

# ADB Assignment # 02

Q1-

$B = 4096$  bytes

$r = 10,000,000$

$R = 150$  bytes

75000 records per department

Primary Key :- ROUNO

(a) Select \* from Student where ROUNO = 9137  
(file not ordered)

As file is not ordered, so linear search will be used.

$$Bfr = \left\lfloor \frac{B}{R} \right\rfloor = 27$$

$$b = \left\lceil \frac{r}{Bfr} \right\rceil = 370371$$

So number of block fetches =  $b = 370371$

(b) As search is on ROUNO and file is also ordered on ROUNO which is primary key (unique column). So binary search used.

$$\text{number of block fetches} = \lceil \log_2 b \rceil = 19$$



(c) As file is not ordered, so linear search.

Number of block fetches =  $b = 370371$

(d) As search is on deptNo and file is ordered on deptNo but it is not unique column. So,

$$\text{Blocks to be fetched} = \left\lceil \log_2(b) + \frac{s}{Bfr} - 1 \right\rceil$$

where  $s$  is selectivity. = 75000

$$\text{Blocks} = \left\lceil \log_2(370371) + \frac{75000}{27} - 1 \right\rceil$$

Blocks to be fetched = 2796

Q2 ✓ Customer ID values:-

{ 11, 24, 8, 2, 41, 6, 37, 27, 16 }

(a) 5 buckets

max 2 records in bucket

$$h(k) = k \bmod 5$$

loading records.



primary buckets

overflow buckets

0		
1	11, 41	→ 6, 16
2	2, 37	→ 27
3	8	
4	24	

$$11 \bmod 5 = 1$$

$$24 \bmod 5 = 4$$

$$8 \bmod 5 = 3$$

$$2 \bmod 5 = 2$$

$$41 \bmod 5 = 1$$

$$6 \bmod 5 = 1 \text{ (overflow)}$$

$$37 \bmod 5 = 2$$

$$27 \bmod 5 = 2 \text{ (overflow)}$$

$$16 \bmod 5 = 1 \text{ (overflow bucket)}$$

(b) Average no. of block access.

For 11 :- 1 block access

For 24 :- 1 block access

For 8 :- 1 block access

For 2 :- 1 block access

For 41 :- 1 block access

For 6 :- 2 blocks access

For 16 :- 2 blocks access

For 37 :- 1 block access

For 27 :- 2 blocks access

So Total = 12

So,

$$\text{average blocks access} = \frac{12}{9} = 1.33$$



11, 24, 8, 2, 41, 6, 37, 27, 16

## (c) Extendible hashing

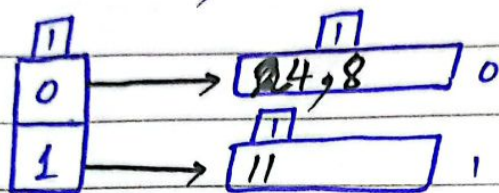
$$h(K) = K \bmod 6$$

max 2 records in bucket

(use MSB)

initially  $d=0, d'=0$

then,



$$11 \bmod 6 = 101$$

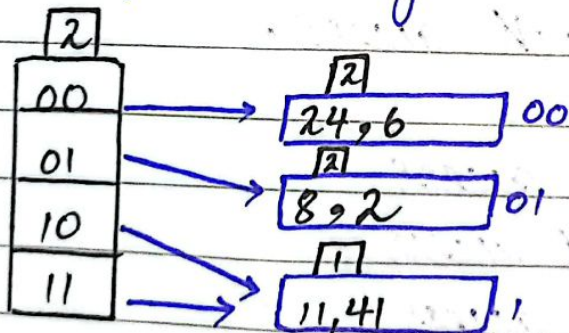
$$24 \bmod 6 = 000$$

$$8 \bmod 6 = 010$$

$$2 \bmod 6 = 010$$

(overflow, so split bucket 0)

Double directory size as local depth is equal to global depth



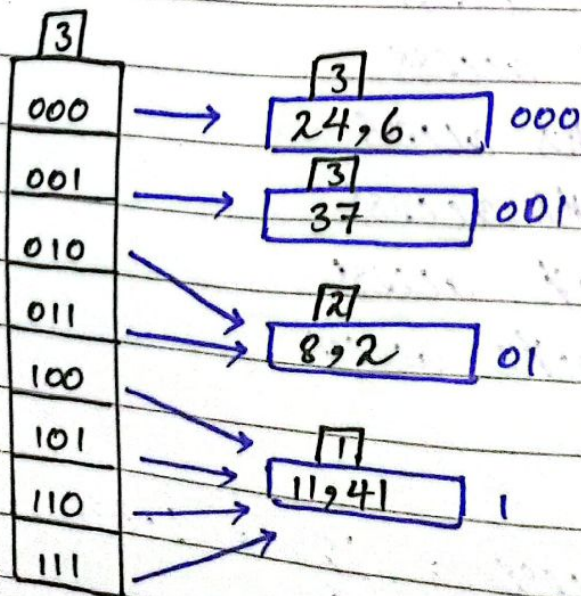
$$41 \bmod 6 = 101$$

$$6 \bmod 6 = 000$$

$$37 \bmod 6 = 001$$

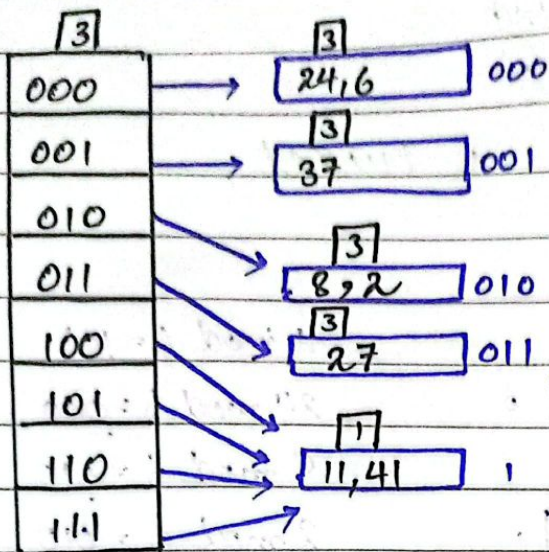
so overflow

split bucket 00 & double directory as local & global Depth same.

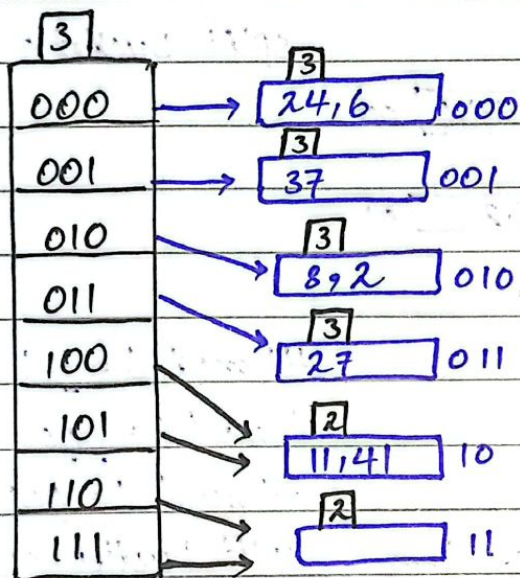




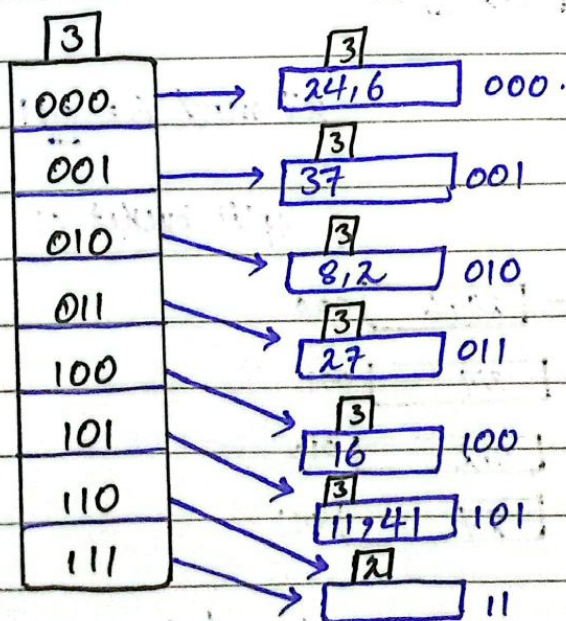
$27 \bmod 6 = 011$   
 so split bucket 01  
 but no need to  
 double directory  
 as local depth = 2 <  
 global depth



$16 \bmod 6 = 100$   
 overflow split bucket  
 but don't double  
 directory



Still 16 cause  
 overflow in bucket  
 10, again split





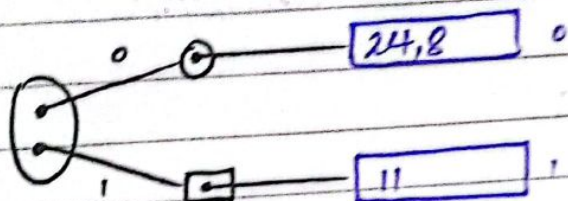
11, 24, 8, 2, 41, 6, 37, 27, 16

(d) Dynamic Hashing

$$h(k) = k \bmod 6$$

max 2 records in bucket.

Use MBB



$$11 \bmod 6 = 101$$

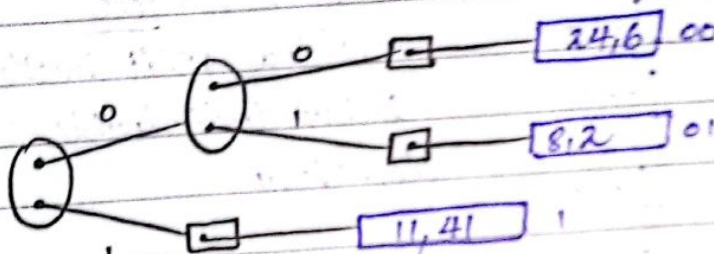
$$24 \bmod 6 = 000$$

$$8 \bmod 6 = 010$$

$$2 \bmod 6 = 010$$

overflow,

split bucket 0

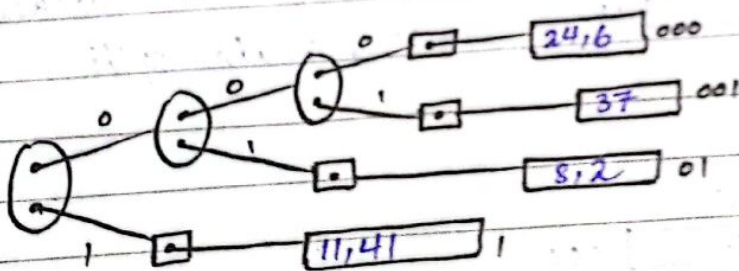


$$41 \bmod 6 = 101$$

$$6 \bmod 6 = 000$$

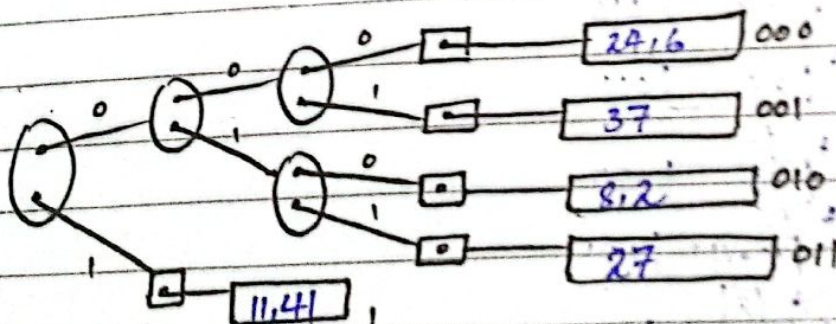
$$37 \bmod 6 = 001$$

split bucket 00



$$27 \bmod 6 = 011$$

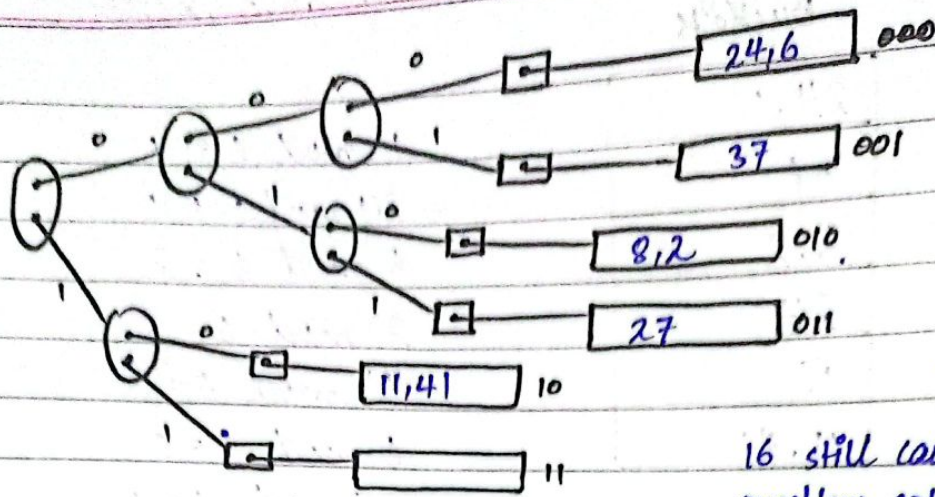
split bucket 01



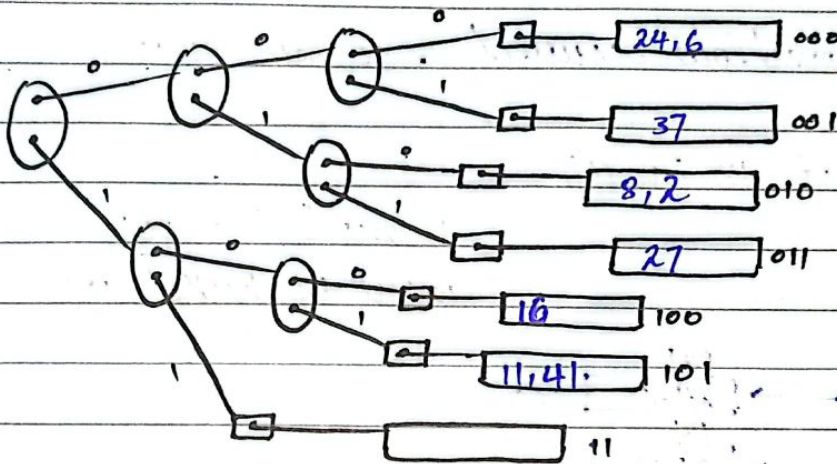
$$16 \bmod 6 = 100$$

split bucket 1





16 still cause  
overflow split  
bucket 10



### (c) Linear Hashing

2 max records per bucket

$$h(K) = K \bmod 6$$

Initially we will have 6 buckets (0-5)

If overflow occurs, put key in overflow bucket and <sup>increment</sup> double the number of buckets as new hash function =  $K \bmod 2n$  and split bucket pointed by  $n$  using new hash function

if  $h_1(K) \geq n$  (use initial hash function)

if  $h_1(K) < n$  (use new hash function)



n = 0

11, 24, 8, 2, 41, 6, 37, 27, 16

primary  
buckets

0	24, 6
1	37
2	8, 2
3	27
4	16
5	11, 41

$$11 \bmod 6 = 5$$

$$24 \bmod 6 = 0$$

$$8 \bmod 6 = 2$$

$$2 \bmod 6 = 2$$

$$41 \bmod 6 = 5$$

$$6 \bmod 6 = 0$$

$$37 \bmod 6 = 1$$

$$27 \bmod 6 = 3$$

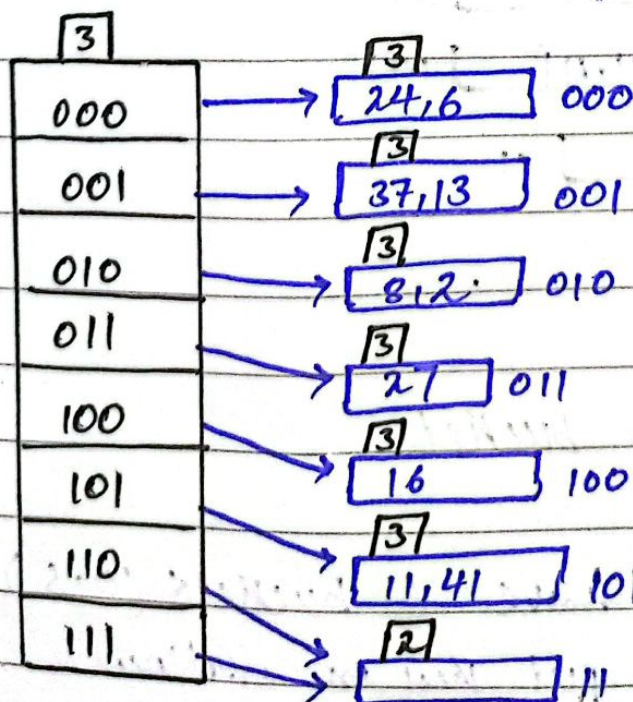
$$16 \bmod 6 = 4$$

no overflow occurred, so no split

(b) Insert 13 in (c)

$$13 \bmod 6 = 1$$

insert in bucket 01

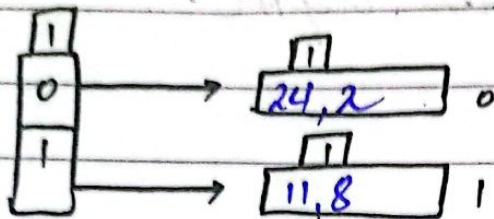




## (g) original solution

As 18 continue to cause overflow in bucket 0000 everytime so change hash function to  $K \bmod 12$  (rehash & reallocate all keys)

To insert :- 11, 24, 8, 2, 41, 6, 37, 27, 16, 13, 18



$$11 \bmod 12 = 1011$$

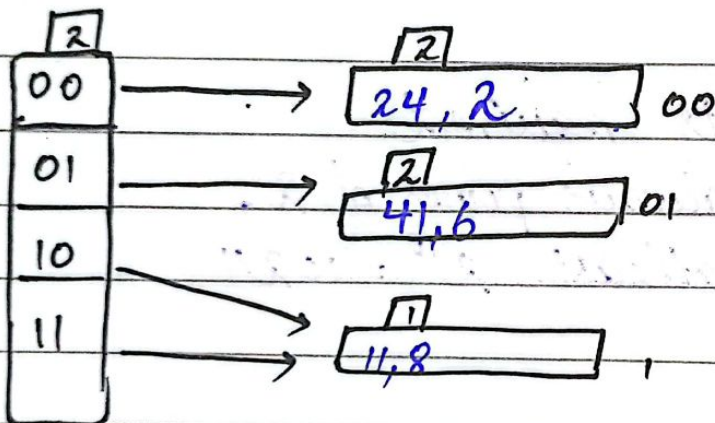
$$24 \bmod 12 = 0000$$

$$8 \bmod 12 = 1000$$

$$2 \bmod 12 = 0010$$

$$41 \bmod 12 = 0101$$

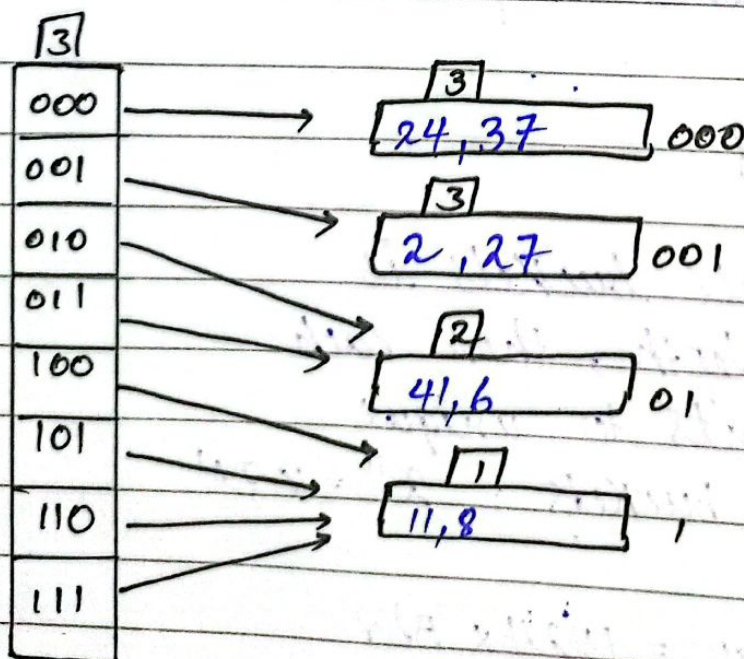
split 0



$$6 \bmod 12 = 0110$$

$$37 \bmod 12 = 0001$$

split 00

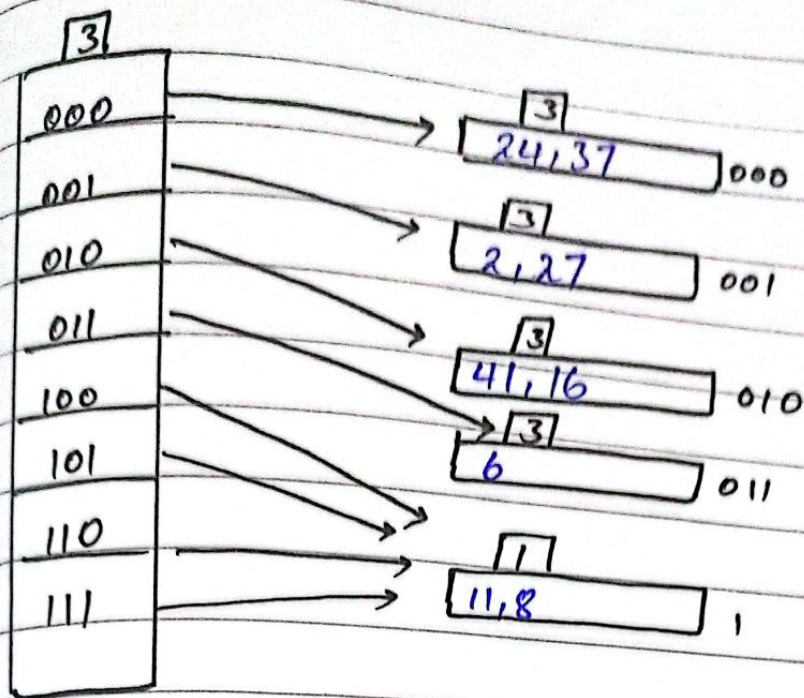


$$27 \bmod 12 = 0011$$

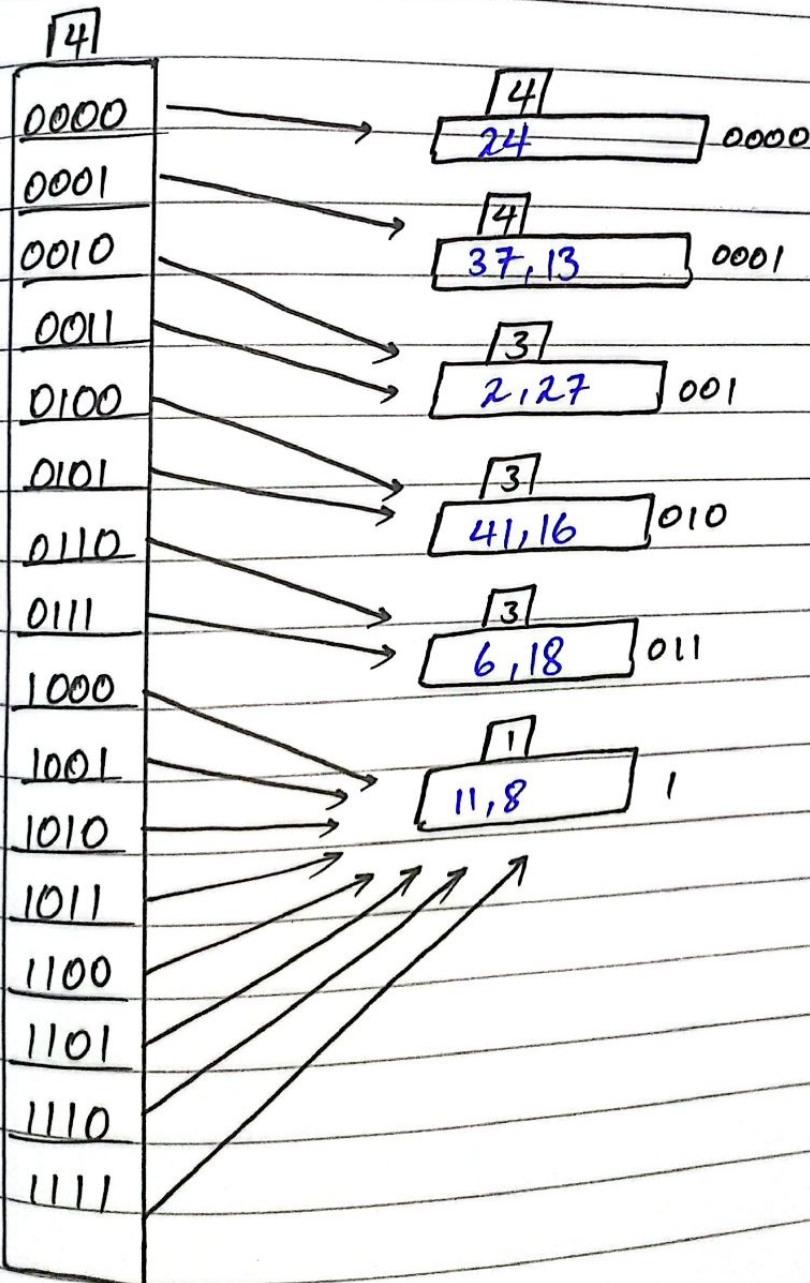
$$16 \bmod 12 = 0100$$

split 01





13 mod 12 = 0001  
split 000



18 mod 12 = 0110

Completed



### Q3 Extendible hash.

$$T = 100,000$$

$$R = 16 + 16 = 32 \text{ bytes}$$

$$B = 4096 \text{ bytes}$$

(a) lowest possible global depth.

$$Bfr = \left\lfloor \frac{B}{R} \right\rfloor = 128$$

$$b = \left\lceil \frac{T}{Bfr} \right\rceil = 782 \text{ buckets}$$

Atleast 782 buckets required.

Since directory is always power of 2, so it will have atleast  $2^{10} = 1024$  entries.

So lowest possible global Depth = 10

(b) Average occupancy.

If local depth of all buckets is same as global depth, then each directory entry points to unique bucket so total buckets =  $2^{10} = 1024$

$$\text{They will have capacity} = 1024 \times Bfr$$

$$= 1024 \times 128$$

$$\text{Total capacity} = 131072$$

$$\text{Avg occupancy of bucket} = \frac{100,000}{131072} \times 100 = 76.29\%$$