

**DISCRETE MATHEMATICS MIDTERM EXAM**

1) (30pts) Prove that  $n < n+1$  with any proof method for all positive integers  $n$ .

2) (30pts) There is a Boolean expression given below.

- a) Draw the logic gates figure of the expression.
- b) Simplify the expression.
- c) Draw the logic gates figure of the simplified expression.

$$xyz + xy\bar{z} + xy + xyz + \bar{x}yz$$

3) (40 pts) Prove that  $1 \cdot 2 + 2 \cdot 3 + \dots + n(n+1) = n(n+1)(n+2)/3$  for all positive integers  $n$ .

You have 60 minutes, good luck