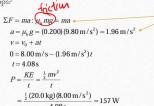
7. Work and Energy Part 1

Practice Question 7

A 20.0 kg rock is sliding on a rough, horizontal surface at 8.00 m/s and eventually stops due to friction. The coefficient of kinetic friction between the rock and the surface is 0.200. What average thermal power is produced as the rock stops?



Which will be negative.

a is the acceleration that friction force is providing.

Practice Question 5

A 0.100 kg potato is tied to a string with length 2.50 m, and the other end of the string is tied energy. The spring is released and the crate sheles 5.60 m beft to a rigid support. The potato is held straight our horizontally from the point of support, with speed of the crate when it is 2.00 m from its minal positions, the string palled taut, and is their released, a) What is the sprend of the potato at the lowest when it is 2.00 m from its minal positions. What done is faither appoint to the time is to a least support to the string palled the sprend of the potato at the lowest point of its motion? b) What is the tension in the string palled the point of its motion? b)

a) The kinetic energy of the potato is the work done by gravity (or the energy lost), $\frac{1}{2} an^2 = aggl$, or $v = \sqrt{2gg} = \sqrt{2(9.80 \text{ m/s}^2)(2.50 \text{ m})} = 7.00 \text{ m/s}^2$.

$$T - mg = m - \frac{1}{I} = 2mg$$

so T 3mg 3(0.100 kg)(9.80 m/s²) 2.94 N.

A 600 kg skier starts from set at the top of a ski slope 65.0 m high, a) If frictional forces do -10.5 kg or work on her as the descen how fast is the going at the bottom of the sloper b) Now moving horizontally, the skier crosser a patch of soft mow, where coefficion for kinetic friction in 0.20. If the patch is 82.0 m wide and the average force of air resistance on the skier is 160 N, how fast is the ge after crossing the patch? c) The skier hir a succonditify and penetrates -2.5 m into it before coming to a stop. What is the average force of an experiment of the skier is 160 N, how fast is the average force of a min or before coming to a stop. What is the average force of a min or before coming to a stop. What is the average force of a min or before coming to a stop. What is the average force of a min or before coming to a stop. What is the average force of a min or before coming to a stop. What is the average force of a min or before coming to a stop. What is the average force of a min or before coming to a stop. What is the average force of a min or before coming to a stop. What is the average force of a min or before coming to a stop. What is the average force of an extension of the stop of the stop of the average force of an extension of the stop of the stop

 $v_2 = \sqrt{\frac{2K}{m}} = \sqrt{\frac{2(4957 \text{ J})}{60 \text{ kg}}} = 12.85 \text{ m/s} \approx 12.9 \text{ m/s}$

c) Use the Work-Energy Theorem to find the force. $W=\Delta KE$, $F=KE/d=(4957\ \mathrm{J})/(2.5\ \mathrm{m})=1983\ \mathrm{N}\approx2000\ \mathrm{N}$.

8. Work and Energy Part 2

On a horizontal surface, a crate with mass 50.0 kg is placed against a spring that stores 360 J of energy. The spring is released and the crate slides 5.60 m before coming to rest. What is the

Work done by friction against the crate brings it to a latti- $f_a x =$ potential energy of compressed: $f_a = \frac{360 \text{ J}}{5.60 \text{ m}} = 64.29 \text{ N}$

 $v^2 = \frac{2(231.4 \text{ J})}{60.0 \text{ kg}} = 9.256 \text{ m}^2/\text{s}^2$

10. Momentum and Collisions Part 2

Momentum and Collisions Part 1

Practice Question 3

On a frictionless, horizontal air table, puck A (with mass 0.250 kg) is moving towards puck B (with mass 0.350 kg), that is initially at rest. After the collision, puck A has a velocity of 0.120 m/s to the left, and puck B has velocity 0.659 m/s to the right. a) What was the speed of puck A hefore the collision B) Calculate the change in the total laintic energy of the system that occurs during the collision

 $\Delta K = K_2 - K_1 = \frac{1}{2} m_d v_{dd}^2 + \frac{1}{2} m_d v_{dd}^2 - \frac{1}{2} m_d v_{dd}^2$

Practice Question 4

On a greasy, essentially frictionless lunch counter, a 0.500 kg submarine sandwich, moving 3.00 m/s to the left, collides with an 0.250 kg grilled cheese sandwich moving 1.20 m/s to the right of the two sandwich moving 1.20 m/s to the right of the two sandwiches stick together, what is the final velocity? b) How much mechanical energy dissipates in the collision?

 $\frac{1}{2}(0.500 \text{ kg})(-3.00 \text{ m/s})^2 = \frac{1}{2}(0.250 \text{ kg})(1.20 \text{ m/s})$

11. Rotation and Moment of Inertia Part 1

Practice Question 4

The rotating blade of a blender turns with constant angular acceleration 1.50 rad/s². (a) How much time does it take to reach an angular velocity of 36.0 rad/s, starting from reat? (b) Through how many revolutions does the blade turn in this time interval?

IDENTIFY: Apply the constant angular acceleration equations to the motion. The target variables are t and $\theta - \theta_0$ SET UP: (a) $\alpha_z = 1.50 \text{ rad/s}^2$; $\omega_{0z} = 0$ (starts from rest); $\omega_z = 36.0 \text{ rad/s}$; t = ?

 $\omega_{-} = \omega_{n-} + \alpha_{-}I$

EXECUTE: $t = \frac{\omega_z - \omega_{0z}}{\alpha_z} = \frac{36.0 \text{ rad/s} - 0}{1.50 \text{ rad/s}^2} = 24.0 \text{ s}$ **(b)** $\theta - \theta_0 = ?$

 $\theta - \theta_0 = \omega_{0,t} + \frac{1}{2}\alpha_s t^2 = 0 + \frac{1}{2}(1.50 \text{ rad/s}^2)(2.40 \text{ s})^2 = 432 \text{ rad}$

EVALUATE: We could use $\theta - \theta_0 = \frac{1}{2}(\omega_s + \omega_{r_0})t$ to calculate $\theta - \theta_0 = \frac{1}{2}(0 + 36.0 \text{ rad/s})(24.0 \text{ s}) = 432 \text{ rad}$, which

Practice Question 6

A hall with mass M, moving horizontally at 5.00 m/s, collides elastically with a block of mass 3M that is initially hanging at test from the ceiling on the end of a 50.0 cm wire. Find the maximum angle through which the block swings after it is bit.

EXECUTE: (a) $\frac{1}{2}mv^2 = mgh$ so $v = \pm \sqrt{2gh}$

The impulse is 0.474 kg·m/s, upward.

Collision: Momentum conservation gives $\frac{1}{2}mv_0^2 = \frac{1}{2}mv_1^2 + \frac{1}{2}(3m)v_1^2$ $v_0^2 = v_1^2 + 3v_1^2$

 $x_{\rm f} = \frac{(4.00~{\rm kg})(0.750~{\rm m}) + (3.00~{\rm kg})(-0.900~{\rm m}) + (2.00~{\rm kg})(-1.80~{\rm m})}{0.000~{\rm kg}} = -0.366~{\rm m}$

A steel ball with mass 40.0 g is dropped from a height of 2.00 m onto a horizontal steel slab. The ball rebounds to a height of 1.60 m. (a) Calculate the impulse delivered to the ball during impact. (b) If the ball is in contact with the slab for 2.00 ms, find the average force on the ball during impact.

Practice Question 2

SET UP. Use coordinates with the take at the large and the + and + axes along the horizonal and vertical but in the figure in the problem. Let (x_1, x_1) and (x_1, x_2) be the coordinates of the but before and after the vertical but in protect. Let object 1 be the horizontal but, object 2-beg the vertical but and 5 be the boil.

EXECUTE: $x_1 = \frac{m_1 x_1 + m_2 x_2 + m_3}{m_1 + m_2 + m_3} = \frac{(0.01 \log X_2 + 0.0) + 0.01}{(0.01 \log X_2 + 0.00)} = 0.333 \text{ m}.$ Figure 1. The problem is $(0.01 \log X_2 + 0.00) = 0.033 \text{ m}$.

 $Y_i = \frac{m_b y_1 + m_2 y_2 + m_b y_2}{m_t + m_2 + m_3} = \frac{0 + (3.00 \text{ kg})(0.900 \text{ m}) + (2.00 \text{ kg})(1.80 \text{ m})}{9.00 \text{ kg}} = 0.700 \text{ m}$

 $y_{\ell}=0$. $x_{\ell}-x_{i}=-0.700$ m and $y_{\ell}-y_{i}=-0.700$ m . The center of mass moves 0.700 m to the right and 0.700 m

EVALUATE: The vertical bar moves upward and to the right so it is sensible for the center of mass of the machine

~ Jo:45cm its initial speed is 450 m/s.

Practice Question 4

A 5.00 g bullet is shot through a 1.00 kg wood block suspended on a string 2.00 m long. The center or mass of the block rises a distance of 0.45 cm. Find the speed of the bullet as it emerges from the block

IDENTIFY: Apply conservation of momentum to the collision and conservation of energy to the motion of the block after the collision.

Set The: Let *a be to the right. Let the bullet be A and the block be B. Let F be the velocity of the block joar after

Motion of block after the collision: $K_1 = U_{good}$, $\frac{1}{2}m_gV^2 = m_ggh$ $V = \sqrt{2gh} = \sqrt{2(9.80 \text{ m/s}^2)(0.450 \times 10^{-2} \text{ m})} = 0.297 \text{ m/s}^2$ $\begin{array}{l} = 0.257 \; \mathrm{mis} \; A_{12} + 2.57 \; \mathrm{mis} \; A_{12} + 2.07 \; \mathrm{mi$

Practice Question 6

 $v_{1y} = +\sqrt{2(9.80 \text{ m/s}^2)(2.00 \text{ m})} = 6.26 \text{ m/s}$. $v_{2y} = -\sqrt{2(9.80 \text{ m/s}^2)(1.60 \text{ m})} = -5.60 \text{ m/s}$.

(b) $F_3 = \frac{J_3}{\Delta t} = \frac{-0.474 \text{ kg} \cdot \text{m/s}}{2.00 \times 10^{-3} \text{ s}} = -237 \text{ N}$. The average force on the ball is 237 N, upward. EVALUATE: The upward force on the ball changes the direction of its momentum.

 $J_y = \Delta p_y = m(v_{2y} - v_{ly}) = (40.0 \times 10^{-3} \text{ kg})(-5.60 \text{ m/s} - 6.26 \text{ m/s}) = -0.474 \text{ kg} \cdot \text{m/s}$

A high-speed flywheel in a motor is spinning at 500 rpm when a power failure suddenly occurs. The flywheel has mass 40.0 kg and diameter 75.0 cm. The power is off for 30.0 s, and during this time the flywheel slows due to friction in its aske bearings. During the time the power is off, the flywheel makes 200 complete revolutions. (a) At what tate is the flywheel spinning when the power comes back on? O How long after the beginning of the power failure would it have taken the flywheel to stop if the power had not come back on, and how many revolutions would the wheel have made

IDENTIFY: Apply constant angular acceleration equations. **SET UP:** Let the direction the flywheel is rotating be positive $\theta - \theta_0 = 200$ rev. $\alpha \theta_0 = 500$ rev/min = 8.333 rev/s. t = 30.0 s

EXECUTE: (a) $\theta - \theta_0 = \left(\frac{\omega_{0z} + \omega_z}{2}\right) t$ gives $\omega_z = 5.00 \text{ rev/s} = 300 \text{ rpm}$

(b) Use the information in part (a) to find α : $\omega = \omega_x + \alpha t$ gives $\alpha_x = -0.1111 \text{ rev/s}^2$. Then $\omega_x = 0$. $\alpha_z = -0.1111 \text{ rev/s}^2$, $\omega_{0z} = 8.333 \text{ rev/s}$ in $\omega_z = \omega_{0z} + \alpha_z t$ gives t = 75.0 s and $\theta - \theta_0 = \left(\frac{\omega_{0z} + \omega_z}{2}\right) t$ gives

 $\theta-\theta_0=312~\text{rev}$. EVALUATE: The mass and diameter of the flywheel are not used in the calculation

12. Rotation and Moment of Inertia Part 2 Practice Question 4

A thin, rectangular sheet of metal has mass M and sides of length a and b. Use the parallel-axis theorem to calculate the moment of Inertia of the sheet for an axis that is perpendicular to the plane of the sheet and that passes through one corner of the sheet.

Execute: $I_P = I_{cm} + Md^2$



 $I_{cm} = \frac{1}{12}M(a^2 + b^2).$ The distance d of P from the cm is $d = \sqrt{(a/2)^2 + (b/2)^2}.$

Thus $I_p = I_{cos} + Md^2 = \frac{1}{12}M(a^2 + b^2) + M(\frac{1}{4}a^2 + \frac{1}{4}b^2) = (\frac{1}{12} + \frac{1}{4})M(a^2 + b^2) =$ $\frac{1}{2}M(a^2+b^2)$

Practice Question 9

According to the shop manual, when drilling a 12.7-mm-diameter hole in wood, a drill should have a speed of 1250 rev/min. For a 12.7-mm-diameter drill bit turning at a constant 1250 rev/min, find (a) the maximum linear speed of any part of the bit and (b) the maximum radial acceleration of any part of the

IDENTIFY: $v = r\omega$ and $a_{rad} = r\omega^2 = v^2/r$ **SET UP:** $2\pi \text{ rad} = 1 \text{ rev}$, so $\pi \text{ rad/s} = 30 \text{ rev/min}$ EXECUTE: (a) $\omega r = (1250 \text{ rev/min}) \left(\frac{\pi \text{ rad/s}}{30 \text{ rev/min}} \right) \left(\frac{12.7 \times 10^{-8} \text{m}}{2} \right) = 0.831 \text{ m/s}.$ **(b)** $\frac{v^2}{r} = \frac{(0.831 \text{ m/s})^2}{(12.7 \times 10^{-3} \text{ m})/2} = 109 \text{ m/s}^2.$

EVALUATE: In $v = r\omega$, ω must be in rad/s.

Practice Question 8

required radius of the centrifuge. Is the claim realistic?

Set Up: $a_{\rm nd} = r\omega^2$ so $r = a_{\rm rad}/\omega^2$, where ω must be in rad/s EXECUTE: $a_{\text{rnd}} = 3000g = 3000(9.80 \text{ m/s}^2) = 29,400 \text{ m/s}^2$ $\omega = (5000 \text{ rev/min}) \left(\frac{1 \text{ min}}{60 \text{ s}}\right) \left(\frac{2\pi \text{ rad}}{1 \text{ rev}}\right) = 523.6 \text{ rad/s}$ Then $r = \frac{a_{\text{rad}}}{\omega^2} = \frac{29,400 \text{ m/s}^2}{(523.6 \text{ rad/s})^2} = 0.107 \text{ m}.$

EVALUATE: The diameter is then 0.214 m, which is larger than 0.127 m, so the claim is not realistic

A passenger bus in Zunich, Switzerhard, derived its motive power from the energy stored in a large flywheel. The wheel was brought up to speed periodically, when the bus storped at a station, by an electric motor, which could thus be attached to the electric power lines. The flywheel was a solid cylinder with mass 1000 kg and dameter 130 m. Its rop angular speed was 3000 w/cm/cm/cm/c/. At this angular speed, what is the kinetic energy of the fly webself (b) if the average power required to operate the bus is 18 to 1000, Nuo long could in operate between stopic.

IDENTIFY: $K = \frac{1}{2}I\omega^2$, with ω in rad/s. $P = \frac{\text{energy}}{I}$

SET UP: For a solid cylinder, $I = \frac{1}{2}MR^2$. 1 rev/min = $(2\pi/60)$ rad/s EXECUTE: (a) $\omega = 3000 \text{ rev/min} = 314 \text{ rad/s}$, $I = \frac{1}{2}(1000 \text{ kg})(0.900 \text{ m})^2 = 405 \text{ kg} \cdot \text{m}^3$

 $K = \frac{1}{2} (405 \text{ kg} \cdot \text{m}^2)(314 \text{ rad/s})^2 = 2.00 \times 10^7 \text{ J}$

(b) $t = \frac{K}{P} = \frac{2.00 \times 10^7 \text{ J}}{1.86 \times 10^4 \text{ W}} = 1.08 \times 10^3 \text{ s} = 17.9 \text{ min}$ **EVALUATE:** In $K = \frac{1}{2}I\omega^2$, we must use ω in rad/s.

About what axis will a uniform sphere have the same moment of inertia as does a thin-walled, hollow, lead sphere of the same mass and radius, with the axis along a diameter?

> SET UP: For a thin-walled hollow sphere, axis along a diameter. $I = \frac{2}{3}MR^2$ For a solid sphere with mass M and radius R, $I_{con} = \frac{2}{3}MR^2$, for an axis along a diameter

EXECUTE: Find d such that $I_n = I_m + Md^2$ with $I_n = \frac{2}{3}MR^2$.

 $\frac{2}{3}MR^2 = \frac{2}{3}MR^2 + Md^2$

The factors of M divide out and the equation becomes $(\frac{2}{3} - \frac{2}{5})R^2 = d^2$

 $d = \sqrt{(10-6)/15}R = 2R/\sqrt{15} = 0.516R.$

The axis is parallel to a diameter and is 0.516R from the center

Work Done Scalar Product of 2 Vectors W = F . S(Constant) $\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$ $W = KE = \frac{1}{2}mv^2(Kinetic)$ $\vec{B} = B_x \hat{\imath} + B_y \hat{\jmath} + B_z \hat{k}$ $\vec{A} \cdot \vec{B} = (A_x \hat{\imath} + A_y \hat{\jmath} - A_z \hat{k}) \cdot (B_z \hat{\imath} + B_y \hat{\jmath} + B_z \hat{k})$ W = GPE = mg $\vec{A} \cdot \vec{B} = A_x B_x + A_y B_y + A_z B_z$ h (Gravitational) $W = SE = \frac{1}{2}kx^2(Spring)$ $F_x = kx$ (Hooke's Law) Cannot arbitrarily assign zero value. $W = KE = \frac{1}{2}mv^{2}_{f} - \frac{1}{2}v^{2}_{i}$ $W = KE_f + GPE_f = KE_i + GPE_i$ (Same idea for GPE & SE when displacement occur) Momentum from start and end is the same(conserved) Reminder **Power** P = mv(Momentum) $F = \mu mg = ma = mg$ $P_{av} = W/t$ $J = F \times T$ SI unit: Watt(W) Properties of conservative force 1 horsepower = 746W Force is independent of path. $1 \text{ kWh} = 10^3 \text{ x} 3600 \text{ Ws} = 3.6 \text{ MJ}$ Force at end = Force at start Two cars, one a compact with mass 1200 kg and the other a large car with mass 3000 kg collide head-on at typical highway speeds, a) Which car has a greater magnitude of momentum change? Which car has a greater velocity change? Calculate the change in the velocity of the small car relative to that of the large granter velocity changes safetante the change in the velocity of the stand of learning car. b) Which car's occupants would you expect to sustain greater injuries? Explain. (a) Mountau contravation tells us that both cars have the same change in mountain, but the smaller or lass a greater velocity change because à lass a smaller mass. $M\Delta V = m\Delta v$ $\Delta v \, (\text{small car}) = \frac{M}{m} \, \Delta V \, (\text{large car})$ $=\frac{3000 \text{ kg}}{1200 \text{ kg}} \Delta V = 2.5 \Delta V \text{ (large car)}$ (b) The occupants of the small car experience 2.5 times the velocity change of those in the large car, so they also experience 2.5 times the acceleration. Therefore the feel 2.5 times the force, which causes whights had not other serious injuries. A ball with mass M, moring horizontally at 5.00 m/s, collides elastically with a block of mass MM that is initially langing at rest from the colling on the end of a 5.00 cm wire. Find the maximum angle through which the block swings after it is hit. Collision Momentum conservation gives $\frac{1}{2}(3m)c_{s}^{2} - (3m)gh - (3m)gl(1 - \cos\theta)$ $\frac{1}{2}mv_{\nu}^{2} = \frac{1}{2}mv_{1}^{2} + \frac{1}{2}(3m)v_{1}^{2}$ Moment of Inertia Kinetic energy can be written as: Moment of inertia, I, is defined as: I =1/2MR^2 For an extended rigid object (divide into small elements): $I = \lim_{\Delta m_i \to 0} \sum_i \Delta m_i r_i^2 = \int r^2 dm = \int ho r^2 dV$ $m_i = r \cdot V$ A measure of the resistance of an object to changes in its rotational motion, just as mass is a measure of the tendency of an object to resists changes in its linear motion. Mass is an intrinsic property of an object, but I depends on the physical arrangement of that mass. Also depends on the axis of rotation. Dimension: ML2; units kg.m2

Parallel axis theorem The moment of inertia about any axis parallel to and at distance D away from the axis that passes through the centre of mass is: $I = I_{\rm CM} + MD^2$ Theorem works for any solids and shapes.

Momentum and Collision

P = mv (Momentum)

$$p=\mathrm{KE}$$
 = $p=\sqrt{2mK}$

$$ec{p}_{
m tot} = ec{p}_1 + ec{p}_2 = {\sf const.}$$

Remember where all forces and momentum are present.

Elastic Collision

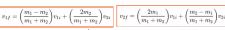






$m_1v_{1i} + m_2v_{2i} = m_1v_{1f} + m_2v_{2f}$ Momentum conservation: $\frac{1}{2}m_1v_{1i}^2 + \frac{1}{2}m_2v_{2i}^2 = \frac{1}{2}m_1v_{1f}^2 + \frac{1}{2}m_2v_{2f}^2$ Energy conservation:

Final Velocity



$$v_{2f} = \left(\frac{2m_1}{m_1 + m_2}\right)v_{1i} + \left(\frac{m_2 - m_1}{m_1 + m_2}\right)v_{2i}$$
 $m_1 + m_2$







$$\vec{v}_f = rac{m_1 \vec{v}_{1i} + m_2 \vec{v}_{2i}}{m_1 + m_2}$$

Inelastic Collision

$$\begin{split} \epsilon &= \frac{\text{Relative speed of separation}}{\text{Relative speed of approach}} \\ &= \frac{v_{2f} - v_{1f}}{v_{1f} - v_{1f}} \end{split}$$

e	Type
0	Perfectly inelastic
<1	Inclastic
1	Elastic
>1	*5

Momentum found at collision.

Angular Motion (Rotational motion of body)

Angular displacement (θ) is the angle through which Angular velocity (ω) is the rate of change of angular

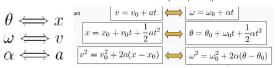
Arc length

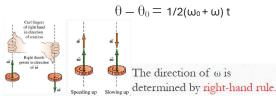
 $r = \frac{v^2}{r} = r\omega^2$ Radial acceleration

Angular acceleration (α) is the rate of change of angular velocity.

> Time present = use at Else use ar (if ask for

Kinematics (Angular vs Linear)

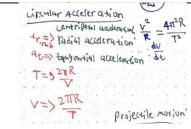




$\theta =>$ can be use to find m and angle/rad

Radians =
$$\left(\frac{\pi}{180^{\circ}}\right) \times \text{ degrees}$$

Degrees =
$$\left(\frac{180^{\circ}}{\pi}\right) \times \text{ radians}$$



Centre of Mass (Shaped object)

$$\frac{m_1x_1 + m_2x_2 + m_3x_3}{m_1 + m_2 + m_3}$$

Centre of Mass (System of particles)

$$\vec{r}_{CM} = \frac{\sum_{i} m_{i} \vec{r}_{i}}{M}$$

Centre of Mass (Extended Object)

$$\vec{r}_{CM} = \frac{1}{M} \int \vec{r} dm$$

Characteristics of CM

For a homogenous (constant density) body that has a geometric centre, the CM is the geometric centre (eg, solid sphere, cube, and cylinder.)

The centre of mass of any symmetric object lies on an axis of symmetry and on any plane of symmetry.

If g is constant over the mass distribution, the centre of gravity coincides with the centre of mass. If an object is hung freely from any point, the vertical line through this point must pass through the centre of mass. CM needs not be within the body itself

Centre of mass (Right angle triangle)

$$x_{CM} = \frac{2}{3}a$$

$$y_{CM} = \frac{1}{3}b$$

Centre of mass (Cone)

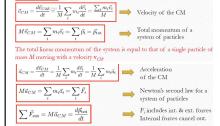
$$z_{CM} = \frac{3}{4}h$$

$$x_{CM} = 0$$

$$y_{CM} = 0$$

Motion of system of particles

 $\vec{r}_{CM} = \frac{\sum_{i} m_i \vec{r}_i}{M}$



The CM moves like an imaginary particle of mass M under the influence of the external resultant force on the system.

Moment of Inertia for different objects

