

Que :- 05

Find radius of convergence from series of simpler terms

a)
$$\sum_{n=2}^{\infty} \frac{n(n-1)(2-2i)^n}{3^n}$$

b)
$$\sum_{n=1}^{\infty} \frac{n}{2} (2-2i)^{2n}$$

c)
$$\sum_{n=1}^{\infty} \frac{3^n n(n+1)(2-i)^{2n}}{5^n}$$

Que :- 06

Find the Taylor of the given function with given centre and determine the radius of convergence.

a) $\sin z, \pi/2$

b) $1/(1-z), 0$

c) $\ln(1-z), 0$

Que :- 07

Determine the location and kind of singularities of the following in case of pole also state the order

a) $z^3 \frac{1}{e^{z-1}}$

b)
$$\frac{1}{\cos z - \sin z}$$

Assignment #03

Ques: 01

For what contours C will it follow from Cauchy's integral theorem that

$$i) \oint_C \frac{1}{z} dz = 0$$

$$ii) \oint_C \frac{\cos z dz}{z^6 \cdot z^2}$$

$$iii) \oint_C \frac{e^{1/2} dz}{z^2 + 9}$$

Que:- 2

Integrate $\int_C Re z dz$ the parabola $y = x^2$ from 0 to $1 + i$

Que:- 03

Find the upper bound of the absolute value of the integral in problem 2.

Que:- 04

Are the following sequences bounded? Convergent find their limit point?

$$a) z_n = \ln(z_n + i)$$

$$b) z_n = (0.9 + 0.1i)^{an}$$

$$c) z_n = (0.9 + 0.1i)^{an}$$