

Mathematical Representation of Signal Waveform

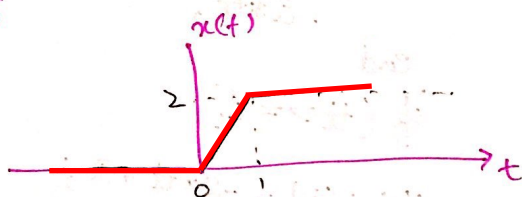
⇒ The mathematical representation is often a combination of RAMP & STEP signals.

→ Waveform with no discontinuities can be represented only ^{as} ramp signals.

→ Waveforms having discontinuities + some ctt values can be represented only with step signals.

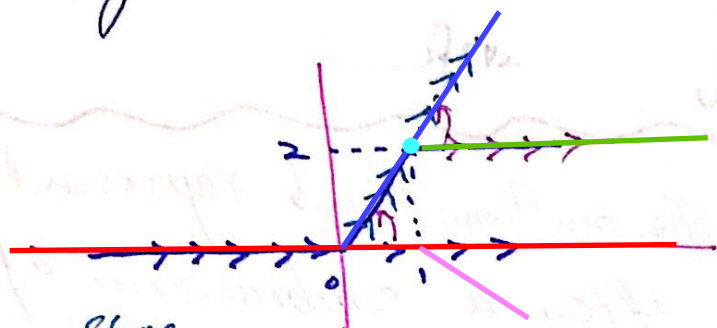
of step signals = # of discontinuities in the signal.

Example 1



Solution ⇒ No discontinuities. So it can be represented using RAMP signals only.

→ Start from the left and follow the signal.



$$x(t) = \underbrace{0}_{\substack{\text{upward turn} \\ \text{at } t=0}} + \underbrace{\frac{2}{1} \delta(t-0)}_{\substack{\text{slope} \\ \text{passing through origin}}} - \underbrace{\frac{2}{1} \delta(t-1)}_{\substack{\text{downward turn} \\ \text{at } t=1}}$$

$$x(t) = 2\delta(t) - 2\delta(t-1)$$

t = 1 : 0.1 : 5;

for k = 1 : length(t)

tt = t(k)

if (tt >= 0)

 x_t(k) = 2 * tt;

end

if (tt >= 1)

 x_t-1(k) = -2 * tt + 2;

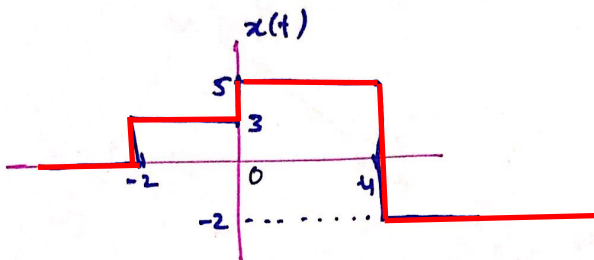
end

end

Plot(t, x_t + x_t-1)

axis([-1 5 -1 3])

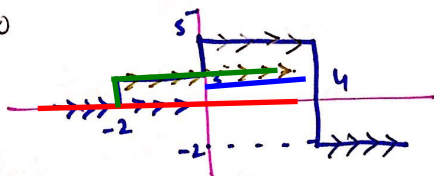
Ex



Solution: 3 discontinuities \rightarrow at $t = -2$ ($0-3$)
 $b \rightarrow$ at $t = 0$ ($3-5$)
 $c \rightarrow$ at $t = 4$ ($5-2$)

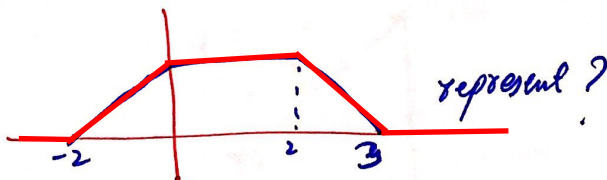
So we can represent using 3 step signals.

$$x(t) = \underbrace{0}_{\substack{\text{upward switching} \\ \text{at } t = -2}} + \underbrace{3U(t+2)}_{\substack{\text{step shifted left} \\ \text{at } t = -2}} + \underbrace{2U(t-0)}_{\substack{\text{upward switching} \\ \text{at } t = 0}} - \underbrace{7U(t-4)}_{\substack{\text{downward switching} \\ \text{at } t = 4}}$$



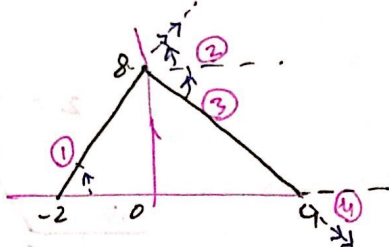
$$x(t) = 3U(t+2) + 2U(t) - 7U(t-4)$$

Q:
H.W



Represent the waveform mathematically?

Q



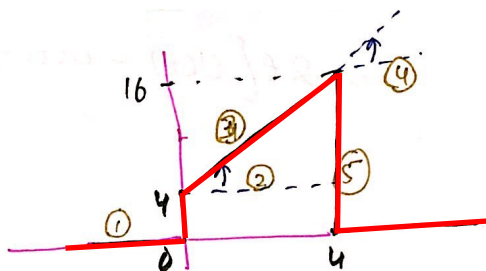
$$x(t) = 0 + \frac{8}{2} \delta(t+2) - \frac{8}{2} \delta(t-0) - \frac{8}{4} \delta(t-0) + \frac{8}{4} \delta(t-4)$$

$$= 4 \delta(t+2) - 4 \delta(t) - 2 \delta(t) + 2 \delta(t-4)$$

$$= 4 \delta(t+2) - 6 \delta(t) + 2 \delta(t-4)$$

Imp \Rightarrow

Whenever there is a turn from one slope to another then first we'll have to settle down to a constant value and then to the next slope

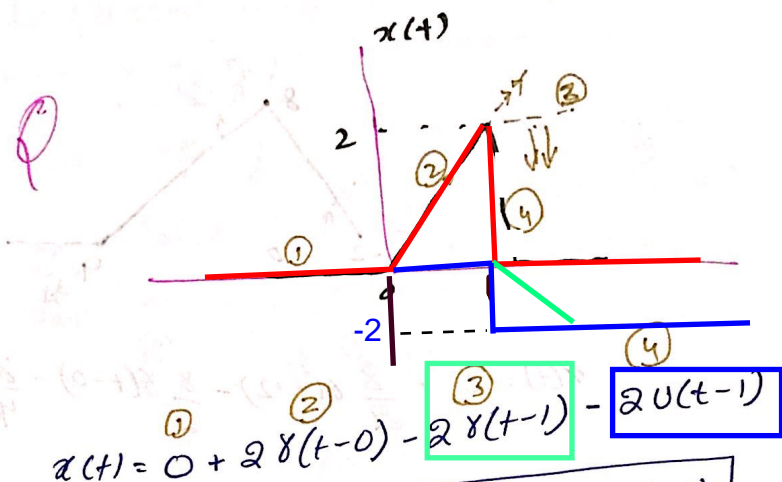


$$x(t) = 0 + 40(t-0) + \frac{12}{4} \delta(t-0) - \frac{12}{4} \delta(t-4) - 160(t-4)$$

Σ

Q:

H.W



$$x(t) = 0 + 2\delta(t-0) - 2\delta(t-1) - 2u(t-1)$$

$$x(t) = 2\delta(t) - 2\delta(t-1) - 2u(t-1)$$

We can also write

$$\delta(t) = t \cdot u(t)$$

So

$$\begin{aligned} x(t) &= 2 \cdot t \cdot u(t) - 2(t-1)u(t-1) - 2u(t-1) \\ &= 2t u(t) - 2t u(t-1) + 2u(t-1) - 2u(t-1) \\ &= 2t u(t) - 2t u(t-1) \\ &= 2t [u(t) - u(t-1)] \end{aligned}$$