

GIT Department of Computer Engineering

CSE 222/505 - Spring 2021

Homework 2 Report

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Part 1

1. Search Product:

```
/**<p>Query furniture is in branch or not using linear search</p>*/  
public boolean queryProduct(Furniture obj){  
  
    if(obj == null)  
        return false;  
    for(int i=0; i<productNumber; ++i)  
        if(products[i].equals(obj))  
            return true;  
    return false;  
}
```

figure 1.1

We got an Furniture[] products let say its lenght is **n**. We use linear search for find wanted search

If its not include wanted furniture that means loop work for n time. **T(n) -> O(n)**

If the wanted furniture is first product that means loop work for just 1 time. **T(n) -> O(1)**

If the wanted furniture is last element that means loop work for just n time. **T(n) -> O(n)**

Best time complexity $O(1)$ worst time complexity $O(n)$ **this time complexity for $T(n) = O(n)$**

```
@Override  
public boolean equals(Object o) {  
  
    if(!(o instanceof OfficeChair ))  
        return false;  
  
    OfficeChair obj = (OfficeChair ) o;  
    return (obj.getModel() == this.getModel() && obj.getColor() == this.getColor());  
}
```

figure 1.2

This function just include constant time complexity $O(1) + O(1) + \dots = O(1)$

For this equals function $T(n) = O(1)$

Admin & Customer:

These users can see all products in all branch.

```
/**<p>It search for the wanted furniture in all branch using linear search</p>*/  
public Branch queryProduct(Furniture obj) {  
    for(int i = 0; i<currentBranchNumber; ++i) {  
        if(branches[i].queryProduct(obj))  
            return branches[i];  
    }  
    return null;  
}
```

figure 1.3

Admin and customer can search a product in all store if accept taht number of branch is **m**:

We see the before **queryProdutc()** time complexity = **O(n)**

Best case for this functions is ; $m = 1, n = 1 \rightarrow T(m, n) = O(1)$

Worst case for if don't have furniture and end of product -----> $T(m, n) = O(m*n)$

This function time complexity for $T(m, n) = O(m * n)$

Employee:

This user can see just own working branch

```
/**<p>Query a product in working branch function</p>*/  
public boolean queryProduct(Furniture obj){  
    return workBranch.queryProduct(obj);  
}
```

figure 1.4

We see that before queryProduct() in figure1.1 **time complexity = $O(n)$**

2. Add/ Remove Product:

Add Product:

```
/**<p>Doubling Product array when it full</p>*/  
public void enlargeProduct() {  
  
    Furniture[] tmpF = new Furniture[ProductsCapacity*2];  
  
    for(int i=0; i<productNumber; ++i)  
        tmpF[i] = products[i];  
  
    products = tmpF;  
    ProductsCapacity *= 2;  
}
```

figure 2.1

enlargeProduct function **time complexity is $T(n) \rightarrow \Theta(n)$**

```
/**<p>adding Product next free space in products array</p>*/  
public boolean addProduct(Furniture newProduct) {  
  
    if(productNumber >= ProductsCapacity)  
        enlargeProduct();  
  
    products[productNumber++] = newProduct;  
    return true;  
}
```

figure 2.2

If there is enough space to add best case is constant **$\Theta(1)$**

If array is full we need to enlarge and we see enlargeProduct time complexity is $\Theta(n)$

These means we have a condition for to be **$\Theta(n)$**

complexity for **addProduct time complexity is $O(n)$**

Remove Product:

```
/**<p>Removing product using array shifting method</p>*/  
public boolean removeProduct(int index) {  
    if(index >= productNumber)  
        return false;  
  
    while(index < productNumber)  
        products[index] = products[++index];  
    productNumber--;  
    return true;  
}
```

figure 2.3

Best case for this method is last element removing it last element it constant time for this its $\rightarrow \Theta(1)$
Worst case is removing first element that happen you need to shift all array its time comp. $\rightarrow \Theta(2)$

According to the removing status it **time complexity for this method is $O(n)$**

3.Query Product

Admin:

```
public void querySupplyFurniture() {  
    for(int i=0; i<getBranchNumber(); ++i) {  
        for (Furniture f : allTypeFurnitureArray) {  
            if(getBranch(i).queryProduct(f) == false) {  
                System.out.println("Need to supplied " + f);  
            }  
        }  
    }  
}
```

figure 3.1

We mention that queryProduct() complexity in figure 1.1 method complexity is $\rightarrow O(n)$

Let accepts number of branch number is = m and all type furniture number is = p

This method has 3 nested loop and all complexity has to complete for this way

function time complexity $T(n, m, p) = \Theta(n * m * p)$ absolute value

Employee:

```
public void querySupplyFurniture() {  
    for (Furniture f : allTypeFurnitureArray) {  
        if(workBranch.queryProduct(f) == false) {  
            System.out.println("Need to supplied " + f);  
        }  
    }  
}
```

figure 3.2

We mention that queryProduct() complexity in figure 1.1 method complexity is -> **$O(n)$**

Let accepts all type furniture count is = m

This method has 2 nested loop and all complexity has to complete for this way

function time complexity $T(n, m) = \Theta(n * m)$ absolute value

Part 2

A)

Big-O gives upper bound, or maximum running time complexity of an algorithm.

Using "at least" here is not the correct way of using with Big-O notations.

At least gives upper - bound

$O(n^2)$ gives upper - bound

B)

Handwritten mathematical derivation:

$$\text{let } h = \max(f(n), g(n))$$
$$f(n) + g(n) \leq 2h$$
$$\text{so } f(n) + g(n) = O(h).$$

If $f(n) + g(n)$ are positive then

$$h \leq f(n) + g(n) \text{ and so } h = \Theta(f(n) + g(n))$$
$$\max(f(n), g(n))$$

figure 2.2

C)

1) if we take the limit to inf

Handwritten limit calculation:

$$\lim_{n \rightarrow \infty} \frac{2^{n+1}}{2^n} \Rightarrow \lim_{n \rightarrow \infty} \frac{2^{\cancel{n}} \cdot 2}{2^{\cancel{n}}} \Rightarrow \lim_{n \rightarrow \infty} 2 = 2$$

figure 2.3.1

That means they are equal time complexity

2)

c is constant

$$\ln 2^{2n} \leq c 2^n$$

$$\ln 2 \cdot 2n \leq \ln c + \ln 2 \cdot n$$

$$2n \leq \ln c + n$$

$$n \leq \ln c$$

figure 2.3.2

Which is clearly wrong because there is no such constant a number that inequality $R = \{ \}$

3)

$f(n) = O(n^2)$ $g(n) = \Theta(n^2)$

this waste case

don't have the information absolutely like Θ

so if we multiply with $O * \Theta =$

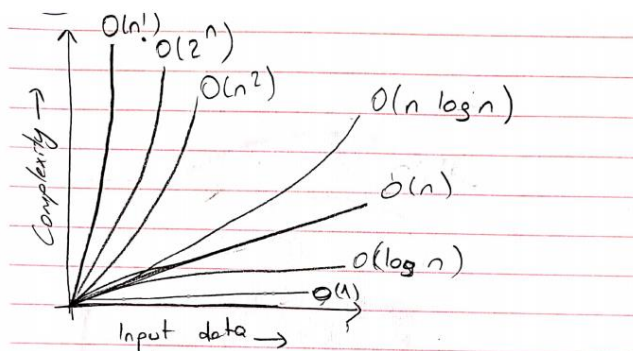
result must be O and $T(n)$ n's must be multiply by normal

$f(n) * g(n) \neq \Theta(n^4) \times$

$f(n) * g(n) = O(n^2 * n^2) = O(n^4) \checkmark$

Figure 2.3.3

Part 3



As we can see the graph we can separate the functions a couple of group firstly

I. group	II. group	3. group
\sqrt{n}	$n^{1.01}$	3^n
$(\log n)^3$	$n \log^2 n$	$n 2^n$
$\log(n)$	$n \log^2 n > n^{1.01}$	2^{n+1}
$5^{\log_2 n}$		2^n
		$3^n > n 2^n > 2^{n+1} > 2^n$
$5^{\log_2 n} > \sqrt{n} > \log(n)^3 > \log(n)$		

According to the absolute value sorted is

$$3^n > n 2^n > 2^{n+1} > 2^n > n \log^2 n > n^{1.01} > 5^{\log_2 n} > \sqrt{n} > \log(n)^3 > \log(n)$$

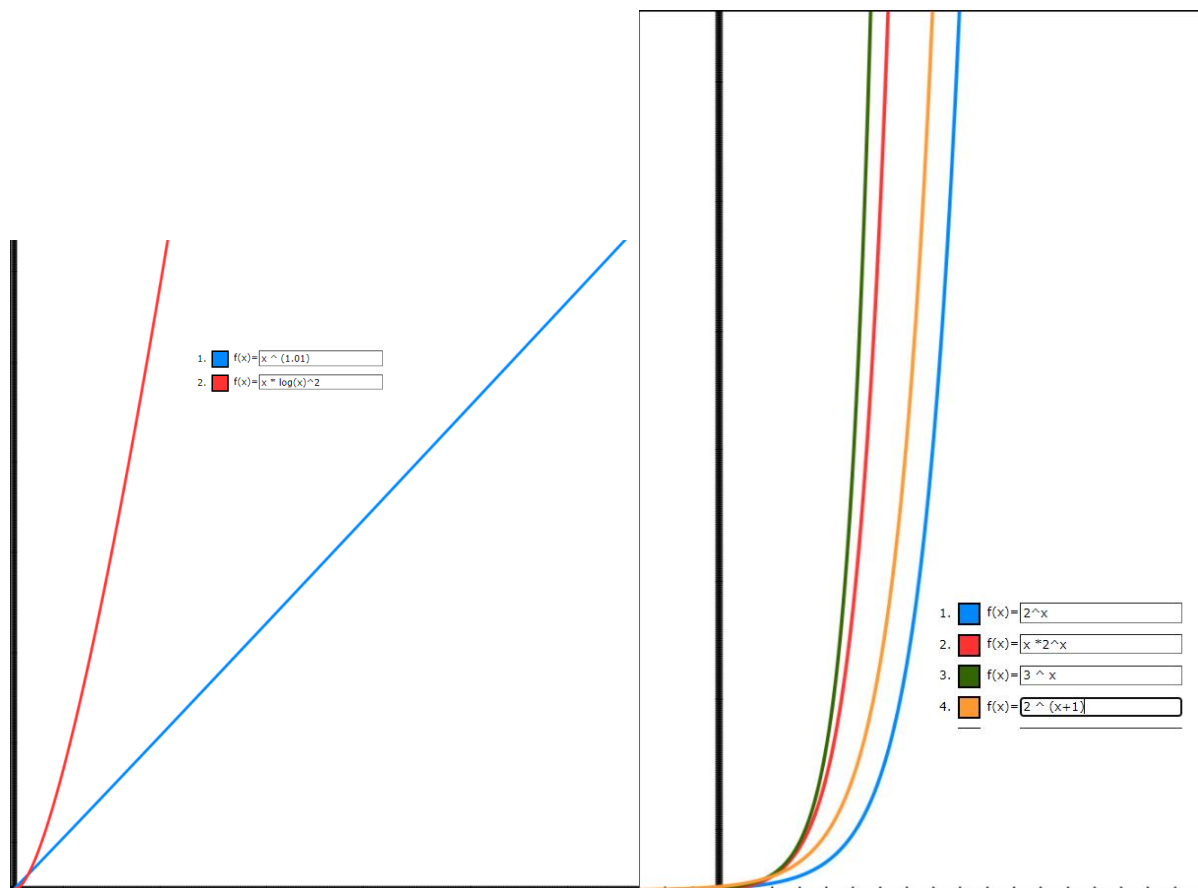
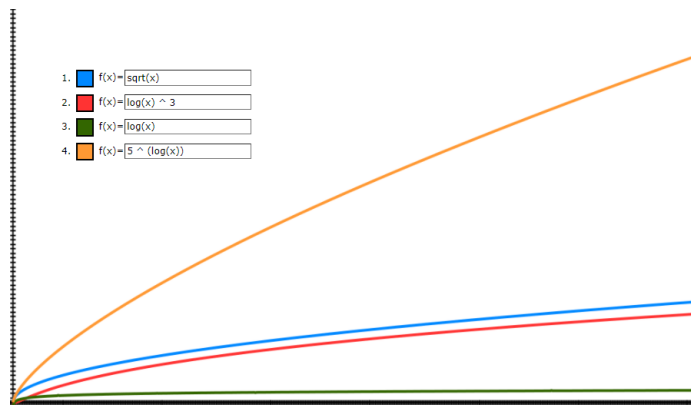
But if we want to sort using Big-O notation we can ignore some constant and result will be like this

$$O(3^n) > O(n 2^n) > O(2^n) = O(2^n) > O(n \log^2 n) = O(n^{1.01}) > O(5^{\log_2 n}) > O(\sqrt{n}) > O(\log(n)^3) > O(\log(n))$$

$$\lim_{n \rightarrow \infty} \frac{2^n}{2^{n+1}} = 0 \checkmark$$

Because of these there are two equality in asymptotic ordering

$$\lim_{n \rightarrow \infty} \frac{n \log^2 n}{n^{1.01}} = 0 \checkmark$$



Part 4

A)

```
1 min_function( arrList )
2
3
4 int min = arrList[0]
5
6 for ( element : arrList )
7     if min < element
8         min = element    // If there is smaller than current number
9                           // take it as a new smallest number
10 return min
11
```




figure 4.1

We are looking all element to find smallest element. It always time complexity is $\rightarrow \Theta(n)$

B)

```
15
16 median_function( arrList )
17
18 if arrList.length % 2 == 0 :
19     boolean r1 = r2 = false
20     int sum = 0
21     for i = 0 ; i < arrList.length; ++i :
22
23         int smallCounter = bigCounter = 0
24         for j = 0; j < arrList.length; ++j
25
26             if arrList[j] > arrList[i] :
27                 bigCounter++
28
29             else if arrList[j] < arrList[i] :
30                 smallCounter++
31
32         if bigCounter - smallCounter == 1
33             r1 = true
34             sum += arrList[i]
35         if smallCounter - bigCounter == 1
36             r2 = true
37             sum += arrList[i]
38
39         if r1 && r2
40             int median = sum / 2
41             return median
42
```

figure 4.2.1

This is work for array length is even because if array length is even there is two median value and return it avg of two values.

Algorithm is we take an number `arrList[i]` and counting smaller numbers and bigger numbers.
if `sCounter - lCounter` is equal is 1 or vice vierre to left side of equality (`lCounter - sCounter == 1`)

Best case is $2n$ for the method = $\Theta(2n)$

Worst case is $n^2 = \Theta(n^2)$

Time Complexity for the even `arrList` length is $\rightarrow O(n^2)$

```

43
44     if arrList.length % 2 != 0 :
45
46         for i=0 ; i<arrList.length; ++i :
47
48             int smallCounter = bigCounter = 0
49             for j=0; j<arrList.length; ++j
50
51                 if arrList[j] > arrList[i]
52                     bigCounter++
53
54                 else if arrList[j] < arrList[i]
55                     smallCounter++
56
57             if smallCounter == bigCounter
58                 int median = arrList[i]
59                 return median
60

```

figure 4.2.2

This is work for array length is odd there is absolute value

Algorithm is we take an number arrList[i] and counting smaller numbers and bigger numbers.
If sCounter == bCounter that means we find the median value of array

Best case is $2n$ for the method = $\Theta(n)$

Worst case is $n^2 = \Theta(n^2)$

Time Complexity for the odd arrayList length is - $\rightarrow O(n^2)$

median_function() time complexity $T(n) \rightarrow O(n^2)$

c)

```

64
65 sum_function( arrList , value):
66
67     map<Integer,Integer> myMap
68
69     int result[] = new int [2]
70     for i = 0 ; i< arrList.length ; ++i:
71
72         if(myMap.containsKey(value - arrList[i])
73             // Look for the need number to reach target
74             // is in the list or not if it in list take it using get
75             return {myMap.get(value - arrList[i]) , i}
76
77         myMap.put(arrList[i], i) //storeing data to reach if need
78
79     return result
80

```

figure 4.3

We could use onether way : iterate over list for each elemet as : $arr[i] + arr[j] == value$ if we use this algorithm our time complexity wolud be $O(n^2)$

But in this way we decrease the complexity using map data structur to reach consider the contains method and **our algorithm time complexity $O(n)$ ignoring constant time operations**

D)

```
86
87~ LinkedList merge_two_sortedArr_getLinkedList( arrL_1, arrL_2 )
88
89     LinkedList<type> ll = new LinkedList<>()
90
91~     for i = 0, j = 0 ; i < arrL_1.size() && j < arrL_2.size(); :
92         // Getting number respectively dont mess up sorted
93         // until one of reach of the array size
94~         if arrL_1.get(i) < arrL_2.get(j) :
95             ll.add(arrL_1.get(i))
96             i++
97~         else :
98             ll.add(arrL_2.get(j))
99             j++
100
101
102     // One of the while is gonna work because
103     // one of the counter reach the array size in for loop
104     while(i < arrL_1.size())
105         ll.add(arrL_1.get(i++))
106
107     while(j < arrL_2.size())
108         ll.add(arrL_2.get(j++))
109
110     return ll
111
```

figure 4.4

if we accepts sizes as arr1.size is -> n and arr2.size -> m

Fisrt for loop wil work time complexity is if $n < m \rightarrow \Theta(2n)$
else $\Theta(2m)$

And then it wil work in while loop if $n > m \rightarrow \Theta(n - m)$
else $\Theta(m - n)$

Ll.add method is working time $T(p) \rightarrow \Theta(1)$ and this is gonna work $n+m$ times to add all element

Our time complexity will gonna be $\rightarrow \Theta((n+m) * 1) = \Theta(n+m)$

Note : we ignore the constant operations.

Part 5

A)

```
a)
int p_1 (int array[]):{
    return array[0] * array[2]
}
```

figure 5.1

All operations of functions is completing in constant time $T(n) = \Theta(1)$

B)

```
b)
int p_2 (int array[], int n):{
    int sum = 0
    for (int i = 0; i < n; i=i+5)
        sum += array[i] * array[i]
    return sum
}
```

Figure 5.2

In $\text{sum} = 0$ & $\text{sum} += \text{arr}[i] + \text{arr}[i]$ & return sum is completing in constant time $\Theta(1)$

But for loop work n time that means time complexity is $\Theta(n / 5) = \Theta(n)$

$T(n) \rightarrow \Theta(n) + \Theta(1) = \Theta(n)$

c)

```
c)
void p_3 (int array[], int n){
    for (int i = 0; i < n; i++)
        for (int j = 1; j < i; j=j*2)
            printf("%d", array[i] * array[j])
}
```

Figure 5.3

$\text{printf}() \Rightarrow \Theta(1)$

$\text{for}(j=1; j < i; j=j*2) \Rightarrow$
 $\Rightarrow 1, 2, 4, 8, 16$

loop will gonna stop
 $\log / 2^k > n$
 $= k > \log n - 2$

Therefore, the number of iterations is only $O(\log n)$
so the total complexity is $O(\log n)$ for 2th loop
 $\text{for}(i=0; i < n; ++i) \Rightarrow \Theta(n)$ for 1th loop

so the total complexity is
 $\Theta(1) * \Theta(n) * O(\log n) \Rightarrow O(n \log n)$
 $n < n \cdot \log(n) < n^2$

figure 5.3.2

$O(n * \log n)$

D)

```
d)
void p_4 (int array[], int n){
    if (p_2(array, n)) > 1000
        p_3(array, n)
    else
        printf("%d", p_1(array) * p_2(array, n))
}
```

figure 5.4

Firstly let do the easy one if the condition is not true in if statment is

Best case : $T(n) = \Theta(1)$

If the if condition is true it would take alot time than else statment

Worst case when the condition is true :

as we calculate the figure 5.2 p_2() time complexity is $T(n) -> \Theta(n)$

p_3() time complexity is in figure 5.3.2 complexity is $T(n) -> O(n * \log n)$

time complexity is

$T(n) -> \Theta(n) + O(n * \log n) = O(n * \log n)$ (we just take dominant term)

P_4() complexity is $T(n) -> O(n * \log n)$

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CSE 222 HW2