

Exercise – Animated point vs static line segment

- We have a point **Bs(-2,2)** that is travelling in one frame time to another point **Be(3,-1)**.
- A bouncy wall is represented by a line segment and located at **L[(0,-3),(0,3)]**
- Find the final point position **Be'** after collision (if any?) and reflection of the point with the wall.

Solution – Following the notes printed and given in class

Step1 – Collision detection – Method 2

- Compute N.Bs, N.P0 and N.Be:
 - $N.Bs = (6,0) \cdot (-2,2) = -12$
 - $N.P0 = (6,0) \cdot (0,-3) = 0$
 - $N.Be = (6,0) \cdot (3,-1) = 18$

We got: $N.Bs < N.P0$ and $N.Be > N.P0$

a- Test passed – no rejection

b- Test Passed – no rejection

c- Compute **N.V**

a. If **(N.V == 0)** then no collision

$$V = Be - Bs = (3,-1) - (-2,2) = (5,-3)$$

$$N.V = (6,0) \cdot (5,-3) = 30 + 0 = 30 \neq 0$$

N.V is $\neq 0$ – no rejection

d- Compute **ti**, the time of intersection where **ti = (N.P0 - N.Bs) / (N.V)**

$$ti = (0 - (-12)) / (30) = 2/5$$

e- If **(ti < 0)** or **(ti > 1)** then reject

$$ti = (0 \leq 2/5 \leq 1)$$

$$Bi = Bs + ti \cdot V = (-2,2) + 2/5 \cdot (5,-3) = (-2,2) + (2, -6/5) = (0, 4/5)$$

f- Test to check if **Bi** is within **P0** and **P1** area. We test if **(Bi - P0) \cdot (Bi - P1) < 0** then return collision at point **Bi**

$$(Bi - P0) \cdot (Bi - P1) = [(0,4/5) - (0,-3)] \cdot [(0,4/5) - (0,3)] = (0,19/5) \cdot (0,-11/5) = -209/25 < 0$$

Step1 – Collision detection – Method 3

If we followed **Method 3** steps, the first two steps would be to compute the **outward** normal of **BsBe** and do the **rejection test** as follow:

- a- \mathbf{M} = Outward normal of $\mathbf{V} = (\mathbf{V.y}, -\mathbf{V.x}) = (-3, -5)$
- b- $(\mathbf{BsP0.M}) * (\mathbf{BsP1.M}) = [(0 - (-2), (-3) - 2) \cdot (-3, -5)] * [(0 - (-2), 3 - 2) \cdot (-3, -5)]$
 $= [(2, -5) \cdot (-3, -5)] * [(2, 1) \cdot (-3, -5)]$
 $= (-6 + 25) * (-6 + (-5)) = 19 * (-11) = -209 < 0$

This means we can proceed and compute **ti** and **Bi** as in **Method 2**

Step2 – Reflection

- a- Compute $\mathbf{Be'}$
 $\mathbf{Be'} = \mathbf{Bi} + \mathbf{i} - 2(\mathbf{i.n}) * \mathbf{n}$
Where \mathbf{i} is the penetration vector and \mathbf{n} is \mathbf{N} -normalized
 $\mathbf{i} = \mathbf{Be} - \mathbf{Bi} = (3, -1) - (0, 4/5) = (3, -9/5)$
 $\mathbf{n} = \mathbf{N} / \text{Length}(\mathbf{N}) = (6, 0) / 6 = (1, 0)$

 $\Rightarrow \mathbf{Be'} = (0, 4/5) + (3, -9/5) - 2 * [(3, -9/5) \cdot (1, 0)] * (1, 0)$
 $\Rightarrow \mathbf{Be'} = (0, 4/5) + (3, -9/5) - 2 * (3) * (1, 0)$
 $\Rightarrow \mathbf{Be'} = (-3, -1)$