

Q1- Draw a PDA for the set of all the strings of the form $0^a 1^b 0^c$ such that $a+c=b$?

Q2-a Write regular expressions for the following languages over the alphabet $\Sigma = \{a, b\}$:

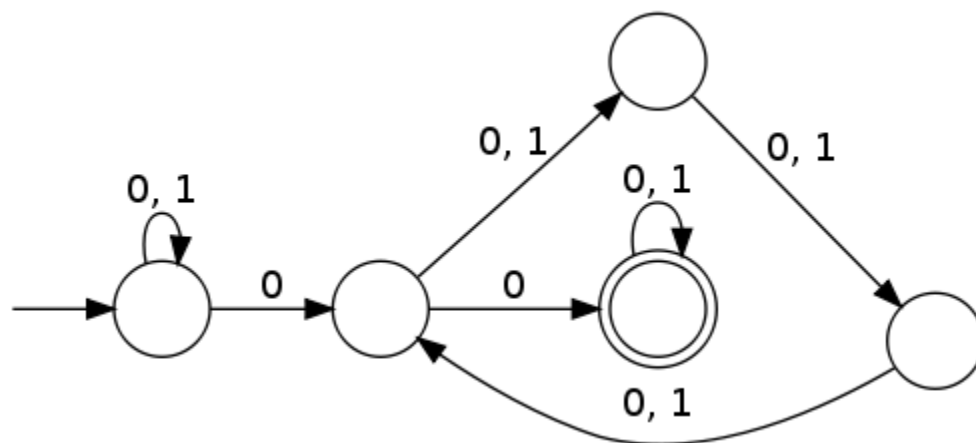
All strings that do not end with aa.

All strings that contain an even number of b's.

All strings which do not contain the substring ba

Q2-b Draw DFAs for each of the languages from Q2-a. None of your DFAs may contain more than 4 states.

Q3- Consider the following non-deterministic finite automaton (NFA) over the alphabet $\Sigma = \{0, 1\}$.



Q3-a: Give a one-sentence description of the language recognized by the NFA. Write a regular expression for this language.

Q4- For each of the following languages over the binary alphabet, determine whether it is context-free and prove your answer:

4a: $\{wvw : w \in \{0,1\}^+, v \in \{0,1\}^*\}$

4b: $\{0^n 1^m 0^k 1^{n+m} : n, m, k \geq 0\}$

4c: Palindromes with equally many 0's and 1's

Q7(a)- Construct an equivalent grammar that does not contain chain rule?

G:

$S \rightarrow AS|A$

$A \rightarrow aA|bB|C$

$B \rightarrow bB|b$

$C \rightarrow cC|B$

Q7(b)- Construct an equivalent grammar without useless symbols?

G:

$S \rightarrow aA|BD$

$A \rightarrow aA|aAB|aD$

$B \rightarrow aB|aC|BF$

$C \rightarrow Bb|aAC|E$

$D \rightarrow bD|bC|b$

$E \rightarrow aB|bC$

$F \rightarrow aF|aG|a$

$G \rightarrow a|b$