

Discrete Mathematics (26.12.2017)

1. Explain the terms Simple Graph, Path, Circuit, Euler Path, Euler Circuit, Tree, Branch and Link by giving an example for each term. (30 pts).
2. Consider the boolean function $f(a, b, c) = abc + ab'c' + a'bc' + a'b'c$. (20 pts).
 - a) Implement $f(a, b, c)$ by using the logic gates without simplifying the function.
 - b) Implement $f(a, b, c)$ by using the logic gates in its simplest form.
3. a) Prove that a strictly increasing function from \mathbb{R} to itself is one-to-one. (05 pts).
 b) Give an example of increasing function from \mathbb{R} to itself that is not one-to-one. (05 pts).
4. Let $a_n = -3a_{n-1} - 3a_{n-2} - a_{n-3} + n^2$ with $a_0 = 1$, $a_1 = 2$ and $a_2 = 3$. Find the solution of this recurrence relation. (40 pts).

$$a_3 = -3a_2 - 3a_1 - a_0 + 9$$

$$a_3 = -3 \cdot 3 - 3 \cdot 2 - 1 + 9 = -9 - 6 - 1 + 9 = -7$$

$$\boxed{a_3 = -7}$$

Duration : 90 minutes.