Information Gain

Pslow =
$$\frac{2}{3}$$
 Pfast = $\frac{1}{3}$

Information = entropy (parent) - [weighted] entropy (children)

gain

grade bumpiness speed entropy of parent = 1.0

entropy = $\sum_{i} -P_{i} \log_{2} P_{i}$

steep smooth yes slow entropy = $\left[-\frac{2}{3}\log_{2}\left(\frac{2}{3}\right) - \frac{1}{3}\log_{2}\left(\frac{1}{3}\right)\right]$

flat bumpy no fast = $\left[-\frac{2}{3}\log_{2}\left(\frac{2}{3}\right) - \frac{1}{3}\log_{2}\left(\frac{1}{3}\right)\right]$
 $= \left[-\frac{2}{3}\log_{2}\left(\frac{2}{3}\right) - \frac{1}{3}\log_{2}\left(\frac{1}{3}\right)\right]$