

# National University of Computer & Emerging Sciences MT-2005 Probability and Statistics



## **Problem Set**

**Question:** A researcher claims that the average cost of men's athletic shoes is less than \$80. He selects a random sample of 36 pairs of shoes from a catalog and finds the following costs (in dollars). (The costs have been rounded to the nearest dollar.) Is there enough evidence to support the researcher's claim at a 0.10? Assume  $\sigma = 19.2$ .

60	70	75	55	80	55
50	40	80	70	50	95
120	90	75	85	80	60
110	65	80	85	85	45
75	60	90	90	60	95
110	85	45	90	70	70

Level of Significance	0.10	0.05	0.01
$H_1$ : $\mu > \mu_0$ or $\mu < \mu_0$	+1.28, - 1.28	+1.64, -1.64	+2.33, -2.33
H1: µ ≠ µ₀	+1.64, -1.64	+1.96, -1.96	+2.58, - 2.58

#### Question:

A researcher wishes to test the claim that the average cost of tuition and fees at a four-year public college is greater than \$5700. She selects a random sample of 36 four-year public colleges and finds the mean to be \$5950. The population standard deviation is \$659. Is there evidence to support the claim at  $\alpha = 0.05$ ? Use the *P*-value method.

Source: Based on information from the College Board.

#### **Question:**

A researcher claims that the average wind speed in a certain city is 8 miles per hour. A sample of 32 days has an average wind speed of 8.2 miles per hour. The standard deviation of the population is 0.6 mile per hour. At  $\alpha = 0.05$ , is there enough evidence to reject the claim? Use the *P*-value method.

#### **Question:**

**Hotel Room Cost:** A survey found that the average hotel room rate in New Orleans is \$88.42 and the average room rate in Phoenix is \$80.61. Assume that the data were obtained from two samples of 50 hotels each and that the standard deviations of the populations are \$5.62 and \$4.83, respectively. At  $\alpha$  = 0.05, can it be concluded that there is a significant difference in the rates?

Find the 95% confidence interval for the difference between the means.

#### **Question:**

A researcher hypothesizes that the average number of sports that colleges offer for males is greater than the average number of sports that colleges offer for females. A sample of the number of sports offered by colleges is shown. At  $\alpha = 0.10$ , is there enough evidence to support the claim? Assume  $\sigma_1$  and  $\sigma_2 = 3.3$ .

		Males					Female	s	
6	11	11	8	15	6	8	11	13	8
6	14	8	12	18	7	5	13	14	6
6	9	5	6	9	6	5	5	7	6
6	9	18	7	6	10	7	6	5	5
15	6	11	5	5	16	10	7	8	5
9	9	5	5	8	7	5	5	6	5
8	9	6	11	6	9	18	13	7	10
9	5	11	5	8	7	8	5	7	6
7	7	5	10	7	11	4	6	8	7
10	7	10	8	11	14	12	5	8	5

Source: USA TODAY.

#### **Question:**

A random of sample of size  $n_1$  = 50 taken from normal population with a standard deviation  $\sigma_1$  = 7.35 has sample mean 181. A second sample of size  $n_2$  = 72 taken from a different normal population with  $\sigma_2$  = 4.81 has sample mean 176. Test the hypothesis at 0.05 level of significance that  $\mu$ 1 =  $\mu$ 2, vs.  $\mu$ 1  $\neq$   $\mu$ 2

## **Question:**

**Hospital Infections:** A medical investigation claims that the average number of infections per week at a hospital in southwestern Pennsylvania is 16.3. A random sample of 10 weeks had a mean number of 17.7 infections. The sample standard deviation is 1.8. Is there enough evidence to reject the investigator's claim at a 0.05?

#### Question:

Substitute Teachers' Salaries: An educator claims that the average salary of substitute teachers in school districts in Allegheny County, Pennsylvania, is less than \$60 per day. A random sample of eight school districts is selected, and the daily salaries (in dollars) are shown. Is there enough evidence to support the educator's claim at  $\alpha$  =0.10?

### **Question:**

**Jogger's Oxygen Uptake:** A physician claims that joggers' maximal volume oxygen uptake is greater than the average of all adults. A sample of 15 joggers has a mean of 40.6 milliliters per kilogram (ml/kg) and a standard deviation of 6 ml/kg. If the average of all adults is 36.7 ml/kg, is there enough evidence to support the physician's claim at  $\alpha = 0.05$ ?