

Question 1

A sorting method with “Big-Oh” complexity $O(n \log_{10} n)$ spends exactly 1 millisecond to sort 1,000 data items. Assuming that time $T(n)$ of sorting n items is directly proportional to $n \log_{10} n$, that is, $T(n) = (cn \log_{10} n)$, where c is a constant. Derive a formula for $T(n)$, given the time $T(N)$ for sorting N items, and estimate how long this method will sort 1,000,000 items.

Question 2

Assume that each of the expressions below gives the processing time $T(n)$ spent by an algorithm for solving a problem of size n . Select the dominant term(s) having the steepest increase in n and specify the lowest Big-Oh complexity of each algorithm.

Expression	Dominant term(s)	Big-Oh complexity
$5 + 0.0001n^3 + 0.025n$		
$500n + 100n^{1.5} + 50n \log_{10} n$		
$n^2 \log_2 n + n(\log_2 n)^2$		

Question 3:

The number of operations executed by algorithms A and B is $8n \lg n$ and $2n^2$, respectively. Determine n^0 such that A is better than B for $n \geq n^0$.