



GEN 500
Engineering System Analysis
Fall 2020

HW #4

Due date: 10/28/2020 @ 5: 00 PM

Two distances are required to specify the location of a point relative to an origin in two-dimensional space (Fig. 1):

The horizontal and vertical distances (x, y) in Cartesian coordinates.

The radius and angle (r, θ) in polar coordinates.

It is relatively straightforward to compute Cartesian coordinates (x, y) on the basis of polar coordinates (r, θ) . The reverse process is not so simple. The radius can be computed by the following formula:

$$r = \sqrt{x^2 + y^2}$$

If the coordinates lie within the first and fourth quadrants (i.e., $x > 0$), then a simple formula can be used to compute θ :

$$\theta = \tan^{-1}\left(\frac{y}{x}\right)$$

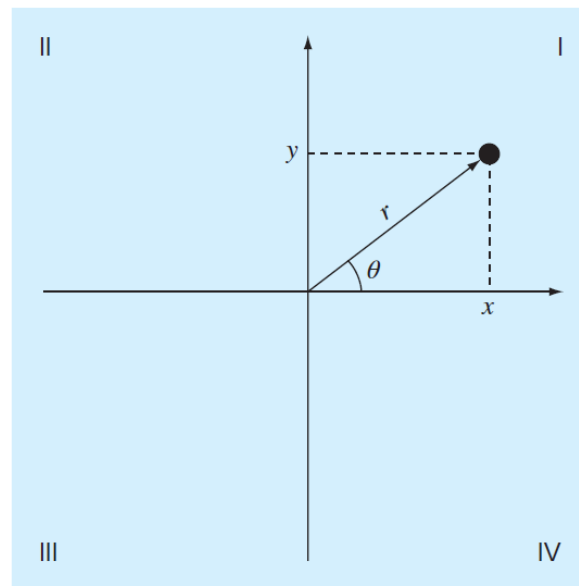


Figure 1



The difficulty arises for the other cases. The following table summarizes the possibilities:

X	Y	Θ
<0	>0	$\tan^{-1}\left(\frac{y}{x}\right) + \pi$
<0	<0	$\tan^{-1}\left(\frac{y}{x}\right) - \pi$
<0	$=0$	π
$=0$	>0	$\pi/2$
$=0$	<0	$-\pi/2$
$=0$	$=0$	0

Write a well-structured M-file using if...elseif structures to calculate r and θ as a function of x and y . Express the final results for θ in degrees. Test your program by evaluating the following cases:

X	Y	r	Θ
2	0		
2	1.5		
0	3.1		
-3	2		
-2	0		
-1	-3		
0	0		
0	-1		
3	3		