

University of Engineering & Technology Peshawar

Programme: B.Sc. Computer Systems Engineering

Semester: 3rd Semester

Paper: Digital Logic Design

Date: January 6, 2021

Exam Type: Midterm

Allowed Time: 120 Minutes	Max Marks: 30
Student's Name:	Student's Registration: pwcse1801
Student's Signature:	

Instructions:

- 1- This exam is OPEN books/notes/Internet.
- 2- Sharing of books, notes and other materials during this exam is not permitted.
- 3- Answer ALL questions.
- 4- There are 9 questions in total. Some questions are harder than others. Answer the easy ones first to maximize your score.
- 5- Questions will not be interpreted during the exam.

Q. 1 Convert decimal +61 and +27 to binary using the signed-2's complement representation and enough digits to accommodate the numbers. Then perform the binary equivalent of $(+27) + (-61)$, $(-27) + (+61)$ and $(-27) + 61$. Convert the answers back to decimal and verify that they are correct.

1)

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Question

No

1

Convert to binary First

$$+61 = 0011101$$

$$+27 = 0001011$$

One's Complement of +61 is

$$11000010$$

$$+1$$

$$2's \text{ complement} \rightarrow 11000011 = (-61)$$

One's Complement of +27

$$11100100$$

$$+1$$

$$2's \text{ complement} 11100101 = (-27)$$

$$+27 = 00011011$$

$$-61 = 11000011$$

$$1101110$$

To verify again 2's Complement of

2)

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To verify take 2's complement
again 11011110

$$\begin{array}{r} 1's \text{ Complement} \quad 00100001 \\ \hline 1 \\ \hline 00100010 \end{array}$$

Verified $(00100010)_2 = (34)$
 $\ln (27) - (64) = (34)$

And

$$\begin{array}{r} -27 \\ +64 \\ \hline \end{array} \quad \begin{array}{r} = 11100101 \\ 00111101 \\ \hline 100100010 \end{array} = (34)$$

3)

And

$$\begin{array}{r} -27 \\ -61 \\ \hline \end{array} = \begin{array}{r} 11100101 \\ 11000011 \\ \hline 11010100 \end{array}$$

Again 2's Complement to verify

$$\begin{array}{r} 01010111 \\ 1 \\ \hline 01011000 \end{array} = (48)$$

$$(-27) + (-61) = (-88)$$

Hence verified

Q. 2 At the least how many bits are needed to represent -18 (read as 3 minus 18) in

- i. Sign-magnitude system
- ii. 1's complement system
- iii. 2's complement system

4)

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Question No 2

i) Sign magnitude System

$$-18 = 110010$$

ii) 1's Complement System

$$\begin{array}{l} 1's \text{ complement of } 18 \\ = \\ 001101 \end{array}$$

iii) 2's Complement System

2's Complement of 18

$$\begin{array}{r} = 001101 \\ \underline{1} \\ 001110 \end{array}$$

Required bits at least:-

In all system 6 bit at least represent -18

Q. 3 In the following table fill the column B with an appropriate decimal 2 number corresponding to the equivalent unsigned binary number given in column A.

Column A	Column B
000	0
001	1
010	3
011	3
100	4
101	5
110	6
111	7

Q. 4 In the following table fill the column B with an appropriate decimal 2 number corresponding to the equivalent 1's complement number given in column A.

Column A	Column B
000	+0
001	+1
010	+2
011	+3
100	-3
101	-2
110	-1
111	-0

Q. 5 In the following table fill the column B with an appropriate decimal 2 number corresponding to the equivalent 2's complement number given in column A.

Column A	Column B
000	+0
001	+1
010	+2
011	+3
100	-4
101	-3
110	-2
111	-1

Q. 6 From the following truth table, directly write the Boolean expression for:

4

i. $F(A,B,C)$ in both the canonical forms.

ii. $\overline{F(A,B,C)}$ in both the canonical forms.

A	B	C	F
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	0

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Question No 6

i) $F(A,B,C)$ in both the canonical form are

1's in Function (F) represent the minterm and 0's the maxterm

Minterm:-

$$F(A,B,C) = \sum m(2, 3, 4, 6)$$

$$F(A,B,C) = m_2 + m_3 + m_4 + m_6$$

Maxterm:-

$$F(A,B,C) = \prod (0, 1, 5, 7)$$

$$F(A,B,C) = M_0 M_1 M_5 M_7$$

ii) $\overline{F(A,B,C)}$ in both form

In this case 0's represent minterm and 1's represent maxterm.

Minterm:-

$$\overline{F(A,B,C)} = \sum (0, 1, 5, 7)$$

$$= m_0 + m_1 + m_5 + m_7$$

Maxterm:-

$$\overline{F(A,B,C)} = \prod (2, 3, 4, 6)$$

$$= M_2 M_3 M_4 M_6$$

Q. 7 Write the truth table for the following Boolean expression/function:

2

$$F(A,B,C) = \bar{B}.C + A.(\bar{B}+C) + \bar{A}.\bar{C}$$

A	B	C	F
0	0	0	1
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

Q. 8 The following gates are available and the unit price is also listed.

4

- Price of 3-input AND gate = \$ 2/-
- Price of 2-input OR gate = \$ 2/-
- Price of NOT gate = \$ 1/-

Implement the following Boolean function using the above gates. Draw its logic diagram and calculate its cost.

$$F(X,Y,Z) = \sum m(1, 7)$$

6)

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Question No 8

3-input AND gate = \$2/-

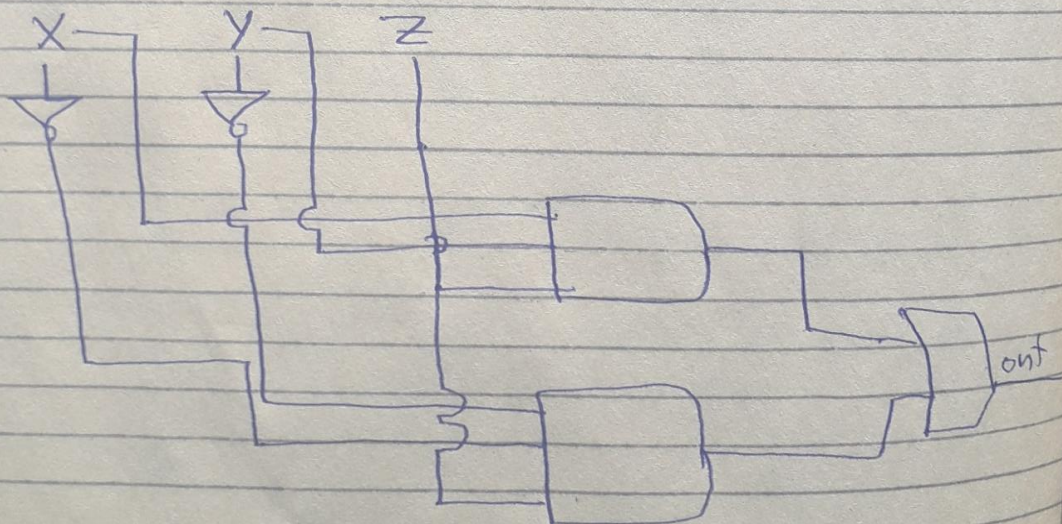
2-input OR gate = \$2/-

Not gate = \$1/-

$$F(X, Y, Z) = \sum_m(1, 7)$$

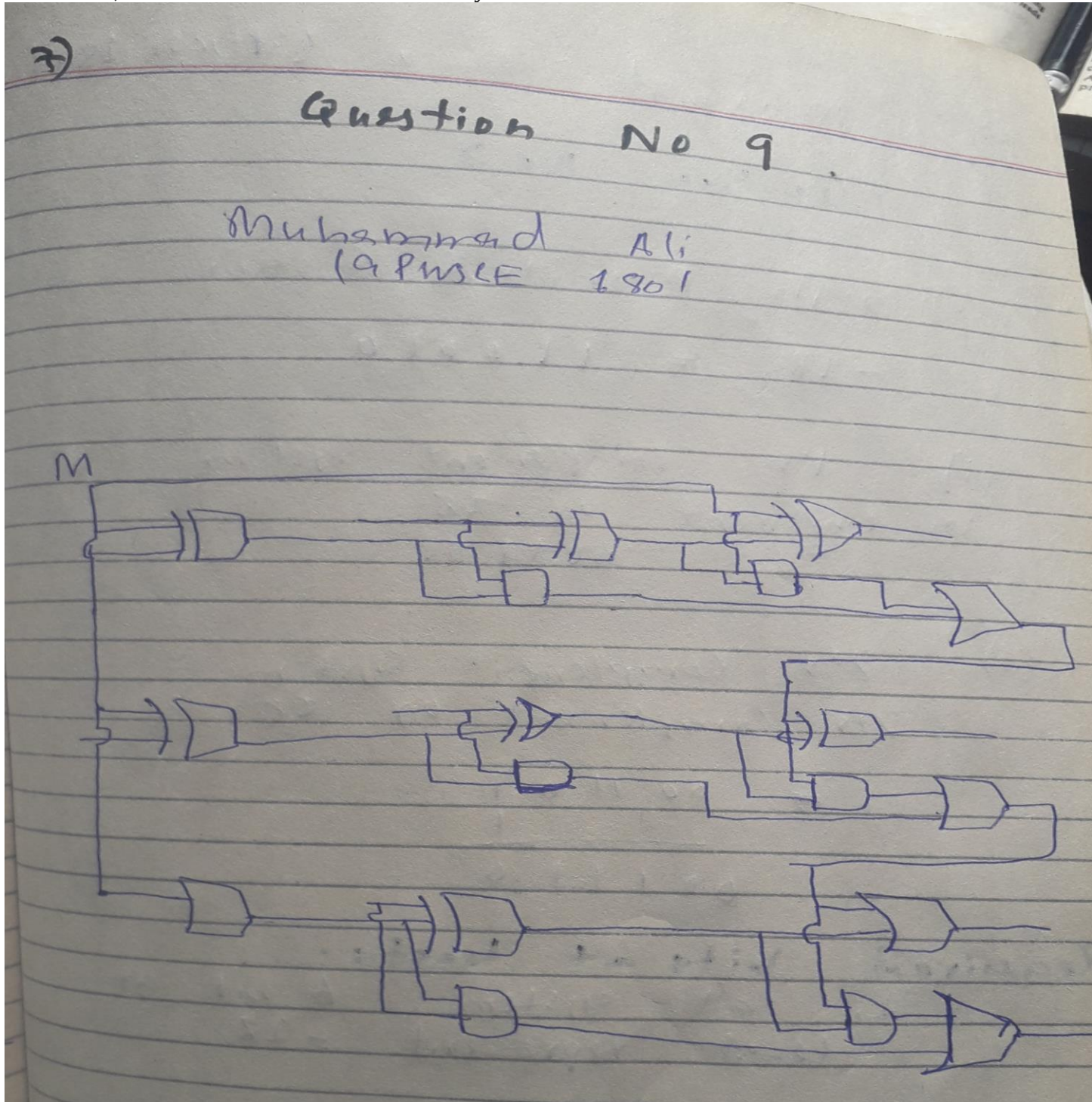
$$\begin{aligned} F(X, Y, Z) &= m_1 + m_7 \\ &= X'Y'Z + XYZ \end{aligned}$$

Logic diagram :-



Cost = 8 \$

Q. 9 Design a 3-bit adder-subtractor circuit using 1-bit binary Full adders and 5 any necessary additional logic gates. The circuit has a mode/control input bit, M , that controls its operation. Specifically, when $M=0$, the circuit becomes a 3-bit adder, and when $M=1$, the circuit becomes a 3-bit subtractor that performs the operation A plus the 2's complement of B , where A and B are two 3-bit binary numbers.



<This page is intentionally left blank. This page can be used for scratch work or as extra space. If you write work here that you want me to grade, be sure to clearly indicate which question(s) the work corresponds to!>