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# Transformational semantics of the combination $\pi$ -*OZ* for mobile processes with data

Masterarbeit

- *post version* -

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# Contents

<b>List of Figures</b>	<b>V</b>
<b>1 Introduction</b>	<b>1</b>
<b>2 Preliminaries</b>	<b>3</b>
2.1 The $\pi$ -calculus . . . . .	3
2.1.1 Intuition . . . . .	3
2.1.2 Syntax . . . . .	4
2.1.3 Semantics . . . . .	6
2.1.4 Visualization . . . . .	8
2.1.5 Mobility . . . . .	8
2.1.6 Strong simulation . . . . .	10
2.2 The Object-Z . . . . .	15
2.2.1 Intuition . . . . .	15
2.2.2 Semantics . . . . .	22
2.2.3 Dynamic OZ . . . . .	23
<b>3 Transformational semantics of OZ</b>	<b>27</b>
3.1 Mapping values . . . . .	28
3.2 Mapping state variables . . . . .	28
3.3 Mapping Data Types . . . . .	29
3.4 Mapping mathematical operations . . . . .	29
3.5 Mapping state schema . . . . .	32
3.6 Mapping initial state schema . . . . .	33
3.7 Mapping operation schema . . . . .	33
3.8 Mapping class . . . . .	33
<b>4 Conclusion and future work</b>	<b>35</b>
<b>5 Appendix</b>	<b>1</b>
5.1 Addition . . . . .	1
<b>Bibliography</b>	<b>3</b>



# List of Figures

2.1	The <i>transition rules</i> [Mil99]. . . . .	7
2.2	The <i>inference tree</i> [Mil99]. . . . .	8
2.3	Stargazer code for the process $P$ . . . . .	8
2.4	The process $P$ reaction . . . . .	8
2.5	Stargazer code for the process $\text{new } x, y (A(x, y) \mid B(x))$ . . . . .	9
2.6	Mobility reaction . . . . .	9
2.7	Transition graphs . . . . .	11
2.8	ABC code for $P$ and $Q$ . . . . .	12
2.9	ABC output: check if $Q$ strongly simulates $P$ . . . . .	13
2.10	ABC output: check if $P$ strongly simulates $Q$ . . . . .	14
2.11	State Space. . . . .	15
2.12	VM <i>class</i> . . . . .	16
2.13	VM class: adding the <i>state schema</i> . . . . .	17
2.14	VM class: adding the <i>initial state schema</i> . . . . .	17
2.15	VM class: adding the <i>operation schema</i> . . . . .	18
2.16	VM class: <i>operation schema using delta operator</i> . . . . .	19
2.17	VM class: <i>with all specifications</i> . . . . .	19
2.18	VM class: <i>talk operation with output parameter</i> . . . . .	21
2.19	VM class: <i>instance reference</i> . . . . .	22
2.20	VM <i>Transition graph</i> . . . . .	23
2.21	Mobile vending machine and shops . . . . .	24
2.22	active shop . . . . .	25
2.23	idle shop . . . . .	25
3.1	0,1,2,3 as $\pi$ -calculus processes. . . . .	28
3.2	variable as a channel . . . . .	29
3.3	adder circuit . . . . .	30
3.4	addition as a process . . . . .	30
3.5	subtractor circuit . . . . .	31

3.6	subtraction as a process . . . . .	31
3.7	comparator circuit . . . . .	32
3.8	comparation as a process . . . . .	32

# 1 Introduction

every entity has a behavior and data. behavior actions can have effects on data. to model this idea we will break down our entity into two components: behavior component and data component. behavior component: represent the behavior that can an entity do during it's life cycle. data component: represents the data of an entity and the changes that can be made on it. we use pi calculus which is a specification language to model the behavior component. we use oz which is a specification language to model the data components. since pi and oz are two different languages used to describe different aspects of entity, we need a way to put them togther to get the model a complete entity. this is done using a simple trick. the trick is: transforming the oz into a pi language. this way we will have : behavior component: in pi. data component: in pi too. this way we can let them play together to represent an entity which have two view: behavior and data.





## 2 Preliminaries

### 2.1 The $\pi$ -calculus

The  $\pi$ -calculus is a process algebra that can be used to describe a behavior. This section introduces the pure polyadic version of the  $\pi$ -calculus as depicted in [Mil99].

#### 2.1.1 Intuition

To explain the  $\pi$ -calculus intuitively we will use the ion example as in [Mil99]. Let us imagine a positive and a negative ion. When those two ions merge, we get a new construct. The merge operation is called a *reaction*, since an ion acts and the other reacts. This reaction can be seen as communication between two processes. The two processes communicate to share some information. One process is the sender and the other is the receiver. By doing the reaction both processes evolve to something new. The reaction, information sharing and evolution concepts are the core of the  $\pi$ -calculus. Using those concepts we can understand the title of Milner's book *communicating and mobile processes: the  $\pi$ -calculus* [Mil99]. The word *communicating* refers to the *reaction* concept. The word *mobile* refers to the *information sharing and evolution* concepts, since the receiver process can use the received information to change its location as we will see in Section 2.1.5.

Intuitively, the  $\pi$ -calculus consists of:

- a set of names starting with capital case letters like  $P, P_1, Q, \dots$  etc used to refer to a process directly.
- a set of names starting with capital case letters like  $A, B, C, \dots$  etc used as a process identifier. The process identifier will be used to define recursion with parameters.
- a set of names starting with lower case letter like  $a, b, x, y, \dots$  etc used as a channel and message name. This set is denoted by  $\mathcal{N}$ .

- operators like:
  - Parallel composition operator: “  $|$  ”.
  - Sequential composition operator: “  $.$  ”.
  - Choice operator: “  $+$  ”.
  - Scope restriction operator: “ new ”.

So a simple example of a process can be:  $\bar{x}\langle y \rangle.0$  this process simply sends the message  $y$  via the channel  $x$  and stops. The full syntax of  $\pi$ -calculus process is given in Definition 2.1.1. In this thesis starting from this point, when we mention the word *names* we refer to  $\mathcal{N}$ . Furthermore, we shall often write  $\vec{y}$  for a sequence  $y_1, \dots, y_n$  of names.

### 2.1.2 Syntax

**Definition 2.1.1 (Process syntax)** The syntax of a  $\pi$ -calculus process  $P$  is defined by:

$$P ::= \sum_{i \in I} \pi_i.P_i \mid P_1 \mid P_2 \mid \underline{\text{new}} \vec{y} P \mid A\langle \vec{v} \rangle$$

where:

- $\sum_{i \in I} \pi_i.P_i$  is the guarded sum.
- $P_1 \mid P_2$  is the parallel composition of processes.
- $\underline{\text{new}} \vec{y} P$  is the restriction of the scope of the names  $\vec{y}$  to the process  $P$
- $A\langle \vec{v} \rangle$  is a process call.  $\triangle$

#### **Guarded sum:**

The guarded sum is the *choice* between multiple guarded processes. If the guard of one process took place, other guarded processes will be discarded. For example, the processes:  $x().P_1 + y().P_2$  will evolve to the process  $P_1$  if the guard  $x()$  occurred.

Furthermore, The process  $0$  is called the *stop process* or *inaction* and stands for the process that can do nothing. It can be omitted.

**Guard:**

The guard is also called *action prefix* and denoted by  $\pi$ . It's syntax is defined by:

**Definition 2.1.2 (Action prefix syntax)**

$$\pi ::= \bar{x}\langle \vec{y} \rangle \mid x(\vec{y}) \mid \tau$$

where:

- $\bar{x}\langle \vec{y} \rangle$ <sup>1</sup> represents the action: send  $\vec{y}$  via the channel  $x$ .
- $x(\vec{y})$ <sup>2</sup> represents the action: receive  $\vec{y}$  via the channel  $x$ .
- $\tau$  represents an internal non observable action.  $\triangle$

The set of all *actions* is defined as  $\mathbf{Act} =_{\text{def}} \mathbf{Out} \cup \mathbf{In} \cup \{\tau\}$ , where:

- $\mathbf{Out}$  is the set of all *output actions*, defined as  $\mathbf{Out} =_{\text{def}} \{\bar{x}\langle \vec{y} \rangle \mid x \in \mathcal{N}\}$ .
- $\mathbf{In}$  is the set of all *input actions*, defined as  $\mathbf{In} =_{\text{def}} \{x(\vec{y}) \mid x \in \mathcal{N}\}$ .

**Parallel composition:**

The parallel composition operator  $|$  represents the concept of concurrency in the  $\pi$ -calculus, where two processes can evolve in concurrent. It represents an interleaving behavior of the concurrency. For example let:  $P =_{\text{def}} P_1 \mid (P_2 \mid P_3)$  where:  $P_1 =_{\text{def}} x(y).Q_1$ ,  $P_2 =_{\text{def}} \bar{x}\langle y \rangle.Q_2$  and  $P_3 =_{\text{def}} x(y).Q_3$ . So  $P =_{\text{def}} x(y).Q_1 \mid (\bar{x}\langle y \rangle.Q_2 \mid x(y).Q_3)$ . Possible evolution cases of  $P$  are:

- $P_1 \mid (Q_2 \mid Q_3)$ .  $P_2$  sends  $y$  via  $x$  to  $P_3$ .
- $Q_1 \mid (Q_2 \mid P_3)$ .  $P_2$  sends  $y$  via  $x$  to  $P_1$ .

The example above illustrated the privacy nature of the parallel operator in the  $\pi$ -calculus. A process can via a channel communicate with only one process pro time, i.e., the channel represents a binary synchronization.  $P_2$  cannot communicate with both  $P_1$ ,  $P_3$  in the same time, while in Communicating Sequential Processes (CSP) a process can communicate with multiple processes in the same time via the same channel by sending multiple copies of the same message, i.e., in CSP the channel represents a multiple synchronization.

---

<sup>1</sup> $\bar{x}\langle \rangle$  means: send a signal via  $x$ .  $\bar{x}\langle y \rangle$  means: send the name  $y$  via  $x$ .  $\bar{x}\langle \vec{y} \rangle$  means: send the sequence  $\vec{y}$  via  $x$ .

<sup>2</sup> $x()$  means: receive a signal via  $x$ .  $x(y)$  means: receive any name  $y$  via  $x$ .  $x(\vec{y})$  means: receive any sequence  $\vec{y}$  via  $x$ . “ $y$  here plays the role of parameter”

**Restriction:**

The expression  $\underline{\text{new}} \vec{y} P$  binds the names  $\vec{y}$  to the process  $P$ . In other words: the visibility scope of the names  $\vec{y}$  is restricted to the process  $P$ . It is similar to declaring a private variable in programming languages. Thus the names  $\vec{y}$  are not visible outside  $P$  and  $P$  cannot use them to communicate with outside. For example, let  $P =_{\text{def}} P_1 \mid P_2$  where:  $P_1 =_{\text{def}} \underline{\text{new}} y \bar{y}\langle z \rangle.Q_1$  and  $P_2 =_{\text{def}} y(z).Q_2$ . The process  $P$  cannot evolve to  $Q_1 \mid Q_2$ , since the name  $y$  in  $P_1$  is only visible inside it, i.e., from the  $P_2$ 's point of view  $P_1$  doesn't have a channel called  $y$ . This takes us to the definition of the Bound and free names.

**Definition 2.1.3 (Bound names)** are all the restricted names in a process.  $\triangle$

**Definition 2.1.4 (Free names)** are all the name that occur in a process except the bound names.  $\triangle$

For example, let  $P_1 =_{\text{def}} \underline{\text{new}} x \bar{x}\langle y \rangle.P_2$  where  $P_2 =_{\text{def}} \underline{\text{new}} z \bar{x}\langle z \rangle.P_3$ . The name  $x$  is bound in  $P_1$  but free in  $P_2$ .

**Process call:**

Let  $P$  be a process and let  $A$  be a process identifier. To be able to use the process  $P$  recursively we use the process identifier  $A$  as follow:  $A(\vec{w}) =_{\text{def}} P$ . Thus, when we write  $A(\vec{v})$  we are using the identifier  $A$  to call the process  $P$  with replacing the names  $\vec{w}$  in  $P$  with the names  $\vec{v}$ . This replacement is called the  $\alpha$ -conversion

For example, let  $P =_{\text{def}} \bar{w}\langle y \rangle.0$  and let  $A(w) =_{\text{def}} P$  be the recursive definition of the process  $P$ , then the behavior of  $A(\vec{v})$  is equivalent to  $\bar{v}\langle y \rangle.0$

### 2.1.3 Semantics

To understand the operational semantics of  $\pi$ -calculus we will use a labelled transition system LTS. Using this LTS we can investigate  $\pi$ -calculus process evolution. The definition of LTS is adapted from [Mil99] pages 39<sup>3</sup>, 91<sup>4</sup>, 132<sup>5</sup> with some changes.

**Definition 2.1.5 (LTS of  $\pi$ -calculus)** The labelled transition system  $(\mathcal{P}^\pi, \mathcal{T})$  of  $\pi$ -calculus processes over the action set  $\text{Act}$  has the process expressions  $\mathcal{P}^\pi$  as its

---

<sup>3</sup>Transition Rules: LTS for concurrent processes not for  $\pi$ -calculus processes.

<sup>4</sup>Reaction Rules: no labels and no LTS.

<sup>5</sup>Commitment Rules: abstractions and concretions are out of this thesis's scope.

states, and its transitions  $\mathcal{T}$  are those which can be inferred from the rules in Figure 2.1. The rule REACT is the most important one. It shows the process evolution when a reaction occurs. The reaction requires two complementary transitions  $P \xrightarrow{\bar{x}(\bar{y})} P'$  and  $Q \xrightarrow{x(\bar{z})} Q'$ , we call them commitments. so the process  $P$  takes a commitment to take part in the reaction, and so does  $Q$ .

$$\begin{aligned}
 \underline{OUT} : \bar{x}(\bar{y}).P &\xrightarrow{\bar{x}(\bar{y})} P & \underline{IN} : x(\bar{y}).P &\xrightarrow{x(\bar{y})} P \\
 \underline{TAU} : \tau.P &\xrightarrow{\tau} P & \underline{SUM} : \alpha.P + \sum_{i \in I} \pi_i.P_i &\xrightarrow{\alpha} P \\
 \underline{L-PAR} : \frac{P \xrightarrow{\alpha} P'}{P \mid Q \xrightarrow{\alpha} P' \mid Q} & \underline{R-PAR} : \frac{Q \xrightarrow{\alpha} Q'}{P \mid Q \xrightarrow{\alpha} P \mid Q'} \\
 \underline{RESTRICTION} : \frac{P \xrightarrow{\alpha} P'}{\underline{new} x P \xrightarrow{\alpha} \underline{new} x P'} & \text{if } \alpha \notin \{\bar{x}, x\} \\
 \underline{PROCESS\_CALL} : \frac{\{\bar{y}/\bar{z}\} P \xrightarrow{\alpha} P'}{A(\bar{y}) \xrightarrow{\alpha} P'} & \text{if } A(\bar{z}) =_{\text{def}} P \\
 \underline{REACT} : \frac{P \xrightarrow{\bar{x}(\bar{y})} P' \quad Q \xrightarrow{x(\bar{z})} Q'}{P \mid Q \xrightarrow{\tau} P' \mid \{\bar{y}/\bar{z}\} Q'} & \triangle
 \end{aligned}$$

Figure 2.1: The *transition rules* [Mil99].

An example of using the transition rules of this LTS to infer a transition is: Let  $P =_{\text{def}} \underline{new} x (A_1\langle x \rangle \mid B_1\langle x \rangle)$ , where:  $A_1(y) =_{\text{def}} \bar{y}().A_2\langle y \rangle$  and  $B_1(z) =_{\text{def}} z().B_2\langle z \rangle$ .  $P$  can do the transition  $\underline{new} x (A_1\langle x \rangle \mid B_1\langle x \rangle) \xrightarrow{\tau} \underline{new} x (A_2\langle x \rangle \mid B_2\langle x \rangle)$ , which is a reaction. The inference tree of this transition is shown in Figure 2.2. Thus, using the LTS we can enumerate sll possible transitions of a  $\pi$ -calculus process.

$$\begin{array}{c}
 \frac{}{\overline{x}\langle \rangle . A_2\langle x \rangle \xrightarrow{\overline{x}\langle \rangle} A_2\langle x \rangle} \text{ by OUT} \qquad \frac{}{x().B_2\langle x \rangle \xrightarrow{x\langle \rangle} B_2\langle x \rangle} \text{ by IN} \\
 \frac{}{A_1\langle x \rangle \xrightarrow{\overline{x}\langle \rangle} A_2\langle x \rangle} \text{ by PROCESS CALL} \qquad \frac{}{B_1\langle x \rangle \xrightarrow{x\langle \rangle} B_2\langle x \rangle} \text{ by PROCESS CALL} \\
 \frac{}{A_1\langle x \rangle \mid B_1\langle x \rangle \xrightarrow{\tau} A_2\langle x \rangle \mid B_2\langle x \rangle} \text{ by REACT} \\
 \frac{}{\text{new } x (A_1\langle x \rangle \mid B_1\langle x \rangle) \xrightarrow{\tau} \text{new } x (A_2\langle x \rangle \mid B_2\langle x \rangle)} \text{ by RESTRICTION}
 \end{array}$$

Figure 2.2: The *inference tree* [Mil99].

### 2.1.4 Visualization

To gain more understanding of the  $\pi$ -calculus we will use *Stargazer*[Star]. Stargazer is a visual simulator for  $\pi$ -calculus. Figure 2.3 shows the code listing of the process  $P =_{\text{def}} \text{new } x (A_1\langle x \rangle \mid B_1\langle x \rangle)$  where:  $A_1(y) =_{\text{def}} \overline{y}\langle \rangle . A_2\langle y \rangle$  and  $B_1(z) =_{\text{def}} z().B_2\langle z \rangle$  in Stargazer syntax.

```

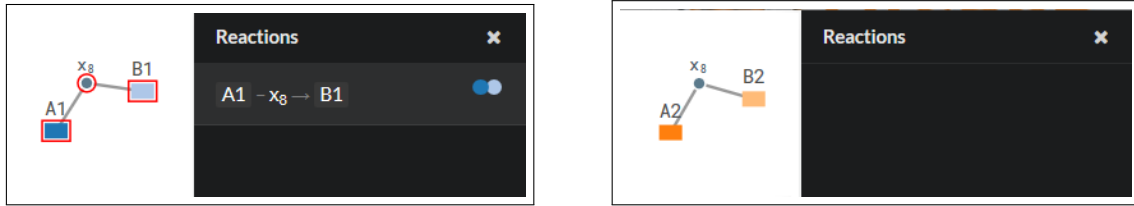
new x . (A1[x] | B1[x])

A1[y] := y<>.A2[y]
B1[z] := z().B2[z]

```

Figure 2.3: Stargazer code for the process  $P$ .

Stargazer can visualize the reaction  $\text{new } x (A_1\langle x \rangle \mid B_1\langle x \rangle) \xrightarrow{\tau} \text{new } x (A_2\langle x \rangle \mid B_2\langle x \rangle)$  as shown in Figure 2.4.



(a) Before reaction occurrence.

(b) After reaction occurrence.

Figure 2.4: The process  $P$  reaction

### 2.1.5 Mobility

As mentioned previously, the word *mobile* refers to the *information sharing and evolution* concepts, since the receiver process can use the received information to change its location. Let us take an example to illustrate the mobility. Let:  $\text{new } x, y (A\langle x, y \rangle \mid B\langle x \rangle)$  where:

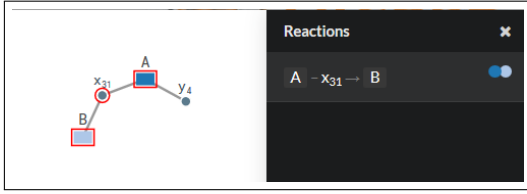
- $A(a, b) =_{\text{def}} \bar{a}\langle b \rangle . A\langle a, b \rangle$
- $B(c) =_{\text{def}} c(d) . B\langle d \rangle$

Figure 2.5 shows the stargazer code listing of the process  $\text{new } x, y \ (A\langle x, y \rangle \mid B\langle x \rangle)$ , Figure 2.6 shows it's visualization before and after the interaction occurrence.

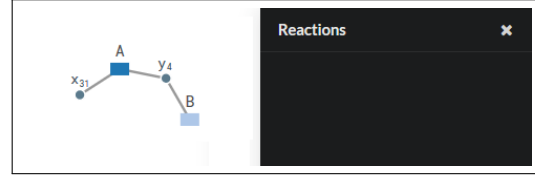
```
new x, y . (A[x, y] | B[x])

A[a, b] := a<b>.A[a, b]
B[c] := c(d) . B[d]
```

Figure 2.5: Stargazer code for the process  $\text{new } x, y \ (A\langle x, y \rangle \mid B\langle x \rangle)$ .



(a) Before reaction occurrence.



(b) After reaction occurrence.

Figure 2.6: Mobility reaction

Intuitively, The mobility can be noticed in Figure 2.6, since  $B$  changed it's position in the connection topology. The following explains the mobility through interaction step by step:

- Initially the process  $A\langle x, y \rangle$  has the channels  $x, y$  and the process  $B\langle x \rangle$  has the channel  $x$ . Thus,  $A\langle x, y \rangle$  and  $B\langle x \rangle$  are connected via channel  $x$ .
- $A\langle x, y \rangle$  has commitment  $\bar{x}\langle y \rangle$ , i.e., send the channel name  $y$  via the channel  $x$ .
- $B\langle x \rangle$  has commitment  $x(d)$ , i.e., receive a message  $d$  via  $x$ .
- That means: a reaction can occur between  $A\langle x, y \rangle$  and  $B\langle x \rangle$ . This reaction is:  $\text{new } x, y \ (\bar{x}\langle y \rangle . A\langle x, y \rangle \mid x(d) . B\langle d \rangle) \xrightarrow{\tau} \text{new } x, y \ (A\langle x, y \rangle \mid B\langle y \rangle)$ .
- Information sharing: the process  $A\langle x, y \rangle$  sends the name  $y$  to  $B\langle x \rangle$  when the interaction occurs.

- Evolution: when interaction occurs  $B\langle x \rangle$  knows about the channel  $y$  and uses it as parameter for the the process call  $B\langle y \rangle$  .i.e, The  $B\langle y \rangle$  now has the channel  $y$ , and no more  $x$ .
- Finally, in other words:
  - before the reaction:  $B$  was connected to  $A$  via  $x$  as shown in Figure 2.6.
  - after the reaction:  $B$  is connected to  $A$  via  $y$  as shown in Figure 2.6.

### 2.1.6 Strong simulation

The *strong simulation* is comparison of processes based on their behavior. To understand this let us start with a simple example: Let  $P =_{\text{def}} \tau.\tau.\mathbf{0}$  and  $Q =_{\text{def}} \tau.\mathbf{0}$ . We can notice that  $P$  can do two  $\tau$  transitions, but  $Q$  can do only one. Thus  $Q$  doesn't strongly simulates  $P$ . The word *strongly* refers to the point that: the strong simulation comparison takes the internal transition  $\tau$  into account. There is another kind of comparison called the *weak simulation*, which doesn't consider the internal transition  $\tau$ , but this kind of comparison is not considered in this thesis. The formal definition of the *strong simulation* is given in Definition 2.1.6, which is adapted from [Gi14] page 32 with some changes.

**Definition 2.1.6 (Strong simulation)** A relation  $\mathcal{S} \subseteq \mathcal{P}^\pi \times \mathcal{P}^\pi$  is called a *strong simulation*, if  $(P, Q) \in \mathcal{S}$  implies that

$$\text{if } P \xrightarrow{\alpha} P' \text{ then } Q' \in \mathcal{P}^\pi \text{ exists such that } Q \xrightarrow{\alpha} Q' \text{ and } (P', Q') \in \mathcal{S}. \quad \triangle$$

An example of checking the strong simulation is:  
Let

- $P =_{\text{def}} \underline{\text{new}} x (A_1\langle x \rangle \mid B_1\langle x \rangle)$
- $Q =_{\text{def}} \underline{\text{new}} x ((A_1\langle x \rangle \mid B_1\langle x \rangle) + \tau.Q)$

where:

- $A_1(y) =_{\text{def}} \bar{y}\langle \rangle.\mathbf{0}$
- $B_1(z) =_{\text{def}} z().\mathbf{0}$



Intuitively, The behavior of  $P$  and  $Q$  can be illustrated using transition graphs as shown in Figure 2.7.  $Q$ 's transition graph is the same as  $P$ 's, except one thing:  $Q$  has a loop with label  $\tau$ . This loop is due to the  $\tau$  transition in  $Q$ 's definition. Hence, we can notice that  $Q$  can do all the transitions that  $P$  can, plus an extra transition  $\tau$ . In other words  $Q$  simulates  $P$ , but  $P$  doesn't simulate  $Q$ .

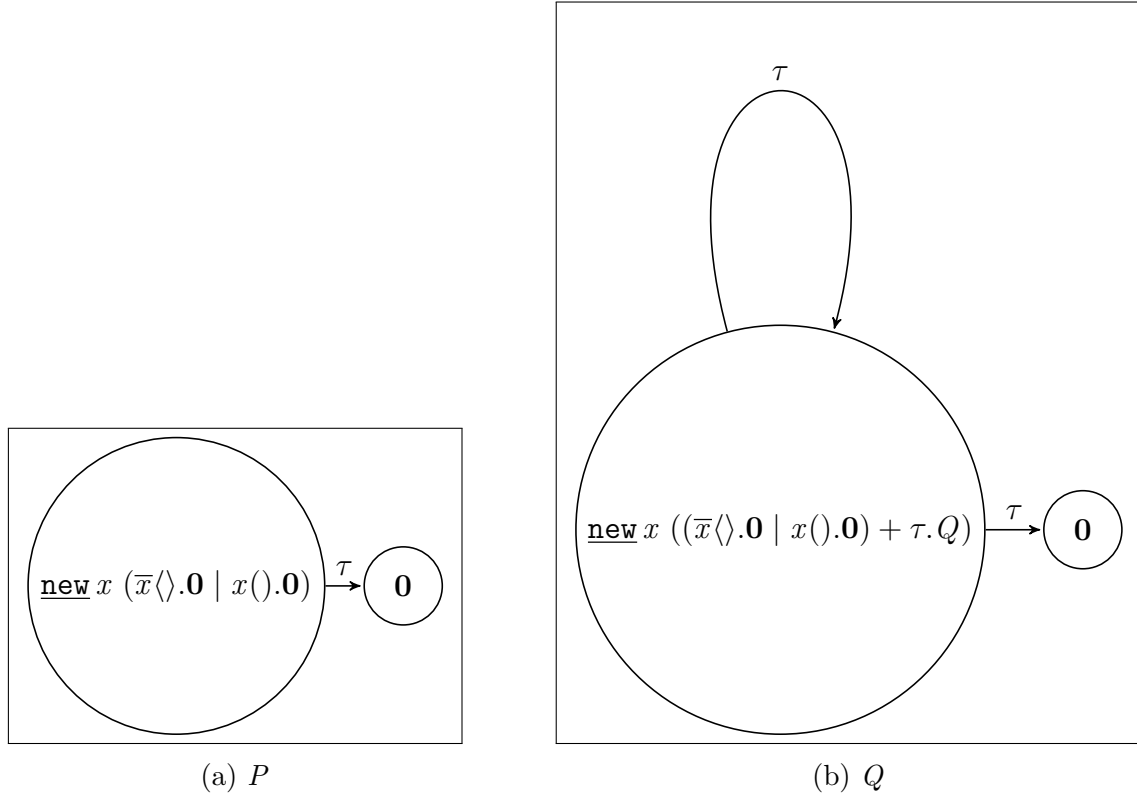


Figure 2.7: Transition graphs

To check the strong simulation we can use *ABC* (*Another Bisimilarity Checker*) [ABC]. ABC is a tool that checks simulation between  $\pi$ -calculus processes. Figure 2.8 shows the code listing of the process  $P$  and  $Q$  in ABC syntax.

Figure 2.9 and Figure 2.10 shows the result of running Figure 2.8, where  $x0$  stands for  $x$ , since ABC renames the channels and messages names internally.

In Figure 2.9 we see the result of the command  $lt\ P\ Q$ , which checks if  $Q$  strongly simulates  $P$ . The result is *yes* and the simulation relation is shown, where  $x0$  stands for  $x$ . In Figure 2.9 we see the two pairs of the simulation relation, where:

- $(0 \{ \} 0)$  stands for the pair  $(\mathbf{0}, \mathbf{0})$ , which means: The state  $\mathbf{0}$  of  $Q$  is as powerful as  $\mathbf{0}$  of  $P$ .

```

agent P = (^x)( A_1 x | B_1 x)

agent A_1(y) = 'y.0
agent B_1(z) = z.0

agent Q = (^x)((A_1 x | B_1 x) + t.Q)

// check if Q strongly simulates P
lt P Q

// check if P strongly simulates Q
lt Q P

```

Figure 2.8: ABC code for  $P$  and  $Q$ .

- $( (^x0)('x0.0 \mid x0.0) \{ \} (^x0)(('x0.0 \mid x0.0) + t.Q) )$  stands for the pair  $(\underline{\text{new}} x (A_1\langle x \rangle \mid B_1\langle x \rangle), \underline{\text{new}} x ((A_1\langle x \rangle \mid B_1\langle x \rangle) + \tau.Q))$ , which means: The state  $\underline{\text{new}} x ((\bar{x}\langle \rangle.0 \mid x().0) + \tau.Q)$  of  $Q$  is as powerful as  $\underline{\text{new}} x (\bar{x}\langle \rangle.0 \mid x().0)$  of  $P$ .

Thus,  $Q$  strongly simulates the behavior of  $P$  and the simulation relation is  $\mathcal{S} = \{(\mathbf{0}, \mathbf{0}), (\underline{\text{new}} x (A_1\langle x \rangle \mid B_1\langle x \rangle), \underline{\text{new}} x ((A_1\langle x \rangle \mid B_1\langle x \rangle) + \tau.Q))\}$ .

```

The two agents are strongly related (2).
Do you want to see the core of the simulation (yes/no) ? yes
{
  (
    0
    { }
    0
  )

  (
    ( $\hat{x}0$ ) ('x0.0 | x0.0)
    { }
    ( $\hat{x}0$ ) (( 'x0.0 | x0.0) + t.Q)
  )
}

```

Figure 2.9: ABC output: check if  $Q$  strongly simulates  $P$ .

In Figure 2.10 we can see the result of the command `lt Q P`, which checks if  $P$  strongly simulates  $Q$ . The result is *no*, since:

- when:
  - $Q$  is in the state  $\underline{\text{new}} x ((\bar{x}\langle \rangle.\mathbf{0} \mid x().\mathbf{0}) + \tau.Q)$ .
  - $P$  is in the state  $\underline{\text{new}} x (\bar{x}\langle \rangle.\mathbf{0} \mid x().\mathbf{0})$ .
- then:
  - $Q$  can do a  $\tau$  transition, which is the loop, to the state  $\underline{\text{new}} x ((\bar{x}\langle \rangle.\mathbf{0} \mid x().\mathbf{0}) + \tau.Q)$ .
  - $P$  can do a  $\tau$  transition, which is a reaction, to the state  $\mathbf{0}$ .
- then:
  - $Q$  can do a  $\tau$  transition, which is a reaction, to the state  $\mathbf{0}$ .
  - $P$  cannot go ahead, denoted by “ $*$ ”, since it is in the state  $\mathbf{0}$ .

Thus,  $P$  doesn't strongly simulates the behavior of  $Q$ .

The two agents are not strongly related (2).  
 Do you want to see some traces (yes/no) ? yes  
 traces of

Q

P

-t->

-t->

( $\hat{x}0$ ) (( 'x0.0 | x0.0) + t.Q)

0

-t->

-t->

0

\*

Figure 2.10: ABC output: check if  $P$  strongly simulates  $Q$ .

## 2.2 The Object-Z

The Object-Z, shortly OZ, is a specifications language used to describe an entity through specifying its data, operations and the effects of those operations on the data. This section introduces the Object-Z as decriped in [Ol18].

### 2.2.1 Intuition

To explain the OZ intuitively, we will start by examining the vending machine example, then we will explain how to build a set mathematically, finally we will explain the main concepts in OZ.

#### **Vending Machine:**

As a preperation, let us imagine that we have the task: specifying a vending machine.

- Let  $cv$  be the ammount of coffee, and  $tv$  be the amount of tea.
- Let  $coffee$  be the selling coffee operation, and  $tea$  be the selling tea operation.

the specifications are:

- It sell  $coffee$  and  $tea$ , and the maximum amount for each if them is 3.
- It's initial state is  $cv = 3$  and  $tv = 3$ .
- When the operation  $coffee$  or  $tea$ , then the amount should be decreased by one.

The state space of the vending machine can be visualized as shown in Figure 2.11, where we see the initial state  $VM(3,3)$ . The arrow indicates a state transition decrementing the amount of coffee. Later in **Main concepts of OZ** we will learn how to write the specifications using OZ language notations.

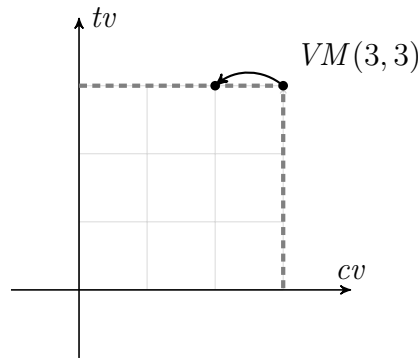


Figure 2.11: State Space.

### Set building:

A set is a collection of things. For example:  $\{5, 7, 11\}$  is a set. But we can also build a set by describing what is in it using the following notation:  $\{ \textit{Declaration} \mid \textit{predicate} \bullet \textit{expression} \}$ . For example:  $\{x : \mathbb{Z} \mid x \geq 0 \bullet x^2\}$  means *the set of all squared  $x$ 's, such that  $x$  is integer and greater than 0*

### Main concepts of OZ:

The main concepts of OZ are:

- *Schema*: It can be seen as a set [SIJ88].
- *Class*: It can be seen as a grouping of a *state schema*, *initial state schema* and *operation schemas* [TDC04]. It represents the object oriented approach

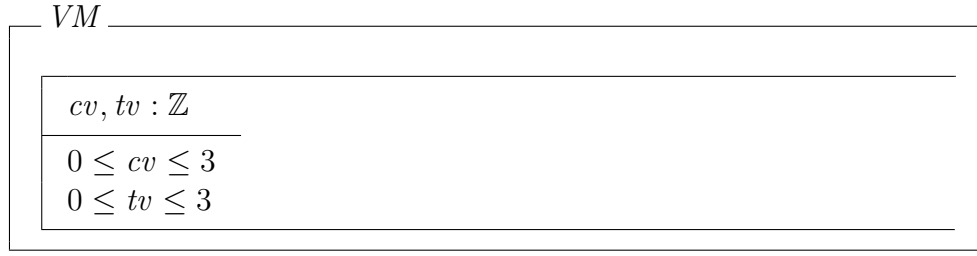
To illustrate those main concepts, consider the vending machine example denoted by *VM*:

- *Class*: To model the vending machine we need to define a class *VM*. Syntactically, in OZ a class definition is a named box as shown in Figure 2.12, where the dots ... refer to details explained next.

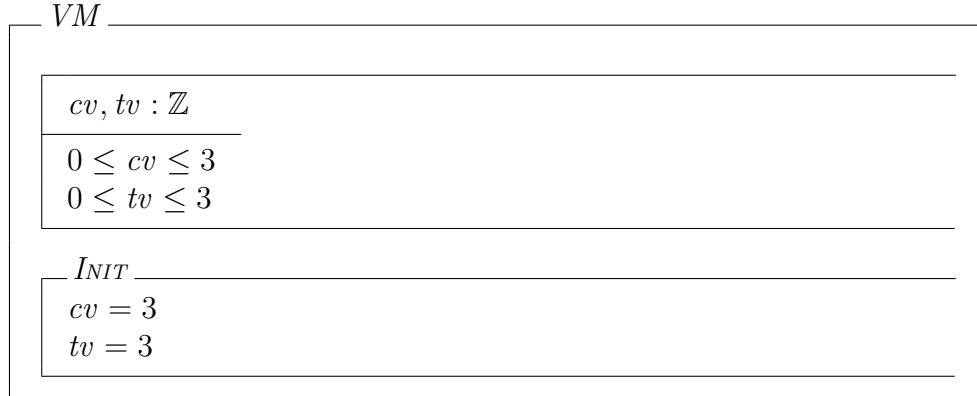


Figure 2.12: VM *class*.

- *State space*: The state space of our vending machine can be seen as a set of all valid states. The set of all valid states is:
  - In mathematics:  $State\_Space = \{cv, tv : \mathbb{Z} \mid (0 \leq cv \leq 3) \wedge (0 \leq tv \leq 3) \bullet (cv, tv)\} = \{(0, 0), \dots, (3, 3)\}$ .
  - In OZ: The set *State\_Space* can be described using a *state schema*, which is a box without name added to the class box as shown in Figure 2.13.

Figure 2.13: *VM* class: adding the *state schema*.

- *Initial state*: Our vending machine has an initial state with  $cv = 3$  and  $tv = 3$ . The set of all possible initial states, that respects those conditions is:
  - In mathematics:  $Initial\_States = \{cv, tv : \mathbb{Z} \mid (0 \leq cv \leq 3) \wedge (0 \leq tv \leq 3) \wedge (cv = 3) \wedge (tv = 3) \bullet (cv, tv)\} = \{(3, 3)\}$ .
  - In OZ: the set *Initial\_States* can be described using a *initial state schema*, which is a box named *INIT* added to the class box as shown in Figure 2.14.

Figure 2.14: *VM* class: adding the *initial state schema*.

- *State transition*: When the vending machine sells a coffee, the amount of coffee should be decreased by one. This is a state transition. The set of all possible state transitions when the selling coffee operation occurs is:
  - In mathematics:  $coffee = \{cv, tv, cv', tv' : \mathbb{Z} \mid (0 \leq cv \leq 3) \wedge (0 \leq tv \leq 3) \wedge (0 \leq cv' \leq 3) \wedge (0 \leq tv' \leq 3) \wedge (tv' = tv) \wedge (cv' = cv - 1) \bullet$

$((cv, tv), (cv', tv')) = \{((3, 3), (2, 3)), \dots, ((1, 0), (0, 0))\}$ , where  $(cv, tv)$  represents the *pre state* and  $(cv', tv')$  represents the *post state* of a state transition.

- In OZ: the set *coffee* can be described using an *operation schema*, which is a box named with the operation name added to the class box as shown in Figure 2.15.

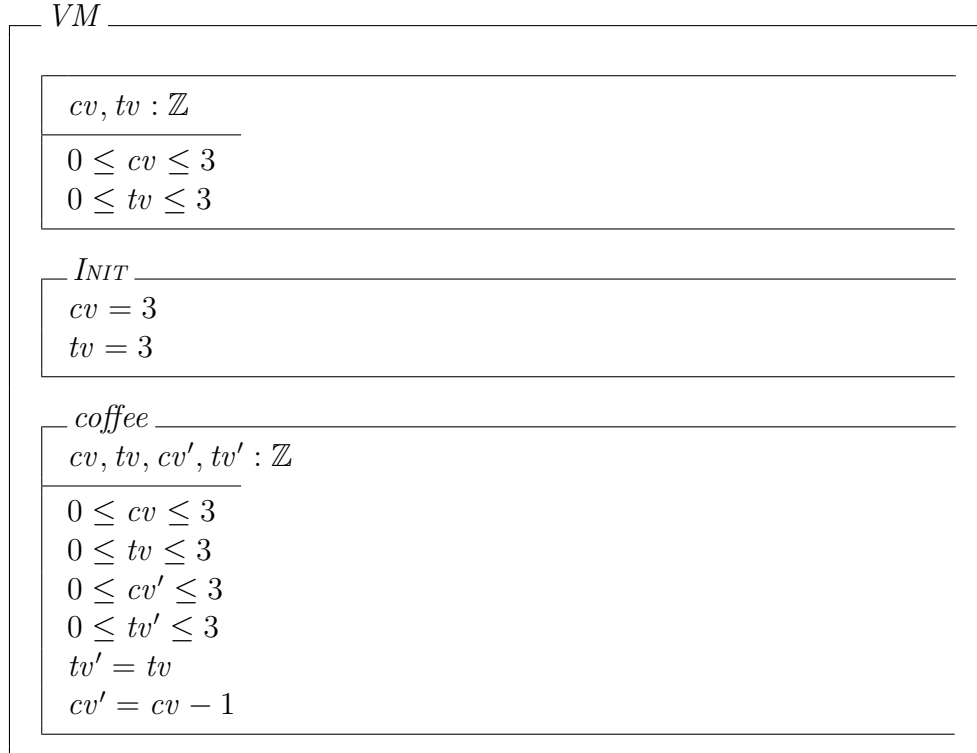


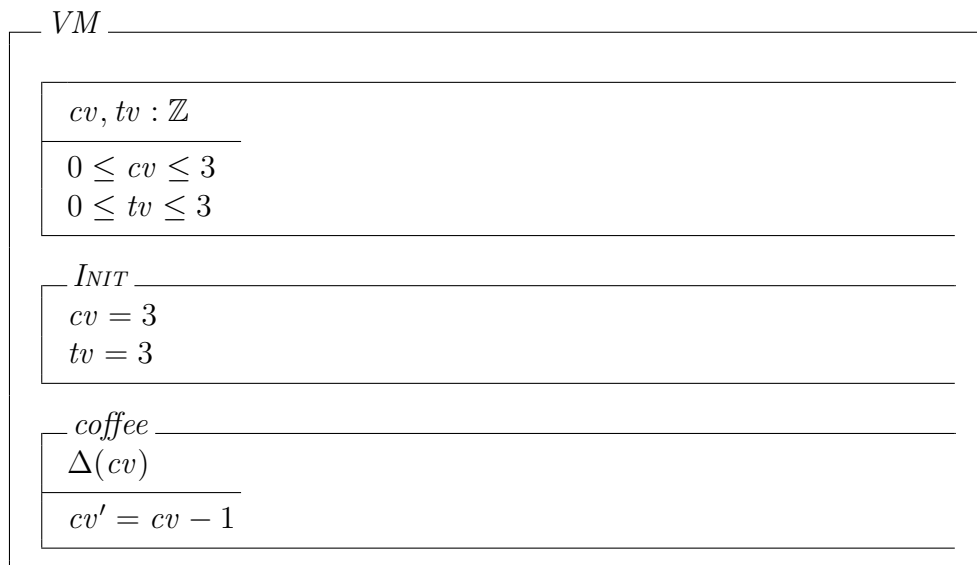
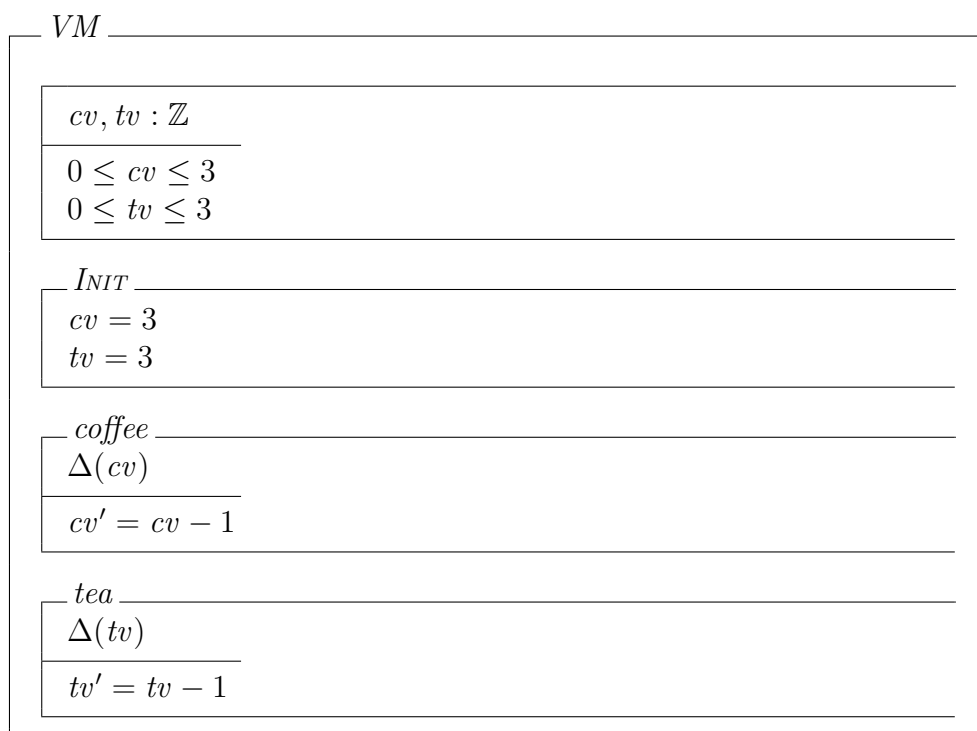
Figure 2.15: *VM* class: adding the *operation schema*.

OZ offers a more nice way to write the operation schema using  $\Delta$ -list. In OZ:

- Operation schema has a  $\Delta$ -list of state variables whose values may change. By convention, no  $\Delta$ -list means no attribute changes value.
- Operation schema implicitly includes the state schema and a primed version of it.

Thus, since the schema operation *coffee* specifies changes on the *coffee* value only, we can write it as shown in Figure 2.16.



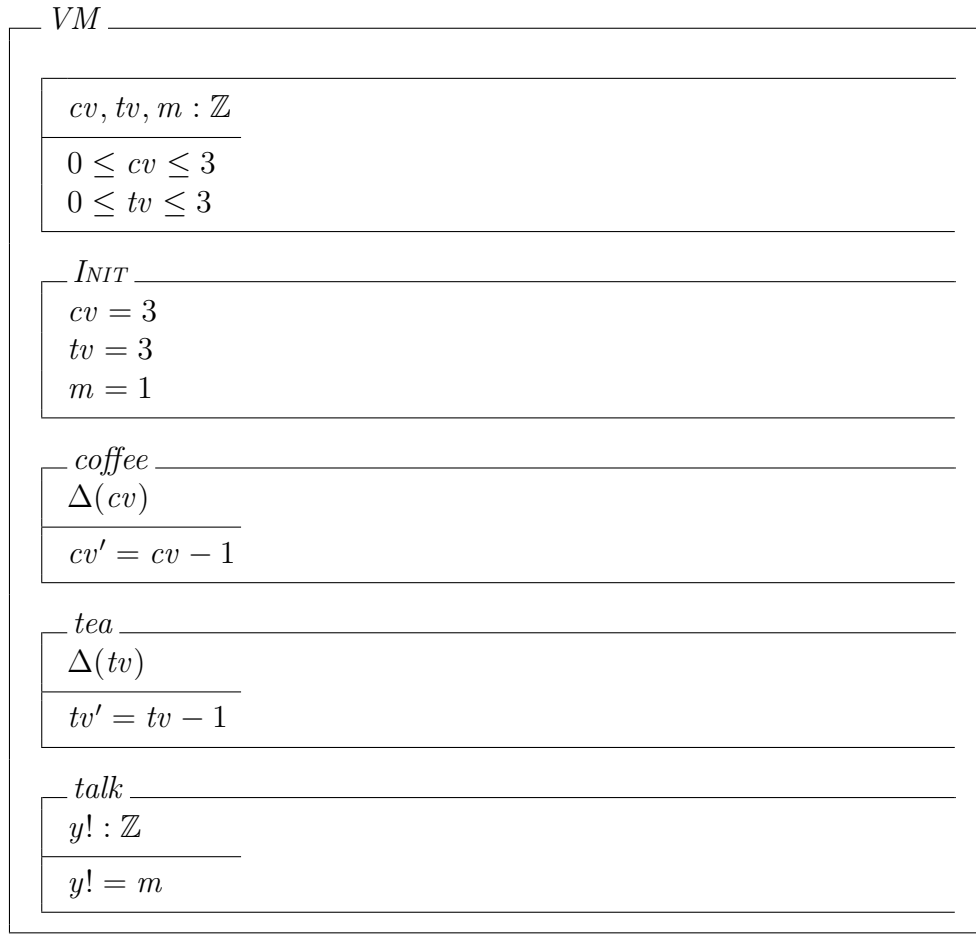
Figure 2.16: *VM* class: operation schema using delta operator.Figure 2.17: *VM* class: with all specifications.

### **Operation's input and output parameters:**

Some operations can have input and output parameters, just like method in programming language, where the method's parameters represent the input, and the returned values represent the output. To illustrate the idea let us extend our vending machine. The new *VM* can talk to a shop sending a message to it. So it has a new operation *talk* and a state variable *m* representing the message to be sent.

The set of all possible state transitions when the *talk* operation occurs is:

- In mathematics:  $talk = \{cv, tv, m, cv', tv', m', y : \mathbb{Z} \mid (0 \leq cv \leq 3) \wedge (0 \leq tv \leq 3) \wedge (0 \leq cv' \leq 3) \wedge (0 \leq tv' \leq 3) \wedge (tv' = tv) \wedge (cv' = cv) \wedge (m' = m) \wedge (y = m) \bullet ((cv, tv, m), (cv', tv', m'))\} = \{((3, 3, 1), (3, 3, 1)), \dots, ((0, 0, 1), (0, 0, 1))\}$ .
- In OZ: the set *talk* can be described using an *operation schema*, as shown in Figure 2.18. We can notice that this operation doesn't change any state variable's value, it just says that the value of the output parameter *y*, written as *y!*, must be equal to the value of the state variable *m*. For input parameter use ? symbol.

Figure 2.18: VM class: *talk* operation with output parameter.**Instance reference:**

OZ is an object oriented approach, Thus every instance of a class needs a unique identifier, i.e., a reference name to refer to it. In OZ this can be seen simply as state constant *self* initialized with some *id* when the instance is created. Furthermore, operations can share the instance identity through output or input the reference name *self* as shown in Figure 2.19 in the operation *talk*.

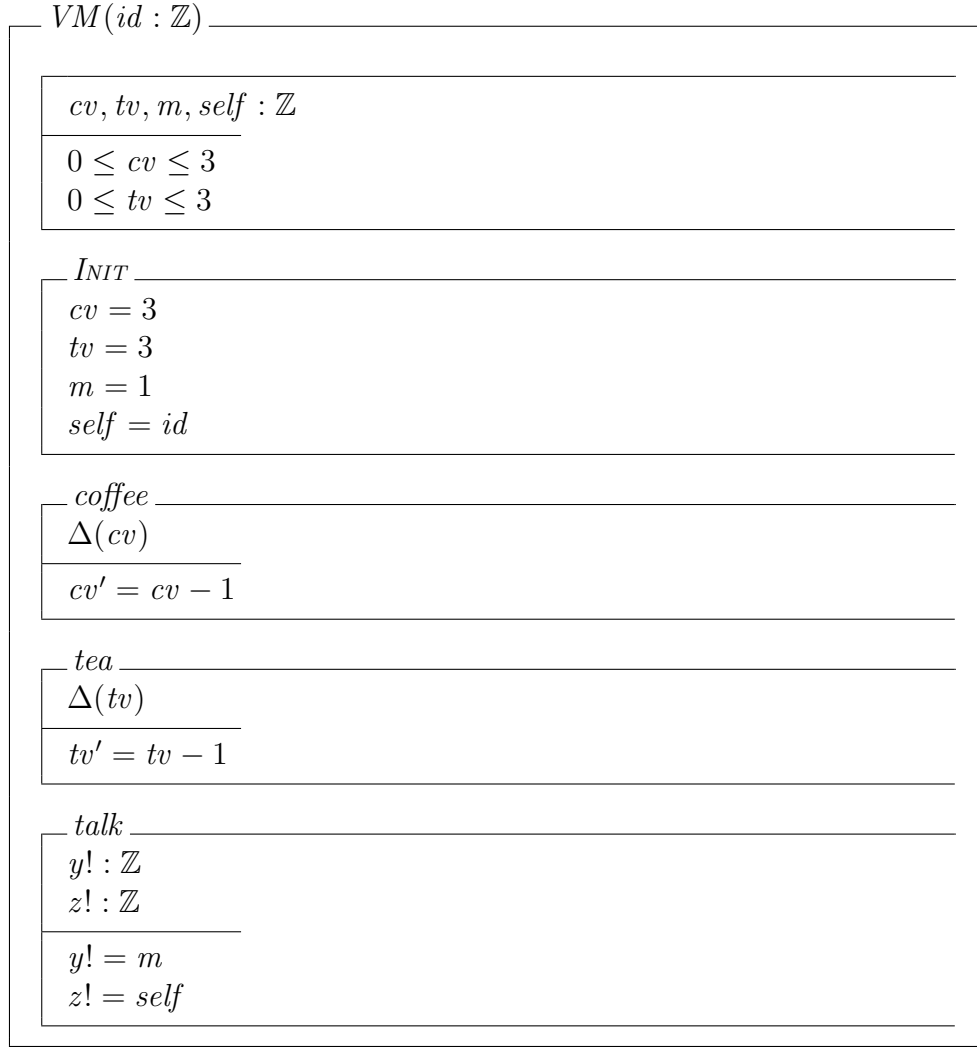


Figure 2.19: *VM* class: *instance reference*.

## 2.2.2 Semantics

To understand the operational semantics of OZ we will use a labelled transition system LTS. Using this LTS we can investigate the state evolution of a OZ object . The definition of this LTS is adapted from Definition 2.1.5 with some changes.

**Definition 2.2.1 (LTS of OZ)** The labelled transition system  $(\mathcal{S}^{OZ}, \mathcal{T})$  of OZ class states over the set of operations, has the valid states  $\mathcal{S}^{OZ}$  as its states and its transitions  $\mathcal{T}$  are those which can be inferred from the following rule:

$$\underline{OPER} : PRE\_STATE \xrightarrow{operation} POST\_STATE. \quad \triangle$$

An example of using the transition rule of this LTS is: drawing the transition graph of vending machine shown in Figure 2.17. The transition graph is shown in Figure 2.20, where we show only a small part of it. The transitions *coffee* and *tea* refer to the operation schema *coffee* and *tea*. Thus, using the LTS we can enumerate all possible states transitions of an OZ state.

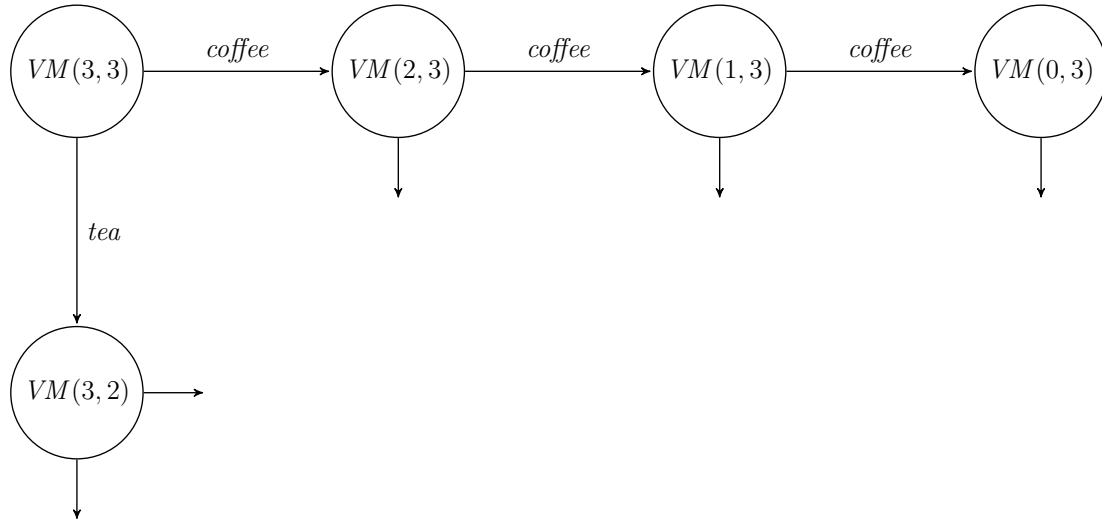


Figure 2.20: VM Transition graph

### 2.2.3 Dynamic OZ

OZ can be used to model an entity with unchanged behavior, but some time we need to model an entity that changes its behavior. The state pattern is used to solve this problem.

#### OZ and state pattern

The state pattern is a behavioral software design pattern. An object changes its class when its internal state changes. To illustrate the idea imagine that our vending machine *VM* is a mobile vending machine and that it is connected by a wireless link *talk* to a shop *Shop1*. On signal fading *Shop1* decides to send the link *talk* to another shop *Shop2* through the link *switch* as shown in Figure 2.21. OZ can be used to model the shop with considering the state pattern. When *switch* occurs

- *Shop1* sends *talk* via *switch* and changes its class from *ActiveShop* to *IdleShop* as shown in Figure 2.22.

- *Shop2* receives *talk* via *switch* and changes its class from *IdleShop* to *ActiveShop* as shown in Figure 2.23.

Notice, when an object changes its class it keeps its state variables and skips the *Init* schema of the new class.

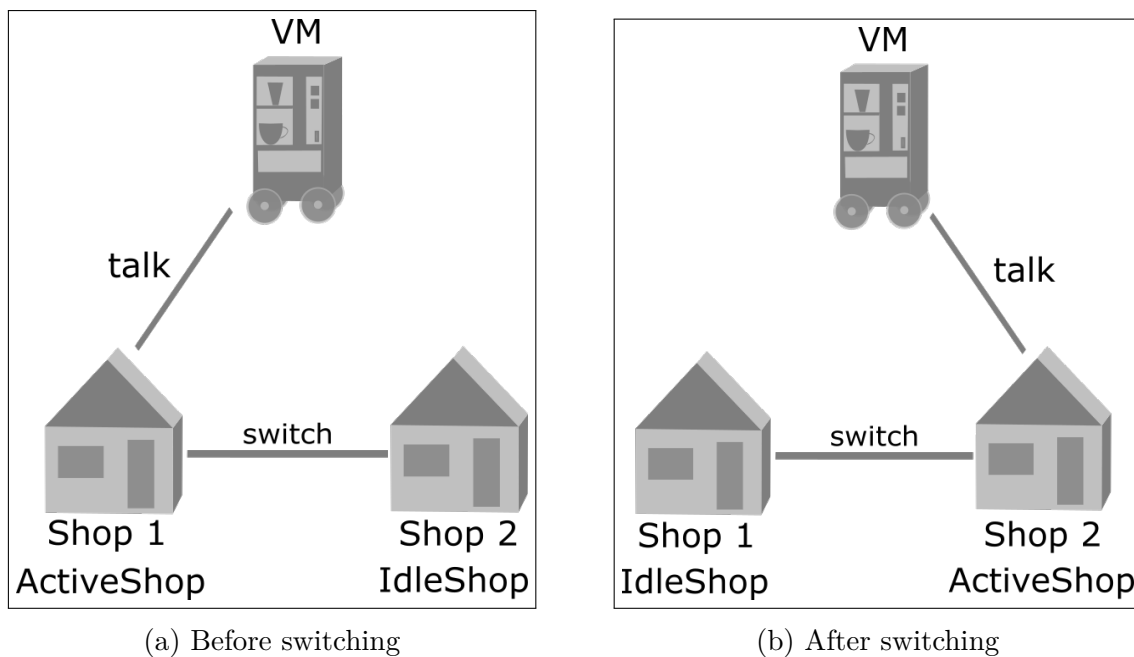


Figure 2.21: Mobile vending machine and shops

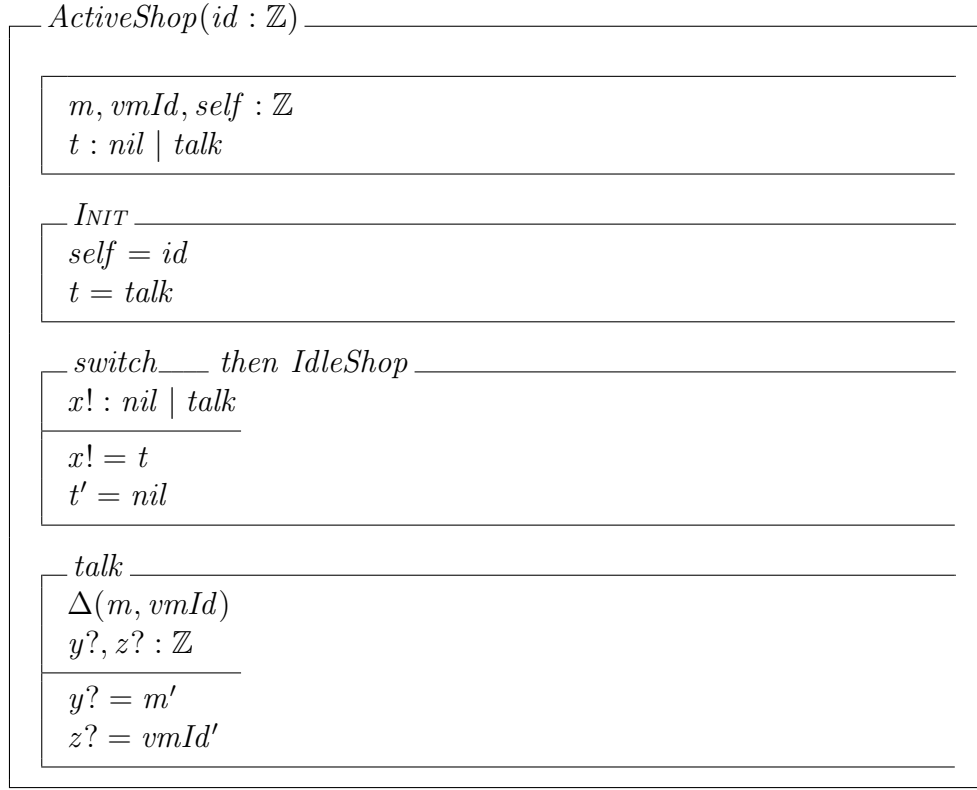


Figure 2.22: active shop

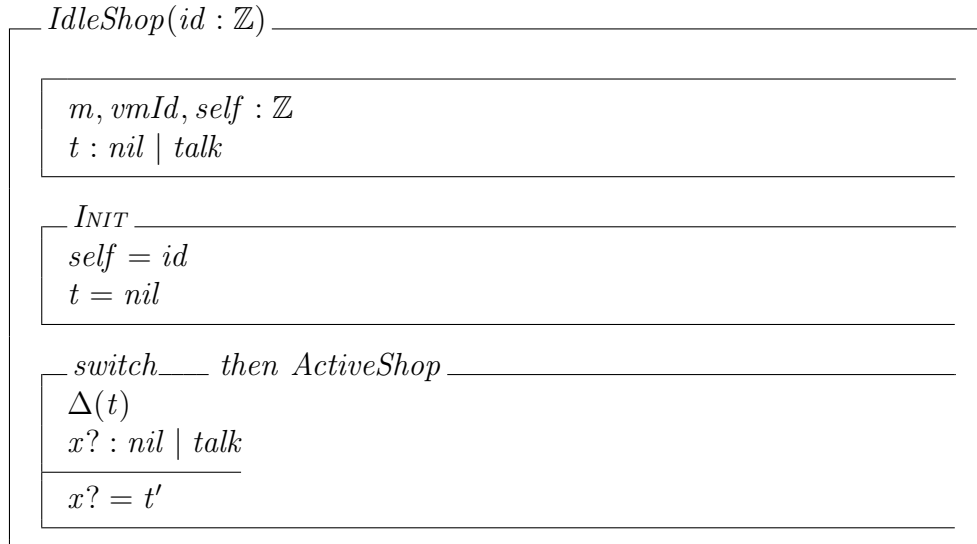


Figure 2.23: idle shop

### Restriction

In this work when we use OZ to model an operation, we restrict our self to use only one type of parameters in the operation schema. Either input or output. This can be noticed in the operation schema *talk* in:

- In Figure 2.19 all the parameters of the operation schema *talk* are output paramaters.
- In Figure 2.22 all the parameters of the operation schema *talk* are input paramaters.

**Question:** why this restriction?

**Answer:** because a channel in  $\pi$ -calculus is unidirectional pro reaction. In the next chapter we will map the OZ class constructs to  $\pi$ -calculus constructs, so we will map an OZ operation to an  $\pi$ -calculus name , .i.e., channel. In  $\pi$ -calculus a processes can send or receive over a channel pro reaction, but not the both together.



### 3 Transformational semantics of OZ

This chapter study the syntactic transformation of OZ class into  $\pi$ -calculus process. The resulting processes is intuitively defined as follow:

$$P_{OZ\_part\_as\_process} = \sqcap_{v\_st} Q(v\_st, v\_self)$$

$$Q(v\_st, v\_self) = (\sqcap_{c, v\_in_c} \sqcap_{v\_st'} c.v\_in_c +$$

$$\sqcap_{c, v\_out_c} \sqcap_{v\_st'} c.v\_out_c) \rightarrow Q(v\_st', v\_self) \text{ where:}$$

- $c$  refers to an operation.
- $v\_st$  refers to the state variables.
- $v\_self$  refers to the instance reference.
- $c.v\_in_c$  refers to the occurrence of the operation  $c$ , where  $v\_in_c$  represents the values of the input parameters of  $c$ .
- $c.v\_out_c$  refers to the occurrence of the operation  $c$ , where  $v\_out_c$  represents the values of the output parameters of  $c$ .
- $\sqcap$  deterministic choice,  $\sqcap$  non deterministic choice,  $+$  choice.

**Question 1:** what is the benefit of transforming an OZ class into  $\pi$ -calculus process?

**Answer:** to combine it, using parallel operator, with a second  $\pi$ -calculus processes.

**Question 2:** what is the benefit of the second processes?

**Answer:** the second processes represents sequences of behavior. This will enable us to study the behavior of an entity as will be shown later in the next chapter.

To transform OZ class into  $\pi$ -calculus process we need to remember that  $\pi$ -calculus has only names and processes, and nothing other. A *name* in  $\pi$ -calculus can be seen as a *channel* or a *memory location*. Thus, in this work when we use the word *channel* we refer to  $\pi$ -calculus *name*. We need to use the names and processes to represent: value, state variable, state schema, initial state schema and operation schema in  $\pi$ -calculus.

## 3.1 Mapping values

In this thesis we restrict ourselves to two bits binary numbers shown Table 3.1. A value can be mapped to a  $\pi$ -calculus processes. Figure 3.1 shows the  $\pi$ -calculus implantation of the values 0,1,2,3 in ABC syntax. The keyword **agent** defines a new processes. The process *Zero* receives two channels *tt*, *ff* via the channel *a*, then it sends two signals via the channel *ff*. A value will be deleted when it receives a signal via *a*.

Decimal	Binary
0	00
1	01
2	10
3	11

Table 3.1: Two bits binary numbers

```
agent Zero(a) = a(tt, ff). 'ff. 'ff. Zero(a) + a.0
agent One(a) = a(tt, ff). 'tt. 'ff. One(a) + a.0
agent Two(a) = a(tt, ff). 'ff. 'tt. Two(a) + a.0
agent Three(a) = a(tt, ff). 'tt. 'tt. Three(a) + a.0
```

Figure 3.1: 0,1,2,3 as  $\pi$ -calculus processes.

## 3.2 Mapping state variables

A variable can be mapped to a channel. Creating a variable *x* and initializing it with the value 0 ( `int x = 0;`) is mapped to creating a new channel *x* and initialize the processes *Zero* with the channel *x* as shown in Figure 3.2. The wide hat refers to creating a new channel.

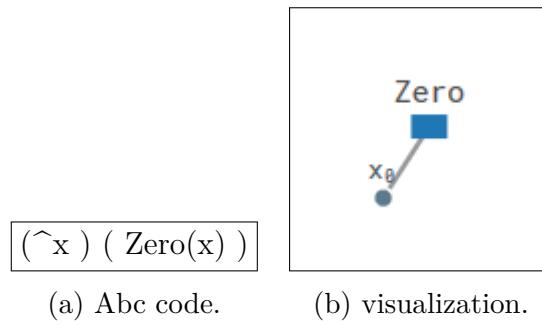


Figure 3.2: variable as a channel

### 3.3 Mapping Data Types

Still under construction.

### 3.4 Mapping mathematical operations

#### **Addition:**

To add two numbers we need an addition processes that mimics the behavior of arithmetic circuits for adding two bits binary numbers shown in Figure 3.3. Figure 3.4 shows visualization of the addition process and the ABC code. The full implementation of *Add* processes can be found in the appendix.

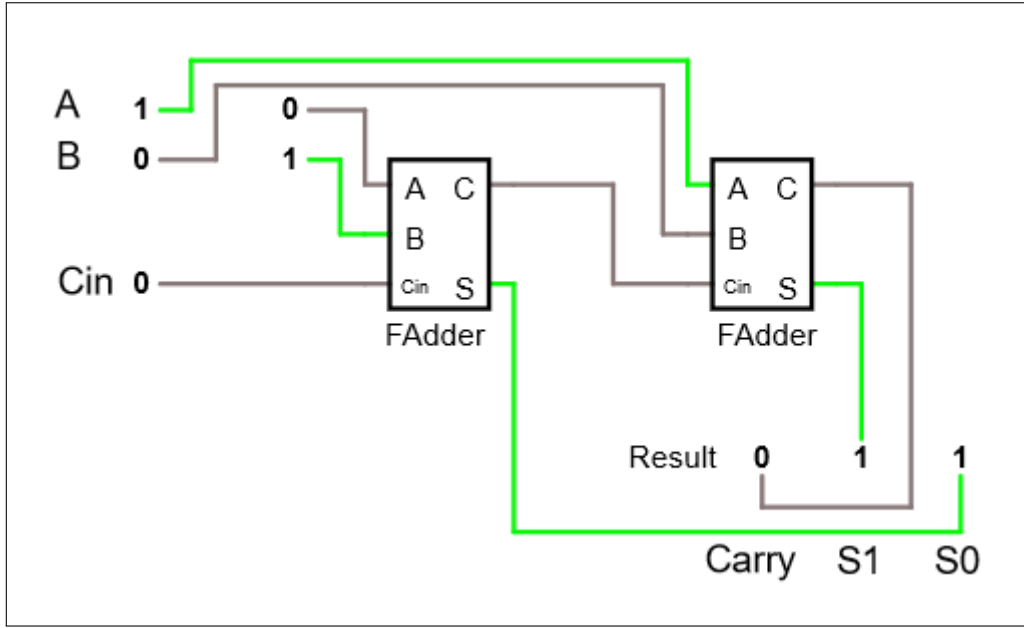
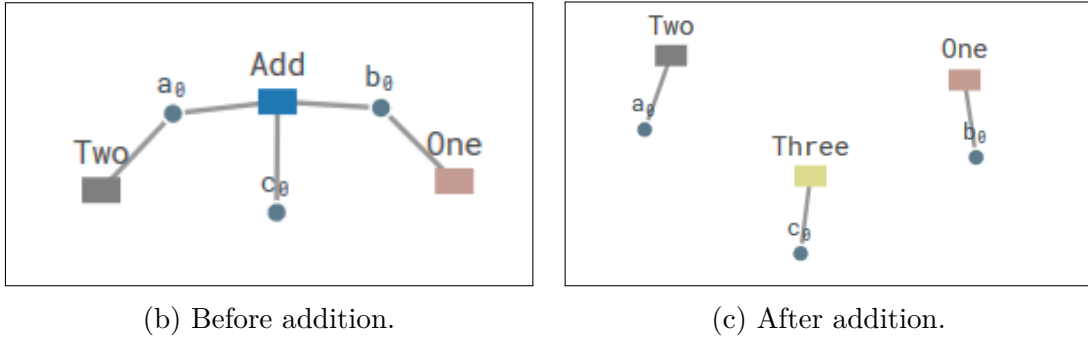


Figure 3.3: adder circuit

$$(\hat{a}, b, c) \ ( \text{Two}(a) \mid \text{One}(b) \mid \text{Add}(a, b, c) )$$

(a) Abc code.



(b) Before addition.

(c) After addition.

Figure 3.4: addition as a process

### **subtraction:**

To subtract two numbers we need an subtraction processes that mimics the behavior of arithmetic circuits for subtracting two bits binary numbers shown in Figure 3.5. Figure 3.6 shows visualization of the subtraction process and the ABC code. The full implementation of *Sub* processes can be found in the appendix.

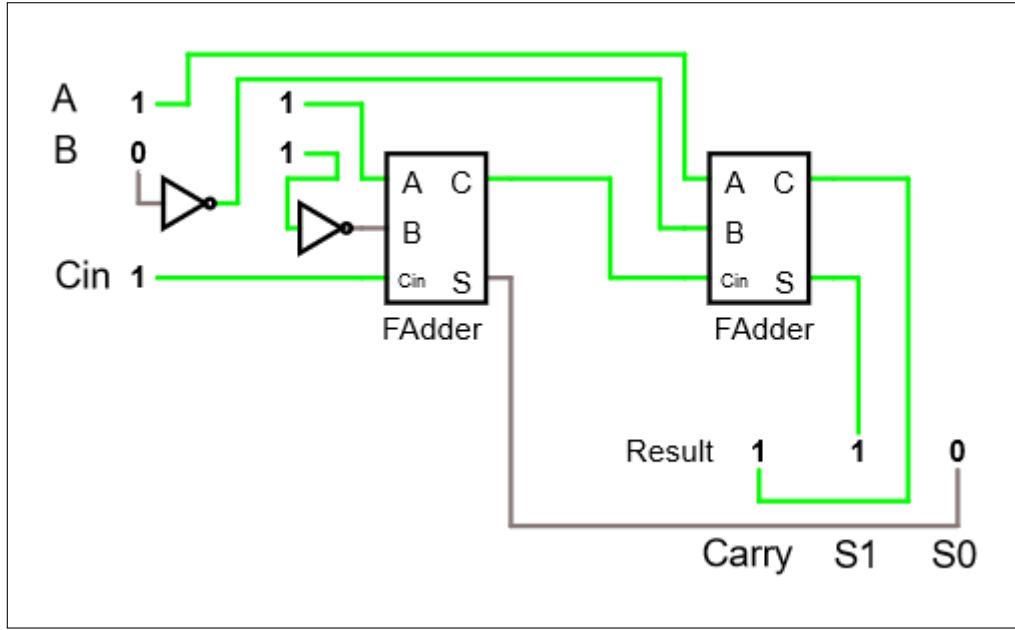
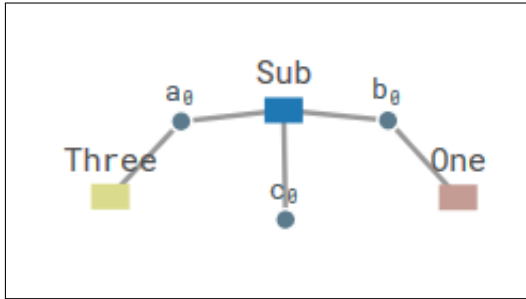


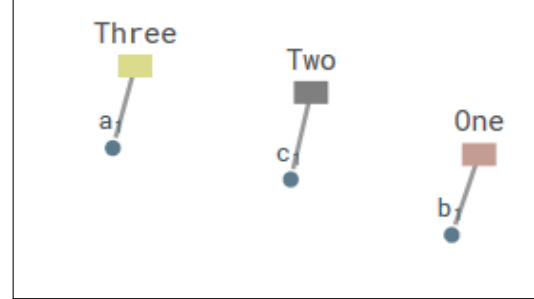
Figure 3.5: subtractor circuit

$$(\wedge a, b, c) ( \text{Three}(a) \mid \text{One}(b) \mid \text{Sub}(a, b, c) )$$

(a) Abc code.



(b) Before subtraction.



(c) After subtraction.

Figure 3.6: subtraction as a process

### comparation:

To compare two numbers we need a processes that mimics the behavior of arithmetic circuits for comparing two bits binary numbers shown in Figure 3.7. Figure 3.8 shows visualization of the comparator process and the ABC code. The full implementation of *Compare* processes can be found in the appendix.

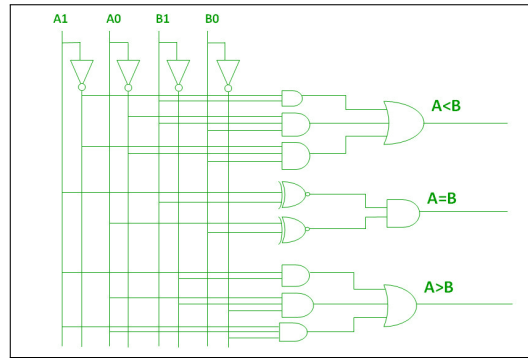
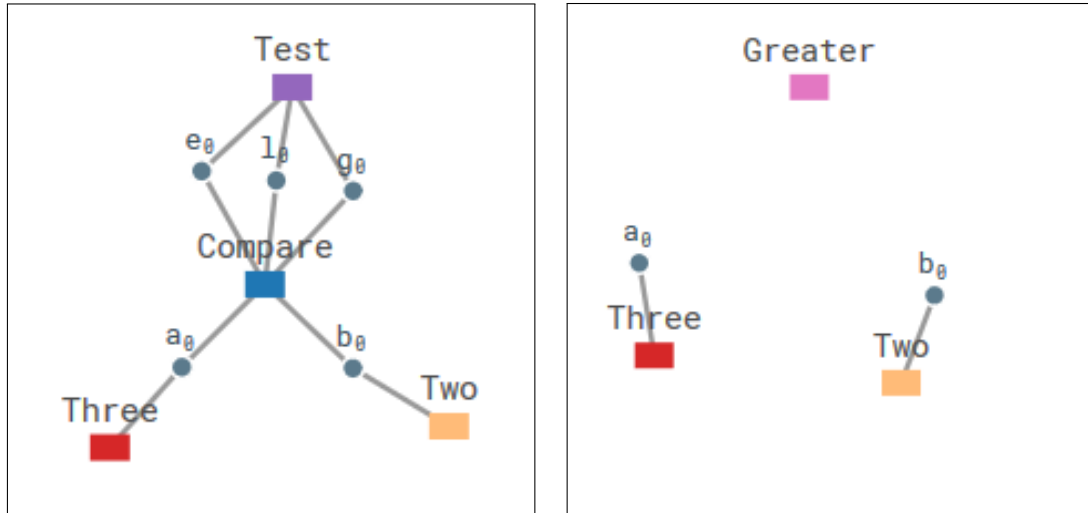


Figure 3.7: comparator circuit

$(\wedge a, b, g, e, l) \ ( \text{Three}(a) \mid \text{Two}(b) \mid \text{Compare}(a, b, g, e, l) \mid \text{Test}(g, e, l) )$

(a) Abc code.



(b) Before comparison.

(c) After comparison.

Figure 3.8: comparison as a process

### ***Set union and subtraction:***

The implementation of set union and abstraction processes can be found in the appendix.

## **3.5 Mapping state schema**

mapping

## 3.6 Mapping initial state schema

mapping

## 3.7 Mapping operation schema

mapping

## 3.8 Mapping class

mapping





## **4 Conclusion and future work**

In this thesis ...



# 5 Appendix

## 5.1 Addition

```
agent Example = (^a,b,c) (Two(a) | One(b) | Add(a,b,c))

agent Add(a,b,c)= (^t1,f1,t2,f2) ('a<t1,f1>.'b<t2,f2>.(^
  cin_t,cin_f,cout_t,cout_f,s2_t,s2_f,cout3_t,cout3_f,s3_t,
  s3_f) ( \
FullAdderWait(t1,f1,t2,f2,cin_t,cin_f,cout_t,cout_f,s2_t,
  s2_f) \
| 'cin_f \
| FullAdderWait(t1,f1,t2,f2,cout_t,cout_f,cout3_t,cout3_f,
  s3_t,s3_f) \
| Result(s2_t,s2_f,s3_t,s3_f,cout3_t,cout3_f,c) \
))

agent Result(s0_t,s0_f,s1_t,s1_f,c_t,c_f,res) = \
s0_f.(s1_f.(c_f.Zero(res) + c_t.Overflow) + s1_t.(c_f.Two(
  res)+ c_t.Overflow)) \
+ s0_t.(s1_f.(c_f.One(res) + c_t.Overflow) + s1_t.(c_f.Three
  (res)+ c_t.Overflow))

agent Overflow = 0

agent FullAdderWait(t1,f1,t2,f2,cin_t,cin_f,cout3_t,cout3_f,
  s3_t,s3_f) = \
```

```
cin_t.( 'cin_t | FullAdder(t1,f1,t2,f2,cin_t,cin_f,cout3_t,
    cout3_f,s3_t,s3_f)) \
+ cin_f.( 'cin_f | FullAdder(t1,f1,t2,f2,cin_t,cin_f,cout3_t,
    cout3_f,s3_t,s3_f))

agent FullAdder(t1,f1,t2,f2,cin_t,cin_f,cout_t,cout_f,s2_t,
    s2_f) = \
(^t1a,f1a,t1b,f1b,t2a,f2a,t2b,f2b,c1_t,c1_f,s1_t,s1_f,c2_t,
    c2_f,s1_ta,s1_fa,s1_tb,s1_fb,cin_ta,cin_fa,cin_tb,cin_fb)
\
( \
HalfAdder(t1,f1,t1a,f1a,t1b,f1b,t2,f2,t2a,f2a,t2b,f2b,c1_t,
    c1_f,s1_t,s1_f) \
| HalfAdder(s1_t,s1_f,s1_ta,s1_fa,s1_tb,s1_fb,cin_t,cin_f,
    cin_ta,cin_fa,cin_tb,cin_fb,c2_t,c2_f,s2_t,s2_f) \
| OR(c1_t,c1_f,c2_t,c2_f,cout_t,cout_f) \
)

agent HalfAdder(t1,f1,t1a,f1a,t1b,f1b,t2,f2,t2a,f2a,t2b,f2b,
    c_t,c_f,s_t,s_f) = (Repeate(t1,f1,t1a,f1a,t1b,f1b) |
    Repeate(t2,f2,t2a,f2a,t2b,f2b) | AND(t1a,f1a,t2a,f2a,c_t,
    c_f) | XOR(t1b,f1b,t2b,f2b,s_t,s_f))

agent AND(t1,f1,t2,f2,o_t,o_f) = f1.(f2.'o_f + t2.'o_f) + t1
    .(f2.'o_f + t2.'o_t)
agent NAND(t1,f1,t2,f2,o_t,o_f) = f1.(f2.'o_t + t2.'o_t) +
    t1.(f2.'o_t + t2.'o_f)

agent OR(t1,f1,t2,f2,o_t,o_f) = f1.(f2.'o_f + t2.'o_t) + t1
    .(f2.'o_t + t2.'o_t)
agent NOR(t1,f1,t2,f2,o_t,o_f) = f1.(f2.'o_t + t2.'o_f) + t1
    .(f2.'o_f + t2.'o_f)
```

```
agent XOR(t1,f1,t2,f2,o_t,o_f) = f1.(f2.'o_f + t2.'o_t) + t1
    .(f2.'o_t + t2.'o_f)
agent XNOR(t1,f1,t2,f2,o_t,o_f) = f1.(f2.'o_t + t2.'o_f) +
    t1.(f2.'o_f + t2.'o_t)

agent Zero(a) = a(tt,ff).'ff.'ff.Zero(a) + a.0
agent One(a) = a(tt,ff).'tt.'ff.One(a) + a.0
agent Two(a) = a(tt,ff).'ff.'tt.Two(a) + a.0
agent Three(a) = a(tt,ff).'tt.'tt.Three(a) + a.0

agent Send(a) = 'a

agent Neg(tt,ff) = tt.'ff + ff.'tt

agent Repeate(tt,ff,ta,fa,tb,fb) = tt.('ta | 'tb) + ff.('fa
    | 'fb)
```



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# Index

## Symbols

$\alpha$ -conversion ..... 13 f  
 $\tau$  process ..... 10  
 $\pi$ -calculus ..... 5, 7 – 29  
    polyadic ..... 8

## A

action ..... 9, 20  
    input ..... 10, 20  
    internal ..... 10  
    output ..... 10, 20  
    silent ..... 10

## B

bisimulation  
    strong ..... 32  
    weak ..... 32

## C

call ..... 11  
channel ..... 8  
choice ..... 10  
commitments ..... 33

## D

## E

## F

free name ..... 12  
    action ..... 20

## G

## I

## K

## L

## M

message ..... 8

## N

name ..... 8  
    bound ..... 12, 20  
    free ..... 12, 20  
    process ..... 12  
    substitution ..... 13

## O

## P

parallel composition ..... 10  
parameter ..... 10  
polyadic  $\pi$ -calculus ..... 8  
prefix ..... 8  
    input ..... 9  
    operator ..... 6  
    output ..... 8  
    process ..... 9  
    silent ..... 9  
process ..... 9  
     $\tau$  ..... 10  
    algebra ..... 1, 7  
    call ..... 11



choice .....	10
input .....	10
output .....	10
parallel .....	10
prefix .....	9
restriction .....	10
stop .....	9

## R

## S

silent	
action .....	10
prefix .....	9
simulation	
strong .....	32
weak .....	32
stop process .....	9
strong	
simulation .....	32
subject .....	10, 38
sum .....	9
summation .....	9

## T

transition system

## U

## V

## W

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# Erklärung

Hiermit versichere ich, dass ich diese Arbeit selbstständig verfasst und keine anderen als die angegebenen Quellen und Hilfsmittel benutzt habe. Außerdem versichere ich, dass ich die allgemeinen Prinzipien wissenschaftlicher Arbeit und Veröffentlichung, wie sie in den Leitlinien guter wissenschaftlicher Praxis der Carl von Ossietzky Universität Oldenburg festgelegt sind, befolgt habe.

Oldenburg, den 11. März 2020

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(Muhammad Ekbal Ahmad)