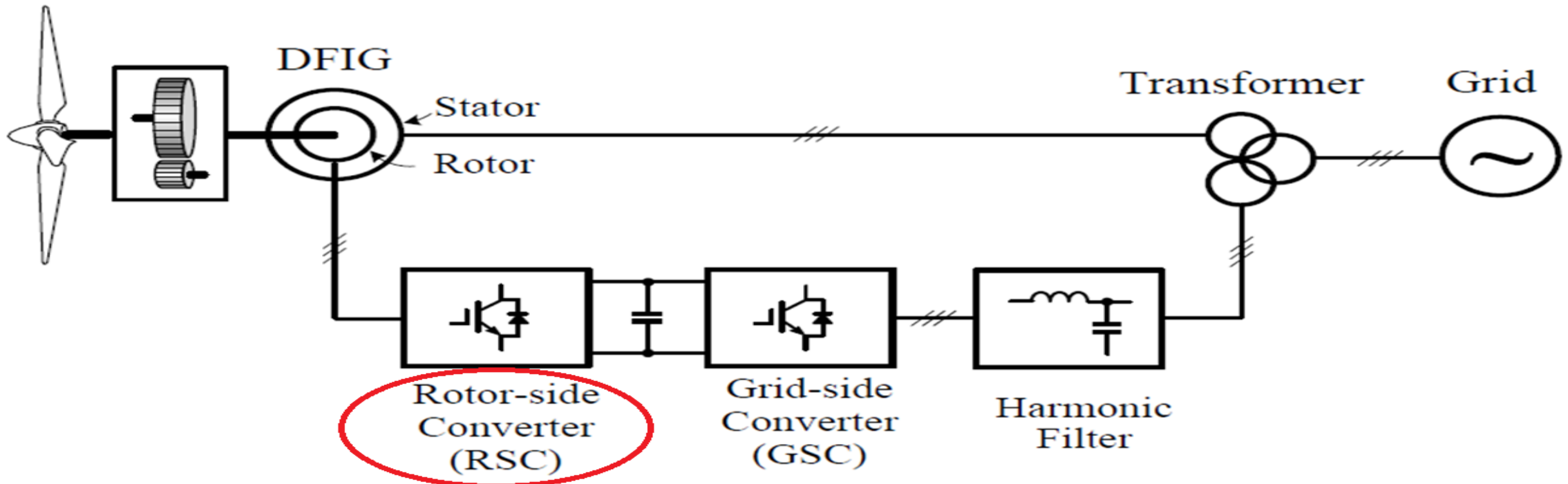


8.3 Unity Power Factor Operation of DFIG

- 1st we shall derive steady-state equivalent impedance for rotor-side converter(RSC).

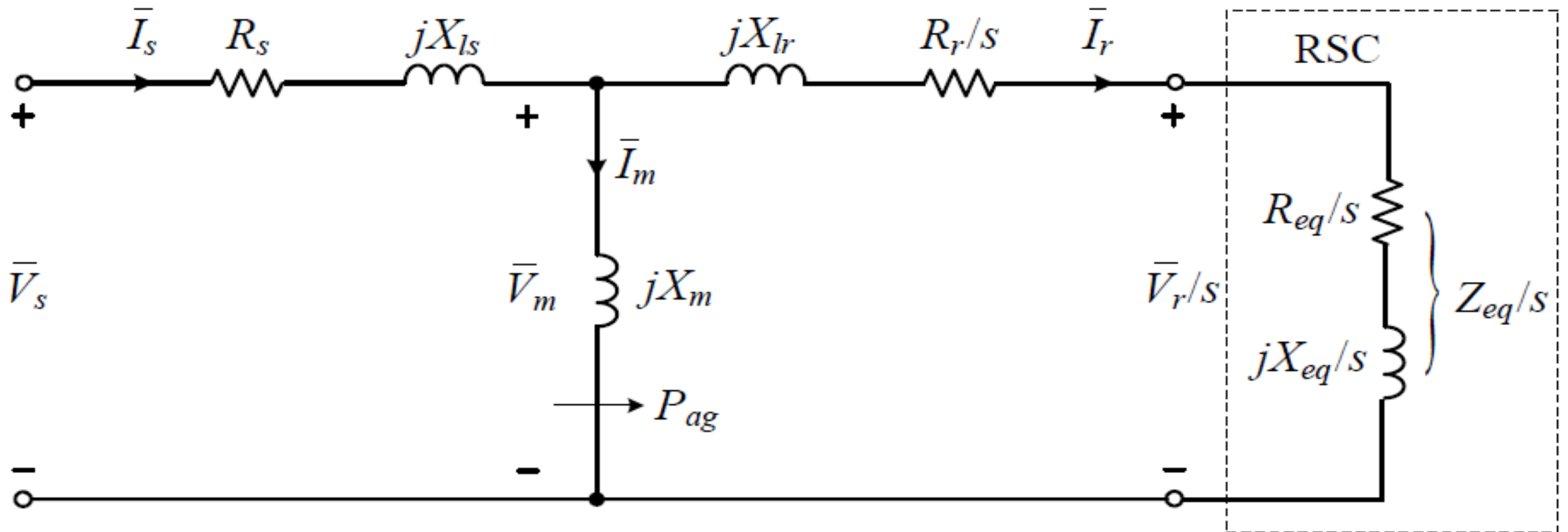


Based on steady-state equivalent impedance for
rotor-side converter(RSC):

- Analysis of DFIG based WECS under unity power factor operation will be performed.
- Torque-slip characteristics of DFIG with rotor-side converter taken into account shall also be developed & analysed.

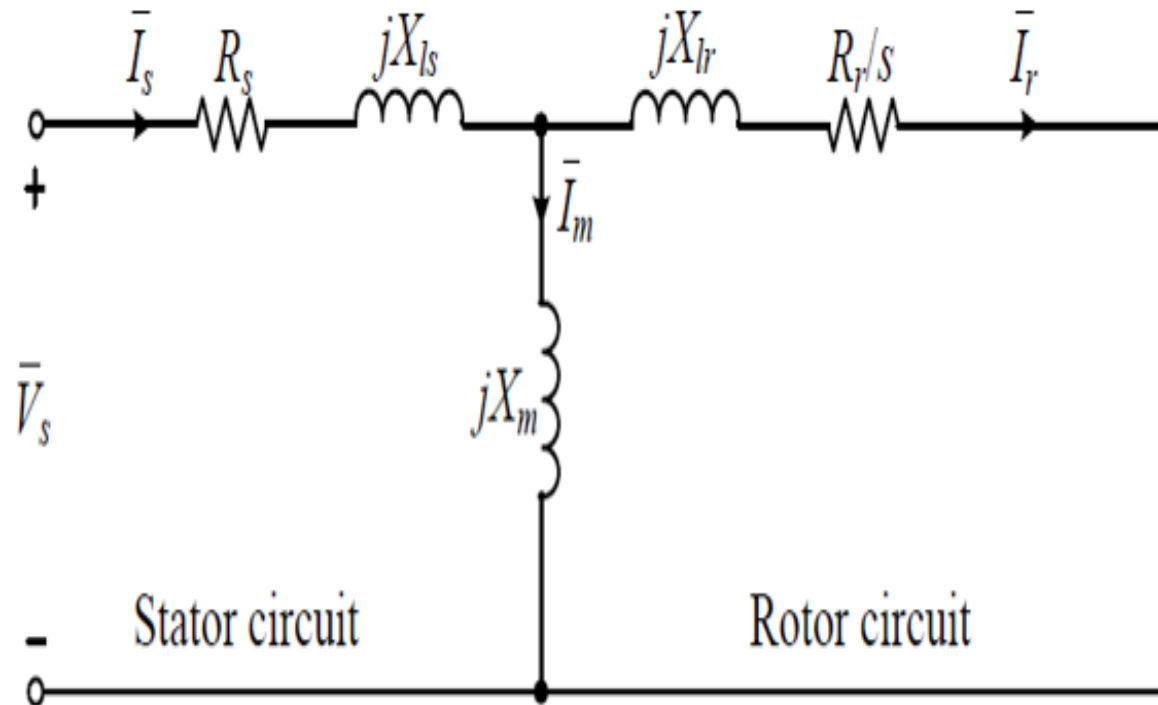
In order to investigate steady-state performance of DFIG based WECS rotor-side converter(RSC) can be modelled by an equivalent impedance(Z_{eq}/s).

- Fig. shows a steady-state equivalent circuit of DFIG WECS.

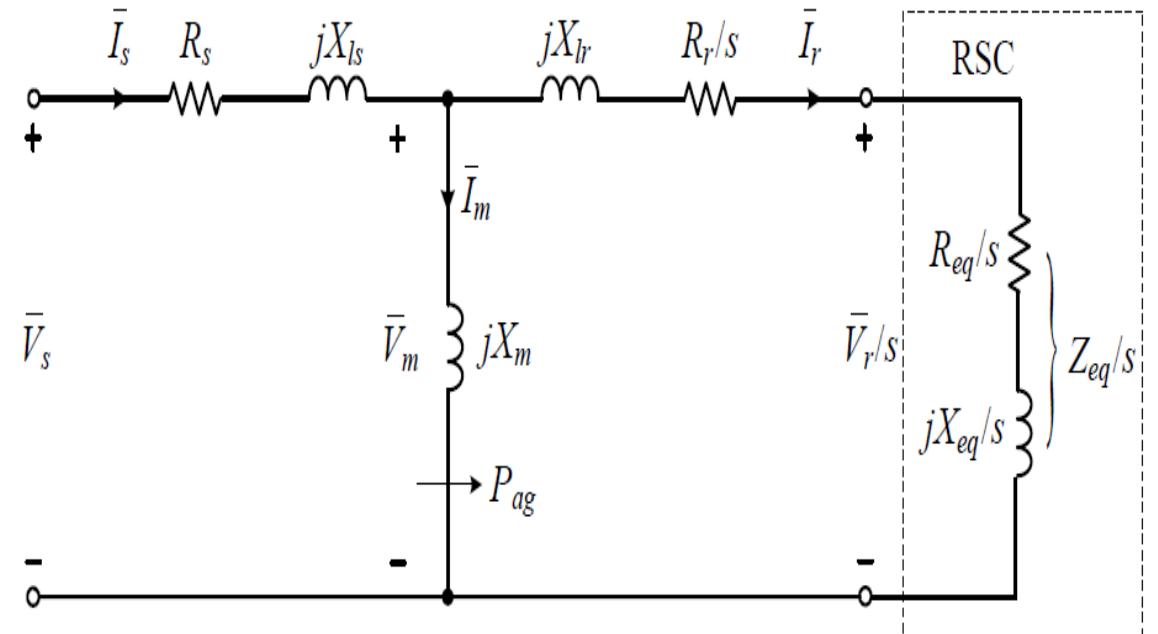


This equivalent circuit is developed by adding converter equivalent impedance Z_{eq}/s to SCIG steady-state model

SCIG steady-state model



DFIG steady-state model



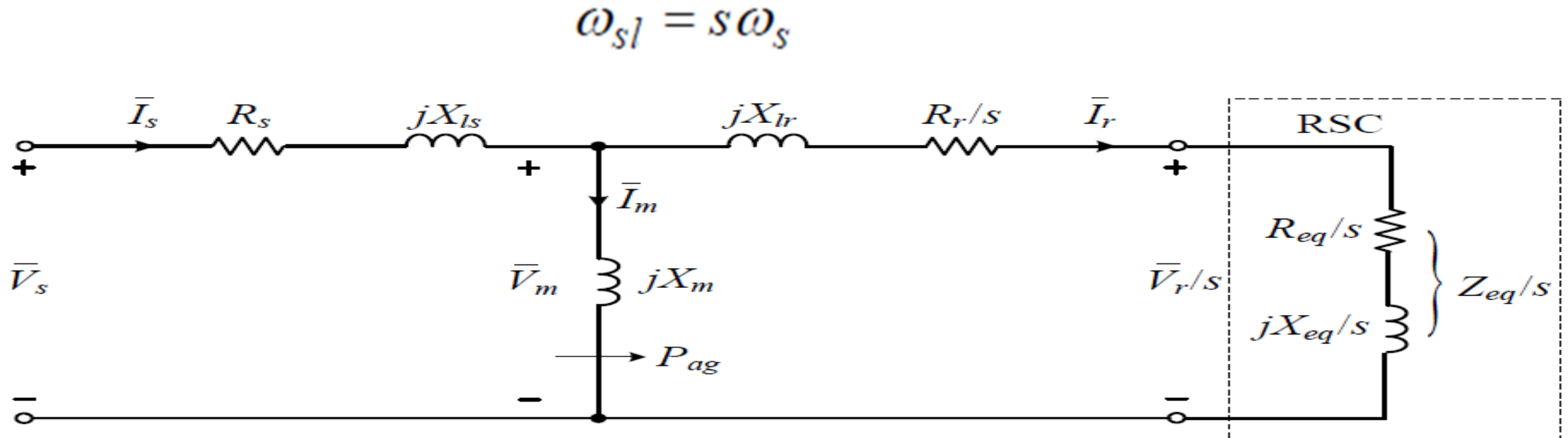
When Angular slip frequency=Stator frequency? i.e

$$\omega_{sl} = \omega_s$$

Equivalent impedance of conv $\bar{Z}_{eq} = R_{eq} + jX_{eq} = R_{eq} + j\omega_{sl}L_{eq}$

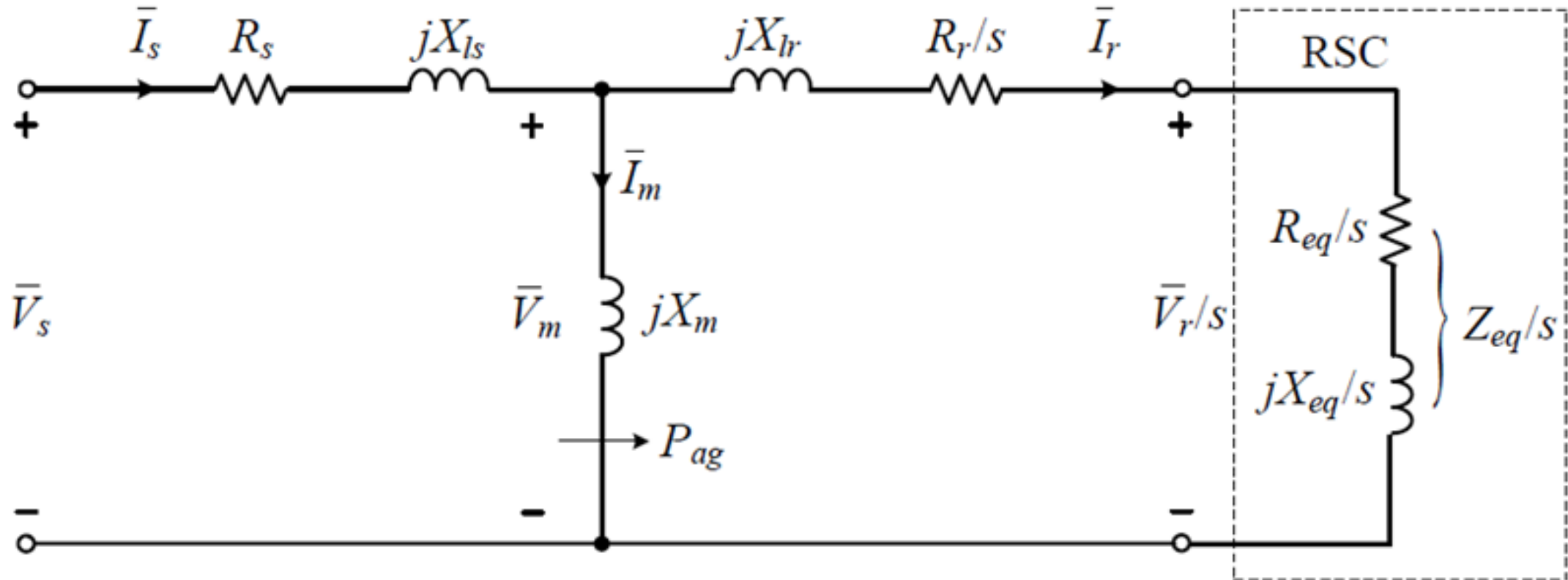
where ω_{sl} is angular slip frequency & L_{eq} is equivalent inductance of RSC.

- Note: Frequency of rotor current in actual rotor winding flowing into converter is ω_{sl} (angular slip frequency), not stator frequency ω_s .



How to integrate converter equivalent impedance \bar{Z}_{eq} into steady-state model with stator frequency ω_s ?

Ans. Equivalent impedance \bar{Z}_{eq} should be divided by slip s .

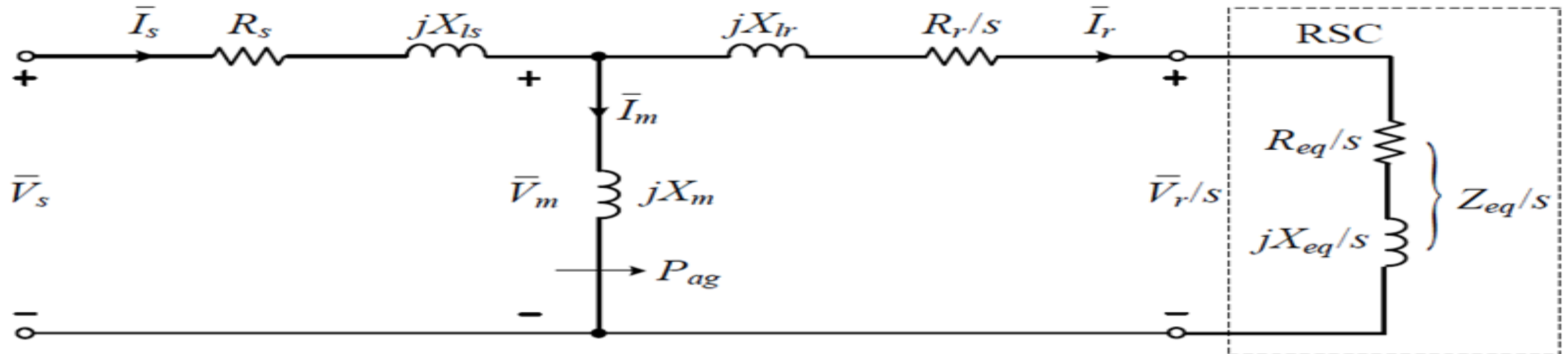


Equivalent impedance \bar{Z}_{eq} referred to stator side is then given by:

$$\bar{Z}_{eq} = R_{eq} + jX_{eq} = R_{eq} + j\omega_{sl}L_{eq}$$

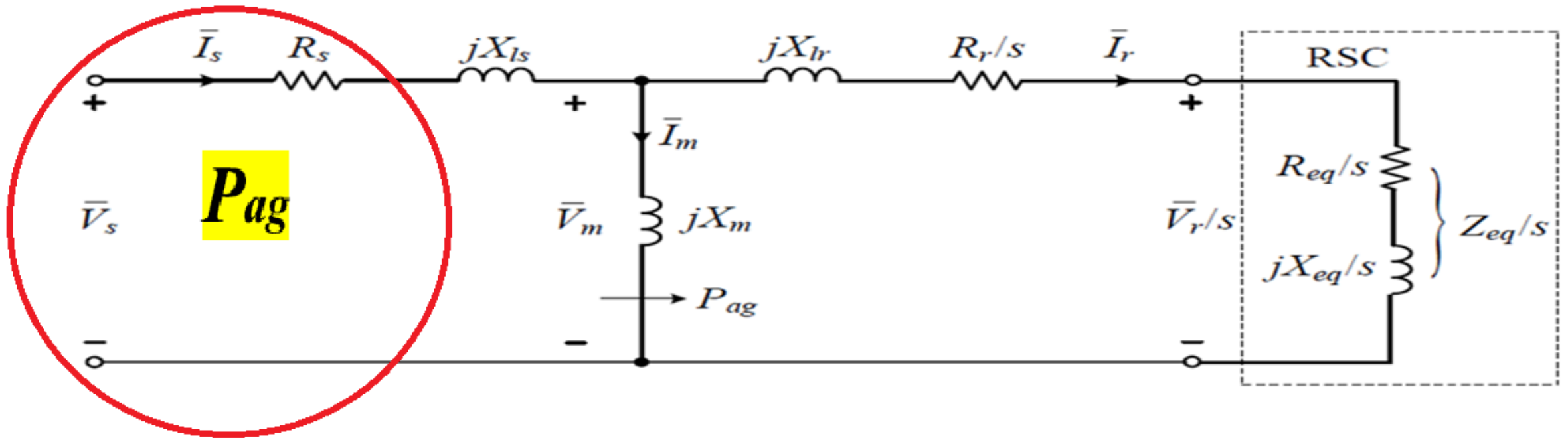
where ω_{sl} is angular slip frequency given by: $\omega_{sl} = s\omega_s$

$$\bar{Z}_{eq}/s = R_{eq}/s + j\omega_{sl}L_{eq}/s = R_{eq}/s + j\omega_s L_{eq} \qquad \omega_s = \frac{\omega_{sl}}{s}$$



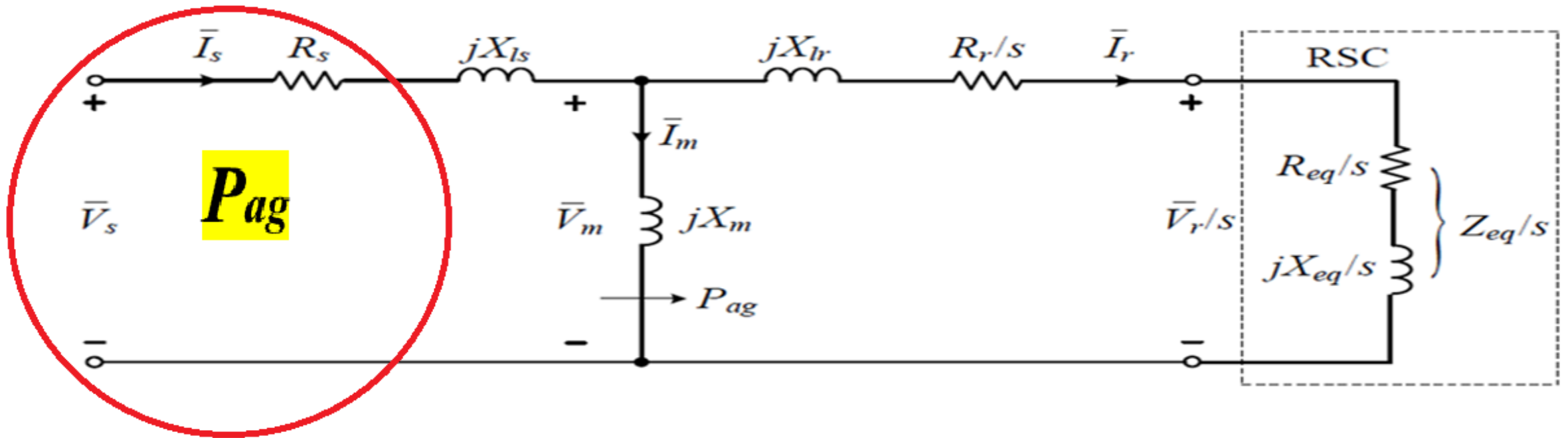
Air-gap power of generator

Assuming that stator operates at a unity power factor, air-gap power of generator?



Air-gap power of generator

Assuming that stator operates at a unity power factor, air-gap power of generator:



$$P_{ag} = 3(V_s - I_s R_s) I_s$$

From induction machine theory, air-gap power can also be calculated by

$$P_{ag} = \frac{\omega_s T_m}{P}$$

where T_m is mechanical torque &
 P is the number of pole pairs of the generator.

By equating following equations:

$$P_{ag} = 3(V_s - I_s R_s)I_s \qquad P_{ag} = \frac{\omega_s T_m}{P}$$

$$\frac{\omega_s T_m}{P} = 3(V_s - I_s R_s)I_s$$

from which

$$R_s I_s^2 - V_s I_s + \frac{\omega_s T_m}{3P} = 0$$

Obtain value of I_s

$$R_s I_s^2 - V_s I_s + \frac{\omega_s T_m}{3P} = 0$$

Applying quadratic formula $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$.

$$R_s I_s^2 - V_s I_s + \frac{\omega_s T_m}{3P} = 0$$

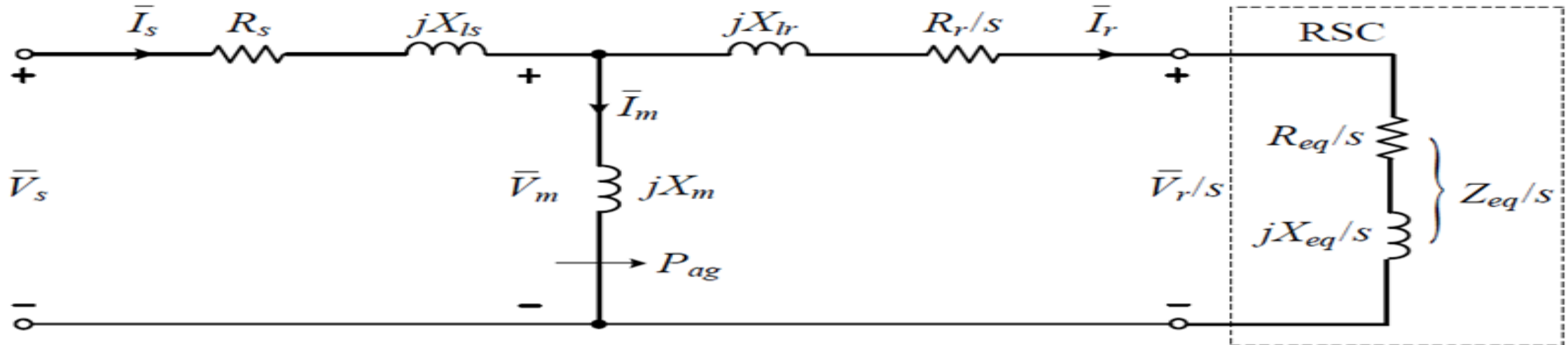
$$ax^2 + bx + c = 0$$

$$I_s = \frac{V_s \pm \sqrt{V_s^2 - \frac{4R_s \omega_s T_m}{3P}}}{2R_s}$$

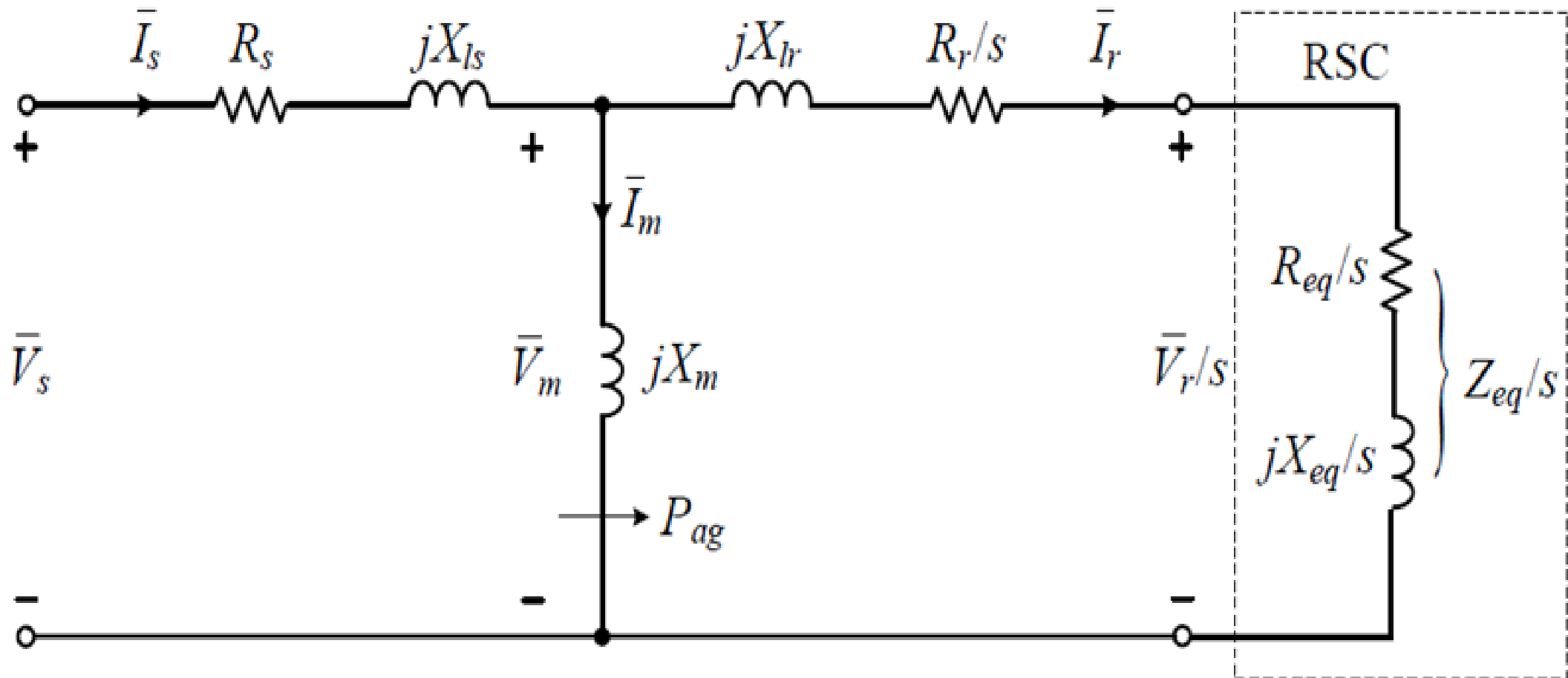
How to find rotor voltage \bar{V}_r & rotor current \bar{I}_r

$$I_s = \frac{V_s \pm \sqrt{V_s^2 - \frac{4R_s\omega_s T_m}{3P}}}{2R_s}$$

With magnitude of stator current I_s calculated, we can use equivalent circuit of Fig. to find rotor voltage \bar{V}_r & rotor current \bar{I}_r .

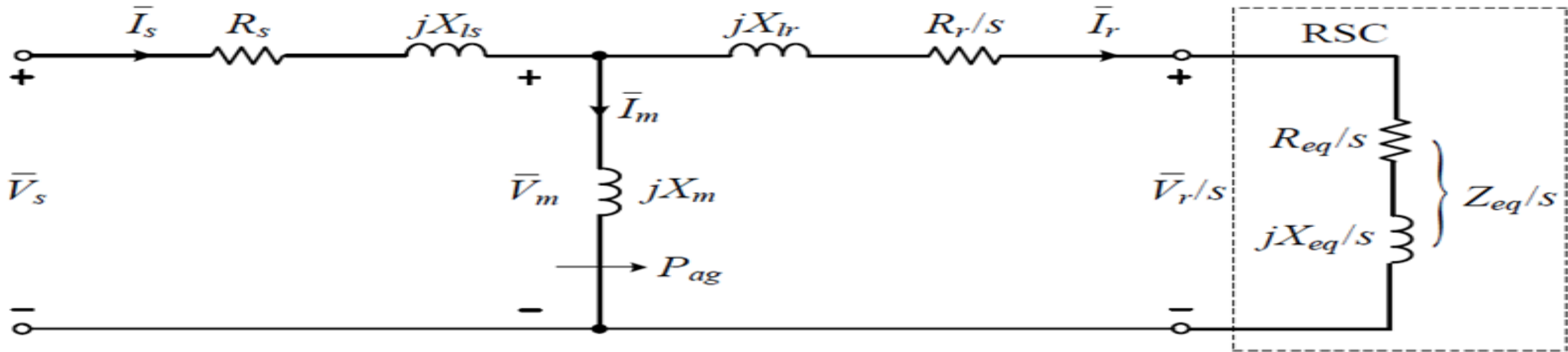


Voltage across magnetizing branch \bar{V}_m ?



Voltage across magnetizing branch \bar{V}_m

$$\bar{V}_m = \bar{V}_s - \bar{I}_s (R_s + j\omega_s L_{ls})$$



where stator voltage & current are given by

$$\bar{V}_s = V_s \angle 0^\circ \quad \text{and} \quad \bar{I}_s = I_s \angle 180^\circ$$

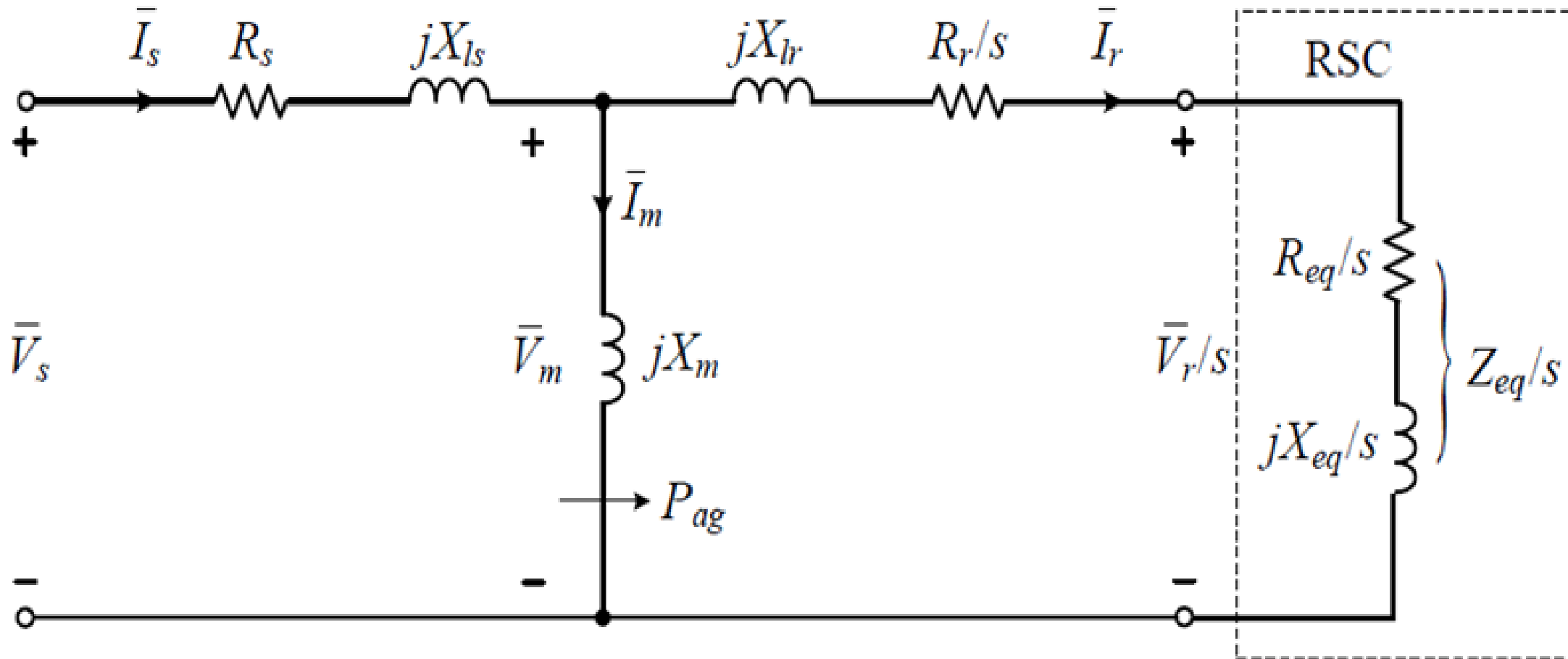
Q. What information we can get if stator voltage & current are 180° out of phase? $\bar{V}_s = V_s \angle 0^\circ$ and $\bar{I}_s = I_s \angle 180^\circ$

Answer. If stator voltage & current are 180° out of phase then:

1. DFIG is in generating mode &

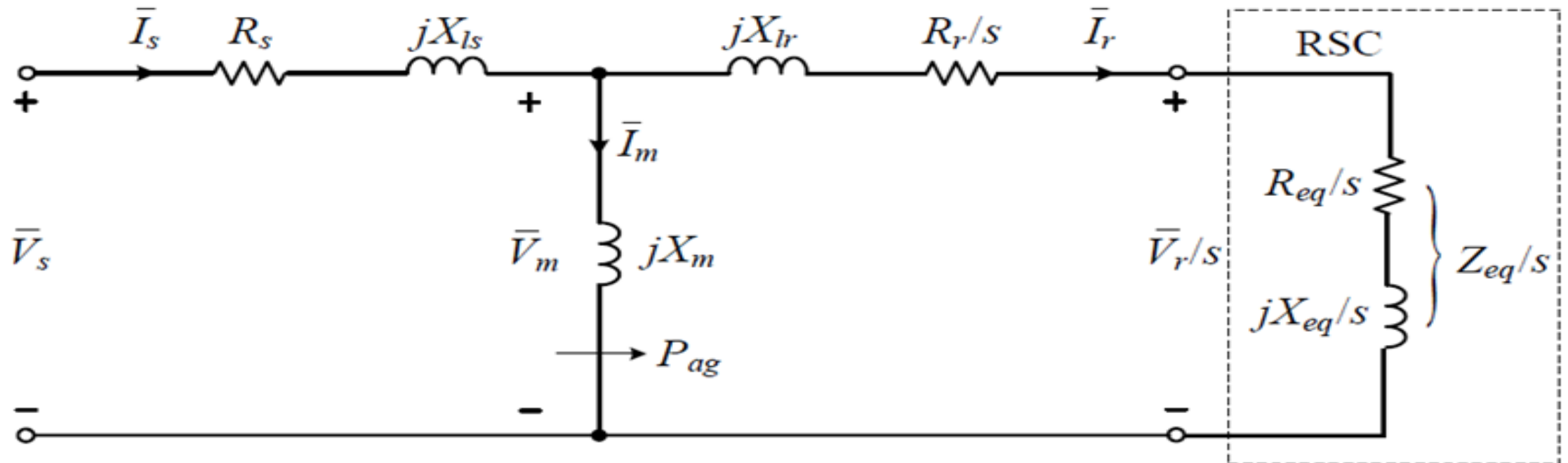
2. Stator power factor (PFs) is unity [$\cos(180^\circ) = -1$].

Write equation for Magnetizing current I_m ?



Magnetizing current can be determined by

$$\bar{I}_m = \frac{\bar{V}_m}{j\omega_s L_m}$$

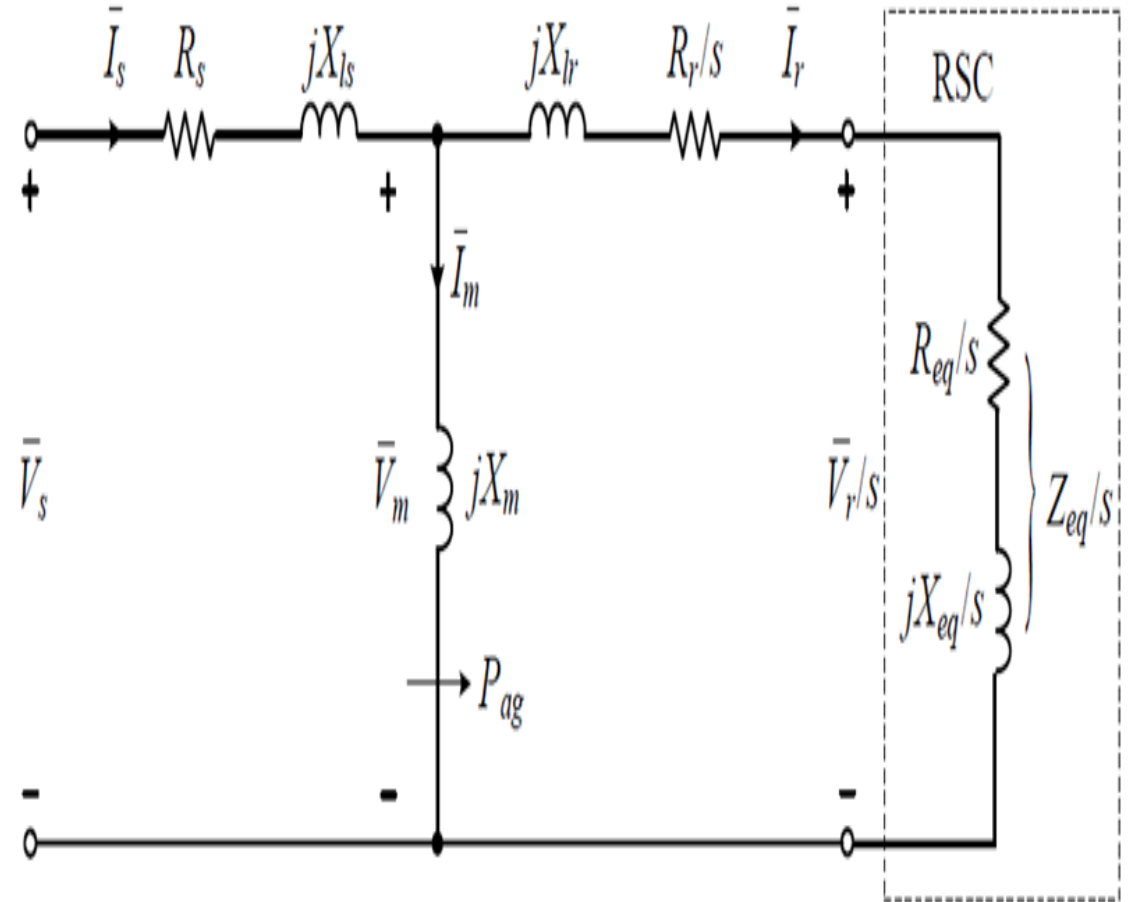


Rotor current \bar{I}_r

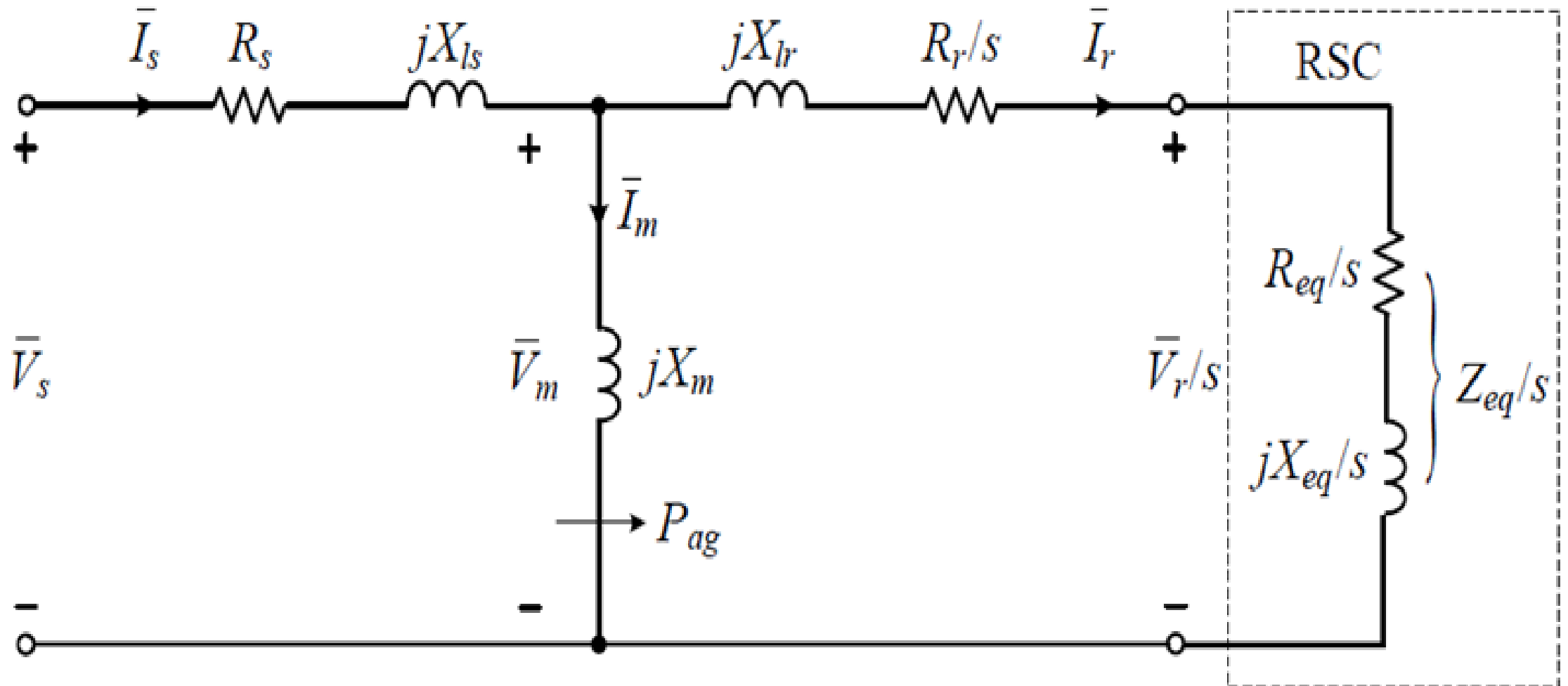
$$\bar{I}_r = \bar{I}_s - \bar{I}_m$$

$$I_s = \frac{V_s \pm \sqrt{V_s^2 - \frac{4R_s \omega_s T_m}{3P}}}{2R_s}$$

$$\bar{I}_m = \frac{\bar{V}_m}{j\omega_s L_m}$$



Rotor voltage V_r can be calculated by?

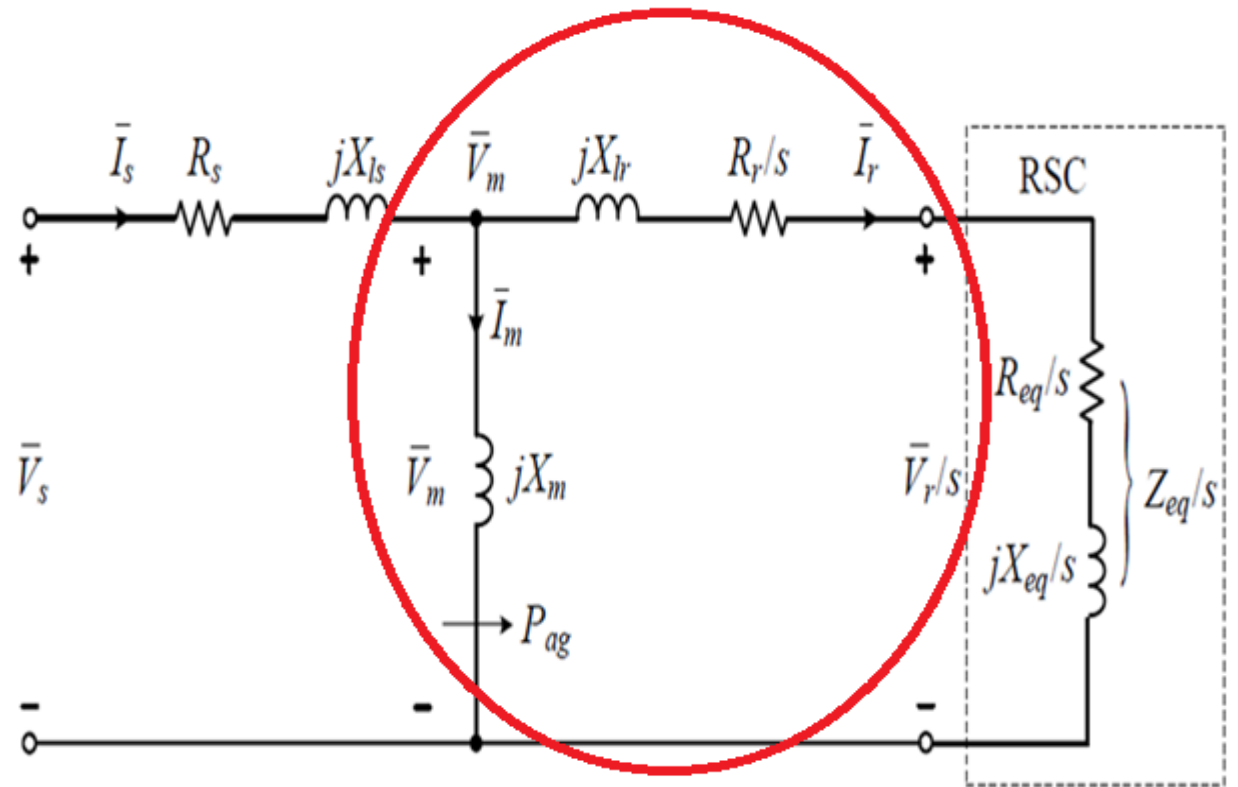


Rotor voltage V_r can be calculated by:

$$\bar{V}_r / s = \bar{V}_m - \bar{I}_r \left(\frac{R_r}{s} + j\omega_s L_{lr} \right)$$

from which

$$\bar{V}_r = s \bar{V}_m - \bar{I}_r (R_r + js\omega_s L_{lr})$$



Rotor voltage & current relate to equivalent resistance
 R_{eq} & reactance X_{eq} by

$$\frac{\bar{V}_r / s}{\bar{I}_r} = R_{eq} / s + jX_{eq} / s$$

$$R_{eq} + jX_{eq} = \frac{\bar{V}_r}{\bar{I}_r}$$

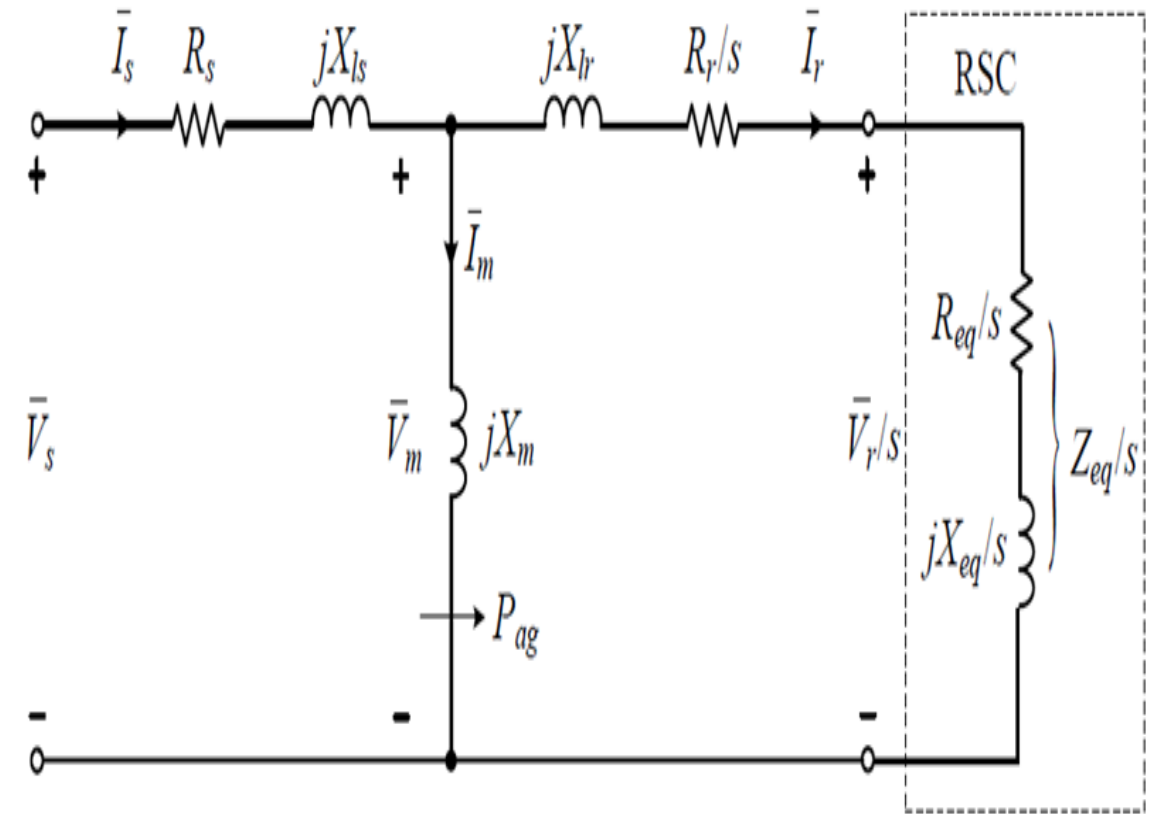
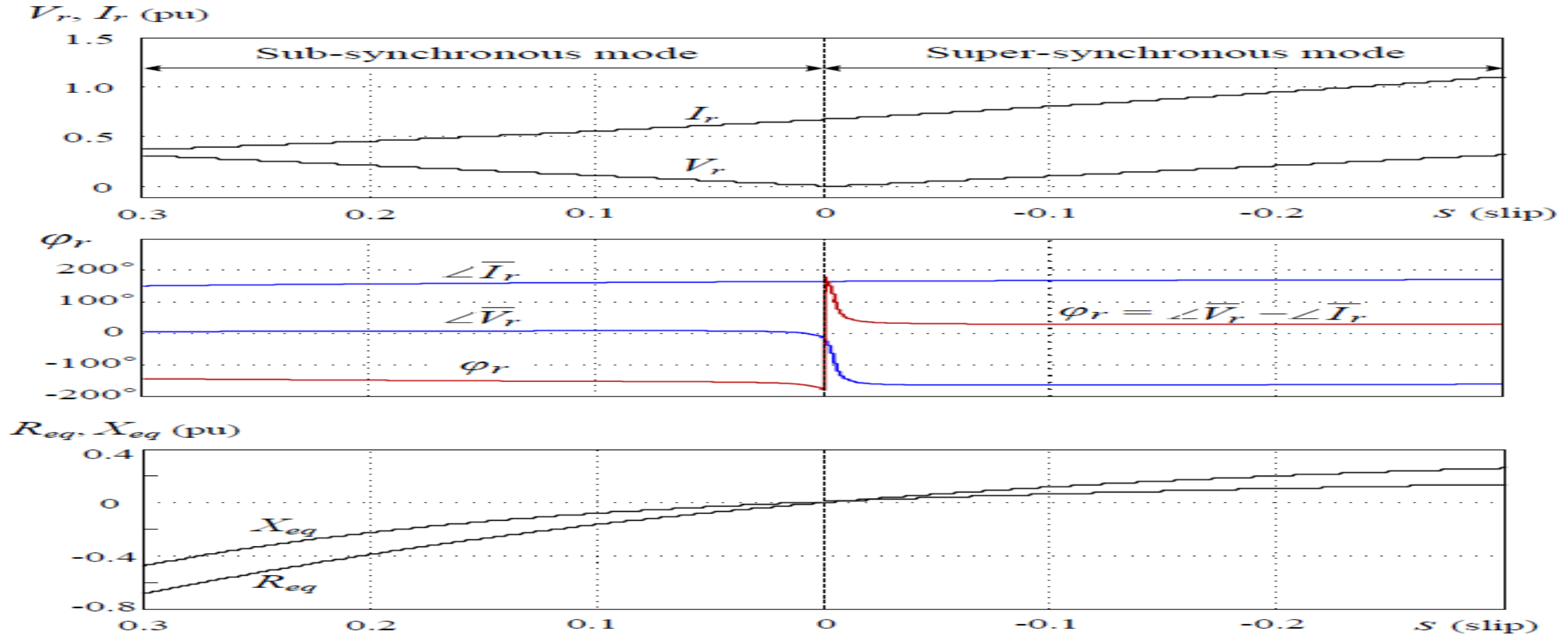
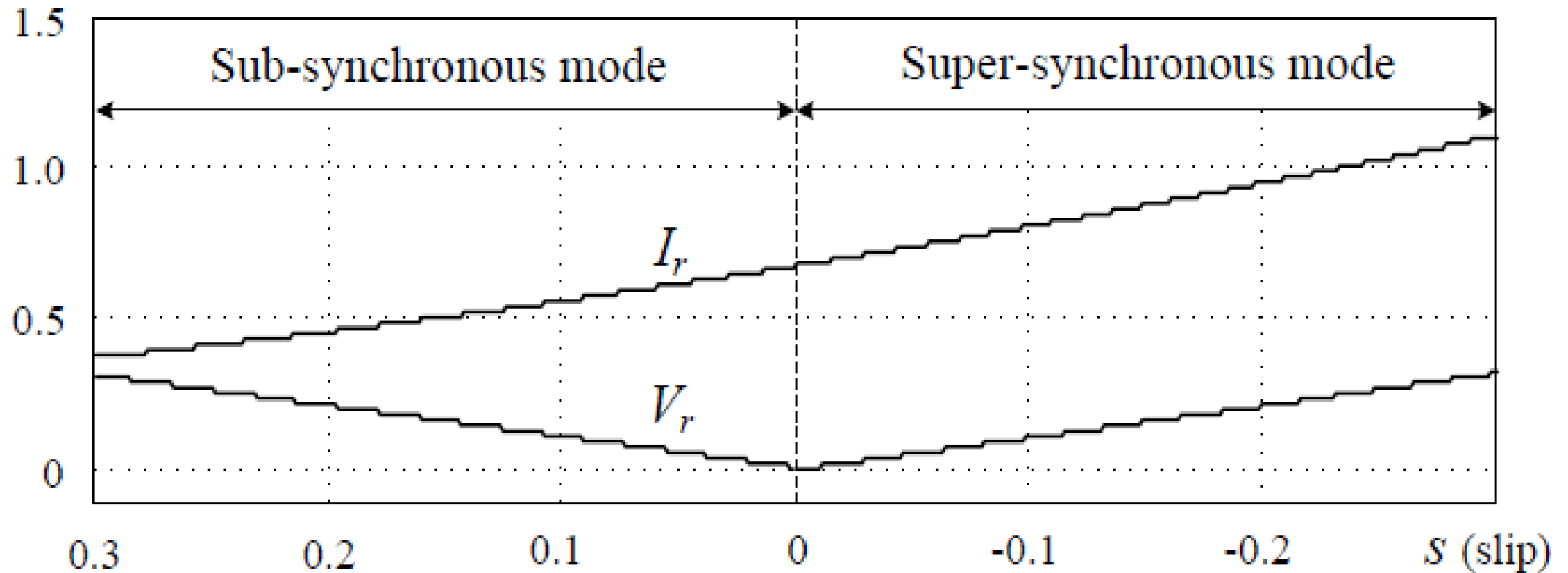


Fig. shows rotor current (I_r), rotor voltage (V_r) & equivalent impedance (Z_{eq}) of rotor-side converter when slip of DFIG varies from +0.3 to -0.3.



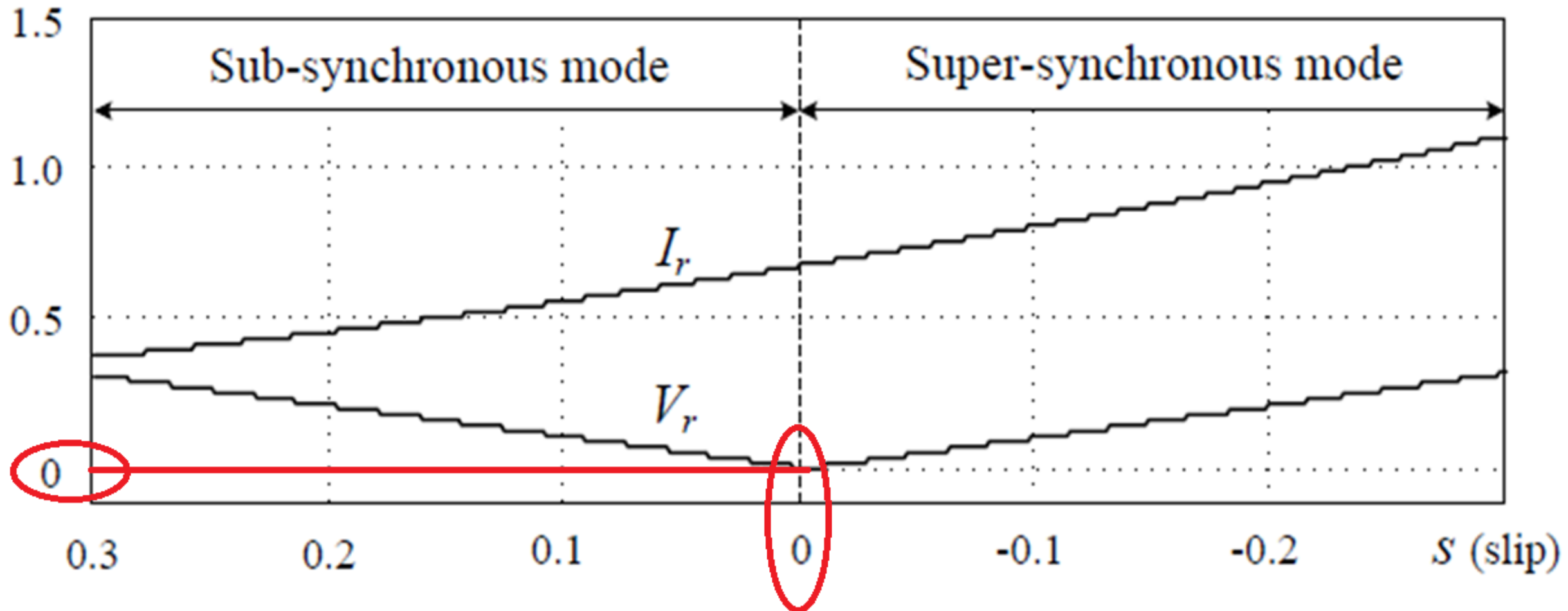
Rotor current I_r increases whether slip is +ve or -ve

V_r, I_r (pu)

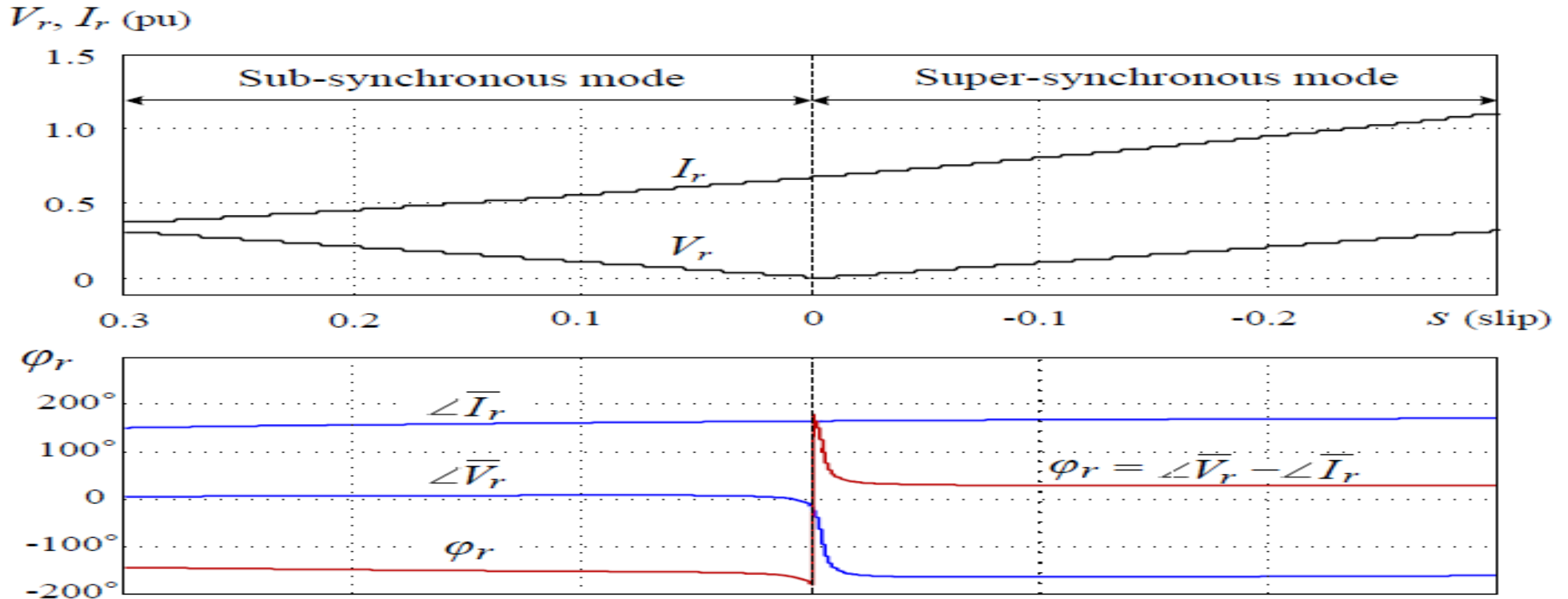


Rotor voltage V_r decreases when slip varies from 0.3 to 0, (at $s = 0, V_r = 0$). V_r increases with a -ve slip.

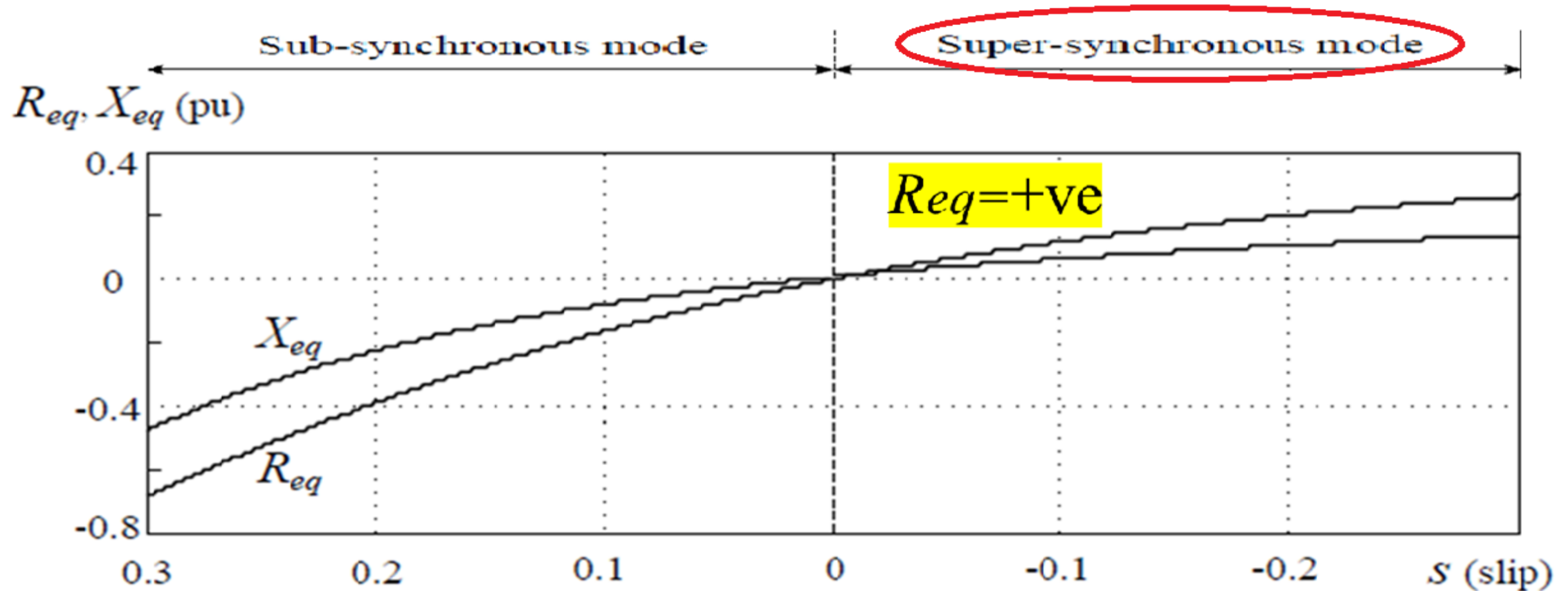
V_r, I_r (pu)



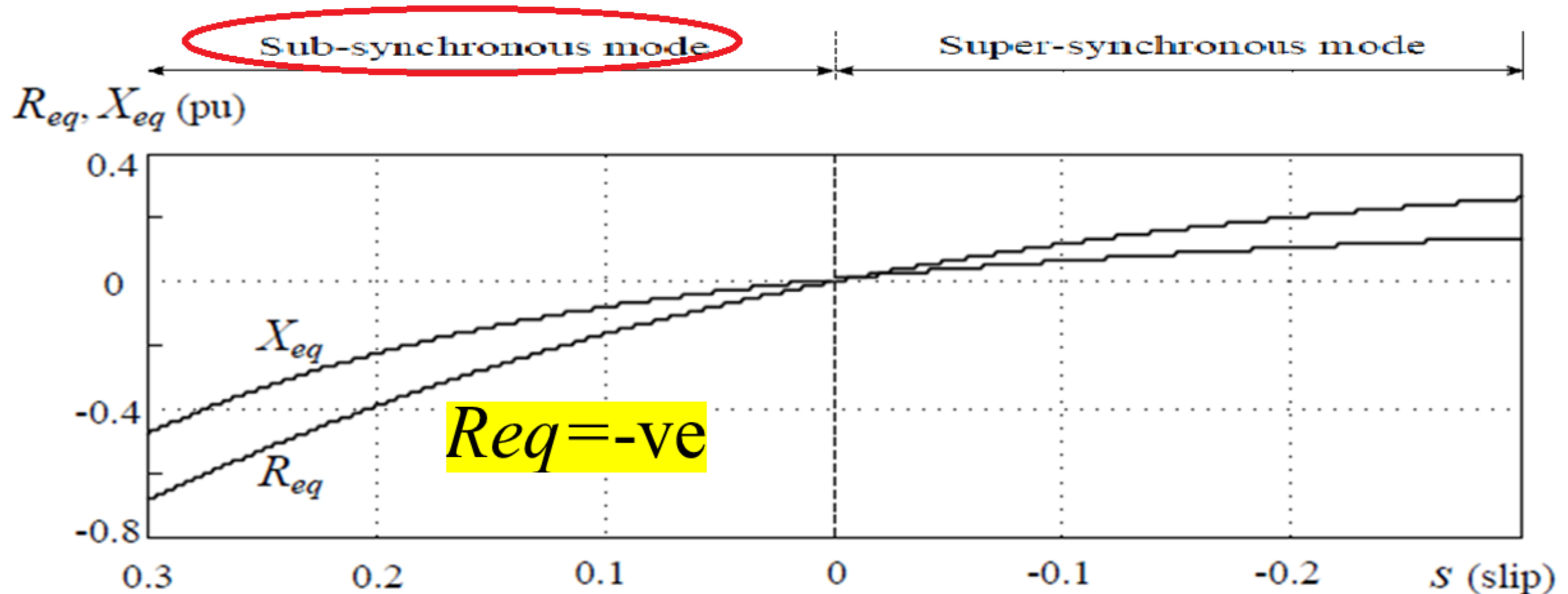
Phase angle of rotor voltage, rotor current, & rotor power factor angle ϕ_r ($\phi_r = \angle V_r - \angle I_r$) are also shown.



When DFIG operates in super-synchronous mode, equivalent resistance R_{eq} of RSC is +ve, indicating that an active power is delivered from rotor to converter.



When generator is in sub-synchronous mode, R_{eq} is -ve, signifying that converter transfers an active power to rotor.



Case Study 8-1 Equivalent Impedance of Rotor-Side Converter

- Consider a 1.5MW/690V/50Hz/1750rpm DFIG wind energy system.
- Parameters of generator are given in Table B-5 of Appendix B.

Generator Type	DFIG, 1.5MW/690V/50Hz	
Rated Mechanical Power	1.5 MW	1.0 pu
Rated Stator Line-to-line Voltage	690 V (rms)	
Rated Stator Phase Voltage	398.4 V (rms)	1.0 pu
Rated Rotor Phase Voltage	67.97 V (rms)	0.1706 pu
Rated Stator Current	1068.2 A (rms)	0.8511 pu
Rated Rotor Current	1125.6 A (rms)	0.8968 pu
Rated Stator Frequency	50 Hz	1.0 pu
Rated Rotor Speed	1750 rpm	1.0pu
Nominal Rotor Speed Range	1200–1750 rpm	0.686–1.0pu
Rated Slip	-0.1667	
Number of Pole Pairs	2	
Rated Mechanical Torque	8.185 kN.m	1.0 pu
Stator Winding Resistance R_s	2.65 m Ω	0.0084 pu
Rotor Winding Resistance R_r	2.63 m Ω	0.0083 pu
Stator Leakage Inductance L_{ls}	0.1687 mH	0.167 pu
Rotor Leakage Inductance L_{lr}	0.1337 mH	0.1323 pu
Magnetizing Inductance L_m	5.4749 mH	5.419 pu
Base Current $I_B = 1.5\text{MW} / (\sqrt{3} \times 690\text{V})$	1255.1 A (rms)	1.0 pu
Base Flux Linkage λ_B	1.2681 Wb (rms)	1.0 pu
Base Impedance Z_B	0.3174 Ω	1.0 pu
Base Inductance L_B	1.0103 mH	1.0 pu
Base Capacitance C_B	10028.7 μF	1.0 pu

Generator operates with an MPPT scheme, & its mechanical torque T_m is proportional to square of rotor speed.

- Stator power factor is unity.
 - This case study is to investigate relationship between:
 - rotor voltage,
 - rotor current, &
 - equivalent impedance of rotor-side converter when DFIG operates at
1. Super-synchronous 2. Synchronous, & 3. sub-synchronous speeds.

i) Converter Equivalent Impedance at 1750rpm (Super-synchronous mode)

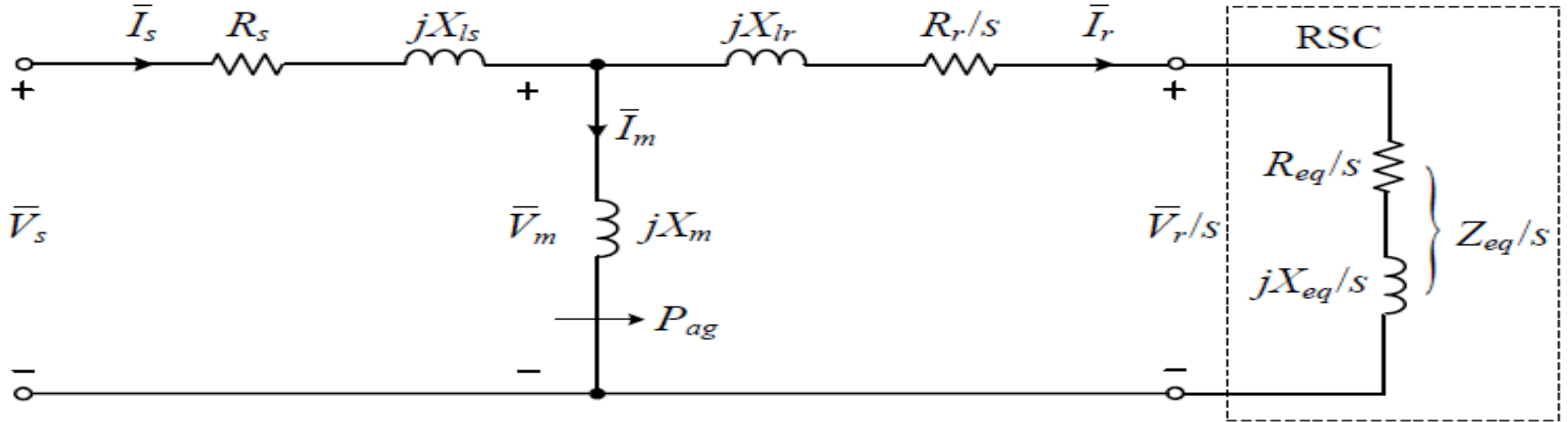
Stator current I_s is calculated by:

$$I_s = \frac{V_s \pm \sqrt{V_s^2 - \frac{4R_s T_m \omega_s}{3P}}}{2R_s} = -1068.2 \text{ A} \quad (\text{the other solution } I_s = 1.514 \times 10^5 \text{ A omitted})$$

where $V_s = 690 / \sqrt{3} \text{ V}$, $T_m = -8185.1 \text{ N.m}$, $\omega_s = 2\pi \times 50 \text{ rad/sec}$, $R_s = 6.25 \text{ m}\Omega$ and $P = 2$

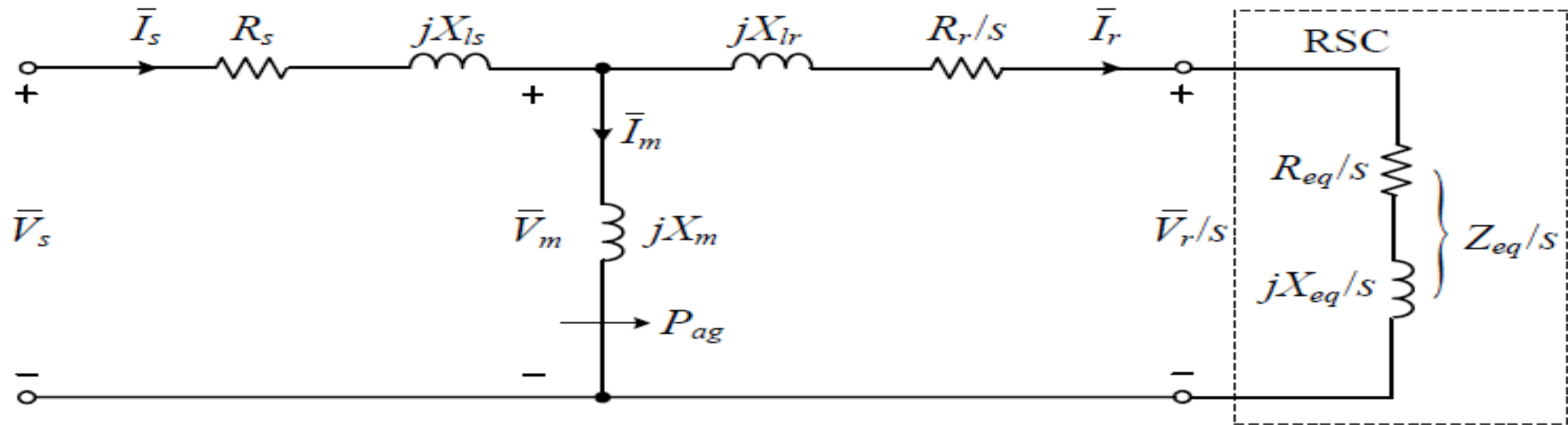
In super synchronous, or synchronous or sub-synchronous modes I_s would be -ve

Using equivalent circuit voltage across magnetizing branch V_m is



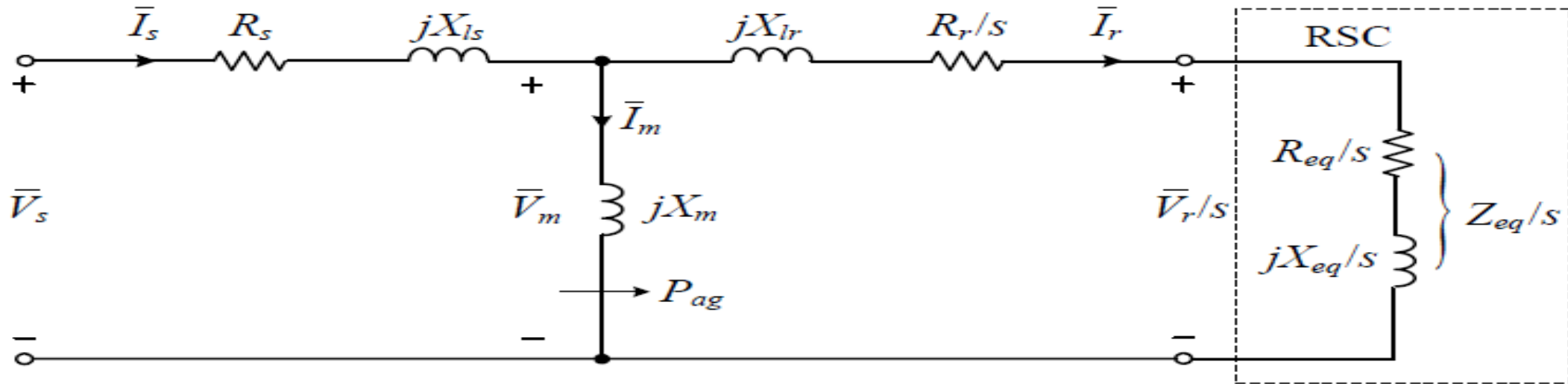
$$\begin{aligned}
 \bar{V}_m &= \bar{V}_s - \bar{I}_s (R_s + j\omega_s L_{ls}) \\
 &= 690 / \sqrt{3} \angle 0^\circ - 1068.2 \angle 180^\circ \times (0.00625 + j100\pi \times 0.1687 \times 10^{-3}) \\
 &= 401.2 + j56.6 = 405.2 \angle 8^\circ \text{ V}
 \end{aligned}$$

Magnetizing current is calculated by



$$\bar{I}_m = \frac{\bar{V}_m}{j\omega_s L_m} = 32.92 - j233.26 = 235.6 \angle -82.0^\circ \text{ A}$$

The rotor current is



$$\bar{I}_r = \bar{I}_s - \bar{I}_m = -1101.1 + j233.26 = 1125.6 \angle 168.0^\circ \text{ A}$$

The rotor voltage is
$$\bar{V}_r = s\bar{V}_m - \bar{I}_r(R_r + js\omega_s L_{lr}) = 67.97 \angle -164.9^\circ \text{ V}$$

where $s = (\omega_s - \omega_r) / \omega_s = -0.1667$

Equivalent impedance for rotor-side converter is given by

$$\bar{Z}_{eq} = \bar{V}_r / \bar{I}_r = 0.05375 \ \Omega + j0.2751 \ \Omega$$

From which

$$\begin{cases} R_{eq} = 0.05375 \ \Omega \\ X_{eq} = 0.2751 \ \Omega \end{cases}$$

ii) Converter Equivalent Impedance at 1500rpm (Synchronous Speed)

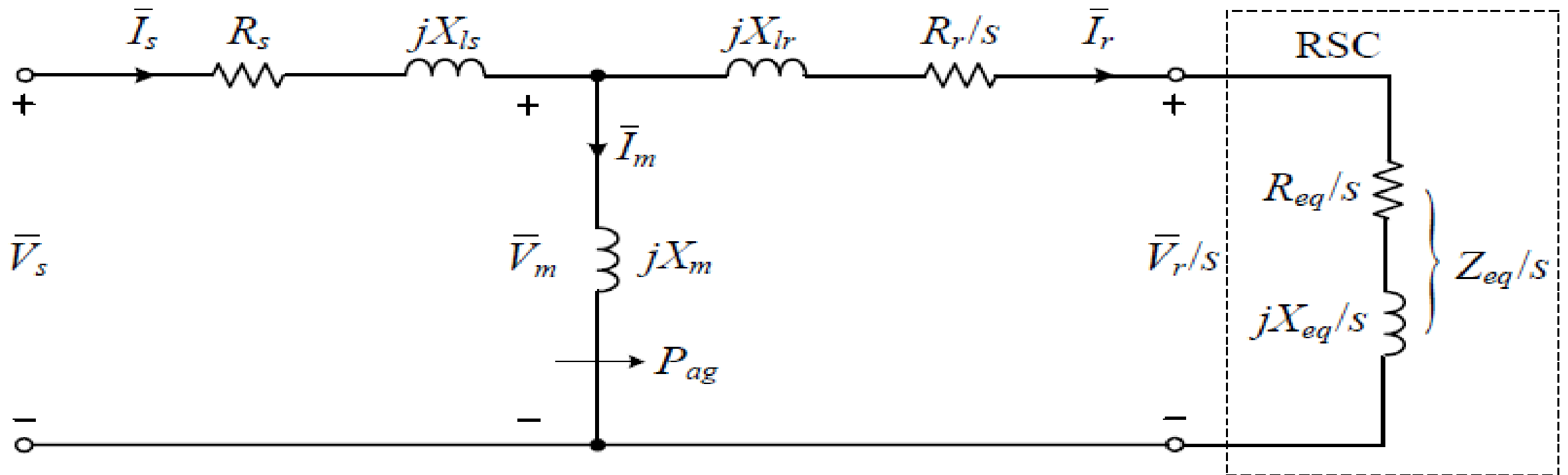
- When generator operates at 1500 rpm, stator current is

$$I_s = \frac{V_s \pm \sqrt{V_s^2 - \frac{4R_s T_m \omega_s}{3P}}}{2R_s} = -786.3 \text{ A} \quad (\text{the other solution } I_s = 1.511 \times 10^5 \text{ A omitted})$$

where $T_m = -(1500 / 1750)^2 \times 8.1851 = -6.0135 \text{ kN.m}$

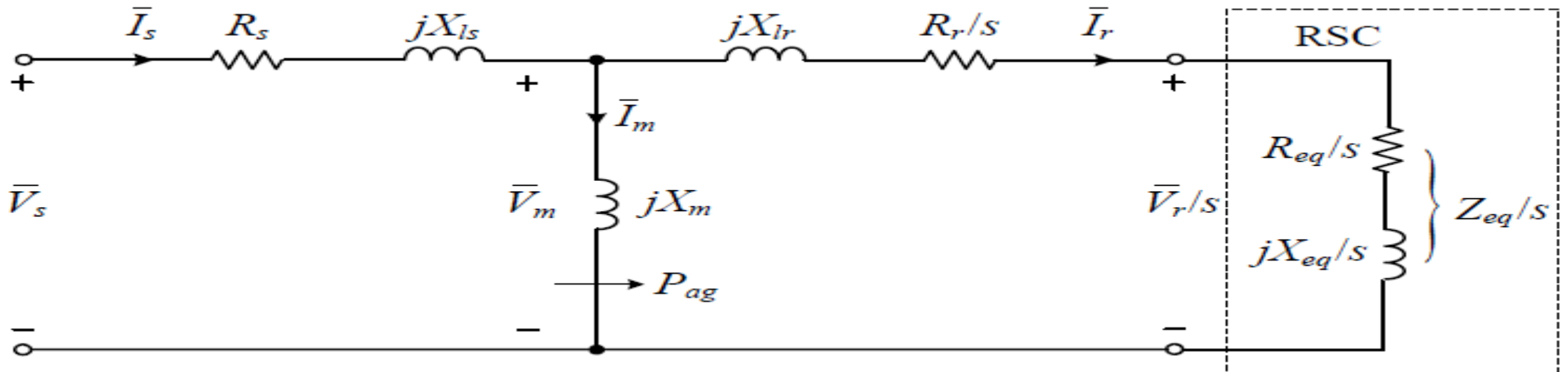
Voltage across magnetizing branch(V_m) is:

$$\bar{V}_m = \bar{V}_s - \bar{I}_s(R_s + j\omega_s L_{ls}) = 400.5 + j41.7 = 402.6 \angle 5.9^\circ \text{ V}$$



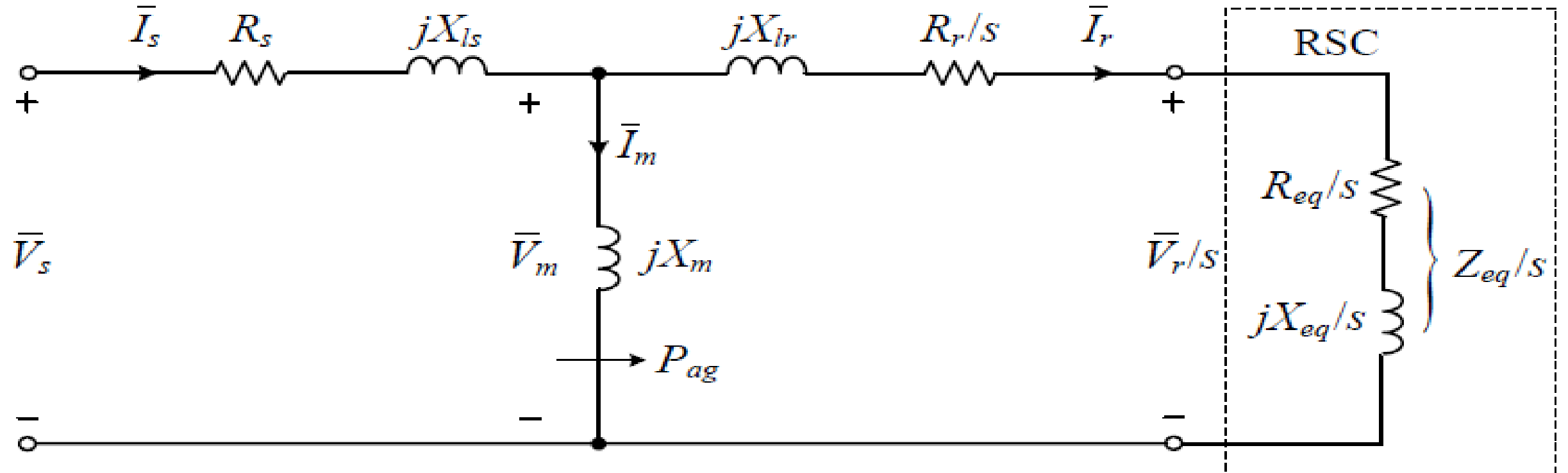
Magnetizing current(I_m) can be determined by

$$\bar{I}_m = \frac{\bar{V}_m}{j\omega_s L_m} = 24.23 - j232.82 = 234.1 \angle -84.1^\circ \text{ A}$$



Rotor current(I_r) is

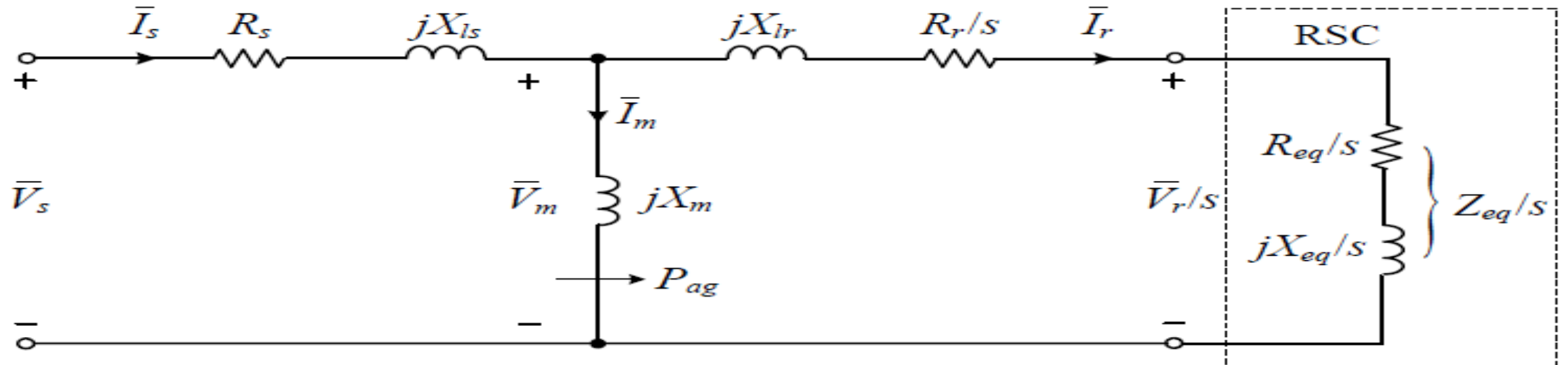
$$\bar{I}_r = \bar{I}_s - \bar{I}_m = -810.50 + j232.82 = 843.28 \angle 164.0^\circ \text{ A}$$



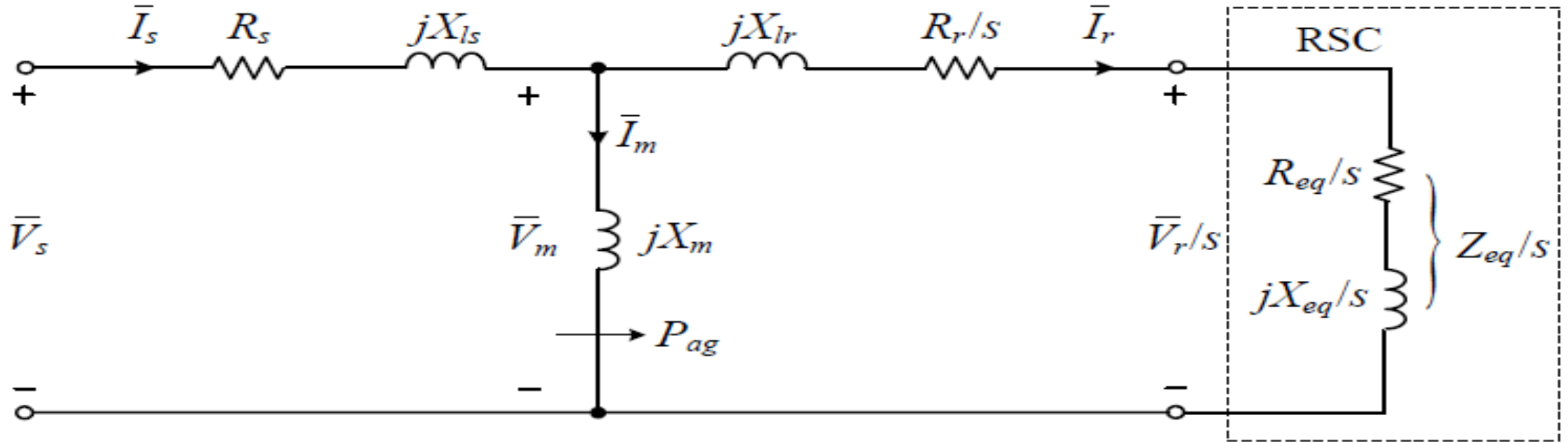
Rotor voltage $\bar{V}_r = s \bar{V}_m - \bar{I}_r (R_r + js\omega_s L_{lr}) = -\bar{I}_r R_r = 2.2178 \angle -16^\circ \text{ V}$

Equivalent resistance & reactance for rotor-side converter are

$$\bar{Z}_{eq} = \bar{V}_r / \bar{I}_r = 0.00263 \angle -180^\circ = -0.00263 + j 0.0 \Omega$$



Alternatively, following equation can be established based on Fig



$$\bar{V}_m - \bar{I}_r (R_r / s + j\omega_s L_{lr}) = \bar{I}_r (R_{eq} / s + jX_{eq} / s)$$

From which

$$s\bar{V}_m - \bar{I}_r (R_r + j s \omega_s L_{lr}) = \bar{I}_r (R_{eq} + j \omega_{sl} L_{eq})$$

$$s\bar{V}_m - \bar{I}_r(R_r + j s \omega_s L_{lr}) = \bar{I}_r(R_{eq} + j \omega_{sl} L_{eq})$$

- At synchronous speed slip $s=0$ & slip frequency $\omega_{sl}=0$, the above equation is simplified to

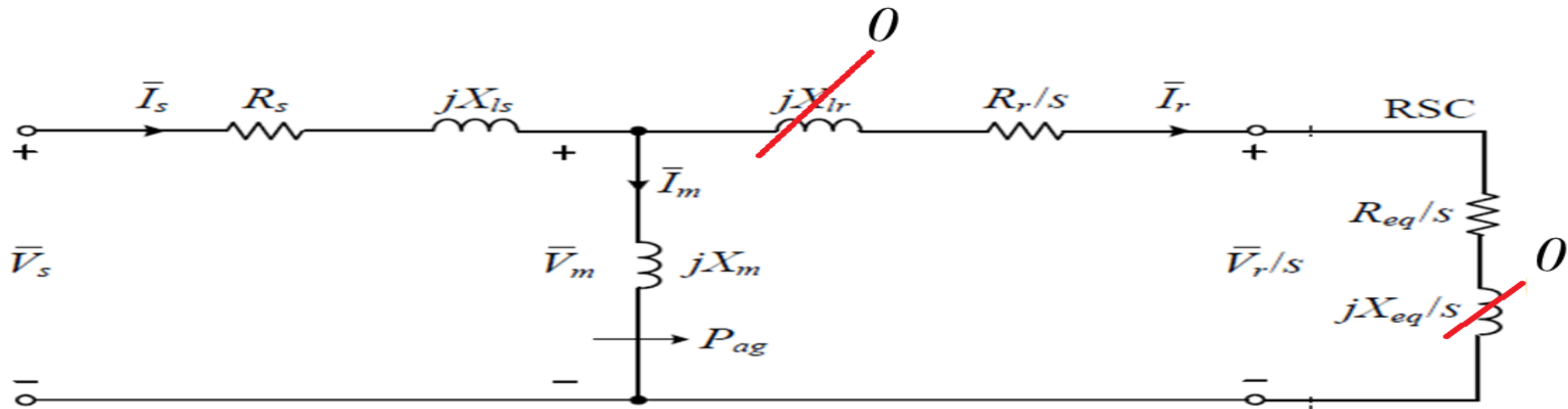
$$-\bar{I}_r R_r = \bar{I}_r R_{eq}$$

Thus equivalent resistance and reactance for rotor-side converter are

$$\begin{cases} R_{eq} = -R_r = -0.00263 \ \Omega \\ X_{eq} = \omega_{sl} L_{eq} = 0 \end{cases}$$

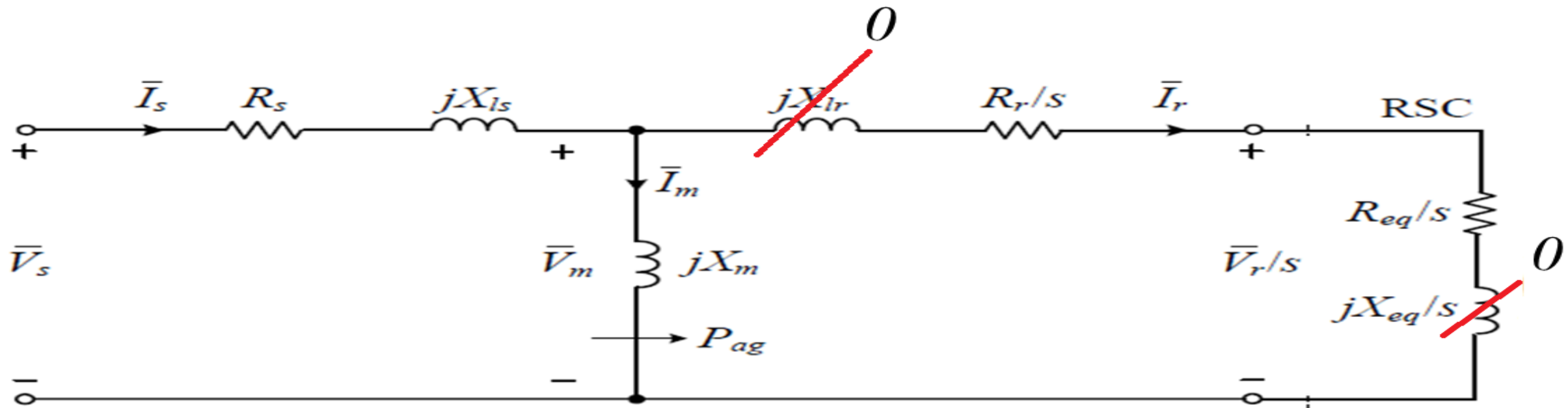
When DFIG operates at synchronous speed, both slip $s=0$ & slip frequency $\omega_s=0$.

- This implies that a dc current flows through rotor circuit, & rotor leakage reactance X_{lr} & equivalent reactance X_{eq} are both 0.



In this case, induction generator operates just like a wound rotor synchronous generator, where rotor flux is produced by a dc current through a dc exciter.

- In DFIG wind energy system, dc excitation is provided by rotor-side converter



iii) Converter Equivalent Impedance at Sub-synchronous Speed

- Following same procedure, calculated rotor voltage, rotor current, & equivalent impedance of rotor-side converter in sub-synchronous mode (1200 & 1350 rpm) are summarized in Table .
- For convenience of comparison, calculated results for DFIG operating in synchronous (1500 rpm) & super-synchronous (1650 & 1750 rpm) modes are also given in table.

Equivalent impedance of RSC in 1.5MW/690V DFIG WECS ($PF_s = 1$)

Sub-synchronous (Synchronous Speed) (Super-synchronous mode)

Rotor Speed (rpm)	1200	1350	1500	1650	1750 (rated)
Slip	0.2	0.1	0	-0.1	-0.1667 (rated)
T_m [kN.m]	3.849	4.871	6.014	7.276	8.185
\bar{V}_r [V]	$83.756 \angle 6.2^\circ$	$43.068 \angle 7.4^\circ$	$2.218 \angle -16.0^\circ$	$39.711 \angle -165.8^\circ$	$67.965 \angle -164.9^\circ$
\bar{I}_r [A]	$569.285 \angle 155.9^\circ$	$697.103 \angle 160.5^\circ$	$843.281 \angle 164.0^\circ$	$1006.991 \angle 166.6^\circ$	$1125.566 \angle 168.0^\circ$
R_{eq} [Ω]	-0.126989	-0.055113	-0.00263	0.034942	0.053751
X_{eq} [Ω]	-0.074293	-0.027918	0	0.018281	0.027513