July hours in study hours in study hours in subject to sichles, that is known as independent variables, that is known as independent variables, that is known as investigate linear Regression.

Trultiple Linear Regression.

The is not straight, it is polynomial regression.

Linear Regression: M= WX + p > 14 percest Dependent Slope m = How much y changes for a unit change in sc. Repression line based on "Least Squared" (Dependent Study time (independent) 1=xample: Deretim Mean Mean Deviction | Product | Sum of Ch) (4) Product Product Square of Price Deviction Ch) Hardy y- Men Deviction Deviction Calculate m = Sun of product of Deviation = 12 = 1.5

Coloulate m = Sun of product of Deviation = 12 = 1.5

Sun of square of Deviation n = 8

Sif you change a by 1', y will change by 1.5.

Calculate b = Mean of y - (m x Mean of 11)

= 13-(1.5 x 10)

= 13-15

-> 30 suppose it someone ask, what will be the price of 20' pizza.

= 30-5 = [58] bregiction.

French Established South Status South Status Status

$$D = \frac{N(\xi_{3}) - (\xi_{3})(\xi_{3})}{N(\xi_{3})^{2} - (\xi_{3})(\xi_{3})^{2}}$$

$$D = \frac{N(\xi_{3}) - (\xi_{3})(\xi_{3})}{N(\xi_{3})^{2} - (\xi_{3})(\xi_{3})^{2}}$$

-> Best case scenario, when all your values are on straight line. When you have a lot of data, the points will be scattered and not on line.

-> R2 is the percent of y' variation explained by 'N'.

-> It tells us, how accurably the regression line predicts or estimates the actual value

-> Distance (actual - mean)

-> Disbance (estimated - mean)

J= Mean of y ig = Estinated value.

g= 13 y= -2 + 1.5x

' EB	(8-5)	Est value	betw Make	(8-3)
-3	9	10	-3	٩
0	0	13	0	0
3	19	16	3	1 9
	18			18

12² = 2 (3-3)² = 18 = 1 (perfect).

Multiple Linear Regression:

-> In Linear regression, I dependent & I independent variable.

-> In Multiple LR, 1 dependent & multiple independent variables.

-> MILR of two variables x, & x, is given as;

In general, for 'n' independent variables

4= a0 + a, x, + a2x2+ + anx1+ &

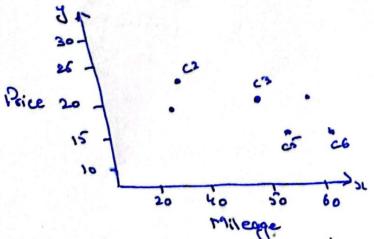
Example:

Car price = intercept + Age + Milage

301		762				
25 1	7	X	•			
er 15		65			28	CG
tice 10 7					-	× ×
7	1	2	3	4	5	3
			Age			

Car	Cir)	Age	Milege
1	29	1	18
2	25	2	25
3	21	2	50
4	18	3	68
5	15	14	75
6	15	15	65

Price = 30,57 + (-3.55) Age -> 0



Price = 32.04 + (-0.23). Milegge -> @

same figure to have a RD plat. Pressions on the

Combining (& ().54) Age + (-0.15) Milegge Price = 34.46, + (-1.54) Age + (-0.15) Milegge

· Age results in to times more in price reduction as compared to milege

. \$1.54k reduction with each year.

. \$0.1514 reduction with each thousand miles.

eg. Con Age= 2

Mileage = 50k miles Price = 34.46 - 1.54 Age - 0.15 Milegge = 34.46 - 1.54(2) - 0.15 (50)

= \$ 21.88 14.

Numerical Example:

-) Matrices	for	١١ هر	
21 = [1	4 5	٩ ٧: ١	6
L',	42		[12]

Coefficient of MUR is

a = [a]

a = [a]

Product 1	Product 2	Saley Saley
-	4	1
2	5	6
3	8	8
4	2	115
	•	

-> Calculate same as linear regression.

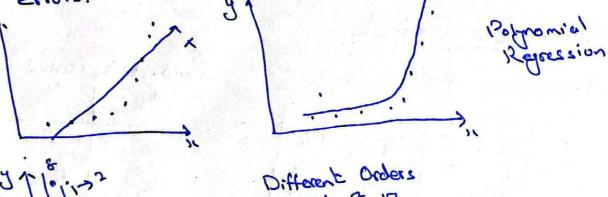
$$X^{T}X = \begin{bmatrix} 1 & 1 & 1 \\ 2 & 3 & 4 \\ 4 & 5 & 8 & 2 \end{bmatrix} \begin{bmatrix} 1 & 1 & 4 \\ 1 & 2 & 5 \\ 1 & 4 & 2 \end{bmatrix} = \begin{bmatrix} 10 & 30 & 46 \\ 19 & 46 & 109 \end{bmatrix}$$

$$(x^{7}x)^{-1} = \begin{bmatrix} 3.15 & -0.59 & -0.3 \\ -0.59 & -0.2 & 0.016 \\ -0.3 & 0.016 & 0.054 \end{bmatrix}_{3}$$

Hence

-> Polynomial Regression:

-) If the relationship between independent and dependent variables is not linear, linear regression will result in



among variables relationship polynomial. by using non-linear

- for example

$$y = a_0 + a_1 x + a_2 x^2 + a_2 x^2 \longrightarrow Third degree$$
 $y = a_0 + a_1 x + a_2 x^2 + a_2 x^2 \longrightarrow Third degree$

Numerical Example: -> For End degree y= ao + a, x + az x² where x y

Coefficients ao, a, az are colculated Where Exi=10; Ey;=89; Exiy;=96; En;= 30; Exiy;= 308 ZIL: = 100; EN = 354

$$Q = \begin{cases} 10 & 30 \\ 10 & 30 & 100 \\ 30 & 100 & 354 \end{cases} \begin{bmatrix} 29 \\ 96 \\ 338 \end{bmatrix}$$

$$\begin{bmatrix} a_0 \\ a_1 \\ a_2 \end{bmatrix} = \begin{bmatrix} -0.75 \\ 0.95 \\ 0.75 \end{bmatrix}$$

y = -0.75 + 0.95x + 0.75x2