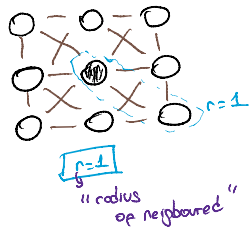


Cellular Neural Network

↳ "Local connection" bağlantısı yapılır  
 ↳ Sadece yakınlardaki ile bağlantı yapar

$(2r+1) \times (2r+1)$  tane  
 "neighborhood" olur

Örnek Çözüm

① Index numarasını  
 sea  
 $b=1$   
 $c=2$   
 $\vdots$

② Yakınlardaki elemler  
 $b \Rightarrow \{c, e, a, b\}$   
 $c \Rightarrow \{b, e, a, e, d, c\}$

③ Numara değeri göre tersi  
 yaz.  
 $b \Rightarrow \{5, 4, 2, 1\}$   
 $c \Rightarrow \{e, a, e, d, c, b\}$

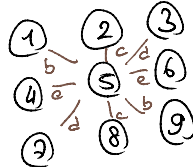
④ Diğer değerleri ekle  
 $-x_i + Ag(x_i) + u_i$   
 index numarası  
 yakınlardaki numarası

Matris işlemleri

↳ "Symmetric Template" düsturları:

$$T: \begin{Bmatrix} b & c & d \\ e & a & e \\ d & c & b \end{Bmatrix} \quad \text{! Simetrik değil}$$

↳ 1, 2, 3 adlandırması yapılır.



↳ "Nonlinear differential equation" gösterimi

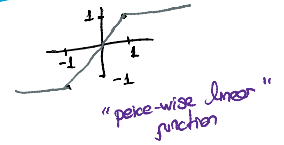
$$\dot{x} = -x + Ag(y(x)) + u$$

$$\dot{x}_i = -x_i + \sum_{j=1}^n a_{ij} \cdot y(x_j) + u_i$$

$x = [x_1, x_2, \dots, x_n]^T$  "State cell"  
 $A = \{a_{ij}\}_{n \times n}$  "Feedback matrix contains weights"  
 $u = [u_1, u_2, \dots, u_n]^T$  "Inputs"  
 $y = [y(x_1), y(x_2), \dots, y(x_n)]^T$  "Outputs"

The Expression for y

$$y(x_i) = \frac{1}{2} [|x_i + 1| - |x_i - 1|]$$



⑤ Matris düsturları numaralı diğer elemleri, diğerleri 0 olur. → "neighbors"

$$b \Rightarrow \{a, e, c, b\} \quad \begin{bmatrix} 1 & 2 & 4 & 5 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$c \Rightarrow \{e, a, e, d, b\} \quad \begin{bmatrix} e & a & e & d & c & b & 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 2 \\ 4 & 5 & 6 \end{bmatrix}$$

$$\dot{x} = -x + A \cdot y(x) + u$$

$$\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \\ \dot{x}_3 \\ \dot{x}_4 \\ \dot{x}_5 \\ \dot{x}_6 \\ \dot{x}_7 \\ \dot{x}_8 \\ \dot{x}_9 \end{bmatrix} = - \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \\ x_7 \\ x_8 \\ x_9 \end{bmatrix} + \begin{bmatrix} a & e & 0 & c & b & 0 & 0 & 0 & 0 \\ e & a & e & d & c & b & 0 & 0 & 0 \\ 0 & e & a & 0 & d & c & 0 & 0 & 0 \\ c & d & 0 & e & 0 & c & b & 0 & 0 \\ b & c & d & e & a & e & d & c & b \\ 0 & b & c & 0 & e & a & 0 & d & c \\ 0 & 0 & 0 & c & d & 0 & a & e & 0 \\ 0 & 0 & 0 & b & c & d & e & a & e \\ 0 & 0 & 0 & 0 & b & c & 0 & e & a \end{bmatrix} \begin{bmatrix} y(x_1) \\ y(x_2) \\ y(x_3) \\ y(x_4) \\ y(x_5) \\ y(x_6) \\ y(x_7) \\ y(x_8) \\ y(x_9) \end{bmatrix} + \begin{bmatrix} u_1 \\ u_2 \\ u_3 \\ u_4 \\ u_5 \\ u_6 \\ u_7 \\ u_8 \\ u_9 \end{bmatrix}$$

Ex:  $T: \begin{Bmatrix} b & c & d \\ e & a & e \\ d & c & b \end{Bmatrix}$

The state equations for the CNN:

$$\begin{aligned} \dot{x}_1 &= -x_1 + a y(x_1) + e y(x_2) + c y(x_4) + b y(x_5) + u_1 \\ \dot{x}_2 &= -x_2 + e y(x_1) + a y(x_2) + e y(x_3) + d y(x_4) + c y(x_5) + b y(x_6) + u_2 \\ \dot{x}_3 &= -x_3 + e y(x_2) + a y(x_3) + d y(x_5) + c y(x_6) + u_3 \\ \dot{x}_4 &= -x_4 + c y(x_1) + d y(x_2) + a y(x_4) + e y(x_5) + c y(x_7) + b y(x_8) + u_4 \\ \dot{x}_5 &= -x_5 + b y(x_1) + c y(x_2) + d y(x_3) + e y(x_4) + a y(x_5) + e y(x_6) + d y(x_7) + c y(x_8) + b y(x_9) + u_5 \\ \dot{x}_6 &= -x_6 + b y(x_2) + c y(x_3) + e y(x_5) + a y(x_6) + d y(x_8) + c y(x_9) + u_6 \\ \dot{x}_7 &= -x_7 + c y(x_4) + d y(x_5) + a y(x_7) + e y(x_8) + u_7 \\ \dot{x}_8 &= -x_8 + b y(x_4) + c y(x_5) + d y(x_6) + e y(x_7) + a y(x_8) + e y(x_9) + u_8 \\ \dot{x}_9 &= -x_9 + b y(x_5) + c y(x_6) + e y(x_8) + a y(x_9) + u_9 \end{aligned}$$