

AI/CH5

## Informed Search

Uses problem-specific knowledge

More efficient than uninformed search

### \* Best-first Search:

→ Expanding due to an evaluation function  $f(n)$

↓  
evaluation measures the distance to the goal

↓  
Node with lowest evaluation is selected for expansion

↓  
Other key component: heuristic function  $h(n)$

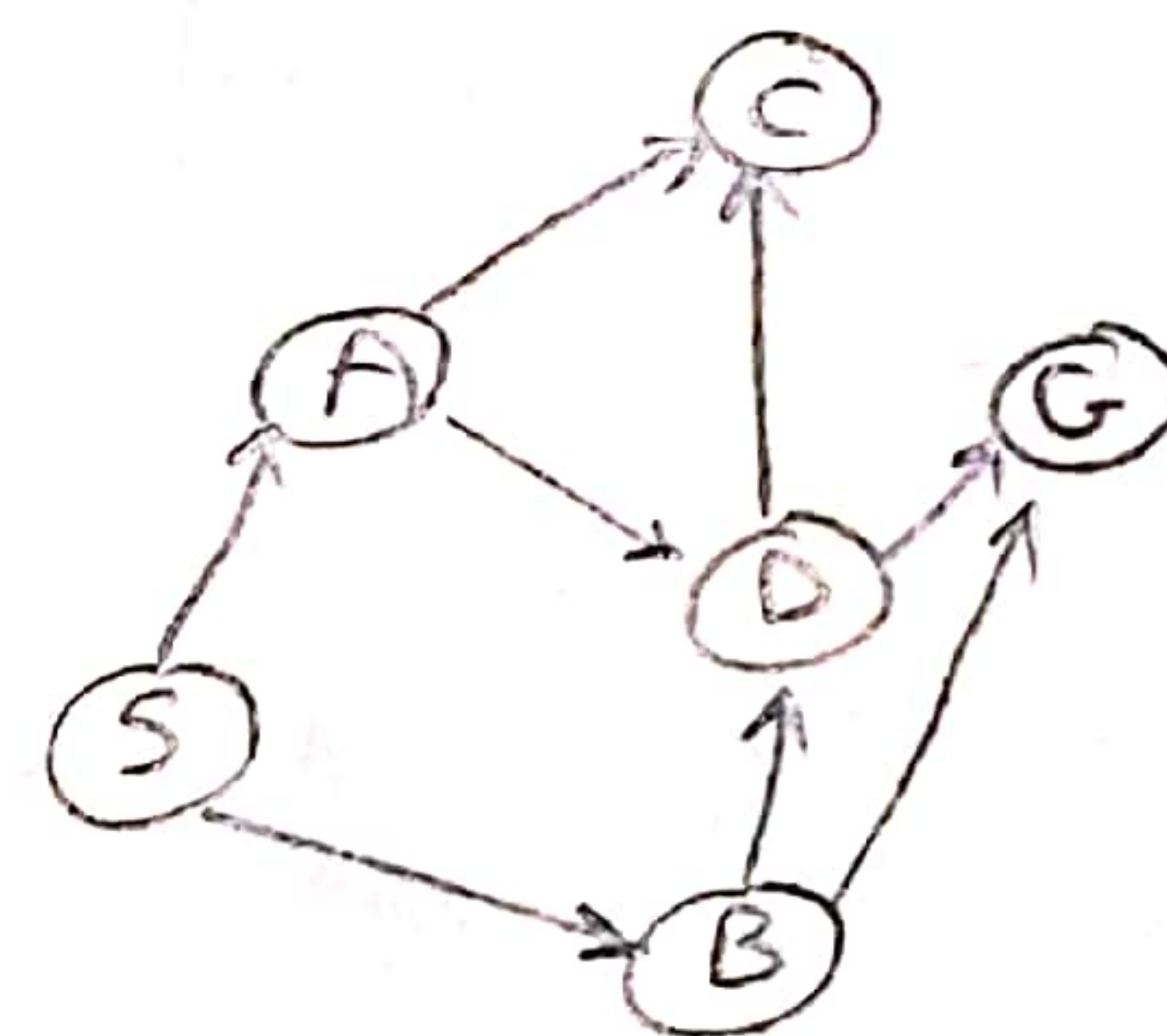
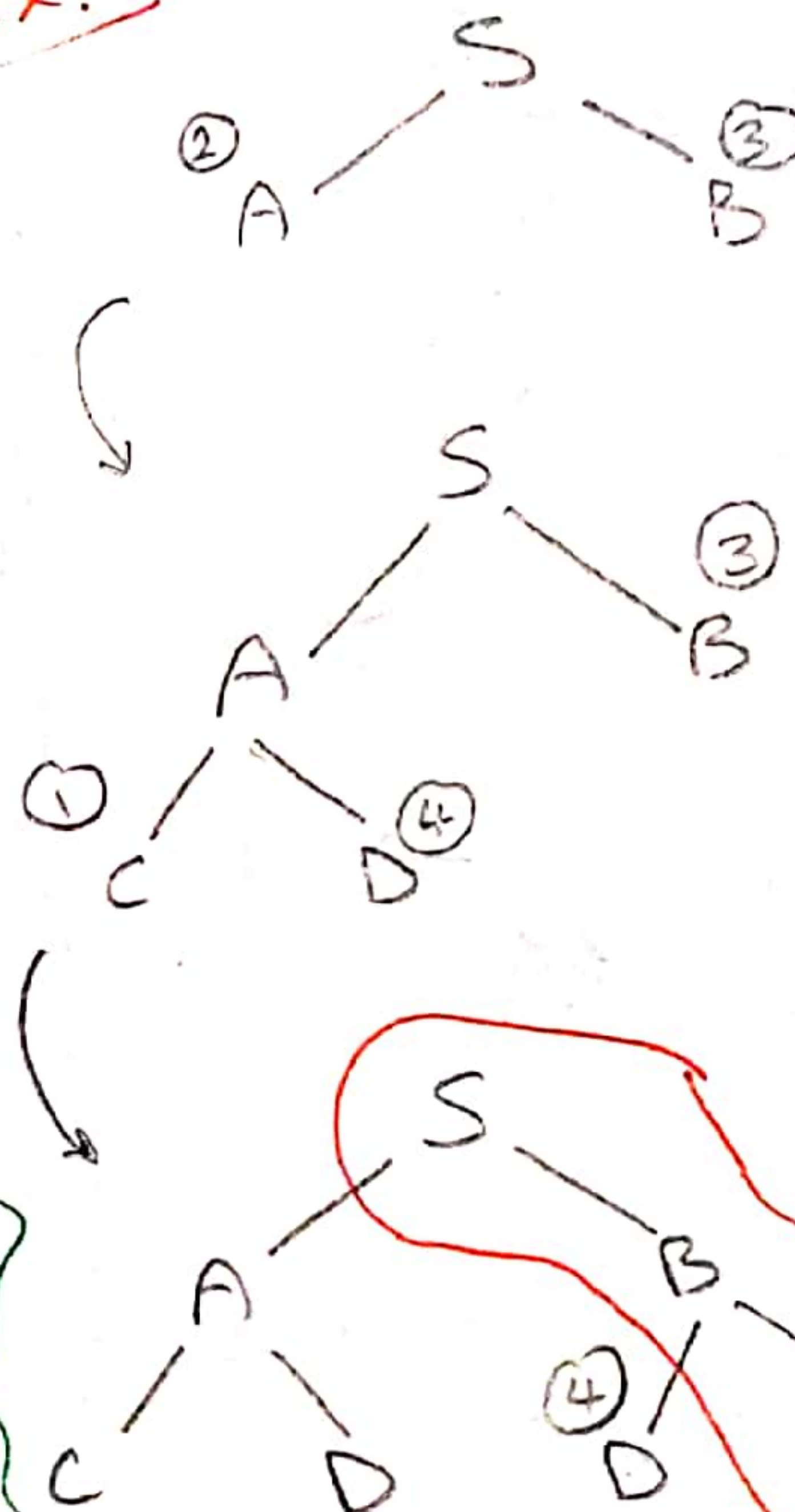
if  $n$  is a goal  $\Rightarrow h(n) = 0$

### \* Greedy best-first search

→ Tries to expand the closest node to the goal

↓  
Evaluates nodes only by the heuristic function

Ex:



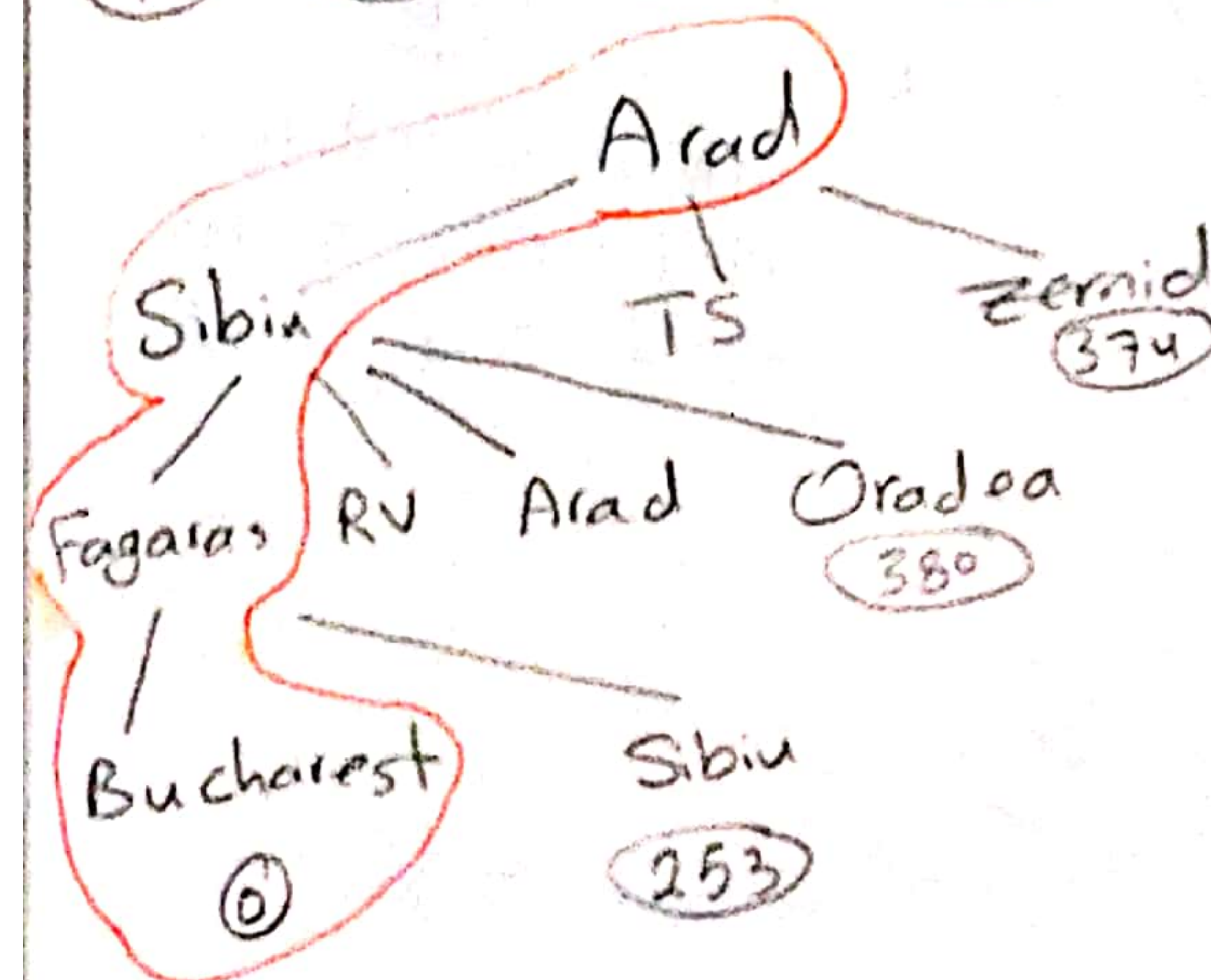
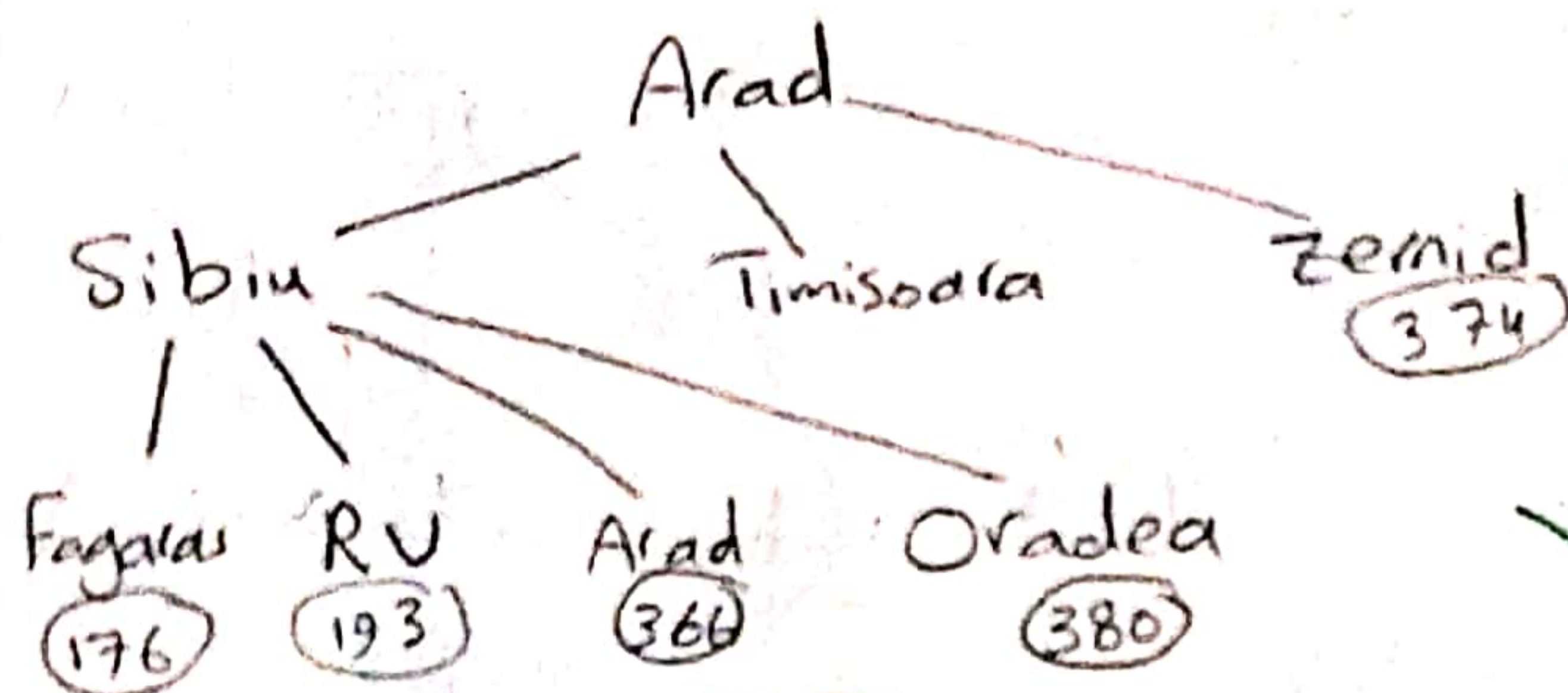
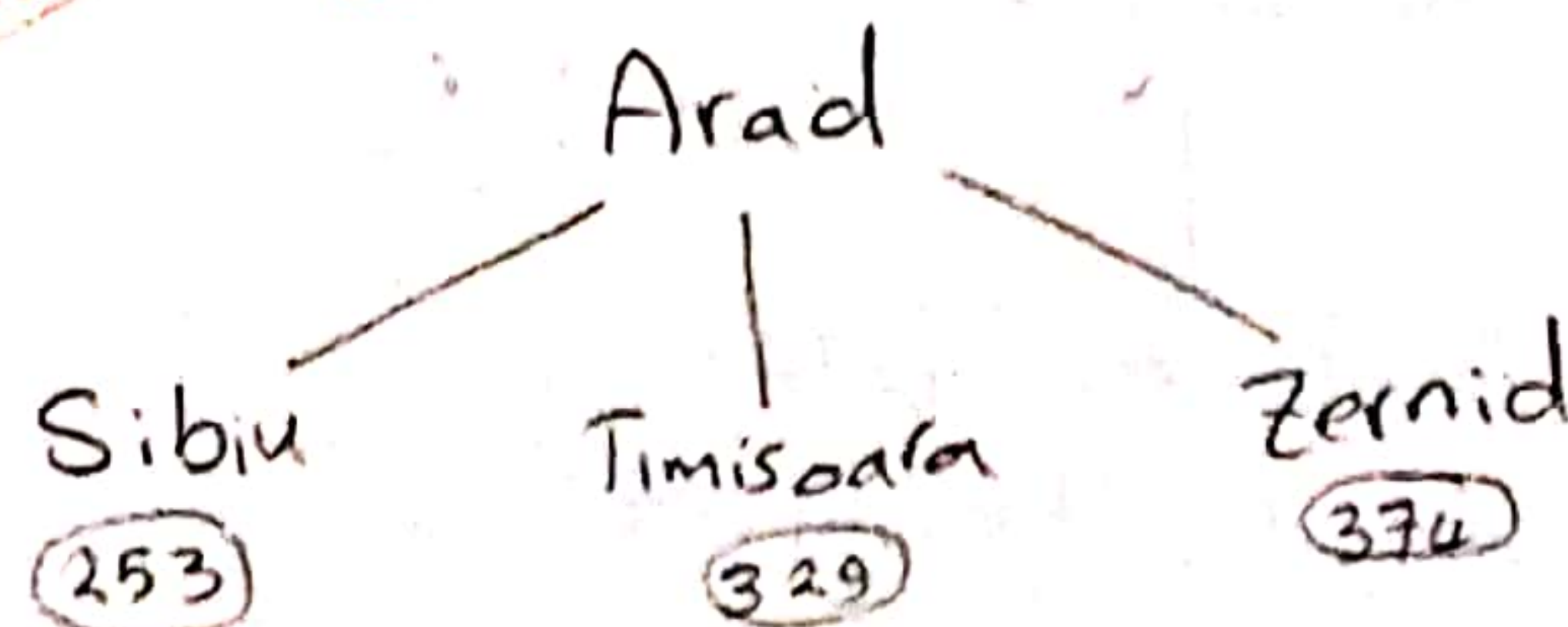
Heuristic Values:  
A=2 C=1 S=10  
B=3 D=4 G=0

→ Path: S B G



Another  
Ex

Arad → Bucharest



\* Properties of Greedy Best-First Search

\* Complete? No

↳ Can get stuck in loops

\* Time?  $O(b^m)$  ( $m$ : max depth,  $b$ : branching factor)  
↳ Good heuristic can improve

\* Space?  $O(b^m)$

\* Optimal? No

↳ Can get stuck in infinite path

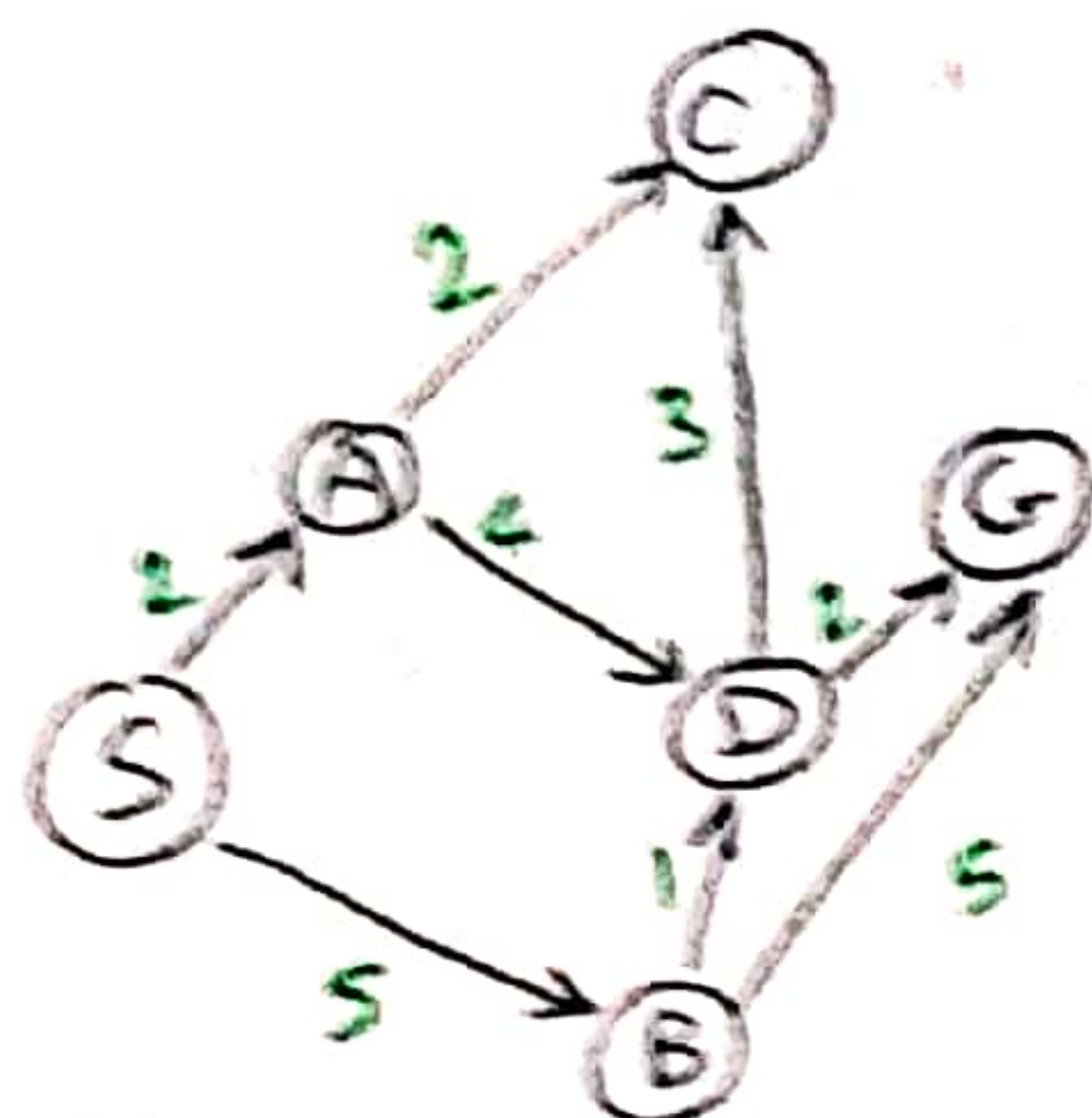
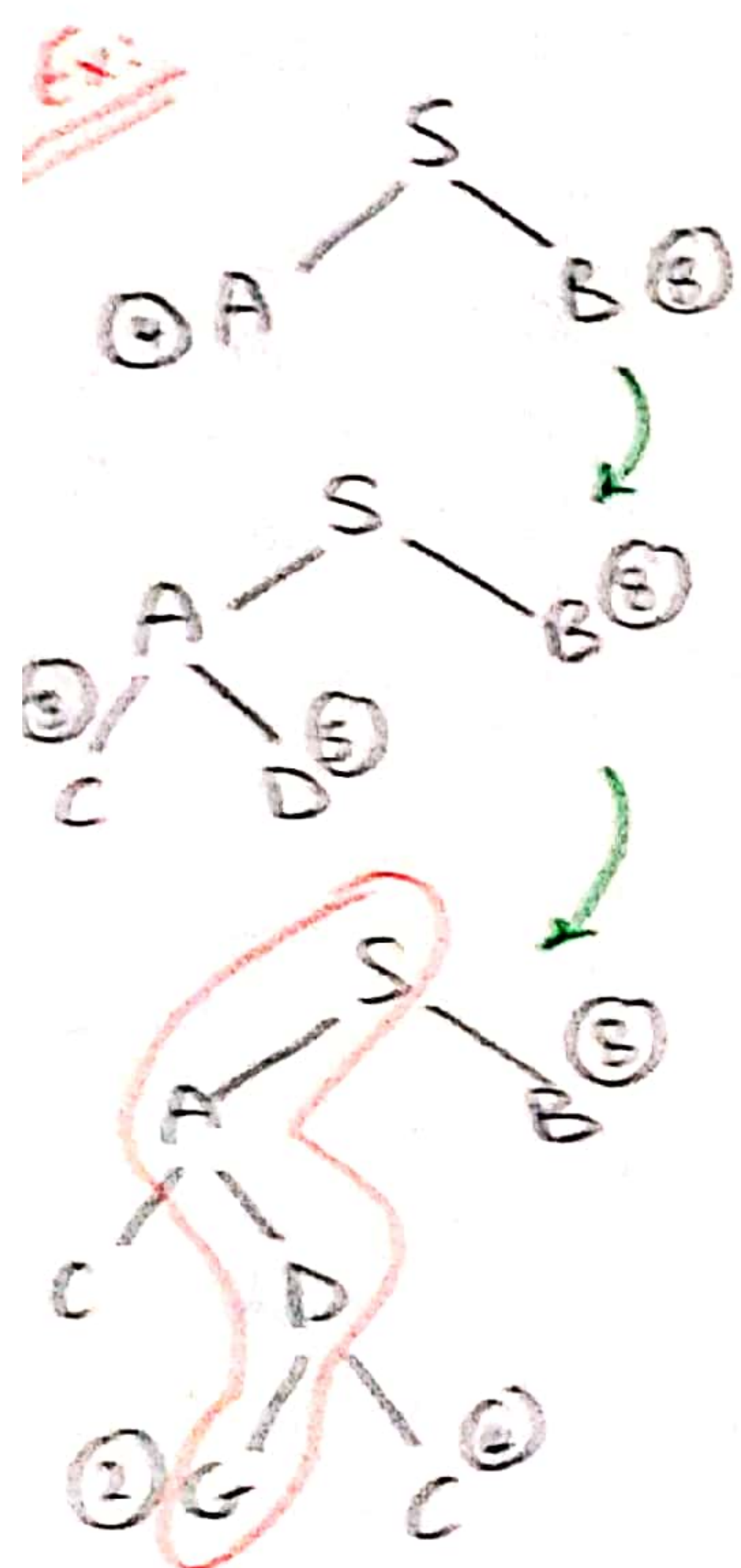
↓  
never return to try  
other possibilities



# A\* Search

$$f(n) = g(n) + h(n)$$

↓ Evaluation function      ↓ Real cost      ↓ Estimated cost (heuristic)



Heuristics  
 A=2 C=1 S=0  
 B=3 D=1 G=0

## Properties:

- \* Complete? yes
- \* Time? Exponential
- \* Space? keeps all nodes in the memory
- \* Optimal? yes

## Admissible heuristic

$$h(n) \leq h^*(n) \rightarrow \text{true cost}$$

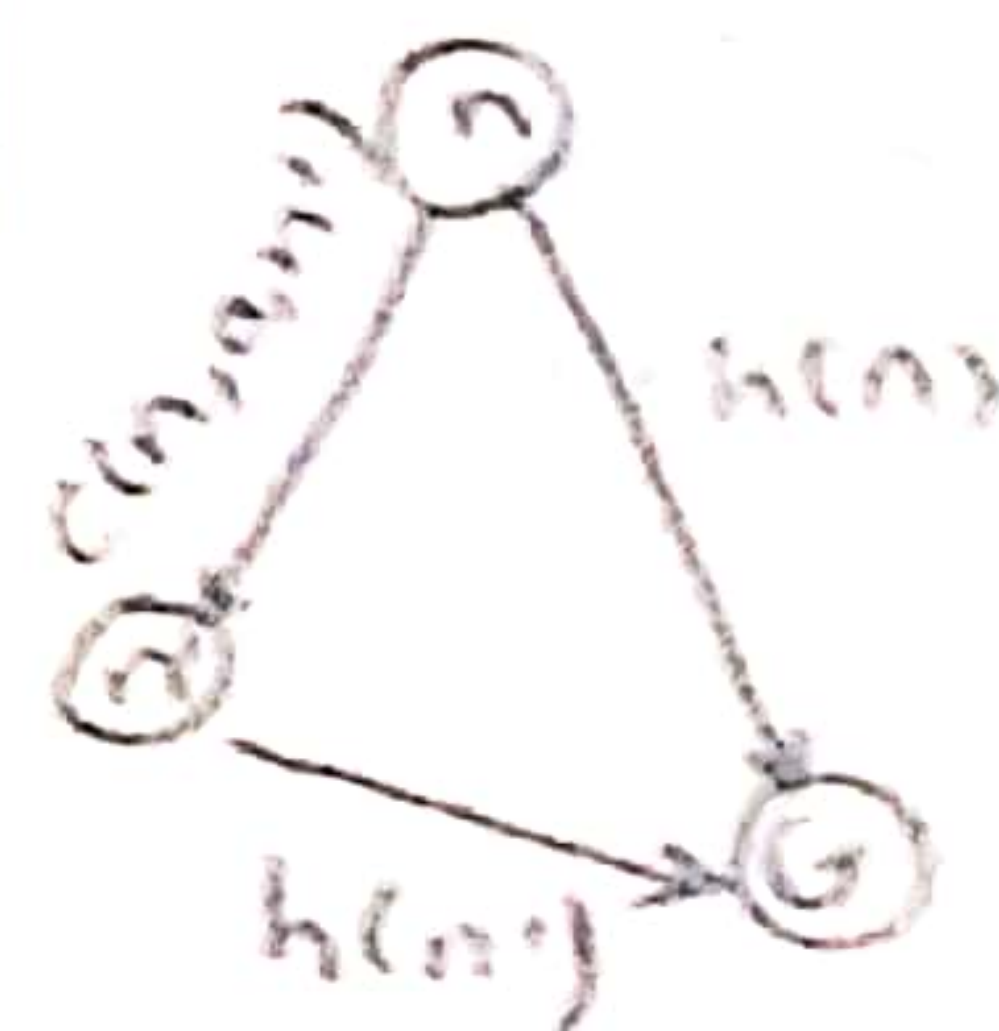
Theorem: If  $h(n)$  is admissible  
 → A\* using Tree-Search is optimal

(stricter than admissibility)

## Consistent Heuristics

$$h(n) \leq c(n, a, n') + h(n')$$

Theorem: If  $h(n)$  is consistent  
 → A\* using Graph-Search is optimal



Note: Uniform cost with admissible estimate is A\* Search



AL/CH5

### \* Dominance:

$$h_2(n) \geq h_1(n) \quad \forall n$$

↓  
 $h_2$  dominates  $h_1$

### \* Relaxed Problem

(Same problem,  
fewer restrictions)

Fewer  
restrictions on  
actions

Cost of optimal sol. of  
relaxed problem is an  
admissible heuristic to  
the original problem

Kısacası: heuristic'leri üretmek için  
kullanılan bir yaklaşımdır.



AI 10116

# Local Search Algorithms

Used when the path to goal doesn't matter

Keeps just one current (or few) state in the memory

Good for problems have large number of states

## General Approach:

- 1- Generate solution
- 2- Test it
- 3- Quit or return to 1

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## \*Hill Climbing Search (HC)

Moves in the direction of increasing value

Terminates when it reaches a peak

## \*Stochastic HC

Generates successors randomly until one better than current

## Disadvantages

Local maximum

Plateau

## Solutions

Moving in several directions

Backtracking

Big jumps

## \*Random Restart HC

Generate start states randomly

Proceed with hill climbing

Scanned by CamScanner



## AF) CH6 \* Simulated Annealing Search (SA)

Escaping local maxima by bad moves, then gradually decrease their frequency

Move bad enough to escape local maxima but not bad enough to escape the global

Temperature  $T$ :

$T \rightarrow 0$  Hill Climbing

$T \rightarrow \infty$  Random walk

## \* Local Beam Search

keeps track of  $K$  state (instead of 1);

starts with  $K$  randomly generated states

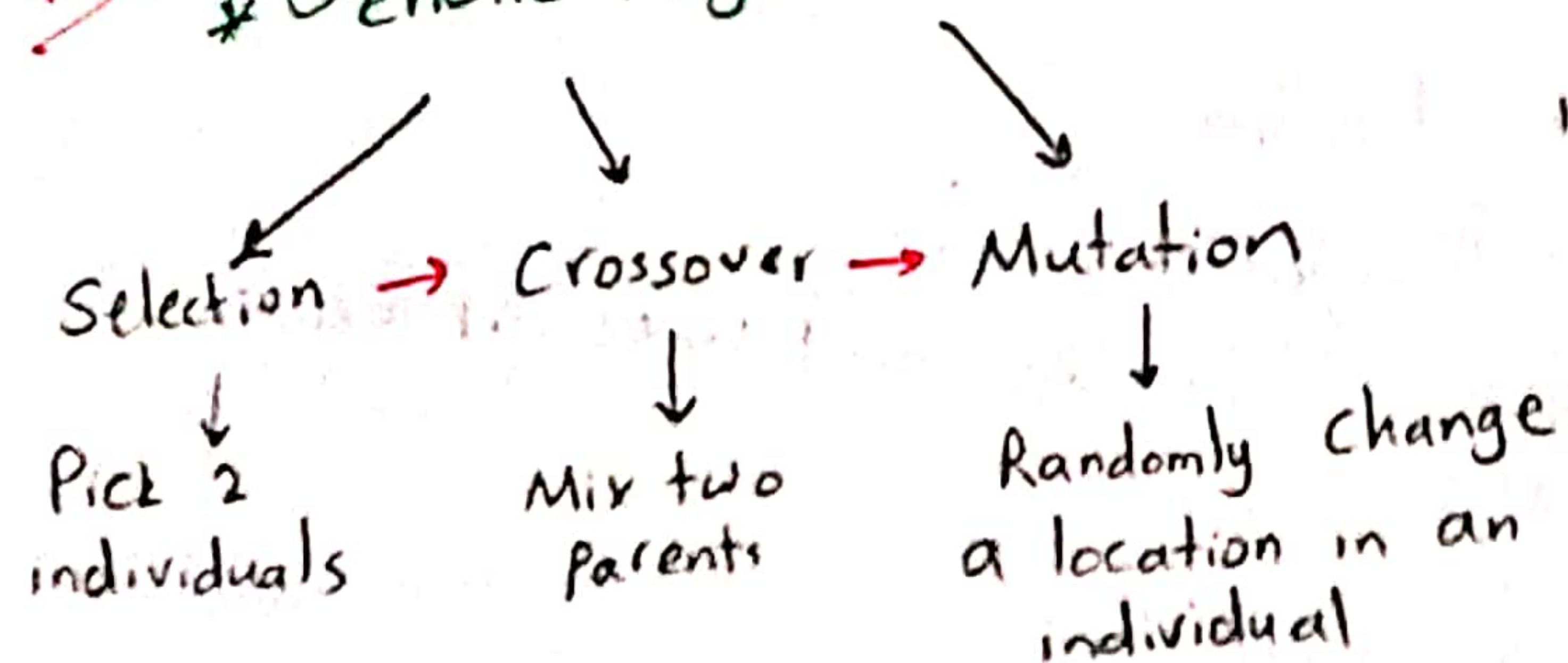
generates all successors of all  $K$  states (at each iteration)

goal state?   
 yes  $\rightarrow$  stop   
 no  $\rightarrow$  select  $K$  best successors and repeat



# AI / CH6

## \* Genetic Algorithms



Ex:  $\pi_i = abcdef$

$$\pi_1 = \begin{matrix} a & b & c & d & e & f \\ 4 & 3 & 5 & 2 & 1 & 6 \end{matrix}$$

$$\pi_2 = 173965$$

$$\pi_3 = 248012$$

$$\pi_4 = 908123$$

$$f(\pi) = (a+c+e) - (b+d+f)$$

① Sorting the chromosomes by their fitness

$$f(\pi_1) = 10 - 11 = -1$$

$$f(\pi_2) = 10 - 21 = -11$$

$$f(\pi_3) = 11 - 6 = 5$$

$$f(\pi_4) = 19 - 4 = 15$$

$$\pi_4 \rightarrow \pi_3 \rightarrow \pi_1 \rightarrow \pi_2$$

2. Crossover

$\pi_3, \pi_4 \rightarrow$  middle

$\pi_3, \pi_1 \rightarrow$  two point (2,4)

$$\text{off}_1 = 248123$$

$$\text{off}_2 = 908012$$

$$\text{off}_3 = 438016$$

$$\text{off}_4 = 245212$$

3. fitness of offspring

$$f(\text{off}_1) = 12 - 8 = 4$$

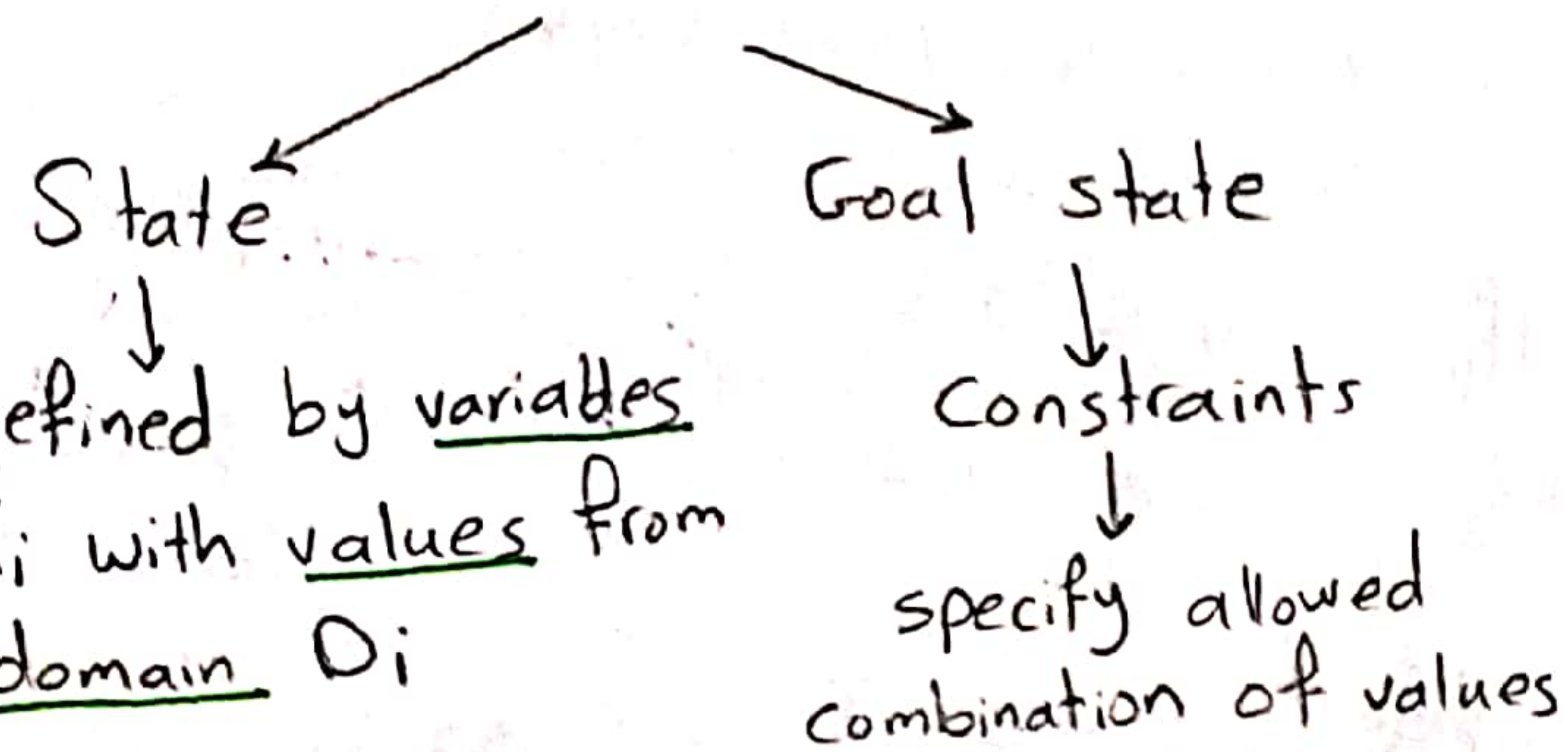
$$f(\text{off}_2) = 18 - 2 = 16$$

$$f(\text{off}_3) = 13 - 9 = 4$$

$$f(\text{off}_4) = 8 - 8 = 0$$



## Constraint Satisfaction Problems (CSP)



**Consistent assignment:** does not violate any constraint

**Complete assignment:** Every variable is mentioned

**Solution:** Complete assignment that satisfies all the constraints

↳ for some problems:  
+ maximizing an objective function

**Binary CSP:** Each constraint relates two variables

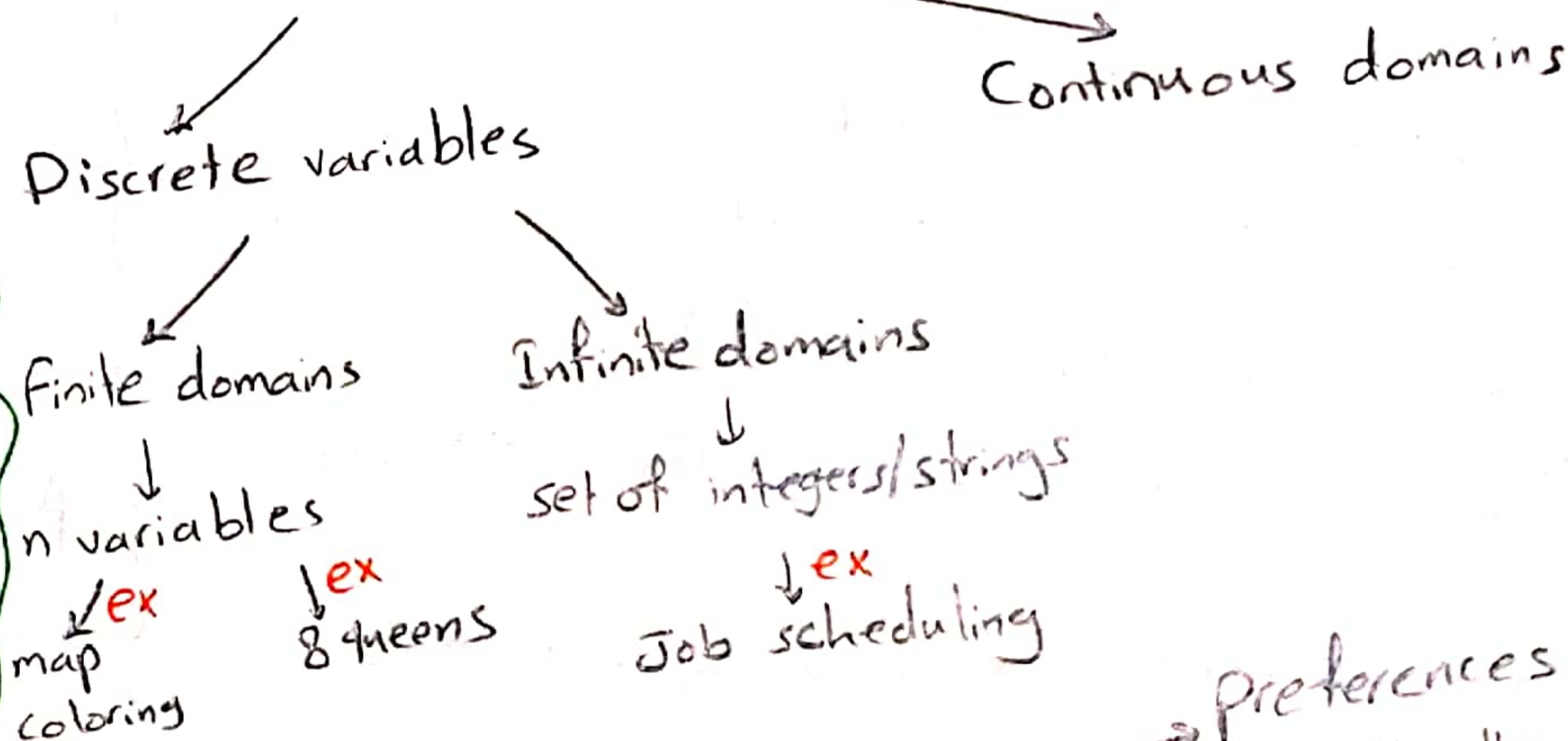
## For Map-Coloring Problem:

Variables: Set of cities

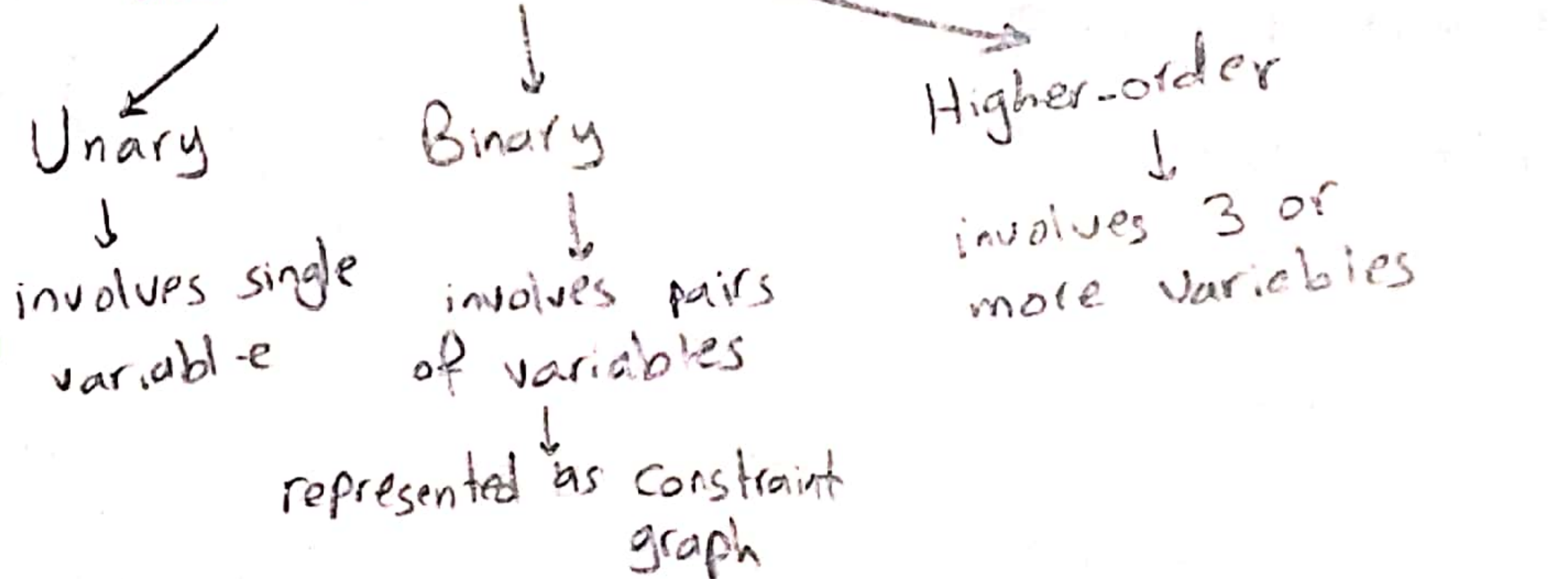
Domains: Set of colors

Constraints: Adjacent regions must have different colors

## Varieties of CSPs:



## Varieties of Constraints





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## \* Backtracking Search

→ Depth first search  
with single var. assignment

← Cumulative  
WA = R, NT = G

same ↓  
NT = G, WA = R

↓  
Assigns single variable  
at each node

## \* Most Constraint Variable

↙ To select the next  
unassigned variable

↓  
Chooses the variable  
with fewest legal  
values

## \* Minimum Remaining Values

↙ Picks variable that  
is most likely to  
cause a failure soon

↓  
stricter than  
MCV

## \* Least Constraining Value

↓  
Chooses values that give maximum  
flexibility to other variables

## \* Degree Heuristic

↓  
Aims to reduce the branching factor  
by selecting variable with largest number  
of constraints

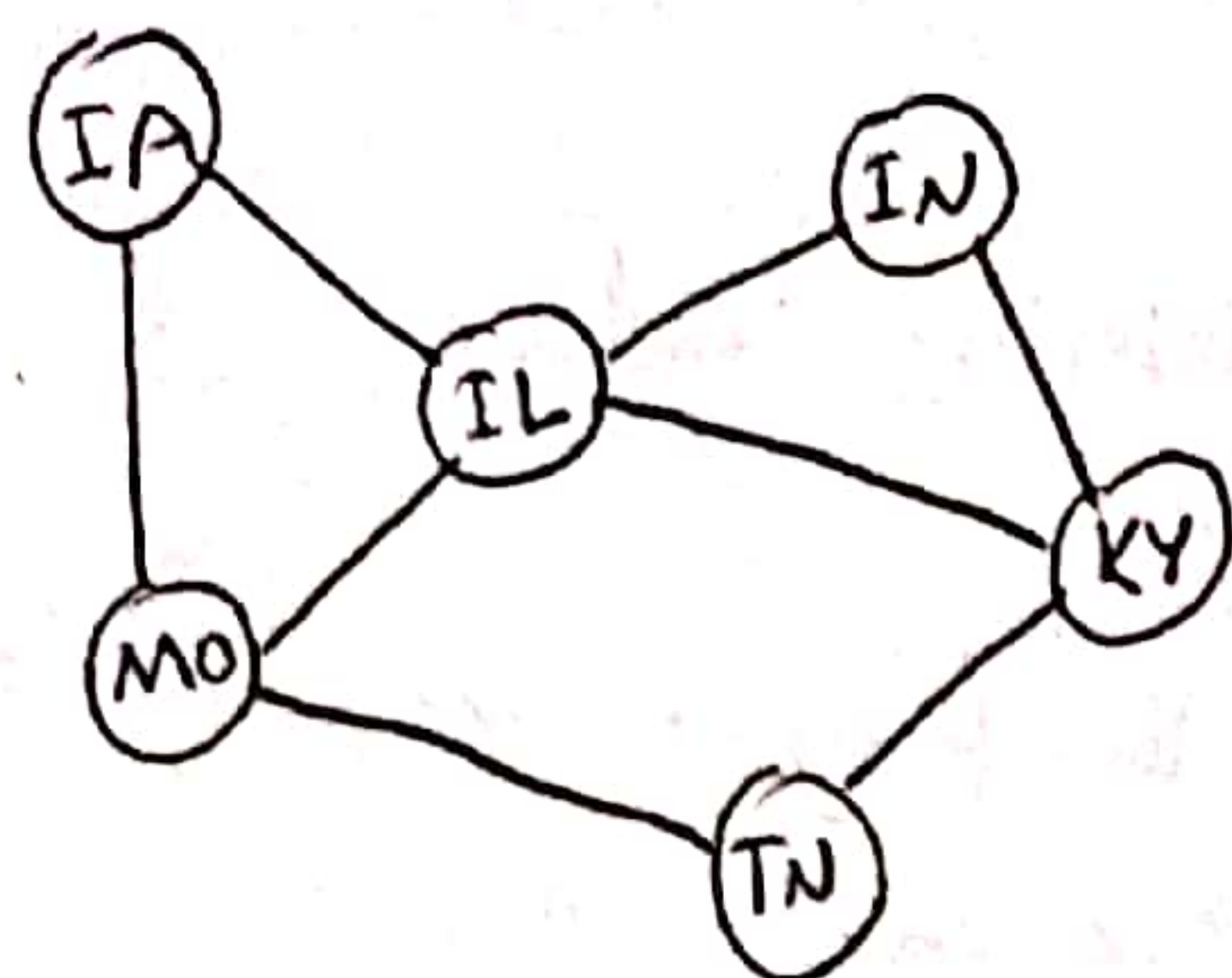
## \* Min - Conflicts Heuristic

↙ Illegal assignment

↘ Chooses value that  
violates the fewest  
constraints



a)



Forward checking

b)

TN	IN	IA	IL	MO	KY
R	RGB	RGB	RGB	<del>RGB</del>	<del>RGB</del>

Arc-consistency

c)

TN	IN	IA	IL	MO	KY
R	RGB	<del>RGB</del>	<del>RGB</del>	G	<del>RGB</del>

(?)

d) MRV: IL, MO

e) DH: IL

f) IA = R



AI / CH8

# Game

Each agent tries to alter the state to benefit itself

two or more agents

Each agent has their own interests

## Types

zero-sum (competitive)

cooperative

## \* Min-Max Algorithm

Depth-first

### Properties

Complete

Optimal

Time

$O(b^m)$

Space

$O(bm)$

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