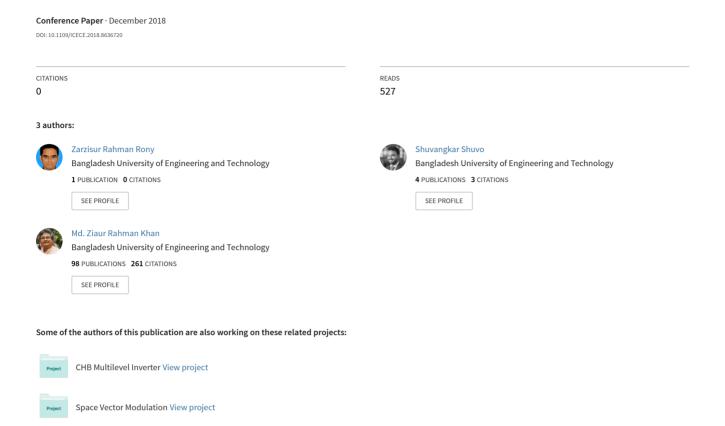
# Space Vector Modulated PWM Generation for Motor Control Systems



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Abstract—Microcontroller based sample Space Modulation for two-level three-phase voltage source inverter is discussed here. The system is designed in ATmega64, which is an8-bit low cost microcontroller. A fixed number of sample is used to produce a full wave. Here, Timer overflow interrupt is used to generate every new sample. All the calculation is done in interrupt subroutine. With simple modification, the system can be integrated to a variable frequency drive (VFD) of induction motor.Simulations are performed in Matlab/Simulink and Proteus Design Suite. Similar results are found in both simulation tools. The simulation results show that the proposed modified method results in reduction of calculation cycle numbers in interrupt routine.

Index Terms—Space Vector Modulation, Scalar Control of Induction Motor, Three Phase Inverter, Arduino Uno.

#### I. INTRODUCTION

Three-phase voltage source inverter has a wide application in power electronics such as industrial motor drive, electric vehicle, alternate energy interfacing to grid etc. It can produce variable voltage with variable frequency, which is widely used in scalar (V/f) control of induction motor. Many modulation techniques such as sine triangle PWM (SPWM), third harmonic injected PWM and space vector modulated PWM (SVM) are available. SVM shows superior performance over SPWM in terms of DC bus utilization. 90.7 percent of the fundamental at the square wave (Line to neutral) is available in the linear region, compared to 78.55 percent in the sinusoidal PWM [1].In addition, SVM has lower switching loss and less harmonic distortion than SPWM [3]. Digital implementation of SVM is also easy relative to other strategies. A significant amount of research work has been done on SVM modulation techniques and it's applications [5-6][10][12-14]. Most of the time SVM is implemented using DSP/DSC controller. Some works are also done on Arduino based platform such as Arduino Mega, Arduino DUE board [7-8]. In this work, SVM is implemented using a low cost ATmega64 microcontroller. The program algorithm is such that it can be implemented also using ATmega328p which is used in Arduino Uno board. A modified method is proposed for systems where frequency doesn't change frequently.A Matlab/Simulink simulation is done and hardware system implementation is checked by Proteus Design Suite software.

## II. PRINCIPLE OF OPERATION OF SPACE VECTOR MODULATED **INVERTER**

Three Phase voltage  $V_{an}$ ,  $V_{bn}$ ,  $V_{cn}$  can be visualized as a reference vector,  $V_{ref}$  rotating in a voltage space. Using Clarke's Transformation  $(\alpha, \beta)$  three phase to two phase model achieved with equations:

$$V_{\alpha} = \frac{2}{3} (V_{an} - 0.5V_{bn} - 0.5V_{cn})(1)$$

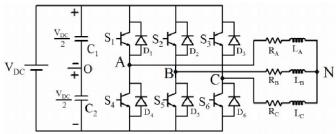


Fig.1 Three Phase Inverter with R-L load

$$V_{\beta} = \frac{2}{3} \left( \frac{\sqrt{3}}{2} V_{bn} - \frac{\sqrt{3}}{2} V_{cn} \right) (2)$$

$$V_{ref} = \sqrt{\left(V_{\alpha}^2 + V_{\beta}^2\right)} \text{ and } \theta = \tan^{-1} \frac{V_{\beta}}{V_{\alpha}}$$
 (3)

Three-leg two-level inverter in Fig.1 has  $2^3 = 8$  switching states, which act as active voltage vectors, and among them, 2 are zero voltage vector. Table 1 shows line to neutral voltages for different vectors. The voltage vectors divide the voltage space into 6 sectors as shown in Fig.2.In each sector reference voltage vector is produced with help of two adjacent active vector's and one zero vector's dwell time  $(T_1, T_r, T_0).T_1, T_r$ can be imagined as time associated to left sided and right sided active vector in a sector. Using volt sec balance in any sector,

$$V_{ref} * T_s = V_r * T_r + V_l * T_l + (V_7 \circ r V_0) * T_0$$

$$T_r = m * T_s * \sin(60 - \theta)$$

$$T_l = m * T_s * \sin \theta$$
And  $T_0 = T_s - T_r - T_l$ 
(6)

$$T_l = m * T_s * \sin \theta \tag{5}$$

$$And T_0 = T_s - T_r - T_l \tag{6}$$

Where  $T_s$  =Sample Time, m=modulation index= $\frac{\sqrt{3}*V_{ref}}{V_{DC}}$ , in linear region m can vary from 0 to 1 [2].

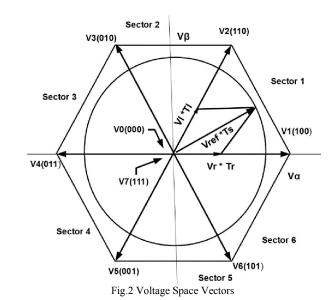


TABLE 1

LINE TO NEUTRAL VOLTAGE FOR DIFFERENT VECTORS

| Vectors | [S1,S2,S3] | $V_{an}$                  | $V_{bn}$             | $V_{cn}$             | $\theta$         |
|---------|------------|---------------------------|----------------------|----------------------|------------------|
| V1      | [1,0,0]    | $\frac{2V_{DC}}{3}$       | $\frac{-V_{DC}}{3}$  | $\frac{-V_{DC}}{3}$  | 0                |
| V2      | [1,1,0]    | $\frac{V_{DC}}{3}$        | $\frac{V_{DC}}{3}$   | $\frac{-2V_{DC}}{3}$ | $\frac{\pi}{3}$  |
| V3      | [0,1,0]    | $\frac{-\bar{V}_{DC}}{3}$ | $\frac{2V_{DC}}{3}$  | $\frac{-V_{DC}}{3}$  | $\frac{2\pi}{3}$ |
| V4      | [0,1,1]    | $\frac{-2V_{DC}}{3}$      | $\frac{V_{DC}}{3}$   | $\frac{V_{DC}}{3}$   | $\pi$            |
| V5      | [0,0,1]    | $\frac{-V_{DC}}{3}$       | $\frac{-V_{DC}}{3}$  | $\frac{2V_{DC}}{3}$  | $\frac{4\pi}{3}$ |
| V6      | [1,0,1]    | $\frac{V_{DC}}{3}$        | $\frac{-2V_{DC}}{3}$ | $\frac{V_{DC}}{3}$   | $\frac{5\pi}{3}$ |
| V7      | [1,1,1]    | 0                         | 0                    | 0                    | -                |
| V0      | [0,0,0]    | 0                         | 0                    | 0                    | -                |

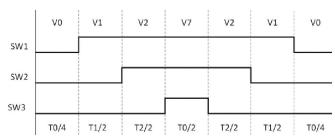


Fig.3 Symmetrical Switching sequence in sector 1

TABLE 2
DUTY CYCLES IN SECTORS

|     | On Times Of Inverter Upper Switch |                      |                      |  |  |  |
|-----|-----------------------------------|----------------------|----------------------|--|--|--|
| Sec | Switch 1                          | Switch 2             | Switch 3             |  |  |  |
| tor |                                   |                      |                      |  |  |  |
| 1   | $T_r + T_l + 0.5T_0$              | $T_l + 0.5T_0$       | $0.5T_{0}$           |  |  |  |
| 2   | $T_r + 0.5T_0$                    | $T_r + T_l + 0.5T_0$ | $0.5T_{0}$           |  |  |  |
| 3   | $0.5T_{0}$                        | $T_r + T_l + 0.5T_0$ | $T_l + 0.5T_0$       |  |  |  |
| 4   | $0.5T_{0}$                        | $T_r + 0.5T_0$       | $T_r + T_l + 0.5T_0$ |  |  |  |
| 5   | $T_l + 0.5T_0$                    | $0.5T_{0}$           | $T_r + T_l + 0.5T_0$ |  |  |  |
| 6   | $T_r + T_l + 0.5T_0$              | $0.5T_{0}$           | $T_r + 0.5T_0$       |  |  |  |

Symmetric strategy gives better performance than right aligned, left aligned, and alternate switching strategy in terms of THD parameter [4]. In symmetrical method, switching frequency is twice of sample frequency. Here active vectors are arranged in such a way that minimizes switching loss. Fig.3 shows switching sequence in sector 1.Table 2 shows duty cycles of upper three legs in different sectors.

#### III. SYSTEM DESIGN

In this work, simulation is performed for Load Resistance= $10\Omega$ , Load Inductance=0.1H,  $V_{DC}=100Volt$ 

## A. Matlab Simulation and results

The block diagram of the system in MATLABSimulink environment is shown in Fig 4. Reference time signals (Fig.5) are generated through Clarke transformation-sector identification-adjacent vector time calculation and vector selection. The reference signals are then compared with triangular wave to generate PWM. Fig.6 to Fig.8 showthe PWM signals, line to neutral voltage of phase A and line

current waveforms, respectively. All these waveforms are of command frequency of 50 Hz and 0.9 modulation index.

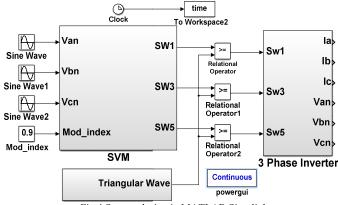


Fig.4 System design in MATLAB Simulink.

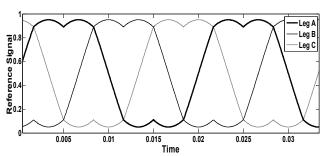
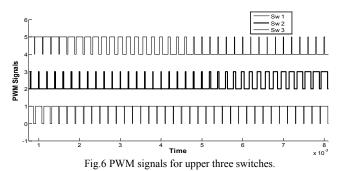


Fig.5 Reference Time Value for Upper Legs



Neutral Voltage

₽

0.005

0.01

Fig.7 Line to neutral voltage of Phase A.

0.02

0.025

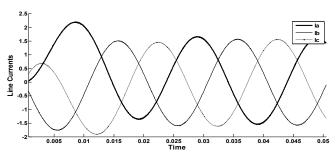


Fig.8 Three phase line current (for f=50 Hz and m=0.9)

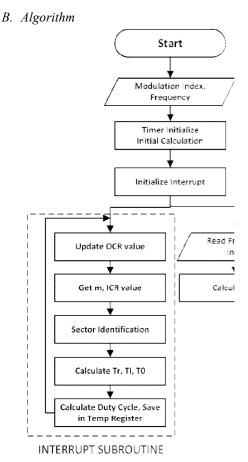


Fig.9 Algorithm of space vector modulation.

The algorithm is designed considering the architecture of ATmega64 microcontroller.ATmega64offers phase corrected PWMthrough which symmetric PWMis generated. When timer counter register's (TCNT) value matches input capture register's (ICR) value it generates a timer overflow interrupt. In interrupts service routine every calculation needed to generate duty cycle for each leg is done. Fig.9 shows algorithm for calculation of duty cycle.

Reference vector's angle calculation is a vital part of space vector modulation. However, angle calculation involves at least two multiplication so to optimize, a fixed number of samples are generated. For example, if 48 samples are used to create a full cycle then every sector contains  $\frac{48}{6}$  =8 samples and every new sample will be shifted from the previous sample by  $\frac{60}{8}$  =7.5 degree. For each sample, there is 2adjutant vector time calculation (Tr, Tl) necessity which involves trigonometric value (4) (5). In the beginning, the systemis initialized. Total sample number, starting frequency and modulation index (m) are specified. To get trigonometric value, two sine look-up table is formed, one for angle  $\theta$  and other for  $(60^{\circ} - \theta)$ . Next, the Timer is initialized, during when 1st sample's duty cycle value is calculated and timer overflow interrupt is set. In the very beginning of interrupt routine duty cycle value is fed to output compare register (OCR) and then next sample's value is calculated. To implement VFD, only ICR value and modulation index (m) need to be changed. To reduce very high starting current of induction motor, frequency is gradually increased. To do this, in interrupt service routine a starting algorithm is implemented. Fig.10 shows the result of changing frequency gradually.

After getting ICR and m values, Tr, Tl and T0 are calculated. Then from table 2 duty cycle values for the upper three legs are estimated in different sectors. These duty cycle values are fed to OCR registers at the beginning of next interrupt subroutine with the help of temporary registers.

As there is only two variable (ICR, m) associated with frequency and voltage, with the help of ADC user's choice of frequency can be synthesized. When a user presses a button or rotates potentiometer, ADC will sense and calculate ICR and m to implement variable frequency drive (VFD). Therefore, this algorithm is more generalized in nature.

Calculation time in interrupt routine can be further reduced. Solving  $T_l = m * T_s * \sin \theta$ involves multiplying two floating-point number and one integer, which takes many cycles. To optimize, sine table value can be modified according to  $sin\theta = m * T_s * sin\theta = K * sin\theta$ , K's value is decided according to frequency outside of interrupt routine. This modification decision is taken assuming that when the system goes steady state, frequency doesn't change for a significant amount of time. Then each sine look-up table value can be modified once and be used instead of repeated multiplication. After modification, this equation,  $T_1 = \sin \theta$ , can be used which is very fast. Fig.11 is generated to compare between generalized and modified method. This figure shows the performance of the system when frequency and modulation index is selected arbitrarily (without using V/f). Table 3 shows the total calculations of principle calculation block between generalized and modified method.

TABLE 3 CALCULATION NUMBERS AT STEADY STATEIN INTERRUPT ROUTINE

|                   | Generalized | Modified |  |
|-------------------|-------------|----------|--|
| Multiplication    | 4           | 0        |  |
| Addition          | 8           | 8        |  |
| Switch Case       | 1           | 1        |  |
| Bitwise Shifting  | 2           | 2        |  |
| Total Cycle Taken | 870         | 190      |  |

The three PWM signals are generated in Atmega 64 using one 16-bit timer. This is also possible in Arduino Uno (ATmega 328p) which has one 16-bit timer and two 8-bit timer. However, in ATmega328p only two PWM generation is possible with every timer. So two of the three Timers should be synchronized using GTCCR register to get three PWM.

# C. Results from Proteus Simulation

The system with the microcontroller is simulated in Proteus. Fig.12 to Fig.14 shows PWM signals,  $V_{AB}$ ,  $V_{AN}$  and current waveforms of 50 Hz and 0.9 modulation index. Fig.10 shows line currents for changing frequency gradually from 5 to 50 Hz with modulation index 0.1 to 0.9 respectively. Fig.15 shows  $V_{AB}$ ,  $V_{AN}$  waveform of this process. Fig.11 shows gradually generating 5, 10,20,30,40Hz line currents with 0.1, 0.5, 0.4, 0.2, 0.7 modulation index respectively.

A comparison of total calculation time between generalized and modified method is observed during generation of Fig.11. 8 MHz internal RC oscillator is used and the Timer's frequency is made to 1Mhz. It has been noted that the average time needed by the modified method is around 60 microseconds while the generalized method needs around 120 microseconds. Also in experiments 48 sample is used. Fig.3 shows that in every sample generation there are two

switchings. Therefore, to generate 50 Hz sine wave, switching frequency is 50 \* 2 \* 48 = 4.8 Khz.

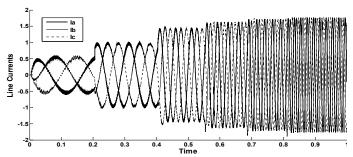


Fig.10Generation of 5, 10, 20,30,40,50 Hz frequency of 0.1, 0.2, 0.4, 0.6, 0.8 and 0.9 modulation index respectively.

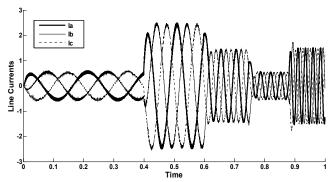


Fig.11 Generation of 5, 10,20,30,40 Hz frequency of 0.1, 0.5, 0.4, 0.2 and 0.7 modulation index respectively

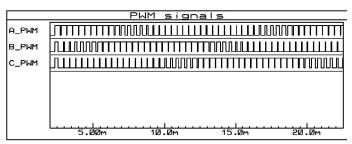


Fig.12 PWM signals

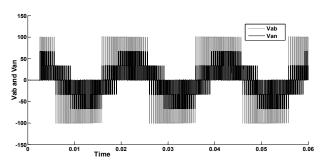


Fig.13 Line to Line and Line to neutral Voltage.

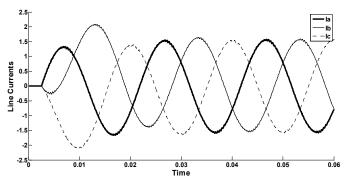


Fig.14 Line currents for f=50, m=0.9.

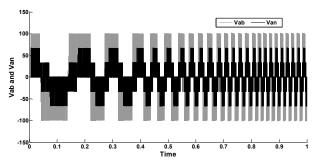


Fig.15 Line to Line and Line to neutral voltage duringgradual increase of modulation index

Each sample period is  $\frac{1}{4.85}$  = 416 microseconds. So when implementing generalized algorithm (416 – 120) = 296 microseconds is available to implement other processes and interfacing.If 16 MHz crystal is used then calculation time should reduce to half. More sample can be generated in a cycle and switching frequency will increase.

#### IV. CONCLUSIONS

Space vector modulation for three-phase two-level inverter is simulated Matlab/Simulink environment implementation with ATmega 64 microcontroller is observed in Proteus. Program design is done in two ways: generalized and modified method. It has been shown modified method needs less computation time then generalized method. The same algorithm can be implemented on Arduino Uno. The generated PWM signal can be made to use for variable frequency drive.

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