

Inverse Document Frequency :-

$$S_1 \Rightarrow \log(3/2) \Rightarrow \text{sunshine} \Rightarrow 0.176 \Rightarrow 0.18$$

$$\log(3/4) \Rightarrow \text{state} \Rightarrow 0.18$$

$$\log(3/1) \Rightarrow \text{enjoy} \Rightarrow 0.48$$

$$\log(3/9) \Rightarrow \text{fox} \Rightarrow 0.18$$

$$\log(3/4) \Rightarrow \text{jump} \Rightarrow 0.48$$

$$\log(3/4) \Rightarrow \text{brown} \Rightarrow 0.48$$

$$\log(3/2) \Rightarrow \text{run} \Rightarrow 0.18$$

$$\log(3/1) \Rightarrow \text{fast} \Rightarrow 0.18$$

$$\log(3/0) \Rightarrow \text{high} \Rightarrow 0$$

TF-IDF Table :-

	Brown	enjoy	fast	fox	high	jump	run	state	sunshine
S_1	0	0.12	0	0	0	0	0	0.04	0.08
S_2	0.14	0	0	0.1	0.01	0.06	0.09	0	0
S_3	0	0	0.09	0.03	0	0	0.03	0.03	0.03

(Cosine Similarity)

$$S_1 \cdot S_3 \Rightarrow 2 \times 1 + 1(1) + 1(0) + 0 + 0 + 0 + 0 + 0 + 0$$

$$= 3$$

$$|S_1| \Rightarrow \sqrt{4+1+1+0+0+0+0+0+0} = \sqrt{6} \Rightarrow 2.449$$

$$|S_3| \Rightarrow \sqrt{1+1+0+0+1+0+0+1+1} = \sqrt{5} \Rightarrow 0.236$$

$$\cos(S_1, S_3) \Rightarrow \frac{S_1 S_3}{|S_1| |S_3|}$$

$$|S_1| |S_3|$$

$$\cosine \Rightarrow \frac{3}{3}$$

$$(2.449)(2.238)$$

$$\Rightarrow 0.54735$$