

# Comparison of Outlier Detection between Statistical Method and Undercomplete Autoencoder

Muhammad Ayaz Hussain, University of  
Saif ur Rahman, University of  
Ioannis Iossifidis, University of  
Christian Klaus, University of

This paper is concerned about the analysis of power consumption data and the comparison of the performance between statistical method and undercomplete autoencoder in the determination of outliers in that given dataset. Firstly, the raw data was analyzed and a feature vector was constructed. Secondly, Tukey's test was implemented on this feature vector to determine the outliers. Finally, an undercomplete autoencoder was also used to detect outliers and the efficiency of both methods (statistical method and undercomplete autoencoder) were compared.

## 1. INTRODUCTION

In modern days, the amount of energy consumption is becoming a more serious issue as several companies and industries are addressing this issue in order to contain their expenses as unexpected variations can incur additional operational costs to their facilities. These fluctuations in electricity consumption can arise from various factors such as excessive use of heavy equipment like electric heaters in winters, room coolers during the summers etc. In order to detect and classify unusual amount of power consumption, outlier detection algorithm is designed and implemented on the provided data and compared its classification efficiency against a semi-supervised autoencoder. Presently, it is very difficult to predict the energy consumption anomalies precisely, since there are many factors influencing the energy usage, such as weather condition [Wang et al. 2012], occupancy [Pan et al. 2007] and operation of appliances [Chenglei et al. 2015; Royapoor and Roskilly 2015]

## 2. RELATED WORKS

There is a sizable literature regarding semi-supervised learning methods on big data, with some relating to power consumption such as, [Bhattacharjee et al. 2018] which also performed semi-supervised analysis to determine and counter data falsifications in power consumption which can be considered as anomalous power consumption. Since data falsification can range from individual customers tampering with the meter for electricity theft to certain groups orchestrating an attack against a rival company in a systematic manner compromising several meters, as their goals can be more complex than just electricity theft. For that, they proposed, a novel metric based on harmonic to the arithmetic mean ratios of daily power consumption. The ratios between harmonic and arithmetic mean remain highly stable over time as compared to just arithmetic mean. During various attacks, there is asymmetric growth(or decay) rates harmonic mean as compared to symmetric growth(or decay) rates of the arithmetic mean, which can help to infer the presence and type of falsification precisely. Their data consisted of real power consumption of 700 houses from Texas and 5000 houses from Ireland that belong to residential customers. One of the most important aspect of this work is that, it enables the quick identification of around or less than 10 days of monitoring, which is quite efficient as compared to pattern-based energy theft detector (CPBETD) which takes around 1 year, autoregressive moving average (ARMA) which took 1 month, or Entropy based method which also took 1 month.

Our statistical approach also deals with the analysis of power consumption data to find any short term anomalous readings, which performs quite well as more than 95%

anomalies were detected successfully using Tukey test (which uses arithmetic means and 1st and 3rd quartiles which is discussed in 3.2)

As far as the use of autoencoder for classification is concerned, those have been used in previous works for classification tasks such as [Fan et al. 2018] which used autoencoder based unsupervised anomaly detection method on a building energy data on a single facility which was in detail as 113 variables were considered which were generally classified into 4 distinct classes which are, (1) time variables (i.e., Month, Day, Hour, Minute and Day type); (2) outdoor variables (e.g., outdoor dry-bulb temperature and relative humidity); (3) operating parameters of the chiller plant (e.g., the temperatures and flow-rates of chilled water and condenser water); (4) energy variables (e.g., the total building cooling load and electricity consumption of the chiller plant).

Semi-supervised learning using Softmax classifier with sparse autoencoder for classification of water quality was used by [Yuan and Jia 2016]. Their dataset consisted of 60 unbalanced classification records, 100 training samples are generated for each water quality assesment grade. Their feature vector consisted of 14 representative features of water quality which were chemical oxygen demand (COD), dissolved oxygen (DO), total phosphorus (TP), 5-day biochemical oxygen demand (BOD5), NH3-N, NO3- N, oil, chlorophyll, PH, electrical conductivity (EC), turbidity, CL, total coliform (TColi) and temperature (T). They used 500 labeled training samples and 7,932 unlabeled records in all. Their proposed method method showed 98.8% accuracy which was greater as compared to other supervised algorithms such as Softmax classifiers, BP-NN, RBF-NN and SVM.

### 3. METHODOLOGY

#### 3.1. Data Preparation and Analysis

Initially, the raw data was provided by the company, which consisted of several entries. Those entries were obtained from the energy consumption data of 227 stores on 15 min basis for around 11 months as shown in the Figure 1. Analysis of Figure 1 shows that there is an obvious increase in power consumption during winters possibly due to the usage of electric heaters and an major drop in the power consumption around Christmas and New Year (just above January).

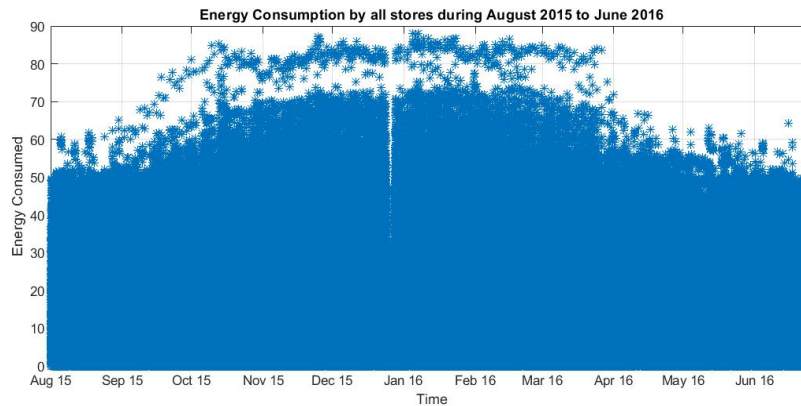


Fig. 1. Energy Consumption by all stores between August 2015 and June 2016

Afterwards, a random month is selected from the whole time period (in this case November 2015) for visualization and energy consumption of all stores is plotted as shown in Figure 2.

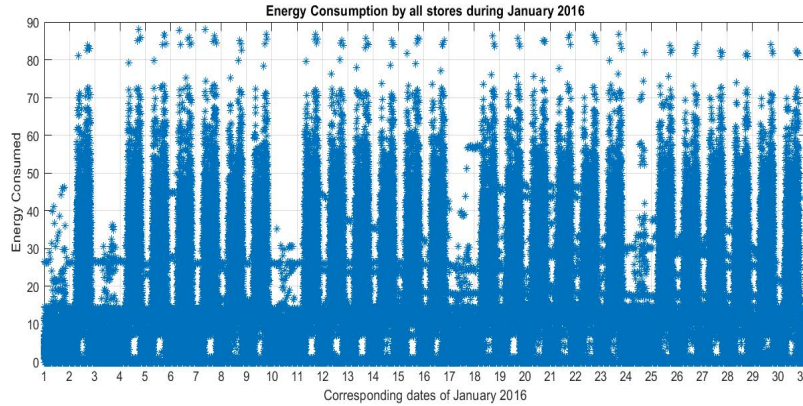


Fig. 2. Energy Consumption by all stores during January 2016

Still, it was difficult to pinpoint or visualize any single store from that plot. Therefore, a random store was chosen (in this case Store 105) for in depth analysis as shown in Figure 3.

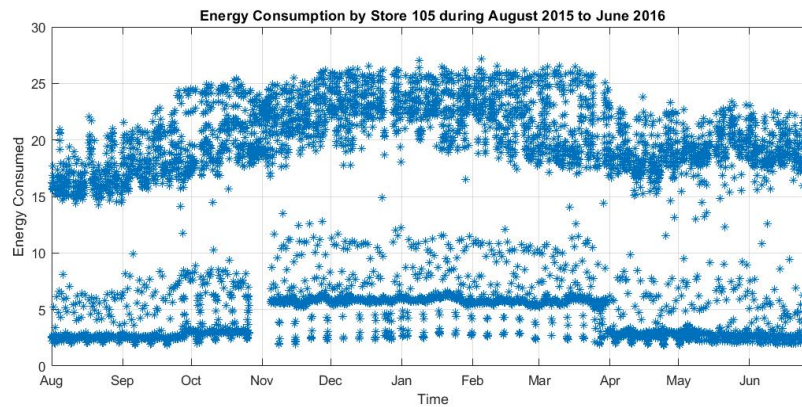


Fig. 3. Energy Consumption by Store 105 between August 2015 and June 2016

We can again see the noticeable increase in energy consumption during winter months from October till April as well as lower consumption during Christmas and New year holidays. Again, we used November which was randomly picked earlier to visualize the energy consumption by Store 105 as shown in Figure 4.

In order to select meaningful features to be implemented in Machine Learning or Statistical Modeling algorithms, it was necessary to analyze the given data thoroughly. After a comprehensive analysis, it was decided that the amount of energy consumption depends upon multiple factors, which are the store itself as all stores differs from

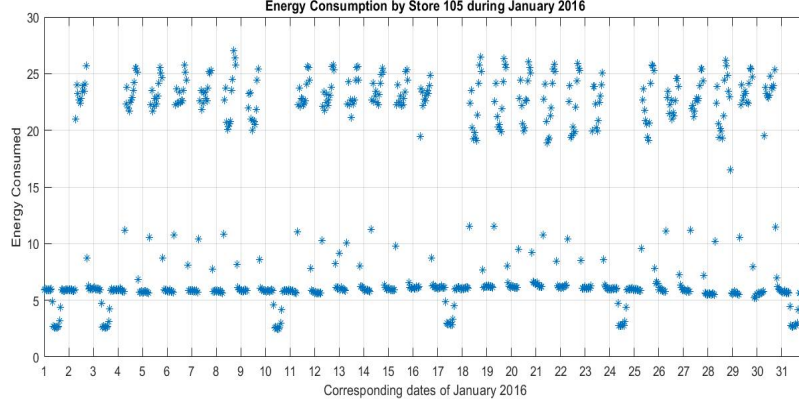


Fig. 4. Energy Consumption by Store 105 during January 2016

one another as each having its particular size, different number of energy consuming equipments and even have different geographical location which affect the amount of energy consumption. Aside from that, time of the day is another factor as during working hours energy consumption is higher. There is also a reduction in power consumption during the day even when the store is closed.

The data consisted of the energy readings from 227 different stores with 238 sensor values (as certain stores had multiple sensors) taken every 15 minute which spanned over a period of 11 months. The provided data was then thoroughly examined and it was subdivided into 2 main categories which were working days and non-working days as energy consumption showed different trends in both categories. Therefore, a Feature Vector was developed which consisted of respective month, hour of the day, store number, energy consumed, a tag for working day or non-working day. As the data was gathered from the sensors in the real world therefore, it was highly unbalanced outliers estimated to be around 2-5% of the total dataset.

### 3.2. Statistical Method for Outlier Detection

In order to detect the outliers, a feature vector was developed, which consisted of the hour of the day, store number, energy consumed, a tag for working and non-working day and on that data a modified version of Tukey's test [Mcgill et al. 1978] was performed, which involves the calculation of median of training data which is referred to  $Q2$  and then again median of values lesser and greater than that of  $Q2$  is calculated. Median of values lower than  $Q2$  is refereed as  $Q1$  (lower quartile) and those having greater than  $Q2$  is referred as  $Q3$  (upper quartile) as shown in Figure 8.

After determining  $Q1$  and  $Q3$ , then Interquartile Range (IQR) is calculated by subtracting the value at  $Q3$  by  $Q1$ .

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$$IQR = Q3 - Q1 \quad (1)$$

After calculating the IQR, we use it to calculate the Tukey's Fences or Inner Fences by the following equation,

$$InnerFenceLowerLimit = Q1 - \alpha(IQR) \quad (2)$$

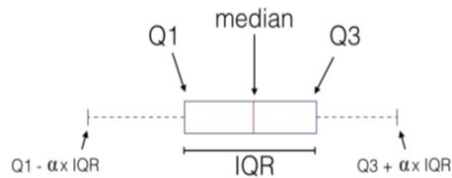


Fig. 5. Depiction of quartiles as used in the detection and removal of Outliers.

$$InnerFenceUpperLimit = Q1 + \alpha(IQR) \quad (3)$$

where,

$\alpha$  is the factor which varies the inner fence limits.

Any value lying beyond inner fence limits (upper and lower) can be considered as an outlier, and therefore, it is removed. The results of designed outlier detection algorithm are shown in Figure 7, 8(a) and 9(a).

As the dataset used in this project was highly varied and there were several energy values that stayed the same for the whole period of time. In order to calculate the quartiles and medians, there must be at least 4 unique values in a dataset, therefore for those dataset having less unique values, some product of their respective average was used to determine Inner and Outer Fences.

### 3.3. Autoencoder

An autoencoder always consists of two parts, the encoder and the decoder, which can be defined as transitions  $\phi$  and  $\psi$  such that:

$$\phi : \mathcal{X} \rightarrow \mathcal{F} \quad (4)$$

$$\psi : \mathcal{F} \rightarrow \mathcal{X} \quad (5)$$

$$\phi, \psi = \arg \min_{\phi, \psi} \|X - (\phi \circ \psi)X\|^2 \quad (6)$$

In a simple case, if there is one hidden layer, the encoder stage of an autoencoder takes the input  $x \in \mathbb{R}^d = \mathcal{X}$  and maps it to  $z \in \mathbb{R}^p = \mathcal{F}$ .

$$z = \sigma(Wx + b) \quad (7)$$

This image  $z$  is usually referred to as *code*, *latent variables* or *latent representation*. Here,  $\sigma$  is an element-wise activation function such as sigmoid function, hyperbolic tangent or a rectified linear unit.  $W$  is weight matrix and  $b$  is a bias vector. After that, the decoder stage of the autoencoder maps  $z$  to the reconstruction  $x'$  of the same shape as  $x$ .

$$x' = \sigma'(W'z + b') \quad (8)$$

where,  $\sigma'$ ,  $W'$  and  $b'$  for the decoder may differ in general from the corresponding  $\sigma$ ,  $W$  and  $b$  for the encoder, depending on the design of the autoencoder.

Autoencoders are also trained to minimize reconstruction errors (such as squared errors):

$$\mathcal{L}(x, x') = \|x - \sigma'(W'(\sigma(Wx + b)) + b')\|^2 \quad (9)$$

where,  $x$  is usually averaged over some input training set.

If the feature space  $\mathcal{F}$  has lower dimensionality than the input space  $\mathcal{X}$ , then the feature vector  $\phi(x)$  can be regarded as a compressed representation of the input  $x$ . If the hidden layers are larger than the input layer, an autoencoder can potentially learn the identity function and become useless. However, experimental results have shown that autoencoders might still learn useful features in these cases.

In case of Undercomplete autoencoders,  $\mathcal{F}$  has lower dimensionality than the input space  $\mathcal{X}$ , then the feature vector  $\phi(x)$  can be regarded as a compressed representation of the input  $x$ .

In this paper, an undercomplete autoencoder was trained in a semi-supervised fashion on the values of normal energy consumption data. Afterwards, the trained model was used and evaluated on a pre-trained dataset.

#### 4. EXPERIMENTS AND RESULTS

Outlier detection algorithm was developed and it performed adequately well in removing the outliers. Figure 6 shows the energy consumption data of each hour for all working days in January 2016, where as, figure 7 shows the same data as in figure 6 after the outlier removal algorithm implemented on it.

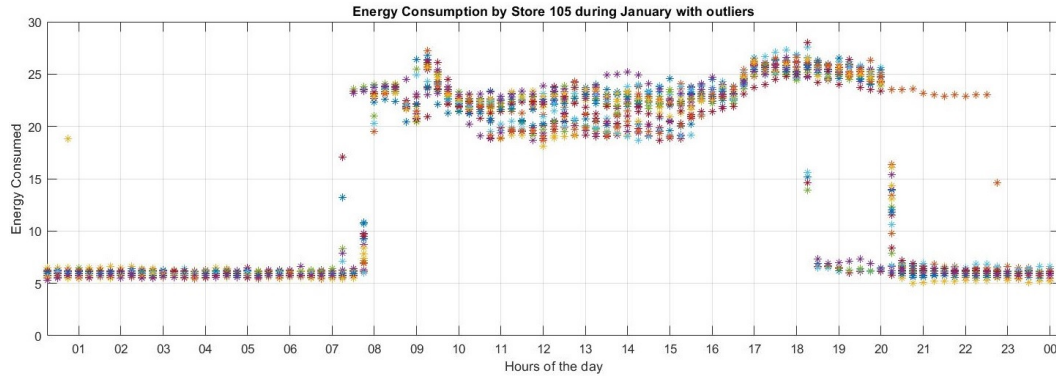


Fig. 6. Energy Consumption by Store 105 during working days of January 2016 with outliers

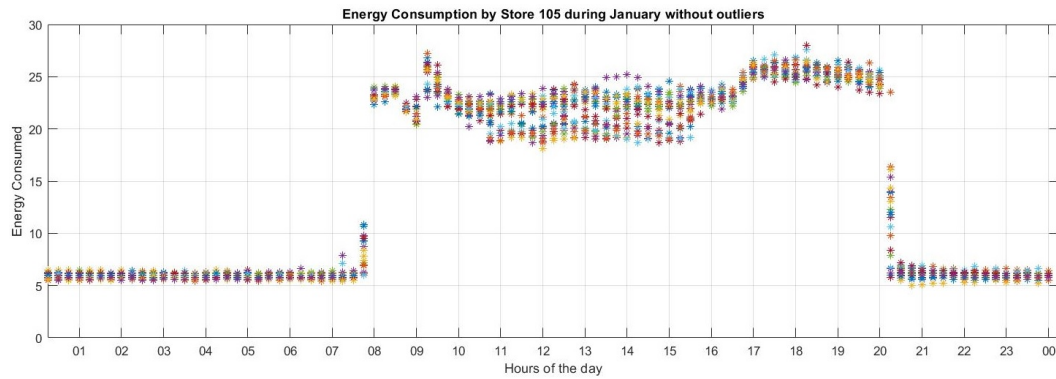


Fig. 7. Energy Consumption by Store 105 during working days of January 2016 without outliers



In Fig 8, we are comparing the accuracy of prediction of both algorithms with manually classified energy data of two stores using confusion matrices.

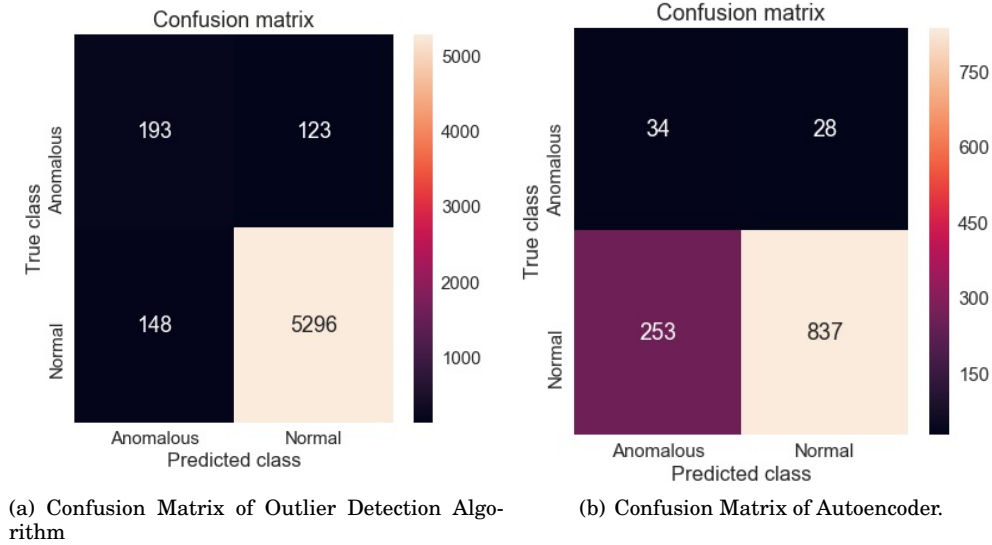


Fig. 8. Confusion Matrices

The same dataset which was used to make confusion matrices in Fig 8 is used to plot Receiver Operating Characteristics curves in Fig 9.

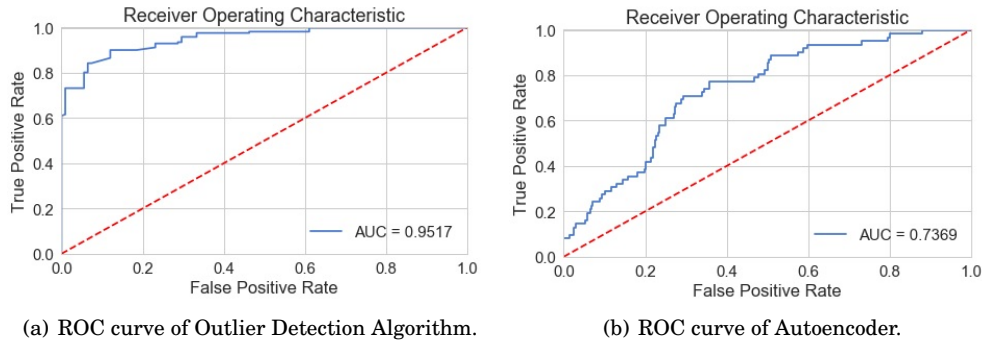


Fig. 9. ROC curves

The same dataset which was used to make confusion matrices in Fig 8 is used to plot Receiver Operating Characteristics curves in Fig 9.

As we can see from the comparison of Fig 8 and Fig 9, we can interpret that the performance of Statistical method which is based on Tukey's test performed remarkably better with around 95% correlation with manual classification but the shortcoming of this method is that the dataset should be arranged in a proper manner as a single

missing values in the dataset can make the classification ineffective. Whereas, classification using Autoencoder performed adequately with around 70-75% correlation with manually classified data but it required pre-classified data containing no outliers.

## 5. DISCUSSION/OUTLOOK/CONCLUSION/FUTURE WORK

In this paper, the performance of a semi supervised Autoencoder and a statistical model for outlier detection was compared. The experiment resulted in the varying results from each algorithms as Autoencoder did not require data to be arranged precisely and were robust against mixed up dataset whereas, Statistical based outlier detection model performed more accurately in detecting outliers but it required careful arrangement of the data.

In future, it is planned to use more variables in the feature vector of energy consumption data such size of the facility, number of energy consuming equipments, occupancy of the building, and other sensor data such as outside temperature and solar radiation. As more data is embedded in the feature vector, there will be more focus on using totally unsupervised learning using Autoencoder to discover and learn new pattern in the given dataset and do the classification more precisely.

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