

ANN Using Back Propagation

```
import numpy as np
```

```
# Sigmoid function and its derivative
```

```
def sigmoid(x):
```

```
    return 1 / (1 + np.exp(-x))
```

```
def sigmoid_derivative(x):
```

```
    return x * (1 - x)
```

```
# Backpropagation training algorithm
```

```
def train_backpropagation(X, y, hidden_neurons, epochs, learning_rate):
```

```
    input_neurons = X.shape[1]
```

```
    output_neurons = y.shape[1]
```

```
# Initialize weights and biases
```

```
weights_input_hidden = np.random.rand(input_neurons, hidden_neurons)
```

```
weights_hidden_output = np.random.rand(hidden_neurons, output_neurons)
```

```
bias_hidden = np.random.rand(hidden_neurons)
```

```
bias_output = np.random.rand(output_neurons)
```

```
for epoch in range(epochs):
```

```
    # Forward pass
```

```
    hidden_layer_input = np.dot(X, weights_input_hidden) + bias_hidden
```

```
    hidden_layer_output = sigmoid(hidden_layer_input)
```

```

    output_layer_input = np.dot(hidden_layer_output, weights_hidden_output) +
    bias_output

    predicted_output = sigmoid(output_layer_input)

    # Backward pass
    error = y - predicted_output
    d_predicted_output = error * sigmoid_derivative(predicted_output)

    error_hidden_layer = d_predicted_output.dot(weights_hidden_output.T)
    d_hidden_layer = error_hidden_layer * sigmoid_derivative(hidden_layer_output)

    # Update weights and biases
    weights_hidden_output += hidden_layer_output.T.dot(d_predicted_output) *
    learning_rate
    weights_input_hidden += X.T.dot(d_hidden_layer) * learning_rate
    bias_output += np.sum(d_predicted_output, axis=0) * learning_rate
    bias_hidden += np.sum(d_hidden_layer, axis=0) * learning_rate

    if epoch % 100 == 0:
        print(f"Epoch {epoch} error: {np.mean(np.abs(error))}")

    return weights_input_hidden, weights_hidden_output, bias_hidden, bias_output

# Example usage: training XNOR gate
X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
y = np.array([[1], [0], [0], [1]]) # XNOR gate output

hidden_neurons = 2

```

```
epochs = 10000
```

```
learning_rate = 0.1
```

```
weights_input_hidden, weights_hidden_output, bias_hidden, bias_output =  
train_backpropagation(  
    X, y, hidden_neurons, epochs, learning_rate)
```

```
# Testing
```

```
def predict_backpropagation(input_data, weights_input_hidden, weights_hidden_output,  
    bias_hidden, bias_output):
```

```
    hidden_layer_input = np.dot(input_data, weights_input_hidden) + bias_hidden
```

```
    hidden_layer_output = sigmoid(hidden_layer_input)
```

```
    output_layer_input = np.dot(hidden_layer_output, weights_hidden_output) + bias_output
```

```
    predicted_output = sigmoid(output_layer_input)
```

```
    return predicted_output
```

```
# Test the network with new inputs
```

```
test_input = np.array([1, 0])
```

```
prediction = predict_backpropagation(test_input, weights_input_hidden,  
    weights_hidden_output, bias_hidden, bias_output)
```

```
print(f"Prediction for {test_input}: {prediction}")
```