

## Data Communication:

### Thermal Noise: "White noise"

The amount of thermal noise to be found in bandwidth of 1 Hz in any device:  $N_0 = K \cdot T \text{ (W/Hz)}$

where:

$N_0$ : noise power density in watts per 1 of bw

$K$ : Boltzmann's constant =  $1.38 \times 10^{-23} \text{ J/K}$

$T$ : Temperature in Kelvins

Thermal noise in watts percent in a bw of B Hz

$$N = K \cdot T \cdot B$$

### decible Notation:

$$\begin{aligned} N &= 10 \log k + 10 \log T + 10 \log B \\ &= -228.6 \text{ dBW} + 10 \log T + 10 \log B \end{aligned}$$

Ex: Given a receiver with an effective noise temperature of 294K and a 10 MHz bw, the thermal noise at receiver output?

$$\begin{aligned} \text{Sol: } N &= 10 \log k + 10 \log T + 10 \log B \\ &= -228.6 \text{ dBW} + 10 \log(294) + 10 \log(10^7) \\ &= -228.6 \text{ dBW} + 24.7 + 70 = -133.9 \text{ dBW} \end{aligned}$$

### \* Nyquist Bandwidth:

# Data rate is simply limited by bw  
A if the rate of signal transmission is  $2B$ , then a signal with frequency no greater than  $B$  is sufficient to carry the signal rate

or Given a bw of  $B$ , the highest signal rate that can be carried is  $2B$

Note: channel is error free

Ex: Room temperature is  $17^\circ\text{C}$

$$\begin{aligned} N_0 &= K \cdot T = 1.38 \times 10^{-23} \times 290 \\ &= 4 \times 10^{-21} \text{ W/Hz} \\ &= -204 \text{ dBW/Hz} \end{aligned}$$

if the signals are experiences in two no huge levels the rate can be supported by BHZ is 2B bps

### Nyquist to Multilevel signaling:

$$C = 2B \log_2 M$$

where

M: the number of discrete signal or voltage levels

Ex: Consider a voice channel used via modem to transmit digital data. Assume a bw of 3100 Hz

$$\begin{aligned} \text{Nyq. } C &= 2B \log_2 M \quad (M=8) \text{ örnek} \\ &= 2 \cdot 3100 \log_2 8 = 18600 \text{ bps} \end{aligned}$$

### SHANNON CAPACITY:

channel is not error free

For a given level of noise, we would expect that a precents signal strength would improve the ability to receive data correctly in present of signal - to - noise

Signal - to - noise Ratio (SNR) (S/N)

\* The ratio of power in a signal to the power contained in the noise in any particular point of transmission

Type Measured at receiver:

$$\text{SNR}_{dB} = 10 \log_{10} \frac{\text{Signal power}}{\text{Noise power}} \quad \text{Ratio}$$

Note A high SNR will mean high - quality signal and a low number of required intermediate repeaters

### Shannon's Maximum channel capacity:

$$C = B \cdot \log_2 (1 + \text{SNR})$$

C: bps

B: HZ

Ex: Suppose that the spectrum of a channel is between 3MHz and 4MHz, SNR = 24dB

$$\text{sol: } B = 4 - 3 = 1 \text{ MHz}$$

$$\text{SNR}_{dB} = 24 \text{ dB}$$

we have:

$$\text{SNR}_{dB} = 10 \log_{10} (\text{SNR})$$

$$24 = 10 \log_{10} (\text{SNR})$$

$$\text{SNR} = 251$$

$$C = B \log_2 (1 + \text{SNR})$$

$$= 1 \times \log_2 (1 + 251)$$

$$= 1 \times \log_2 (252)$$

$$\approx 8 \text{ Mbps}$$

Ödev1:

Consider a channel with a 1 MHz capacity and SNR of 63, what is the upper limit of the data rate of this channel?

Sol:

$$C = B \times \log_2(1 + \text{SNR})$$

$$= 1 \times \log_2(1 + 63)$$

$$= 1 \times \log_2(64) = 6 \text{ Mbps}$$

Ödev2:

A digital signaling system is required to operate at 9600 bps if a signal element is encoding a 4-bit word.

What is the maximum required bw of the channel?

Sol:

$$M = 4\text{-bit}, C = 9600 \text{ bps}$$

$$C = 2B \log_2 M$$

$$9600 = 2B \cdot \log_2 4$$

$$4 \times B = 9600$$

$$B = 2400 \text{ Hz}$$

Ödev2:

Given a channel with intended capacity of 20 Mbps, the bw of the channel is 3 MHz. What signal to noise ratio is required to achieve this capacity?

Sol:  $C = 20 \text{ Mbps}$

$$B = 3 \text{ MHz}$$

we have:  $C = B \times \log_2(1 + \text{SNR})$

$$20 = 3 \times \log_2(1 + \text{SNR})$$

$$1 + \text{SNR} = 101 \Rightarrow \text{SNR} = 100$$

Kişisel Gözümdür!

hocanın Gözü mü değildir



### Data Communication:

## Effective Area of an isotropic Antenna:

$$A_e = \frac{\lambda^2}{4\pi} \text{ with a power gain of } 1$$

**Exy** For a parabolic reflective antenna with a diameter of 2m operating at 12GHz. What are  $A_e$  and  $G$ ?

**Sol:**  $2r = 2m \Rightarrow r = 1m$

$$f = 12 \text{ GHz} = 12 \times 10^9 \text{ Hz}$$

$$\lambda = c/f = \frac{3 \times 10^8}{12 \times 10^9} = 0.025 \text{ m}$$

$$A = \pi r^2 = \pi (1)^2 = \pi$$

$$A_e = 0.5 A$$

$$= 0.5(\pi) = 0.5\pi$$

$$G = \frac{7A}{\lambda^2} = \frac{7\pi}{(0.025)^2} = 35.186$$

$$G_{dB} = 10 \log G = 10 \log (35.186)$$

$$= 45.46 \text{ dB}$$

## Effective Area of a parabolic reflective with face area of A

$$A_e = 0.5 A$$

$$\text{Power gain is } \frac{7A}{\lambda^2}$$

## Summary

Type	$A_e$	Power gain
Isotropic	$\lambda^2/4\pi$	1
Parabolic faces area A	$0.56 A$	$7A/\lambda^2$
Infinitesimal	$1.5 \lambda^2/4\pi$	1.5
Half wave dipole	$1.64 \lambda^2/4\pi$	1.64
Horn/Mouth area of A	$0.81 A$	$10A/\lambda^2$
Turnstile	$1.15 \lambda^2/4\pi$	1.15

## Data Communication:

### Optical LOS:

The term optical line of sight refers to the straight line propagation of light waves

$$d = 3.57 \sqrt{h}$$

$\downarrow$  km                       $\downarrow$  m

### Radio LOS:

The term radio line of sight or effective LOS, refers to propagation of radio waves bent by curves of earth

$$d = 3.57 \sqrt{k \cdot h}$$

where:

k: is an adjustment factor to account

$$k = 4/3$$

\* Maximum distance btw two antenna for LOS propagation:

$$d = 3.57(\sqrt{k \cdot h_1} + \sqrt{k \cdot h_2})$$

where:

$h_1, h_2$  are the highest of two antenna

Ex: a) what is the maximum distance btw two antenna, if one antenna is 100m high and the other is at ground level?

$$h_1 = 100 \text{ m}$$

$$\text{ground level } (h_2) = 0 \text{ m}$$

$$d = 3.57(\sqrt{k \cdot h_1} + \sqrt{k \cdot h_2})$$

$$= 3.57(\sqrt{\frac{4}{3} \cdot 100} + \sqrt{\frac{4}{3} \cdot 0})$$

$$= 41 \text{ km}$$

b): Now suppose that the receiving antenna is 10m high. To achieve the same distance, how high must the transmitting antenna be?

Sol:

$$\text{We have } d = 41 \text{ km}$$

$$d = 3.57(\sqrt{k \cdot h_1} + \sqrt{k \cdot h_2})$$

$$41 = 3.57(\sqrt{\frac{4}{3} \cdot h_1} + \sqrt{\frac{4}{3} \cdot 10})$$

$$41 = 3.57(\sqrt{\frac{4}{3} \cdot h_1} + \sqrt{13.3}) \Rightarrow$$

$$h_1 = 46.2 \text{ m}$$

Free Space: is same attenuation in guided and unguided media

Free Space Loss: for other types of antennas

$$\frac{P_t}{P_r} = \frac{(4\pi)^2 \cdot d^2}{G_t \cdot G_r \cdot \lambda^2} = \frac{(\lambda d)^2}{A_t \cdot A_r} = \frac{(c \cdot d)^2}{f^2 \cdot A_t \cdot A_r}$$

where:

$G_t$ : gain of transmit antenna

$\lambda$ : carrier wavelength

$d$ : propagation distance btw antennas

$c$ : speed of light ( $3 \times 10^8 \text{ m/s}$ )

$A_r$ : Ae of receiving antenna

$$L_{dB} = 20 \log(f) + 20 \log(d) - 169.54 \text{ dB}$$

$$L_{dB} = 20 \log(f) + 20 \log(d) - 10 \log(A_t A_r)$$

$$= -20 \log(f) + 20 \log(d) - 10 \log(A_t A_r) +$$

$$+ 169.54 \text{ dB}$$