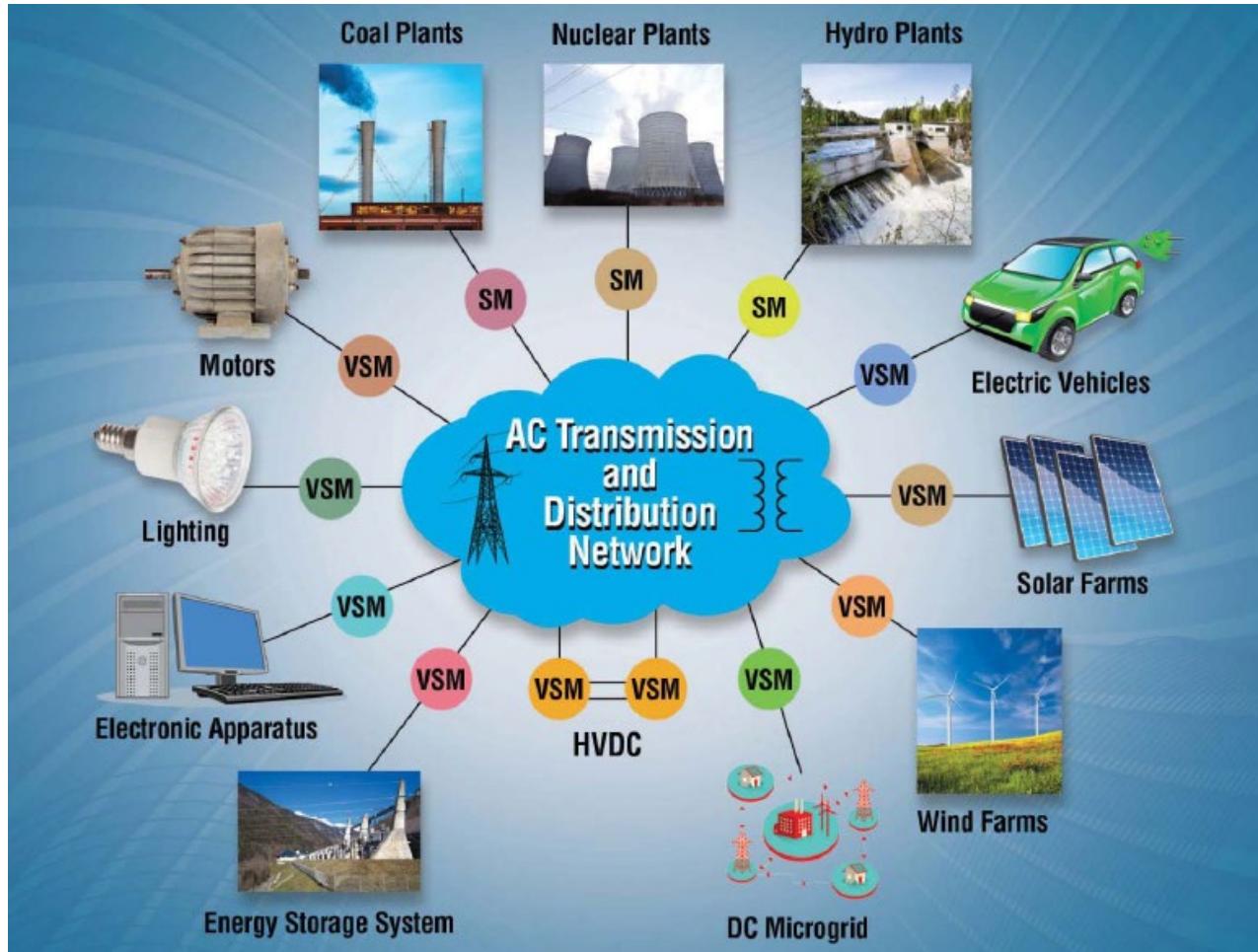
- Diodes
- Thyristors
- Transistors



# Application – Electric Vehicle



# Further applications



**Power electronics is a key enabling technology for a sustainable world.**



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# Classification of Power Converters

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Electrical supplies: AC or DC

—————→ 4 input output combinations

**AC input/DC output – Rectifier**

Half-wave, full-wave rectifier, etc.

**DC input/AC output – Inverter**

Half-bridge, full-bridge, multilevel inverter, etc.

**DC input/DC output – DC-DC converter**

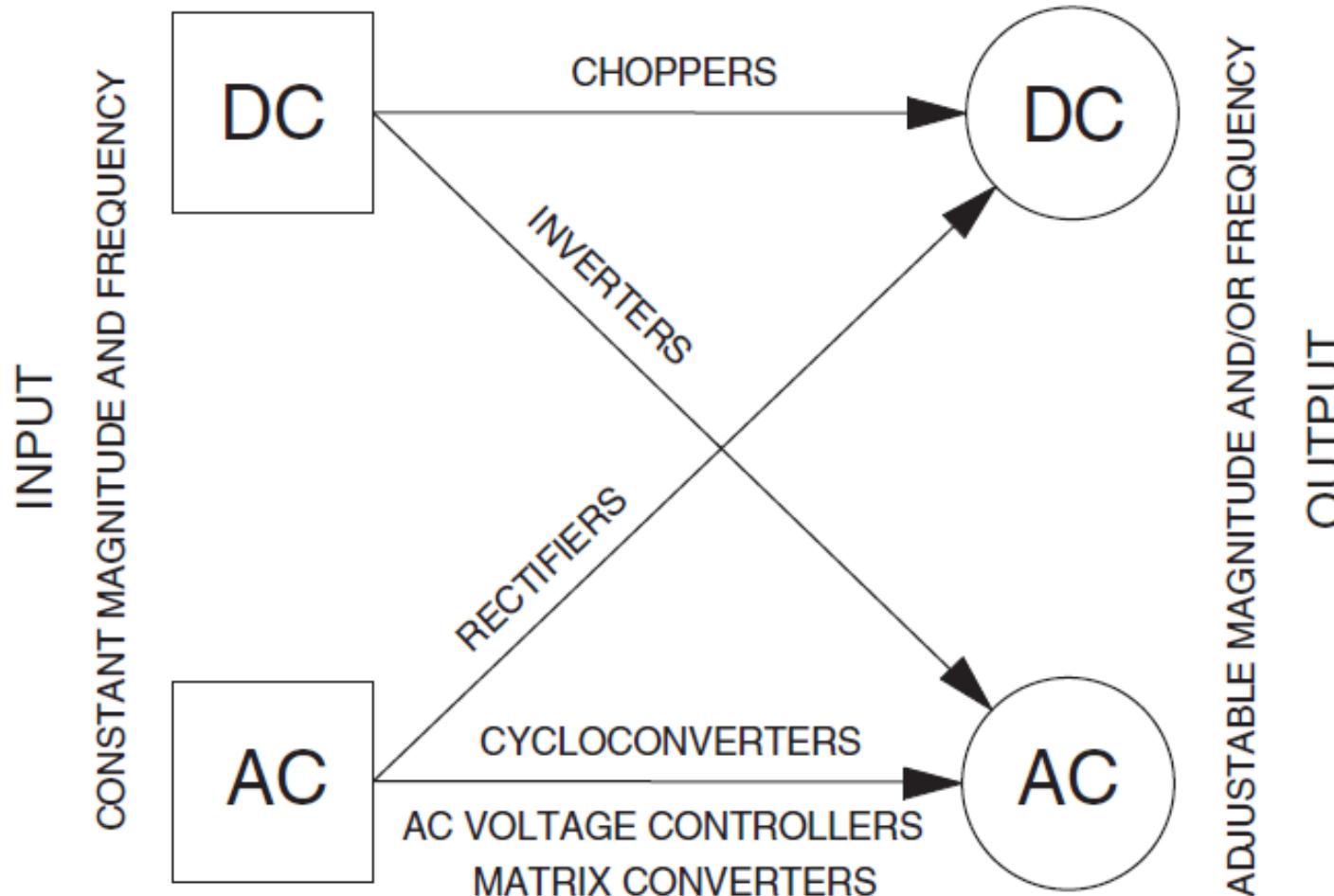
Buck, boost, buck-boost, etc.

**AC input/AC output – AC-AC converter**

Matrix converter, cycloconverter, etc.



# Classification of Power Converters

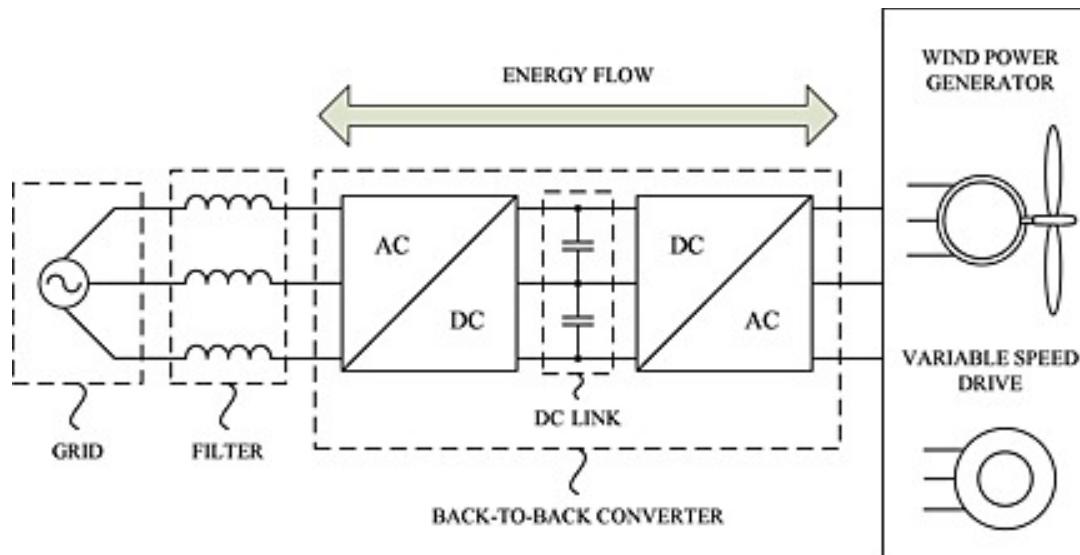


# Power Converters - Features

- The voltages on either side of a power converter do not have to be equal.
- For AC supplies, the frequency and phase angle on either side of a power converter can be the same or different.
- Power conversion can be a multistep process (combination of multiple power converters) involving more than one type of converter.

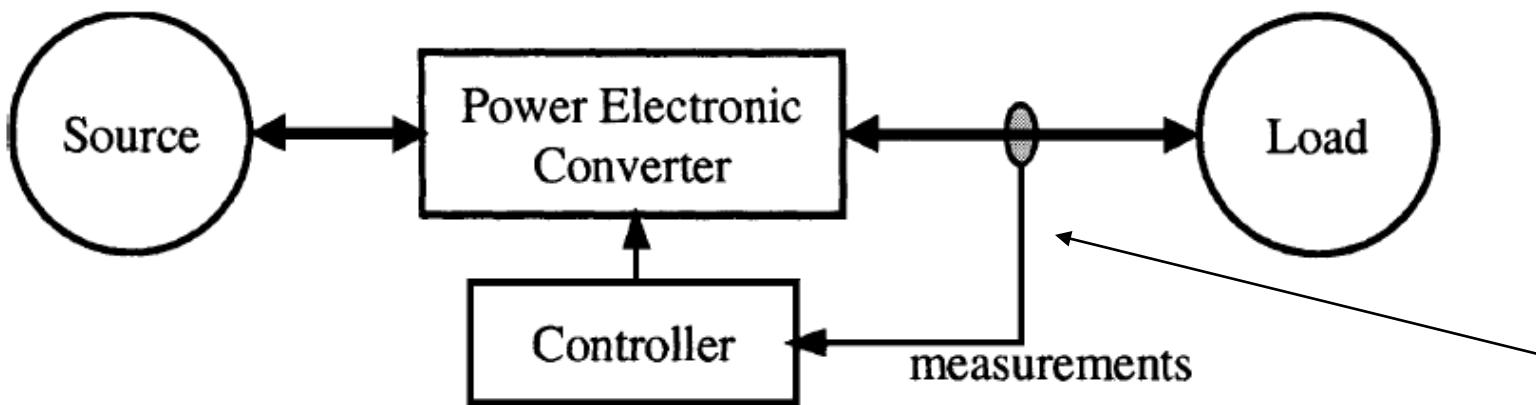
Example:

AC to DC then DC to AC  
for motor drive system.



# Power Converter Systems

- Power converter system consists of semiconductor devices as **power switches** and **passive components** as filter or energy storage elements to synthesize voltage and current waveforms according to the demand.
- Power supply with constant (in most cases) magnitude and frequency.
- Demand with specific magnitude and frequency which is different from the source.



Feedback for  
safe operation



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# Circuit analysis revision

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## 1. Passive components

- Capacitors
- Inductors

## 2. Wave form analysis

- Fourier series

## 3. Circuit analysis

- KVL, KCL, RMS

## 4. Average power

## 5. Ideal vs Practical switches



# Capacitors

Capacitors can store energy in electric field.

Amount of charge stored is proportional to the voltage:

$$Q(t) = Cv_c(t)$$

$$\Delta Q = C\Delta V$$

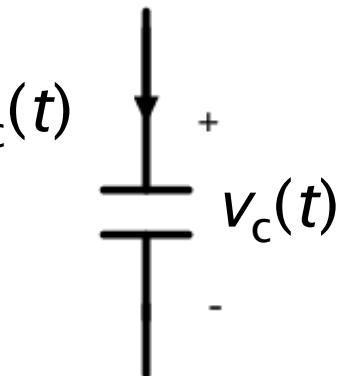
**Energy stored**

$$w(t) = \frac{1}{2}Cv_c^2$$

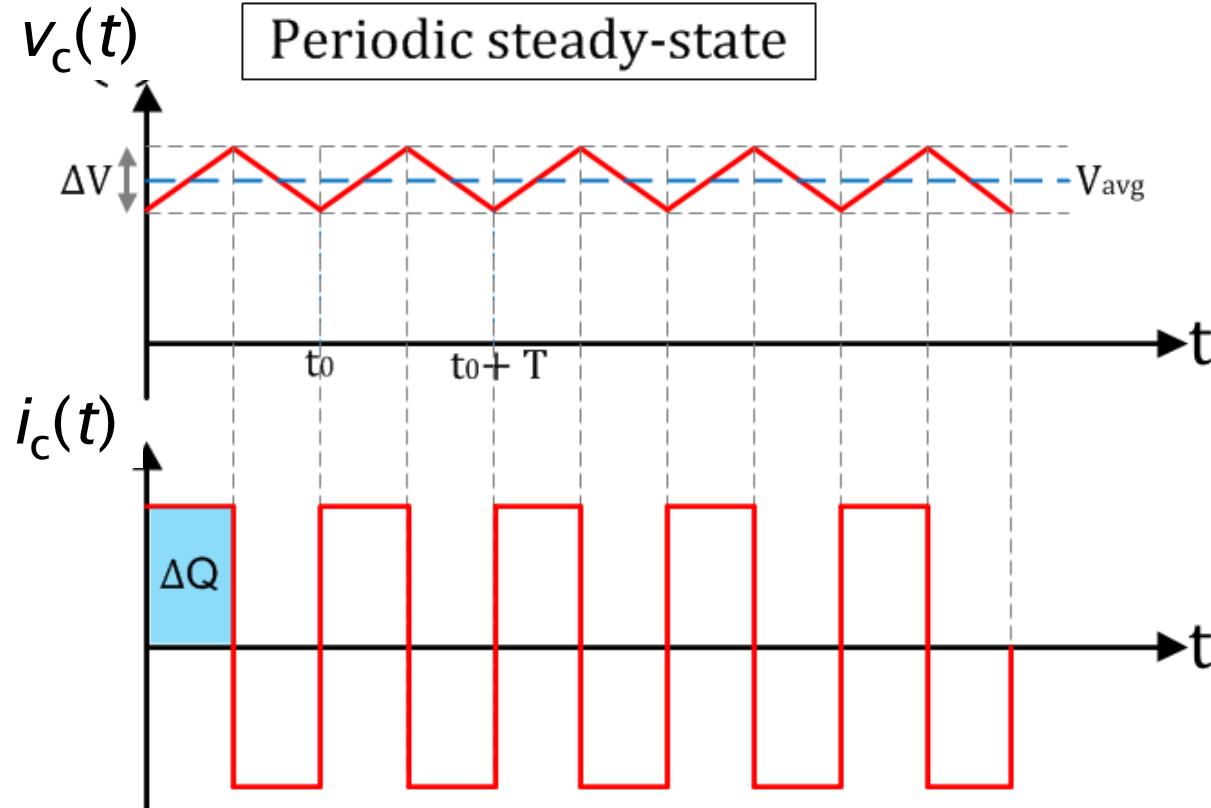
**Current and voltage**

$$i_c(t) = C \frac{dv_c(t)}{dt}$$

$$v_c(t) = \frac{1}{C} \int_{t_0}^t i_c(t) dt + v_c(t_0)$$



# Capacitors



Response to periodic voltage waveform at steady state

$$v_c(t + T) = v_c(t)$$

$$i_c(t) = C \frac{dv_c(t)}{dt}$$

$$\begin{aligned}\langle i_c(t) \rangle &= I_C \\ &= \frac{1}{T} \int_t^{t+T} i_c(t) dt = 0\end{aligned}$$

Average current is zero.

Average power:  $P_C = 0$



# Inductors

Inductors can store energy in magnetic field.



Flux linkage is proportional to the current:

$$\lambda(t) = Li_L(t) \quad \Delta\lambda = L\Delta I$$

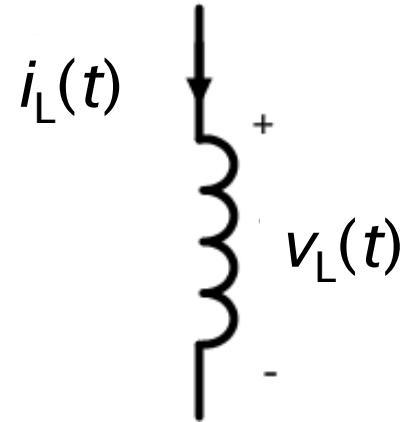
**Energy stored**

$$w(t) = \frac{1}{2} Li_L^2$$

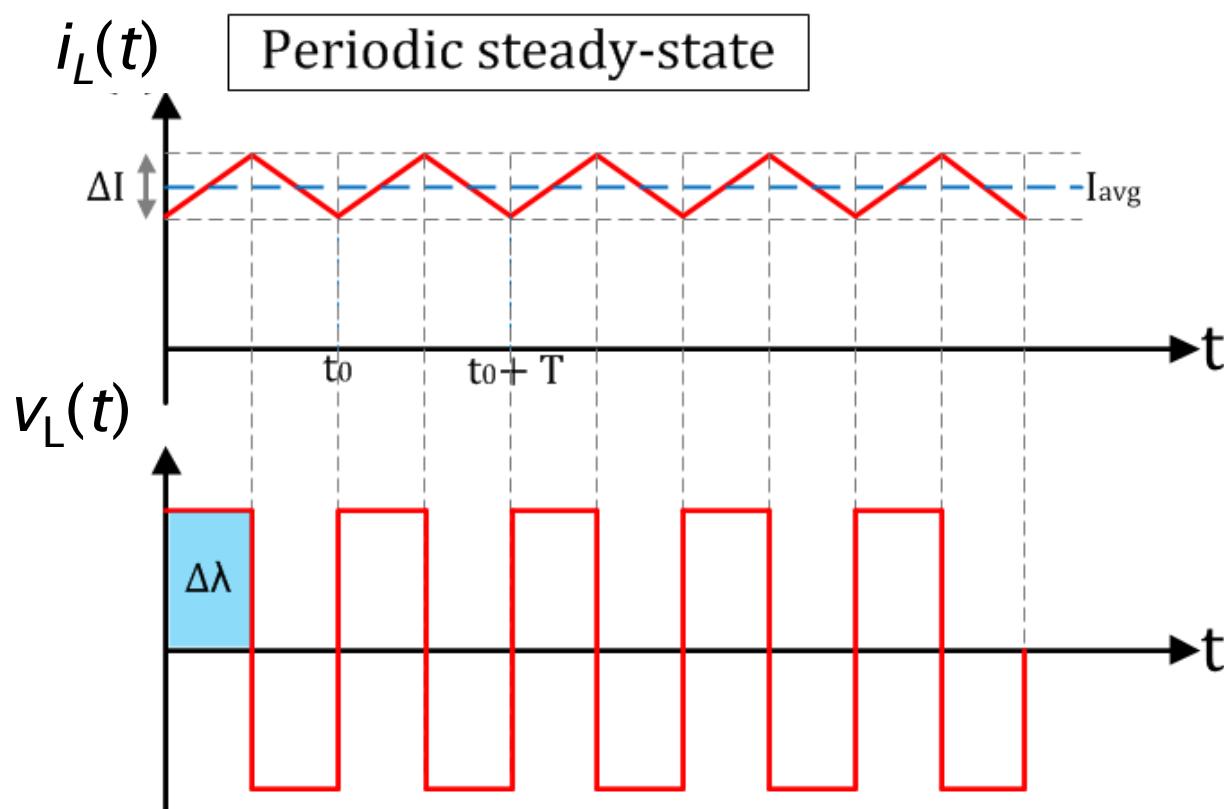
**Voltage and current**

$$v_L(t) = L \frac{di_L(t)}{dt}$$

$$i_L(t) = \frac{1}{L} \int_{t_0}^t v_L(t) dt + i_L(t_0)$$



# Inductors



Response to periodic current waveform at steady state

$$i_L(t + T) = i_L(t)$$

$$v_L(t) = L \frac{di_L(t)}{dt}$$

$$\begin{aligned}\langle v_L(t) \rangle &= V_L \\ &= \frac{1}{T} \int_t^{t+T} v_L(t) dt = 0\end{aligned}$$

Average voltage is zero.

Average power:  $P_L = 0$



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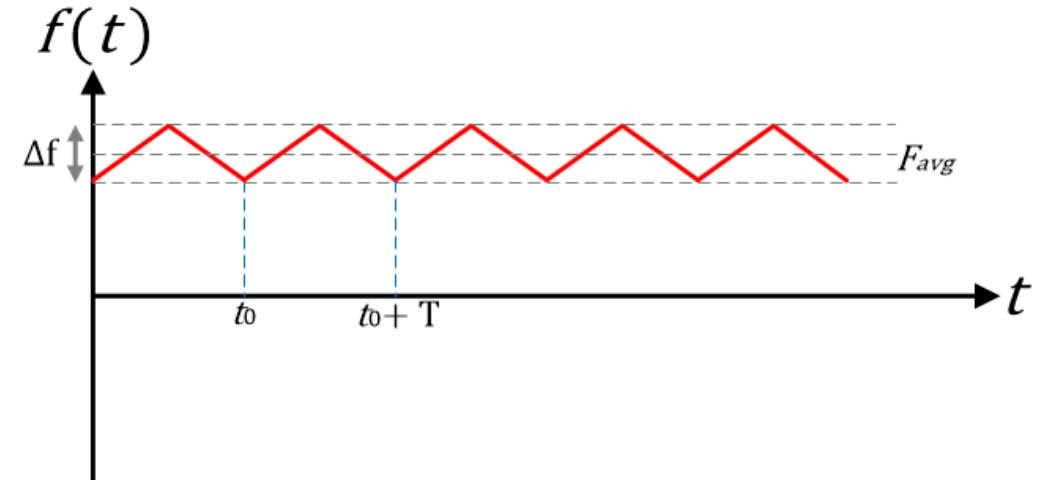
# Analysis of Waveform

## Periodic waveforms

The magnitude at the end of one period is the same as the beginning.

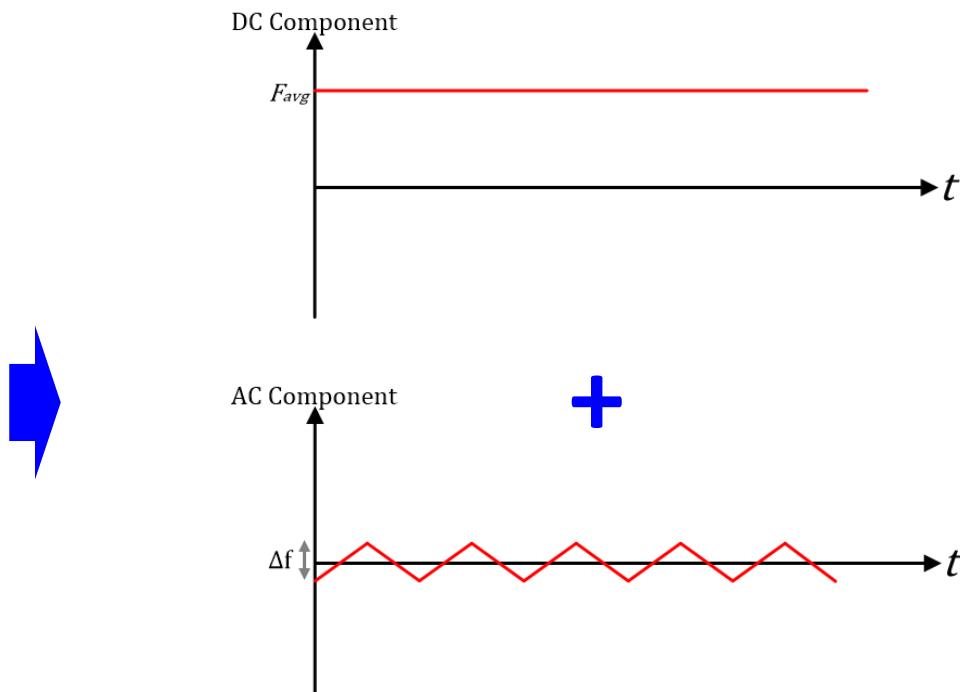
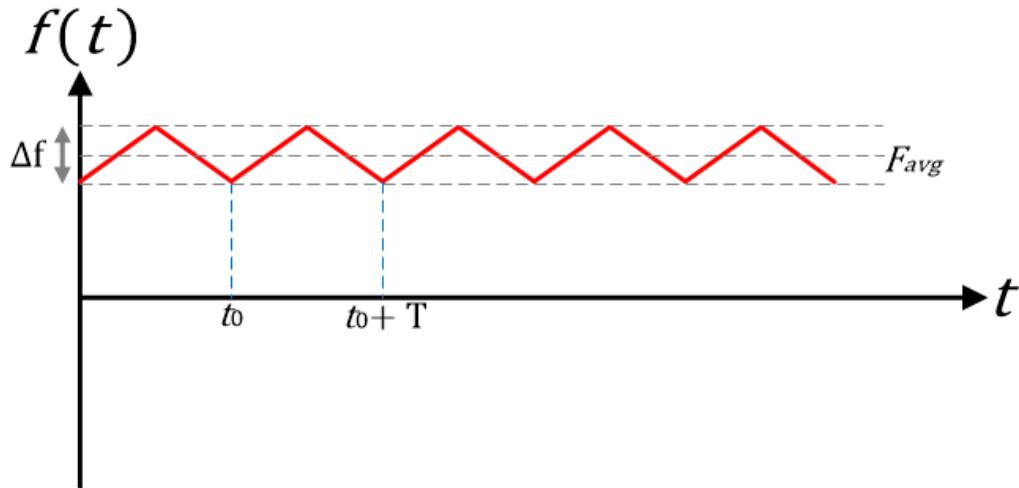
$$f(t + T) = f(t)$$

The periodic waveform consists of DC and AC components and can be described by a **Fourier Series** of sinusoids.



# Analysis of Waveform

## Periodic waveforms



## Fourier Series

$$f(t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} [a_n \cos(n\omega_0 t) + b_n \sin(n\omega_0 t)]$$
$$= \frac{a_0}{2} + \sum_{n=1}^{\infty} c_n \cos(n\omega_0 t + \theta_n)$$

AC components

DC component



# KVL and KCL

$$v(t) = V_{dc} + \sum_{n=1}^n V_n \cos(n\omega_0 t + \theta_n)$$

$$i(t) = I_{dc} + \sum_{n=1}^n I_n \cos(n\omega_0 t + \phi_n)$$

Circuit analysis methods, KVL and KCL apply individually to DC and AC components.

**KVL**

$$v(t) = V_{dc} + v_{ac}(t)$$

**KCL**

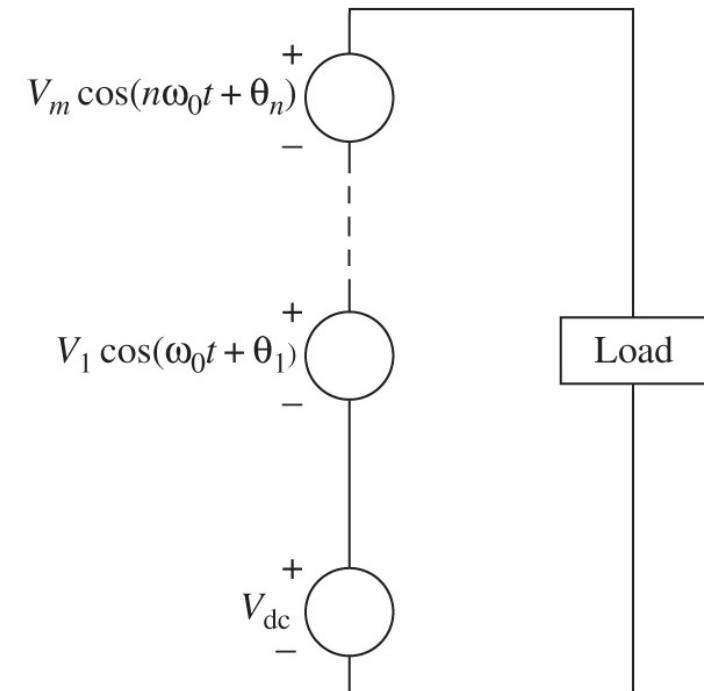
$$i(t) = I_{dc} + i_{ac}(t)$$

$$\sum_{loop} V_{dc} = 0$$

$$\sum_{node} I_{dc} = 0$$

$$\sum_{loop} v_{ac}(t) = 0$$

$$\sum_{node} i_{ac}(t) = 0$$



# Root Mean Square (RMS)

RMS of a function  $f(t)$

$$F_{rms} = \sqrt{\frac{1}{T} \int_{t_0}^{t_0+T} f^2(t) dt}$$

If  $f(t)$  is sum of  $N$  periodic waveforms:  $f(t) = f_1(t) + f_2(t) + \dots + f_N(t)$

$$F_{rms} = \sqrt{F_{1,rms}^2 + F_{2,rms}^2 + \dots + F_{N,rms}^2} = \sqrt{\sum_{n=1}^N F_{n,rms}^2}$$

If  $f(t)$  is Fourier Series:  $f(t) = \frac{a_0}{2} + \sum_{n=1}^{\infty} C_n \cos(n\omega_0 t + \theta_n)$

$$F_{rms} = \sqrt{\sum_{n=1}^{\infty} F_{n,rms}^2} = \sqrt{\left(\frac{a_0}{2}\right)^2 + \sum_{n=1}^{\infty} \left(\frac{C_n}{\sqrt{2}}\right)^2}$$

# Power

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Average of a function  $f(t)$ :

$$F_{mean} = \frac{1}{T} \int_{t_0}^{t_0+T} f(t) dt$$

## Power

Instantaneous power

$$p(t) = v(t)i(t)$$

Average power/real power

$$P = \frac{1}{T} \int_{t_0}^{t_0+T} p(t) dt = \frac{1}{T} \int_{t_0}^{t_0+T} v(t)i(t) dt$$

DC average power

$$P = V_{dc}I_{dc} \quad \text{if } v(t) = V_{dc} \text{ and } i(t) = I_{dc}.$$

If  $v(t)$  and  $i(t)$  are sinusoidal waveforms,

AC average power

$$P = V_{rms}I_{rms} \cos(\theta - \phi)$$

$\theta$  : Phase of voltage  
 $\phi$  : Phase of current

Power factor

$$pf = \cos(\theta - \phi)$$



# Power

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If  $v(t)$  and  $i(t)$  are non-sinusoidal periodic waveforms,

$$v(t) = V_{dc} + \sum_{n=1}^{\infty} V_n \cos(n\omega_0 t + \theta_n) \quad i(t) = I_{dc} + \sum_{n=1}^{\infty} I_n \cos(n\omega_0 t + \phi_n)$$

Average power

$$P = V_{dc}I_{dc} + \sum_{n=1}^{\infty} V_{n,rms}I_{n,rms} \cos(\theta_n - \phi_n)$$

Power factor

$$pf = \frac{P}{S} = \frac{P}{V_{rms}I_{rms}}$$

$$S = V_{rms}I_{rms}$$

Magnitude of apparent power



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# Ideal power devices

## Ideal characteristics of power switches

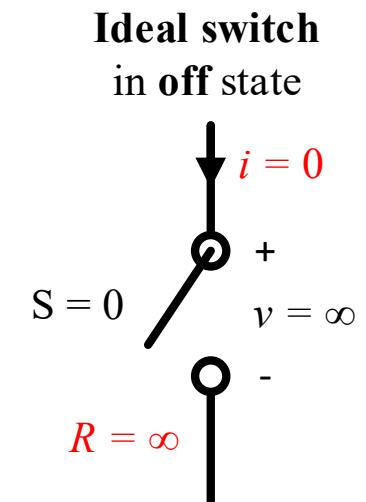
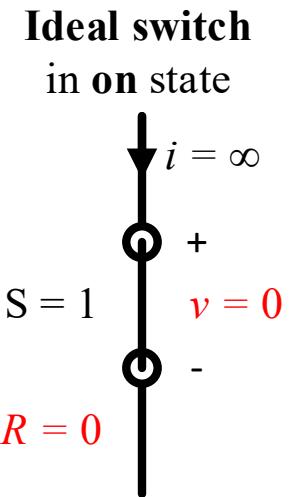
- Turn on and off instantaneously without delay
- High speed switching
- Zero power loss

### Ideal ON-state

Zero voltage drop across the switch and it can conduct infinite current due to zero impedance.

### Ideal OFF-state

Zero current flow due to infinite impedance and it can block infinite voltage.



# Practical power devices

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- Real power switches are semiconductor devices.
- They consume some power during operation.
- **Leakage current flows during Off state.**
- **Voltage drop occurs during On state** due to on resistance.
- Semiconductor power devices does not switch instantly. Delay during switching instant causes **switching loss**.
- Switching loss limits the switching frequency.
- Voltage and current of semiconductor power devices should be kept within **the safe operating value** to prevent failure.
- Due to power losses, **cooling by attaching the devices to heat sink is usually required** to keep the temperature of the devices within limits.

**We need to study Power Electronics!**