

Date March 10th, 2022

IPO

↓
first time = initial public offering
offering shares

SEO

↓
second and so = seasoned equity offering
on time offering
shares

Session II

from pandas - datareader import
date as web
read from web
take this data
from this website
• msft = web.Datareader('MSFT', 'yahoo', '2012-0-01',
'2013-12-30')

Shifting and lagging time-series data:

msft
Jan 1 '12
Jan 2 '12
Jan 3 '12
each time series

↓
msft remains same but time period
is changing, dates.

cross-sectional data: msft changes but date remains

msft same
Jan 1 '12

Pandas: panel data analysis

↓
where both time-series + cross sectional data

1.063

1.065

Date

Shifting time series

• Shift - forward = $\text{myTAC} = \text{myT} ['Adj' \text{ Close}']$
 $\text{myTAC}.\text{shift}(1) \rightarrow$

2012-01-03	1	-01-03	NaN
04	2	01-04	1
05	3	01-3	2

last value gets lost.

• Shift - backward = $\text{myTAC}.\text{shift}(-2)$
 (2 indices back)

2012-01-03	1	2012-01-03	3
-04	2	-04	
-05	3	-05	

• Shift - 1sec = $\text{myTAC}.\text{shift}(1, \text{freq} = 'S')$
 (shift from 1 sec forward)
 (no value lost, no NaNs)

Theory

Investors

Return ↑
 Risk ↓

net return: when we subtract -1 from returns val
 gross return: own investment + profit

Google

Jan - 1 - 2022 → \$10
 - 2 - → \$11
 - 3 - → \$11.5
 - 4 - → \$10.25
 - 5 - → \$12

returns
 $-1 = 0.1$
 $\frac{11}{10} = 1.1$
 $\frac{11.5}{10} = 1.045$
 $\frac{10.25}{11} = 0.89$
 $\frac{12}{10.25} = 1.17$

we standardise using ratios
 we can see return on our \$1 investment

$1.1 \times 1.045 \rightarrow 1.1495$

$1.1495 \times 0.89 \rightarrow 1.023$

$1.023 \times 1.17 \rightarrow 1.197 - 1$

$\frac{12}{10} = 1.2$

cumulative Product

+ 0.1
 + 0.45
 - 0.11
 + 0.17

0.205

→ cumulative return

1.1 means yesterday the share had \$1 now today it's has \$1.1 worth

Date	Return	Net return	
1-Jan-22	→ \$10 → 10	0	
2	→ 11 → $\frac{11}{10} = 1.1$	-1 = 0.1	Cum product
3	→ 11.5 → $\frac{11.5}{11} = 1.045$	-1 = 0.045	$1.1 \times 1.045 = 1.1495$
4	→ 10.25 → $\frac{10.25}{11.5} = 0.89$	= 0.11	$1.1495 \times 0.89 = 1.023$
5	→ 12 → $\frac{12}{10.25} = 1.17$	+ 0.17	$1.023 \times 1.17 = 1.197$
		0.205	$1.197 - 1 = 0.197 \approx 0.2$
	$\frac{12}{10} = 1.2$	cumulative return	

- $\text{mftAC} / \text{mftAC.shift}(1) \rightarrow$ first shift

Then divide

10		NaN		NaN
11	shift	10	÷	11 / 10
11.5	→	11	→	11.5 / 11
10.25		11.5		10.25 / 11.5

- $\text{np.cumprod}(\text{mftAC} / \text{mftAC.shift}(1)) \rightarrow$ gives value of ^{at last date} ~~100~~ \$1 that was invested on Jan 1st
 ↓
 cumulative product

- can plot cumprod and compare investment strategies of diff companies

• $\text{net return} = \text{mft} / \text{mft.shift}(1) - 1$

$\text{net return.asfreq('H')} \rightarrow$ gives hourly

12am 1.12

1am NaN

2am NaN

• $\text{asfreq('H', method='ffill')}$

Jan 1 12am 1.12
 1am 1.12
 2am 1.12

Date March 30th, 2022.

Resampling of time series:

DIY

New NB

Technical Analysis → which stock to buy + which to sell.
• finding pattern in charts/graphs
+ determine which stocks to buy or sell

find undervalued stocks + investing in them = Fundamental Accounting

\$10 item is undervalued to \$8, you buy it after you research that \$10 is true value so it will converge to \$10 + it will give profit of \$2.

cc = 'BTC - USD' → bitcoin USD

tickers = ['GOOG', 'AMZN', 'AAPL']

plt.figure(figsize=(12, 8))

ax1 = plt.subplot2grid((1, 1), (0, 0), rowspan=4, colspan=1,
title='Amazon')

ax2 = " ((7, 1), (4, 0), = 3, = 1, sharex=ax1
5

ax1.plot(data['Adj Close'], label='Price')

ax2.bar(data.index, data['Volume'], label='Volume')

ax1.legend()

ax1.legend(loc='upper right')

plt.show

Date

- import matplotlib.dates as mdates

- Jan 2020 → Sept 2020 trend analysis

Sept
Jan

→ almost 78% return

- 1.78 → \$1 in Jan is now of worth \$1.78 in Sept

Moving Averages: → to smooth out fluctuations in graphs (prices)

→ first 20's mean

data['SMA 20'] = data['Adj Close'].rolling(20).mean()

"['120'] = "

.rolling(120).mean()



SMA 20 surpasses/exceeds

↓
shorter trend

↑
longer trend

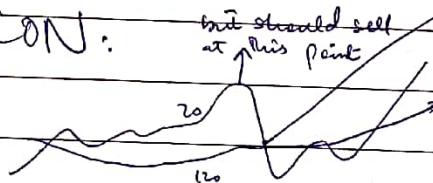
SMA 120

→ signal = buy

hold it till till 20 > 120

when 120 > 20 almost, sell it + make profit

CON:



- investors are demanding more + more shares

- buying pressure

- price goes up so

buying signal not

in near future price will go up

- Buy + hold is better than SMAs

- but in moving avg you note SMAs do better than buy + hold

data = data.drop(columns = ['High']) → remove unneeded cols

Date

- Shift vols of Adj Close
- $\frac{24.7}{24.9}$ after shift 03-01 - $\frac{24.9}{24.9}$ after shift 02-01 \rightarrow -ve value Tells loss
- after shift 02-01 $\frac{24.9}{24.9}$

March 31st, 2022.

$$\frac{24.7}{24.9} \rightarrow 0.99 \rightarrow \text{daily return} \rightarrow \text{\$1's worth}$$

`data['invested-SMA'] = np.where(data['SMA20'] > data['SMA20'], 0, 1)`

`data[data['invested-SMA'] == 1]`

\downarrow
we want cumulation in this frame of time

\$1 grow from \$1 to \$2.9

a	a	} cumulative return
b	$a \times b = c$	
d	$c \times d = e$	
f	$e \times f = g$	

Buy + hold strategy

`data['buy-hold'] = np.cumprod(data['change'])`

\$1 grew from \$1 to \$4.8 in example

so, buy + hold is better than SMA. maybe he gives $1 \times 2 \times$ but SMA would multiple buys + sells so more time paid

we find cempod of all data
so we can plot it & see the
graph - if we do $\frac{2012}{2011}$ then gives
only one value.
vining avg:

only one value

in notebook - gives values from start not from row 20 or 120 like SMA.

$EWM_{12} > EWM_{26}$ $\frac{1}{2}$ buy
 \leq sell

\$1 to \$7 \rightarrow cumulative product

- EWM better than buy + hold which is better than SMA for AAPL only. It varies for every firm.
- Example comparison of Amazon, coke, Tesla, USFT, apple in notebook

MPT = modern portfolio theory
Harry Markowitz (1952)

William Sharpe (1964)

April 6th, 2022

μ population parameter

\bar{x} sample statistic

Probabilistic Model

$$E(R_A) = 15\%$$

exp. return
of A

Prob.

q

stock returns

P_i

X_i

$P_i X_i$

0.1

30%

3%

0.2

25%

5%

0.4

18%

7.2%

0.2

-10%

-2%

0.1

-25%

-2.5%

$$\text{Std. deviation} = \sqrt{\frac{\sum (X_i - \bar{X})^2}{N-1}}$$

of small sample
space + not
population

↓

if population?
then 'N'

'N'

μ

\bar{x}

30%

25%

18%

we do N-1 to
decrease denominator
+ increase variance
which decreases
biasness in sample.

↓
underestimation

average

expected
return

we don't divide

by 5 cuz that

would mean

we give equal

weight to all

returns which

is wrong

- if we have past returns + not probabilistic returns then we take avg of past returns

$$E(R_{\text{Tesla}}) = 15\%$$

$$\sigma_{\text{Tesla}} = 17\%$$

$$E(R_{\text{BoA}}) = 10\%$$

$$\sigma_{\text{BoA}} = 9\%$$

- investing in BoA because less risk (9%) = conservative approach
can't tolerate higher risk
- investing in Tesla cuz more exp. return but = risk tolerance
more risky
- make portfolio: contains shares of proportion (different risk)
of both BoA + Tesla (aversion levels)
= Diversification

simple finance : Return & Risk
 Portfolio: no compromise on return
 + decrease risk

Date

Portfolio Scenario

60% investment in Tesla, 40% in BofA

→ weight

$$E(R_p) = W_{Tesla} \cdot E(R_{Tesla}) + W_{BoFA} \cdot E(R_{BoFA})$$

$$= 60\% \cdot 15\% + 40\% \cdot 10\%$$

$$Cov = \sigma_T \cdot \sigma_{BoFA} \cdot \text{corr}_{T,BoFA}$$

$$\sigma_p^2 = W_T^2 \cdot \sigma_T^2 + W_{BoFA}^2 \cdot \sigma_{BoFA}^2 + 2 W_T W_{BoFA} Cov$$

$$= 60\% \cdot 17\% + 40\% \cdot 9\%$$

can be replaced by correlation T/BoFA

covariance: what happens to the other variable when 1st variable changes

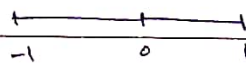
pos covariance

GPA	# hours
1.1	1
2.3	2
3.0	3
3.5	5

pos

pos

correlation:



if return of 1st inc. by 1%
 one firm's return dec. by 1%
 other's return weak

pos relation
 one ↑ and ↑ by 1%
 by 1%
 Strong

Example: covariance

has no definition so value of 900 can't tell

if relation b/w variable is strong or weak

Correlation tells us about relationship b/w variables.

- In σ_p^2 , if cov. is pos then risk is decreased

$$E(R_p) \uparrow \quad \sigma_p^2 \downarrow$$

This is why portfolio is better than investing only in Tesla or BoFA

- If we change weights, exp. return, & σ_p^2 changes as well so this tells we can make infinite portfolios. It is crucial to find best portfolio.

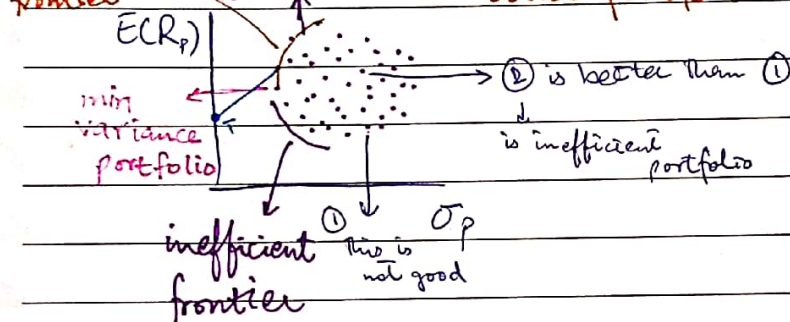
Date April 7th, 2022.
3 firms

Assigned
weighted moving avg
simple moving avg
long + hold
for any 1 firm

$$\sigma_p^2 = W_T^2 \cdot \sigma_T^2 + W_{BAC}^2 \cdot \sigma_{BAC}^2 + W_{AAPL}^2 \cdot \sigma_{AAPL}^2 + 2 W_T \cdot W_{BAC} \cdot \text{cov}_{T, BAC} + 2 W_T \cdot W_{AAPL} \cdot \text{cov}_{T, AAPL} + 2 W_{BAC} \cdot W_{AAPL} \cdot \text{cov}_{BAC, AAPL}$$

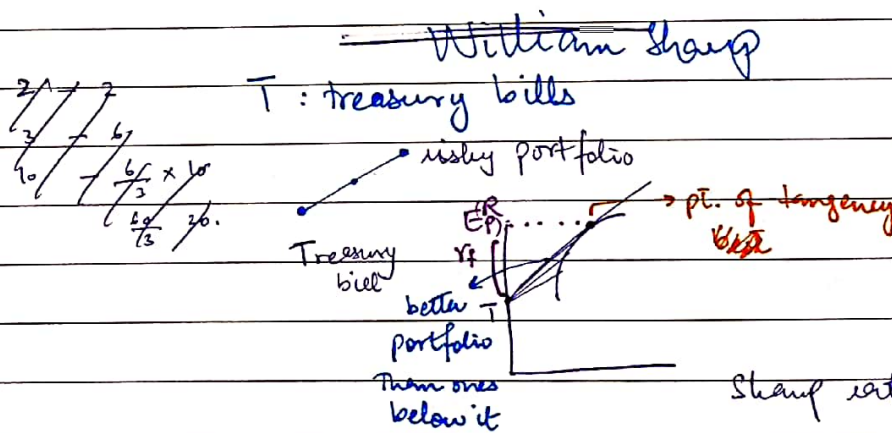
- covariance tells us more about risk.

If 10 firms, 10 W_s and 90 covs
min variance frontier efficient frontier better portfolios
more imp!



- investors are interested in maximising return + minimising risk

- from min variance frontier investors choose portfolio which falls in their preferred risk. Risk aversion level



$$\text{Sharpe ratio} = \frac{E(R_p) - r_f}{\sigma_p} \rightarrow \text{risk free rate} = 1.3$$

Sharpe ratio at tangent line of portfolios is higher

for every 1 unit of std. your return ↑ 1.3 above risk premium

Date April 13th, 2022.

Variance Covariance Matrix

	W_A A	W_B B
W_A A	$W_A \cdot W_A = W_A^2$ $\sigma_A \cdot \sigma_A = \sigma_A^2$	$W_A \cdot W_B$ $\sigma_A \cdot \sigma_B$ $\text{Cov}_{A,B}$
W_B B	$W_B \cdot W_A$ $\sigma_B \cdot \sigma_A$ $\text{Cov}_{A,B}$	$W_B \cdot W_B = W_B^2$ $\sigma_B \cdot \sigma_B = \sigma_B^2$

In covariance
self variance
A's A's

.	.
.	.
.	.
.	.
.	.
25	25

- variance

when we calculate
A's covariance w/
A it's equal to
variance of A

Date Portfolio Optimization

- $\text{returns} \rightarrow \text{pct_change}()$
- random weights
 $\text{np.sum(random weights)}$
- $\text{returns.mean}() \rightarrow$ investing \$1 will give return \$0.002 on daily returns
- sharp ratio maximum = best portfolio

$$E(R_p) = \text{daily mean return}_T * \text{weight}_T + \text{dMR}_{BAC} * w_{BAC}$$

$$\left(\begin{aligned} &= 0.001428 \rightarrow \$1 \text{ will give } \$0.0014 \text{ return} \\ &\text{np.sum(returns.mean * weights)} \end{aligned} \right)$$

$$* 252 = 0.36$$

(stock market is open)
for days in a year

- \$1 investment gives \$0.36 returns annually when user invests 0.528 in T and rest in BAC.
0.472

36% per annum

- $\text{returns.cov}()$ ← covariance matrix

- weights.T

Date April 20th, 2022

$$\text{sharpe} = \frac{\text{return}}{\text{std (risk)}}$$

$$\sigma_P^2 = W_A^2 \sigma_A^2 + W_{A1}$$

↑
variance

$\sigma^2 \rightarrow$ gives standard deviation/risk

annual return 0.31
risk 0.32

New year return is going to be 0.31

\$100 \rightarrow to 0.31 \$31

~~actual returns could deviate~~

 ~~$31\% + 32.8\% = 64\%$ by 0.32~~ ~~$31\% - 32.8\% = -1.5\%$~~

- std + variance both are measures of spread / dispersion so both can be used for i.i.d.

but std is used in diff.
in interpretation.

variance units in square
so difficult -

Example: $E(\text{GPA}) = 3.3$

data points

$$\sigma = 0.3$$

$\sigma = 0.5 \rightarrow$ spread / deviation

$$\left[\begin{array}{c} 1 \\ 1 \\ 1 \\ 1 \end{array} \right]$$

↓
mean = 3.3

equal to $E(4PA)$

$$3 \cdot 3 + 0 \cdot 5 = 3 \cdot 8$$

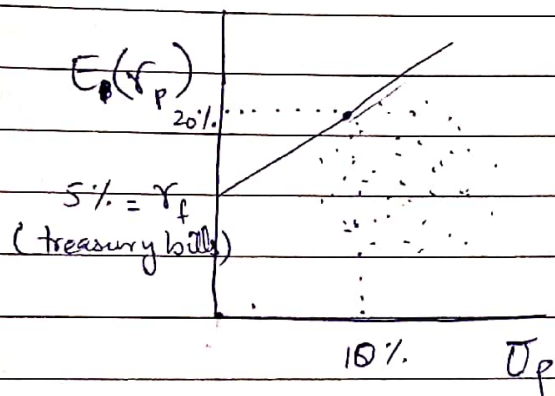
$$3 \cdot 3 - 0 \cdot 5 = 2 \cdot 8$$

Date April 21st, 2022.

risk free rate

annual return - risk free rate

$$\text{Sharpe ratio} = \frac{\text{annual return} - r_f}{\text{portfolio std}}$$



$$\frac{E(r_p) - r_f}{\sigma_p}$$

risk premium: use ^{getting} ~~willing~~
 \uparrow * return cuz he
 willing to
 take 10%
 risk

$$= \frac{20 - 5}{10} = 1.5 = 1.5\%$$

interpret ¹⁰ consider it
 as 1
 interpret ¹⁰ consider it
 for numerator

minimum risk / variance portfolio:
 having the minimum risk
 in datapoints

1% risk \rightarrow return increases
 increase by 1.5%

1% risk \rightarrow return by 1.2

1.5% one is better portfolio