

CSD3186

Machine Learning

Classification – Performance Measurement

TP FP FN TN

		Actual Values	
		Positive (1)	Negative (0)
Predicted Values	Positive (1)	TP	FP
	Negative (0)	FN	TN

- True Positive
 - You predicted positive and it's true(correct)
- False Positive
 - You predicted positive and it's false(wrong)
 - Type 1 Error: false alarm
- False Negative
 - You predicted negative and it's false(wrong)
 - Type 2 Error: miss
- True Negative
 - You predicted negative and it's true(correct)

Confusion Matrix

- Binary-class classification problem

y	y pred	output for threshold 0.6
0	0.5	0
1	0.9	1
0	0.7	1
1	0.7	1
1	0.3	0
0	0.4	0
1	0.5	0

TP 2	FP 1
FN 2	TN 2

Beyond Accuracy - Recall Precision

- Binary-class classification problem

$$\text{Accuracy} = \frac{TP + TN}{Total}$$

- Imbalanced classification problem
 - Dataset: 100 samples, 1 positive, 99 negative
 - Model simply label any sample as negative
 - Accuracy is 99%, **would you buy the model?**
- Metrics

$$\text{Precision} = \frac{TP}{TP + FP}$$

$$\text{Sensitivity/Recall} = \frac{TP}{TP + FN}$$

Imbalanced data

- Dataset: 100 samples, 1 positive, 99 negative

- Model simply label any sample as negative

- Accuracy is 99%
- Precision is 0
- Recall is 0

$$\text{Precision} = \frac{TP}{TP + FP}$$

- Model simply label any sample as positive

- Accuracy is 1%
- Precision is 1%
- Recall is 1.0

$$\text{Sensitivity/Recall} = \frac{TP}{TP + FN}$$

Combining Precision and Call

- F1 score is the harmonic mean of precision and recall taking both metrics into account

$$F1 = \frac{2 * Recall * Precision}{Recall + Precision}$$

- The use of the harmonic mean instead of a simple average because it punishes extreme values.
 - A classifier with a precision of 1.0 and a recall of 0.0 has a simple average of 0.5 but an F1 score of 0.

Confusion Matrix

- Multi-class classification problem

Assuming a sample of 27 animals — 8 cats, 6 dogs, and 13 rabbits

		Actual class		
		Cat	Dog	Rabbit
Predicted class	Cat	5	2	0
	Dog	3	3	2
	Rabbit	0	1	11

Recall Precision

- Multi-class classification problem

$$\text{Precision}(\text{cat}) = \frac{T_{\text{cat}}}{T_{\text{cat}} + F_{\text{cat}}} = \frac{5}{7}$$

$$\text{Recall}(\text{cat}) = \frac{T_{\text{cat}}}{\# \text{ actual cat}} = \frac{5}{8}$$

		Actual class		
		Cat	Dog	Rabbit
Predicted class	Cat	5	2	0
	Dog	3	3	2
	Rabbit	0	1	11

TPR FPR TNR

- True Positive Rate/ Recall / Sensitivity

$$\text{TPR} = \frac{TP}{TP + FN}$$

- False Positive Rate

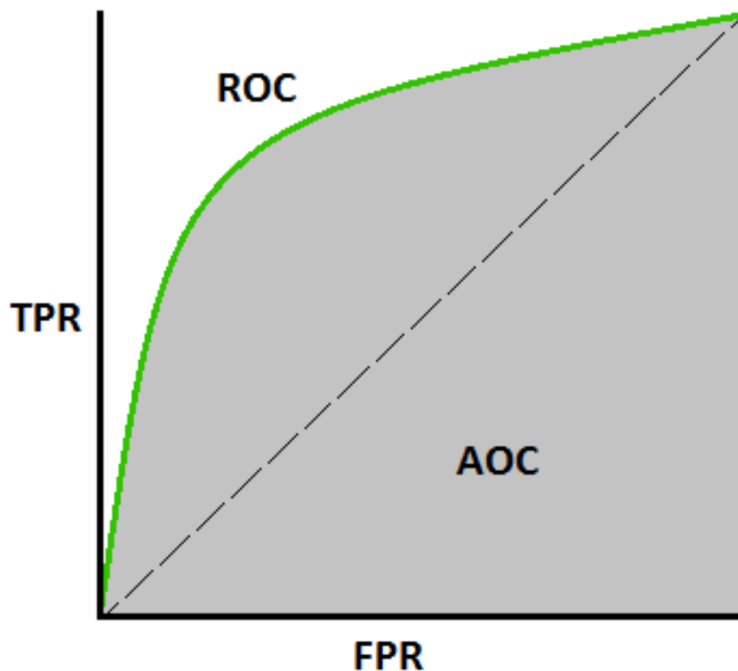
$$\text{FPR} = \frac{FP}{FP + TN}$$

- True Negative Rate/ Specificity

$$\text{TNR} = \frac{TN}{FP + TN}$$

AUROC

- Receiver Operating Characteristic
- Area Under The Curve
- Area Under the Receiver Operating Characteristics



ROC Curve and AUC (Area Under the Curve)

- **ROC Curve:** Plots the **True Positive Rate (Recall)** against the **False Positive Rate (FPR)** at different thresholds.
- **AUC:** Measures the model's ability to differentiate between classes.
 - **AUC = 1.0: Perfect classifier.**
 - **AUC = 0.5:** Random guessing.

Example:

If $AUC = 0.85$, the model has an 85% chance of distinguishing between a positive and a negative instance.