Tempest

For Manual/Intelligence

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Standard Code Library

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Chapter 1

数论算法

1.1 $O(m^2 \log n)$ 求线性递推数列第 n 项

```
已知 a_0, a_1, ..., a_{m-1}
    a_n = c_0 * a_{n-m} + \dots + c_{m-1} * a_{n-1}
    求 a_n = v_0 * a_0 + v_1 * a_1 + \dots + v_{m-1} * a_{m-1}
   void linear_recurrence(long long n, int m, int a[], int c[], int p) {
1
2
        long long v[M] = \{1 \% p\}, u[M << 1], msk = !!n;
 3
        for(long long i(n); i > 1; i >>= 1) {
 4
             msk <<= 1;
 5
        for(long long x(0); msk; msk >>= 1, x <<= 1) {
 6
 7
             fill n(u, m << 1, 0);
8
             int b(!!(n & msk));
9
             x = b;
10
             if(x < m) {
11
                 u[x] = 1 % p;
12
13
                 for(int i(0); i < m; i++) {</pre>
                      for(int j(0), t(i + b); j < m; j++, t++) {</pre>
14
15
                           u[t] = (u[t] + v[i] * v[j]) % p;
16
                      }
17
                 for(int i((m << 1) - 1); i >= m; i--) {
18
19
                      for(int j(0), t(i - m); j < m; j++, t++) {
20
                           u[t] = (u[t] + c[j] * u[i]) % p;
21
22
                 }
23
             }
24
             copy(u, u + m, v);
25
        //a[n] = v[0] * a[0] + v[1] * a[1] + ... + v[m-1] * a[m-1].
26
27
        for(int i(m); i < 2 * m; i++) {</pre>
```

```
28
             a[i] = 0;
29
             for(int j(0); j < m; j++) {
30
                 a[i] = (a[i] + (long long)c[j] * a[i + j - m]) % p;
31
             }
32
33
        for(int j(0); j < m; j++) {</pre>
34
             b[j] = 0;
35
             for(int i(0); i < m; i++) {</pre>
36
                 b[j] = (b[j] + v[i] * a[i + j]) % p;
37
38
39
        for(int j(0); j < m; j++) {</pre>
40
             a[j] = b[j];
41
        }
42
   }
```

1.2 NTT

```
1 const int modulo(786433);
   const int G(10);//原根
 3
   int pw[999999];
 4
   void FFT(int P[], int n, int oper) {
 5
        for(int i(1), j(0); i < n - 1; i++) {
 6
            for(int s(n); j ^= s >>= 1, ~j & s;);
 7
            if (i < j)
 8
                swap(P[i], P[j]);
 9
10
        int unit p0;
11
        for(int d(0); (1 << d) < n; d++) {</pre>
12
            int m(1 \ll d), m2(m * 2);
13
            unit_p0 = oper == 1?pw[(modulo - 1) / m2]:pw[modulo - 1 - (modulo - 1) / m2];
14
            for(int i = 0; i < n; i += m2) {</pre>
15
                int unit(1);
16
                for(int j(0); j < m; j++) {</pre>
                     int &P1 = P[i + j + m], &P2 = P[i + j];
17
                     int t = (long long)unit * P1 % modulo;
18
19
                    P1 = (P2 - t + modulo) % modulo;
20
                    P2 = (P2 + t) % modulo;
21
                     unit = (long long)unit * unit_p0 % modulo;
22
                }
23
            }
24
        }
25
   }
26
27
   int nn;
28
   int A[N], B[N], C[N];
   //A * B = C;
29
30
   //len = nn
```

1.3. 中国剩余定理 9

```
31 void multiply() {
32
        FFT(A, nn, 1);
33
        FFT(B, nn, 1);
34
        for(int i(0); i < nn; i++) {</pre>
            C[i] = (long long)A[i] * B[i] % modulo;
35
36
37
        FFT(C, nn, -1);
38 }
39
40 int main() {
41
        pw[0] = 1;
42
        for(int i(1); i < modulo; i++) {</pre>
            pw[i] = (long long)pw[i - 1] * G % modulo;
43
44
45 }
```

1.3 中国剩余定理

包括扩展欧几里得, 求逆元, 和保证除数互质条件下的 CRT

```
1 LL x, y;
 2 void exGcd(LL a, LL b)
3
   {
4
        if (b == 0) {
5
            x = 1;
 6
            y = 0;
7
            return;
8
        exGcd(b, a % b);
9
       LL k = y;
10
11
        y = x - a / b * y;
12
        x = k;
13 }
14
15 LL inversion(LL a, LL b)
16 {
17
        exGcd(a, b);
18
        return (x % b + b) % b;
19 }
20
21 LL CRT(vector<LL> m, vector<LL> a)
22 {
23
        int N = m.size();
24
        LL M = 1, ret = 0;
        for(int i = 0; i < N; ++ i)</pre>
25
26
            M *= m[i];
27
        for(int i = 0; i < N; ++ i) {</pre>
28
            ret = (ret + (M / m[i]) * a[i] % M * inversion(M / m[i], m[i])) % M;
29
```

```
30  }
31  return ret;
32 }
```

1.4 中国剩余定理 (可不互质)

```
namespace number_theory_basic {
        inline void euclid(const long long &a, const long long &b, long long &x, long
           long &y) {
 3
            if (b == 0) {
                x = 1;
 4
 5
                y = 0;
 6
            } else {
 7
                euclid(b, a % b, x, y);
                x = a / b * y;
 8
 9
                swap(x, y);
10
            }
11
        }
12
13
   namespace chinese_remainder_theorem {
        inline bool crt(int n, long long r[], long long m[], long long &remainder, long
14
           long &modular) {
            remainder = modular = 1;
15
16
            for (int i = 1; i <= n; ++i) {</pre>
                long long x, y;
17
18
                euclid(modular, m[i], x, y);
19
                long long divisor = gcd(modular, m[i]);
20
                if ((r[i] - remainder) % divisor) {
21
                    return false;
22
23
                x *= (r[i] - remainder) / divisor;
24
                remainder += modular * x;
25
                modular *= m[i] / divisor;
26
                ((remainder %= modular) += modular) %= modular;
27
28
            return true;
29
        }
30
   }
```

1.5 Miller Rabin

miller_rabin_32 是针对 32 位以下整数的; miller_rabin_64 是针对 64 位以下整数的. 直接调用 prime() 函数, 当返回值是 true 时表示是素数, 否则不是质数.

```
namespace miller_rabin_32 {
   int const n = 3;
   int const base[] = {2, 7, 61};
```

1.5. MILLER RABIN

```
4
 5
        inline long long power(int x, int k, int p) {
 6
            long long ans = 1, num = x % p;
            for (int i = k; i > 0; i >>= 1) {
7
                 if (i & 1) {
8
9
                     (ans *= num) %= p;
10
11
                 (num *= num) %= p;
12
13
            return ans;
14
        }
15
16
        inline bool check(int p, int base) {
17
            int n = p - 1;
18
            while (!(n & 1)) {
                 n >>= 1;
19
20
21
            long long m = power(base, n, p);
            while (n != p - 1 \&\& m != 1 \&\& m != p - 1) {
22
23
                 (m *= m) %= p;
                 n <<= 1;
24
25
26
            return m == p - 1 \mid \mid (n \& 1) == 1);
27
        }
28
29
        inline bool prime(int p) {
30
            for (int i = 0; i < n; ++i) {</pre>
31
                 if (base[i] == p) {
32
                     return true;
33
                 }
34
35
            if (p == 1 | | !(p \& 1)) {
36
                 return false;
37
38
            for (int i = 0; i < n; ++i) {</pre>
                 if (!check(p, base[i])) {
39
40
                     return false;
41
                 }
42
43
            return true;
44
        }
45 }
46
   namespace miller rabin 64 {
47
48
        int const n = 9;
49
        int const base[] = {2, 3, 5, 7, 11, 13, 17, 19, 23};
50
51
        inline long long multiply(const long long &x, const long long &y, const long long
             &p) {
```

```
52
            long long ans = 0, num = x % p;
53
            for (long long i = y; i > 0; i >>= 1) {
                if (i & 1) {
54
55
                     (ans += num) %= p;
56
57
                 (num += num) %= p;
58
59
            return ans;
60
        }
61
62
        inline long long power(const long long &x, const long long &k, const long long &p
63
            long long ans = 1, num = x % p;
64
            for (long long i = k; i > 0; i >>= 1) {
65
                if (i & 1) {
66
                     ans = multiply(ans, num, p);
67
68
                num = multiply(num, num, p);
69
70
            return ans;
71
        }
72
73
        inline bool check(const long long &p, const long long &base) {
74
            long long n = p - 1;
75
            while (!(n & 1)) {
76
                n >>= 1;
77
78
            long long m = power(base, n, p);
79
            while (n != p - 1 \&\& m != 1 \&\& m != p - 1) {
80
                m = multiply(m, m, p);
81
                n <<= 1;
82
83
            return m == p - 1 \mid \mid (n \& 1) == 1;
84
        }
85
        inline bool prime(const long long &p) {
86
87
            for (int i = 0; i < n; ++i) {</pre>
88
                if (base[i] == p) {
89
                     return true;
90
91
            if (p == 1 | | !(p \& 1)) {
92
93
                return false;
94
            for (int i = 0; i < n; ++i) {</pre>
95
96
                 if (!check(p, base[i])) {
97
                     return false;
98
                }
99
            }
```

1.6. POLLARD RHO

1.6 Pollard Rho

```
模板需要配合miller\ rabin一起使用.
   调用factor()函数, 会返回vector<long long>, 表示分解结果. (例如分解12, 会返回2, 2和3)
 2
3
   namespace pollard_rho {
 4
       //可以改成LL*LL%LL的形式
5
       inline long long multiply(const long long &x, const long long &y, const long long
            } (q&
 6
           long long ans = 0, num = x % p;
 7
           for (long long i = y; i > 0; i >>= 1) {
8
               if (i & 1) {
9
                   (ans += num) %= p;
10
11
               (num += num) %= p;
12
           }
13
           return ans;
14
15
       inline long long gcd(long long x, long long y) {
16
17
           while (y > 0) {
18
               x %= y;
19
               swap(x, y);
20
21
           return x;
22
       }
23
24
       inline long long pollard_rho(const long long &n, const long long &c) {
25
           long long x = rand() % (n - 1) + 1, y = x;
           int head = 1, tail = 2;
26
27
           while (true) {
28
               x = multiply(x, x, n);
               if ((x += c) >= n) {
29
30
                   x -= n;
31
32
               if (x == y) {
33
                   return n;
34
35
               long long d = gcd(abs(x - y), n);
36
               if (d > 1 \&\& d < n) {
37
                   return d;
38
39
               if ((++head) == tail) {
40
                   y = x;
```

```
41
                    tail <<= 1;
42
                }
43
            }
44
        }
45
46
        inline vector<long long> mergy(const vector<long long> &a, const vector<long long
           > &b) {
47
            vector<long long> vec;
48
            for (int i = 0; i < (int)a.size(); ++i) {</pre>
49
                vec.push_back(a[i]);
50
51
            for (int i = 0; i < (int)b.size(); ++i) {</pre>
52
                vec.push_back(b[i]);
53
            }
54
            return vec;
55
        }
56
57
        inline vector<long long> factor(const long long &n) {
58
            if (n <= 1) {
59
                return vector<long long>();
60
61
            if (miller rabin::prime(n)) {
62
                return vector<long long>(1, n);
63
64
            long long p = n;
65
            while (p \ge n) {
66
                p = pollard_rho(n, rand() % (n - 1) + 1);
67
            return mergy(factor(n / p), factor(p));
68
69
        }
70
   }
```

1.7 离散对数

```
1 #include <iostream>
 2 #include <cstdio>
   #include <cstdlib>
 4 #include <algorithm>
 5 #include <cmath>
 6 #include <map>
 7
   #include <cstring>
 8
 9
   using namespace std;
10
11 typedef long long int64;
12
   struct hash table {
13
       static const int MAXN = 100003;
```

1.7. 离散对数 15

```
15
        int first[MAXN], key[MAXN], value[MAXN], next[MAXN], tot;
16
        hash table() : tot(0) {
17
            memset(first, 255, sizeof first);
18
        void clear() {
19
20
            memset(first, 255, sizeof first);
21
            tot = 0;
22
23
        int &operator[] (const int &o) {
24
            int pos = o % MAXN;
25
            for (int i = first[pos]; i != -1; i = next[i])
26
                if (key[i] == 0)
27
                     return value[i];
28
            next[tot] = first[pos];
29
            first[pos] = tot;
30
            key[tot] = o;
31
            return value[tot++];
32
        bool has key(const int &o) {
33
34
            int pos = o % MAXN;
            for (int i = first[pos]; i != -1; i = next[i])
35
36
                if (key[i] == 0)
37
                     return true;
38
            return false;
39
        }
40 };
41
42
   int discrete_log(int base, int n, int mod) {
        int block = int(sqrt(mod)) + 1;
43
44
        int val = 1;
45
        hash_table dict;
46
        for (int i = 0; i < block; ++i) {</pre>
47
            if (dict.has key(val) == 0)
48
                dict[val] = i;
49
            val = (int64)val * base % mod;
50
51
        int inv = inverse(val, mod);
52
        val = 1;
53
        for (int i = 0; i < block; ++i) {</pre>
54
            if (dict.has key((int64)val * n % mod))
                return dict[(int64)val * n % mod] + i * block;
55
56
            val = (int64)val * inv % mod;
57
        }
58
        return -1;
59
   }
60
61
   int main() {
62
        int base, n, p;
63
        while (scanf("%d_{\square}%d_{\square}%d", &p, &base, &n) == 3) {
```

1.8 原根

```
int primitive_root(int p) {
 1
 2
        int n = p - 1;
 3
        while (true) {
 4
            int root = rand() % (p - 1) + 1, m = n;
 5
            bool found = true;
 6
            for (int i = 0; i < (int)prim.size(); ++i) {</pre>
 7
                int cur = prim[i];
 8
                if (m / cur < cur)</pre>
 9
                     break;
                if (m % cur == 0) {
10
11
                     if (pow_mod(root, n / cur, p) == 1) {
12
                         found = false;
13
                         break;
14
15
                     while (m % cur == 0)
                         m /= cur;
16
17
                }
18
19
            if (m > 1)
20
                if (pow_mod(root, n / m, p) == 1)
21
                     found = false;
22
            if (found)
23
                return root;
24
        }
25
   }
26
27
   vector<int> discrete_root(int expo, int n, int mod) {
28
        if (n == 0)
29
            return vector<int>(1, 0);
30
        int g = primitive root(mod);
31
        int e = discrete_log(g, n, mod);
32
        int64 u, v;
33
        int d = extend_euclid(expo, mod - 1, u, v);
34
        if (e % d != 0)
35
            return vector<int>();
36
        int64 delta = (mod - 1) / d;
37
        u = u * e / d % delta;
38
        if (u < 0)
```

1.9. 离散二次方根 17

1.9 离散二次方根

```
1 inline bool quad_resi(int x, int p) {
 2
        return pow_mod(x, (p-1) / 2, p) == 1;
3
   }
 4
5
   struct quad_poly {
 6
        int zero, one, val, mod;
7
8
        quad_poly(int zero, int one, int val, int mod) : zero(zero), one(one), val
9
                (val), mod(mod) {}
10
        quad_poly multiply(quad_poly o) {
11
12
            int z0 = (zero * o.zero + one * o.one % mod * val % mod) % mod;
13
            int z1 = (zero * o.one + one * o.zero) % mod;
14
            return quad poly(z0, z1, val, mod);
15
16
       quad_poly pow(int x) {
17
18
            if (x == 1)
19
                return *this;
20
            quad_poly ret = this->pow(x / 2);
21
            ret = ret.multiply(ret);
22
            if (x & 1)
23
                ret = ret.multiply(*this);
24
            return ret;
25
        }
26
   };
27
28 inline int calc(int a, int p) {
29
        a %= p;
30
        if (a < 2)
31
            return a;
32
        if (!quad_resi(a, p))
33
            return p;
                                 // no solution
34
        if (p % 4 == 3)
35
            return pow_mod(a, (p + 1) / 4, p);
        int b = 0;
36
37
       while (quad_resi((my_sqr(b) - a + p) % p, p))
```

1.10 牛顿迭代求平方根

```
//use \ newton-method to solve f(x) = 0
 1
 2 //init x0
 3 //xi -> x(i + 1) = xi - f(xi) / f'(xi)
 4 //O(N^2\log N)
 5 int64 square_root(int64 x) {
 6
        if (x \le 0)
 7
            return 0;
        int64 last_root = -1, root = 1 << (bit_length(x) / 2);
 8
 9
        while (true) {
10
            int64 next_root = (root + x / root) >> 1;
11
            if (next root == last root)
12
                return min(next root, root);
13
            last root = root;
14
            root = next root;
15
        }
16
   }
```

1.11 Pell 方程求根

```
x^2 - n * y^2 = 1
   pair<int64, int64> solve_pell64(int64 n) {
 2
        const static int MAXC = 111;
 3
        int64 p[MAXC], q[MAXC], a[MAXC], q[MAXC], h[MAXC];
 4
        p[1] = 1; p[0] = 0;
 5
        q[1] = 0; q[0] = 1;
 6
        a[2] = square_root(n);
 7
        g[1] = 0; h[1] = 1;
        for (int i = 2; ; ++i) {
 8
            g[i] = -g[i - 1] + a[i] * h[i - 1];
 9
            h[i] = (n - g[i] * g[i]) / h[i - 1];
10
11
            a[i + 1] = (g[i] + a[2]) / h[i];
12
            p[i] = a[i] * p[i - 1] + p[i - 2];
13
            q[i] = a[i] * q[i - 1] + q[i - 2];
14
            if (p[i] * p[i] - n * q[i] * q[i] == 1)
15
                return make pair(p[i], q[i]);
16
        }
17
   }
```

1.12. 直线下整点个数

19

1.12 直线下整点个数

```
\label{eq:continuity} \hat{\mathbb{R}} \ \sum_{i=0}^{n-1} \lfloor \frac{a+bi}{m} \rfloor \text{.} typedef long
```

```
1 typedef long long LL;
2
3 LL count(LL n, LL a, LL b, LL m) {
       if (b == 0) {
5
           return n * (a / m);
6
       if (a >= m) {
7
           return n * (a / m) + count(n, a % m, b, m);
9
       if (b >= m) {
10
           return (n - 1) * n / 2 * (b / m) + count(n, a, b % m, m);
11
12
13
       return count((a + b * n) / m, (a + b * n) % m, m, b);
14 }
```

Chapter 2

数值算法

2.1 FFT

```
1
   void FFT(Complex P[], int n, int oper) {
2
        for (int i(1), j(0); i < n - 1; i++) {
3
            for (int s(n); j ^= s >>= 1, ~j & s;);
 4
            if (i < j)
 5
                 swap(P[i], P[j]);
 6
7
        Complex unit p0;
 8
        for (int d(0); (1 << d) < n; d++) {
9
            int m(1 \ll d), m2(m * 2);
            double p0(pi / m * oper);
10
11
            unit p0.imag(sin(p0));
12
            unit_p0.real(cos(p0));
13
            for (int i(0); i < n; i += m2) {</pre>
14
                Complex unit = 1;
15
                 for (int j = 0; j < m; j++) {</pre>
16
                     Complex &P1 = P[i + j + m], &P2 = P[i + j];
17
                     Complex t = unit * P1;
18
                     P1 = P2 - t;
19
                     P2 = P2 + t;
20
                     unit = unit * unit_p0;
21
                }
22
            }
23
        }
24 }
25 void multiply() {
26
        FFT(a, n, 1);
27
        FFT(b, n, 1);
28
        for(int i(0); i < n; i++) {</pre>
29
            c[i] = a[i] * b[i];
30
31
        FFT(c, n, -1);
```

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```
32     for(int i(0); i < n; i++) {
33         ans[i] += (int)(c[i].real() / n + 0.5);
34     }
35 }</pre>
```

2.2 解一元三次方程 + 求三阶二次型的标准型

```
double sqr(const double & x) {
 2
       return x * x;
 3
   }
 4
   double eps(1e-8);
 5
   int main() {
 6
        double A, B, C, D, E, F;
 7
        for(;6 == scanf("%lf%lf%lf%lf%lf%lf%lf", &A, &B, &C, &D, &E, &F);) {
 8
            D /= 2; E /= 2; F /= 2;
 9
            complex < double > a(1), b(-A - B - C), c(A * B + B * C + C * A - sqr(D) - sqr(E)
               ) - sqr(F)), d(-A * B * C - 2 * D * E * F + A * sqr(D) + B * sqr(E) + C *
               sqr(F));
            complex<double> delta(pow(pow(b * c / 6. / a / a - b * b * b / 27. / a / a /
10
               a - d / 2. / a, 2) + pow(c / 3. / a - b * b / 9. / a / a, 3), 0.5));
            complex<double> p(pow(b * c / 6. / a / a - b * b * b / 27. / a / a - d /
11
               2. / a + delta, 1. / 3));
            complex<double> q(pow(b * c / 6. / a / a - b * b * b / 27. / a / a - d /
12
               2. / a - delta, 1. / 3));
13
            complex < double > omega1(-0.5, 0.5 * sqrt(3.)), omega2(-0.5, -0.5 * sqrt(3.));
            complex < double > x1(-b / 3. / a + p + q), x2(-b / 3. / a + omega1 * p + omega2
14
                * q), x3(-b / 3. / a + omega2 * p + omega1 * q);
15
            printf("%.10f\n", min(min(sqrt(1 / x1.real()), sqrt(1 / x2.real())), sqrt(1 /
                x3.real())));
16
        }
17
   }
```

2.3 高斯消元

```
1
   vector<double> operator* (const vector<double> &a, double b) {
 2
        vector<double> ret;
 3
        for (int i = 0; i < (int)a.size(); ++i)</pre>
 4
            ret.push_back(a[i] * b);
 5
        return ret;
 6
   }
 7
 8
   vector<double> operator+ (const vector<double> &a, const vector<double> &b) {
 9
        vector<double> ret;
10
        for (int i = 0; i < (int)a.size(); ++i)</pre>
11
            ret.push back(a[i] + b[i]);
12
        return ret;
```

2.3. 高斯消元 23

```
13 }
14
15 vector<double> operator- (const vector<double> &a, const vector<double> &b) {
        vector<double> ret;
        for (int i = 0; i < (int)a.size(); ++i)</pre>
17
18
            ret.push_back(a[i] - b[i]);
19
        return ret;
20 }
21
22 struct solution {
23
        int size, dimension;
24
        vector<vector<double> > null_space;
25
        vector<double> special;
26
        solution(int size = 0, int dimension = 0) : size(size), dimension(dimension)
27
            special = vector<double>(size, 0);
28
29
            null_space = vector<vector<double> >(size, vector<double>(dimension,
30
                     0));
31
        }
32
   };
33
34 solution gauss elimination(vector<vector<double> > a, vector<double> b) {
35
        int n = (int)a.size(), m = (int)a[0].size();
36
        static const int MAX SIZE = 211;
37
        int index[MAX SIZE], row = 0;
38
        bool pivot[MAX SIZE];
39
        fill(index, index + n, -1);
40
        fill(pivot, pivot + m, false);
41
42
        for (int col = 0; row < n && col < m; ++col) {</pre>
43
            int best = row;
44
            for (int i = row + 1; i < n; ++i)</pre>
45
                if (fabs(a[i][col]) > fabs(a[best][col]))
46
                    best = i;
47
            swap(a[best], a[row]);
48
            swap(b[best], b[row]);
49
            if (fabs(a[row][col]) < EPS)</pre>
50
                continue;
51
            pivot[col] = true;
52
            index[row] = col;
53
            double coef = a[row][col];
54
            a[row] = a[row] * (1. / coef);
            b[row] = b[row] * (1. / coef);
55
            for (int i = 0; i < n; ++i)
56
57
                if (i != row && fabs(a[i][col]) > EPS) {
58
                     double coef = a[i][col];
59
                    a[i] = a[i] - a[row] * coef;
60
                    b[i] = b[i] - b[row] * coef;
61
                }
```

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```
62
            ++row;
63
        }
64
65
        for (int i = row; i < n; ++i)</pre>
             if (fabs(b[i]) > EPS)
66
67
                 return solution(0, 0);
                                                              //no solution
68
69
        solution ret(m, m - row);
70
        for (int i = 0; i < row; ++i)</pre>
71
             ret.special[index[i]] = b[i];
72
73
        int cnt = 0;
74
        for (int i = 0; i < m; ++i)</pre>
             if (!pivot[i]) {
75
76
                 for (int j = 0; j < row; ++j)</pre>
77
                      ret.null_space[index[j]][cnt] = a[j][i];
78
                 ret.null_space[i][cnt++] = -1;
79
             }
80
        return ret;
81 }
```

2.4 最小二乘法

```
// calculate argmin ||AX - B||
   solution least_squares(vector<vector<double> > a, vector<double> b) {
 3
        int n = (int)a.size(), m = (int)a[0].size();
 4
        vector<vector<double> > p(m, vector<double>(m, 0));
 5
        vector<double> q(m, 0);
 6
        for (int i = 0; i < m; ++i)</pre>
 7
            for (int j = 0; j < m; ++j)</pre>
 8
                for (int k = 0; k < n; ++k)
 9
                    p[i][j] += a[k][i] * a[k][j];
10
        for (int i = 0; i < m; ++i)</pre>
11
            for (int j = 0; j < n; ++j)
12
                q[i] += a[j][i] * b[j];
13
        return gauss_elimination(p, q);
14 }
```

2.5 多项式求根

```
1 const double eps=1e-12;
2 double a[10][10];
3 typedef vector<double> vd;
4 int sgn(double x) { return x < -eps ? -1 : x > eps; }
5 double mypow(double x,int num) {
6 double ans=1.0;
```

2.5. 多项式求根 25

```
7
        for(int i=1;i<=num;++i)ans*=x;</pre>
8
        return ans;
9
   }
   double f(int n,double x){
10
11
        double ans=0;
12
        for(int i=n;i>=0;--i)ans+=a[n][i]*mypow(x,i);
13
        return ans;
14
15
   double getRoot(int n,double 1,double r){
16
        if(sqn(f(n,1))==0)return 1;
17
        if(sgn(f(n,r))==0)return r;
18
        double temp;
19
        if(sgn(f(n,1))>0)temp=-1;else temp=1;
20
        double m;
21
        for(int i=1;i<=10000;++i){</pre>
22
            m=(1+r)/2;
23
            double mid=f(n,m);
24
            if(sgn(mid)==0){
25
                 return m;
26
27
            if(mid*temp<0)l=m;else r=m;</pre>
28
29
        return (1+r)/2;
30 }
31 vd did(int n){
32
        vd ret;
33
        if(n==1){
34
            ret.push_back(-1e10);
35
            ret.push_back(-a[n][0]/a[n][1]);
36
            ret.push back(1e10);
37
            return ret;
38
        }
39
        vd mid=did(n-1);
        ret.push_back(-1e10);
40
        for(int i=0;i+1<mid.size();++i){</pre>
41
42
            int t1=sgn(f(n,mid[i])),t2=sgn(f(n,mid[i+1]));
43
            if(t1*t2>0)continue;
44
            ret.push_back(getRoot(n,mid[i],mid[i+1]));
45
        ret.push back(1e10);
46
47
        return ret;
48
   int main(){
49
50
        int n; scanf("%d",&n);
51
        for(int i=n;i>=0;--i){
52
            scanf("%lf",&a[n][i]);
53
54
        for(int i=n-1;i>=0;--i)
55
            for(int j=0;j<=i;++j)a[i][j]=a[i+1][j+1]*(j+1);</pre>
```

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```
56     vd ans=did(n);
57     sort(ans.begin(),ans.end());
58     for(int i=1;i+1<ans.size();++i)printf("%.10f\n",ans[i]);
59     return 0;
60 }</pre>
```

2.6 自适应辛普森

```
1 namespace adaptive_simpson {
 2
       template<typename function>
 3
        inline double area(function f, const double &left, const double &right) {
 4
            double mid = (left + right) / 2;
 5
            return (right - left) * (f(left) + 4 * f(mid) + f(right)) / 6;
 6
        }
 7
 8
       template<typename function>
 9
        inline double simpson(function f, const double &left, const double &right, const
           double &eps, const double &area_sum) {
10
            double mid = (left + right) / 2;
11
            double area_left = area(f, left, mid);
12
            double area right = area(f, mid, right);
13
            double area_total = area_left + area_right;
            if (fabs(area_total - area_sum) <= 15 * eps) {</pre>
14
15
                return area_total + (area_total - area_sum) / 15;
16
17
            return simpson(f, left, right, eps / 2, area_left) + simpson(f, mid, right,
               eps / 2, area_right);
18
       }
19
20
       template<typename function>
21
        inline double simpson(function f, const double &left, const double &right, const
           double &eps) {
            return simpson(f, left, right, eps, area(f, left, right));
22
23
        }
24 }
```

Chapter 3

计算几何

3.1 圆与多边形交

```
1 #include <cstdio>
 2 #include <cstdlib>
 3 #include <algorithm>
 4 #include <cmath>
5 #include <vector>
6 using namespace std;
8 const double eps = 5e-7;
9 const int N = 2222;
10 const double pi = acos(-1.0);
11
12 int sign(double x) {
13
       return x < -eps ? -1 : x > eps;
14 }
15
16 double sqr(double x) {
17
       return x * x;
18 }
19
20 struct Point {
21
       double x, y;
       Point (double x = 0, double y = 0) : x(x), y(y) {}
22
23
       friend inline Point operator +(const Point &a, const Point &b) {
24
           return Point(a.x + b.x, a.y + b.y);
25
26
       friend inline Point operator - (const Point &a, const Point &b) {
27
           return Point(a.x - b.x, a.y - b.y);
28
29
       friend inline Point operator *(const Point &a, double k) {
           return Point(a.x * k, a.y * k);
30
31
       }
```

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```
32
        friend inline Point operator /(const Point &a, double k) {
33
            return Point(a.x / k, a.y / k);
34
35
       double dist() const {
36
            return hypot(x, y);
37
            return sqrt(x * x + y * y);
38
39
       double dist2() const {
40
           return x * x + y * y;
41
42
        double ang() const {
43
           return atan2(y, x);
44
        }
45
   };
46
47
   vector<Point> convex;
48
49 int n;
50 double radius;
51 Point points[N][2];
52 Point target;
53
54
   double det(Point a, Point b, Point c) {
55
       return (b.x - a.x) * (c.y - a.y) - (c.x - a.x) * (b.y - a.y);
56
  }
57
58 double dot(Point a, Point b, Point c) {
59
       return (b.x - a.x) * (c.x - a.x) + (b.y - a.y) * (c.y - a.y);
60
   }
61
62
   double det(Point a, Point b) {
63
       return a.x * b.y - b.x * a.y;
64
  }
65
  double dot(Point a, Point b) {
66
       return a.x * b.x + a.y * b.y;
67
68
   }
69
70
   inline bool point_on_line(const Point &a, const Point &b, const Point &c) {
       return sign(det(Point(0, 0), a - b, c - b)) == 0 \&\& dot(Point(0, 0), b - a, c - a)
71
           ) < eps;
72
   }
7.3
74
   double point_to_line(const Point &a, const Point &b, const Point &c) {
75
       return fabs(det(Point(0, 0), c - b, a - b)) / (b - c).dist();
76
   }
77
78
   Point project_to_line(const Point &p, const Point &a, const Point &b) {
       return a + (b - a) * dot(Point(0, 0), p - a, b - a) / sqr((b - a).dist());
79
```

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```
80
    }
 81
 82 Point intersect(Point a, Point b, Point c, Point d) {
        double s1 = det(a, b, c);
 84
         double s2 = det(a, b, d);
 85
         return (c * s2 - d * s1) / (s2 - s1);
 86
    }
 87
 88 inline Point line_to_circle(const Point &a, const Point &b) {
 89
         double x = sqrt(sqr(radius) - sqr(point to line(Point(0, 0), a, b)));
 90
         return project_to_line(Point(0, 0), a, b) - (b - a) / (b - a).dist() * x;
 91 }
 92
 93
    inline double area tri(Point a, Point b) {
         return det(Point(0, 0), a, b) / 2;
 94
 95
 96
 97
    inline double area cir(Point a, Point b, double radius) {
98
         if (sign(det(Point(0, 0), a, b)) == 0)
99
             return 0;
         a = a / a.dist() * radius;
100
101
        b = b / b.dist() * radius;
102
        double d = atan2(det(Point(0, 0), a, b), dot(Point(0, 0), a, b));
103
         //printf("%f\n", sqr(radius) * d / 2);
104
         return sqr(radius) * d / 2;
105 }
106
107
    int intersect(const Point &a, const Point &b, Point &u, Point &v, double radius) {
108
         if (point_to_line(Point(0, 0), a, b) + eps > radius)
109
             return 0;
110
        u = line_to_circle(a, b);
111
        v = line_to_circle(b, a);
112
         return point_on_line(u, a, b) + point_on_line(v, a, b);
113 }
114
115 vector<Point> calc(vector<Point> vec, Point a, Point b) {
116
        vector<Point> result;
117
         for(int i = 0; i < (int)vec.size(); i++) {</pre>
118
             Point c = vec[i], d = vec[(i + 1) % (int)vec.size()];
119
             if (det(a, b, c) > -eps) {
                 result.push_back(c);
120
121
             if (sign(det(a, b, c)) * sign(det(a, b, d)) == -1) {
122
123
                 result.push back(intersect(a, b, c, d));
124
             }
125
         }
126
        return result;
127
128 double areaCT(double R, Point pa, Point pb)
```

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```
129
    {
130
         if (pa.dist() < pb.dist()) swap(pa, pb);</pre>
131
         if (pb.dist() < eps) return 0;</pre>
132
         Point pc = pb - pa;
133
         double a = pb.dist(), b = pa.dist(), c = pc.dist();
134
         double cosB = dot(pb, pc) / a / c, B = acos(cosB);
135
         double cosC = dot(pa, pb) / a / b, C = acos(cosC);
136
         double S, h, theta;
137
         if (a > R) {
138
             S = C * 0.5 * R * R;
             h = a * b * sin(C) / c;
139
140
             if (h < R && B < pi * 0.5)
                 S = acos(h / R) * R * R - h * sqrt(max(0.0, R * R - h * h));
141
         } else if (b > R) {
142
143
             theta = pi - B - asin(sin(B) / R * a);
             S = 0.5 * a * R * sin(theta) + (C - theta) * 0.5 * R * R;
144
145
         } else {
146
             S = 0.5 * sin(C) * a * b;
147
148
         return S;
149
    }
150
151
    void solve() {
         scanf("%lf%d", &radius, &n);
152
153
         convex.clear();
154
         convex.push_back(Point(-radius, -radius));
155
         convex.push_back(Point(radius, -radius));
156
         convex.push_back(Point(radius, radius));
157
         convex.push_back(Point(-radius, radius));
         for(int i = 1; i <= n; i++) {</pre>
158
159
             scanf("%lf%lf%lf", &points[i][0].x, &points[i][0].y, &points[i][1].x, &
                points[i][1].y);
160
161
         scanf("%lfu%lf", &target.x, &target.y);
         for(int i = 1; i <= n; i++) {</pre>
162
163
             if (det(points[i][0], points[i][1], target) < -eps) {</pre>
164
                 swap(points[i][0], points[i][1]);
165
166
             convex = calc(convex, points[i][0], points[i][1]);
167
         double ans = 0;
168
169
         for(int i = 0; i < (int)convex.size(); i++) {</pre>
             ans += areaCT(radius, convex[i], convex[(i + 1) % (int)convex.size()]) * sign
170
                 (det(convex[i], convex[(i + 1) % (int)convex.size()]));
171
         printf("%.5f", max(0., fabs(ans) / (pi * radius * radius) * 100));
172
173
         puts("%");
174
    }
175
```

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```
176 int main() {
177
          int test;
          scanf("%d", &test);
178
179
          while(test--) {
180
               static int testCount = 0;
181
               printf("Case<sub>□</sub>%d:<sub>□</sub>", ++testCount);
182
               solve();
183
          }
184 }
```

3.2 动态凸包

```
1 #define x first
 2 #define y second
 3 typedef map<int, int> mii;
 4 typedef map<int, int>::iterator mit;
5 struct point { // something omitted
       point(const mit &p): x(p->first), y(p->second) {}
7 };
   inline bool checkInside(mii &a, const point &p) { // `border inclusive`
8
9
       int x = p.x, y = p.y;
10
       mit p1 = a.lower_bound(x);
11
       if (p1 == a.end()) return false;
12
       if (p1->x == x) return y \le p1->y;
13
       if (p1 == a.begin()) return false;
14
       mit p2(p1--);
       return sign(det(p - point(p1), point(p2) - p)) >= 0;
15
16
17
   inline void addPoint(mii &a, const point &p) { // `no collinear points`
18
       int x = p.x, y = p.y;
19
       mit pnt = a.insert(make_pair(x, y)).first, p1, p2;
20
       for (pnt->y = y; ; a.erase(p2)) {
21
            p1 = pnt;
22
            if (++p1 == a.end())
23
                break;
24
            p2 = p1;
25
            if (++p1 == a.end())
26
                break;
27
            if (det(point(p2) - p, point(p1) - p) < 0)
28
29
30
       for ( ; ; a.erase(p2)) {
31
            if ((p1 = pnt) == a.begin())
32
                break;
33
            if (--p1 == a.begin())
34
               break;
35
            p2 = p1--;
            if (\det(point(p2) - p, point(p1) - p) > 0)
```

32 CHAPTER 3. 计算几何

3.3 farmland

```
1
   const int N = 111111, M = 1111111 * 4;
 3
 4
  struct eglist {
 5
       int other[M], succ[M], last[M], sum;
       void clear() {
 6
 7
            memset(last, -1, sizeof(last));
 8
            sum = 0;
 9
10
       void addEdge(int a, int b) {
            other[sum] = b, succ[sum] = last[a], last[a] = sum++;
11
12
            other[sum] = a, succ[sum] = last[b], last[b] = sum++;
13
        }
14
   }e;
15
16
   int n, m;
17
   struct point {
18
       int x, y;
19
       point(int x, int y) : x(x), y(y) {}
20
       point() {}
21
        friend point operator -(point a, point b) {
22
            return point(a.x - b.x, a.y - b.y);
23
       double arg() {
24
25
           return atan2(y, x);
26
        }
27
   }points[N];
28
   vector<pair<int, double> > vecs;
29
30
   vector<int> ee[M];
31 vector<pair<double, pair<int, int> > edges;
32 double length[M];
33 int tot, father[M], next[M], visit[M];
34
35 int find(int x) {
       return father[x] == x ? x : father[x] = find(father[x]);
36
37
38
39
   long long det(point a, point b) {
40
       return 1LL * a.x * b.y - 1LL * b.x * a.y;
41 }
```

3.3. FARMLAND 33

```
42
43
   double dist(point a, point b) {
        return sqrt(1.0 * (a.x - b.x) * (a.x - b.x) + 1.0 * (a.y - b.y) * (a.y - b.y));
44
45
46
47
   int main() {
48
        scanf("%d_{\sqcup}%d", &n, &m);
49
        e.clear();
50
        for(int i = 1; i <= n; i++) {</pre>
51
            scanf("%d<sub>\\\\\</sub>%d", &points[i].x, &points[i].y);
52
53
        for(int i = 1; i <= m; i++) {</pre>
            int a, b;
54
55
            scanf("%d_{\sqcup}%d", &a, &b);
56
            e.addEdge(a, b);
57
58
        for(int x = 1; x <= n; x++) {</pre>
59
            vector<pair<double, int> > pairs;
            for(int i = e.last[x]; ~i; i = e.succ[i]) {
60
                 int y = e.other[i];
61
                 pairs.push back(make pair((points[y] - points[x]).arg(), i));
62
63
64
            sort(pairs.begin(), pairs.end());
65
            for(int i = 0; i < (int)pairs.size(); i++) {</pre>
66
                 next[pairs[(i + 1) % (int)pairs.size()].second ^ 1] = pairs[i].second;
67
            }
68
        }
69
        memset(visit, 0, sizeof(visit));
70
        tot = 0;
71
        for(int start = 0; start < e.sum; start++) {</pre>
72
            if (visit[start])
73
                 continue;
74
            long long total = 0;
75
            int now = start;
76
            vecs.clear();
77
            while(!visit[now]) {
78
                 visit[now] = 1;
79
                 total += det(points[e.other[now ^ 1]], points[e.other[now]]);
80
                 vecs.push_back(make_pair(now / 2, dist(points[e.other[now ^ 1]], points[e
                     .other[now]])));
81
                 now = next[now];
82
            if (now == start && total > 0) {
83
84
85
                 for(int i = 0; i < (int)vecs.size(); i++) {</pre>
86
                     ee[vecs[i].first].push_back(tot);
87
                 }
88
            }
89
        }
```

34 CHAPTER 3. 计算几何

```
90
 91
         for(int i = 0; i < e.sum / 2; i++) {</pre>
 92
             int a = 0, b = 0;
 93
             if (ee[i].size() == 0)
 94
                 continue;
 95
             else if (ee[i].size() == 1) {
 96
                 a = ee[i][0];
 97
             } else if (ee[i].size() == 2) {
 98
                 a = ee[i][0], b = ee[i][1];
 99
             edges.push_back(make_pair(dist(points[e.other[i * 2]], points[e.other[i * 2 +
100
                  1]]), make_pair(a, b)));
101
         }
102
         sort(edges.begin(), edges.end());
103
         for(int i = 0; i <= tot; i++)</pre>
104
             father[i] = i;
105
         double ans = 0;
106
         for(int i = 0; i < (int)edges.size(); i++) {</pre>
107
             int a = edges[i].second.first, b = edges[i].second.second;
108
             double v = edges[i].first;
             if (find(a) != find(b)) {
109
                 ans += v;
110
111
                 father[father[a]] = father[b];
112
             }
113
114
         printf("%.5f\n", ans);
115 }
```

3.4 farmland 完全体

```
1
 2 const int MAXN = 200;
 3 const int MAXV = MAXN * MAXN;
 4 const int MAXE = MAXV * 6;
 5 const double eps = 1e-8;
 6
   int sign(double x) {
 7
 8
       return x < -eps ? -1 : x > eps;
 9
   }
10
11
   struct Point {
12
       double x, y;
13
14
       Point(int x, int y) : x(x), y(y) {}
15
       Point() {}
16
17
       Point &operator +=(const Point &o) {
18
            x += o.x;
```

3.4. FARMLAND 完全体

```
19
           y += o.y;
20
            return *this;
21
        }
22
23
       Point & operator -= (const Point &o) {
24
           x -= o.x;
25
           y = o.y;
26
           return *this;
27
28
29
       Point &operator *=(double k) {
30
            x *= k;
            y *= k;
31
32
           return *this;
33
       }
34
35
       Point &operator /=(double k) {
36
           x /= k;
37
           y /= k;
38
           return *this;
39
40
41
       double norm2() const {
42
           return x * x + y * y;
43
       }
44
45
       double norm() const {
46
            return sqrt(norm2());
47
48
49
       double arg() const {
50
           return atan2(y, x);
51
       }
52
53
       bool on(const Point &, const Point &) const;
       bool in(const vector<Point> &) const;
54
55 };
56
57 bool operator <(const Point &a, const Point &b) {
       return sign(a.x - b.x) < 0 \mid | sign(a.x - b.x) == 0 && sign(a.y - b.y) < 0;
58
59 }
60
61 bool operator ==(const Point &a, const Point &b) {
62
       return sign(a.x - b.x) == 0 \&\& sign(a.y - b.y) == 0;
63 }
64
65 Point operator +(Point a, const Point &b) {
66
       return a += b;
67 }
```

35

```
68
 69 Point operator - (Point a, const Point &b) {
 70
        return a -= b;
 71 }
 72
 73
    Point operator / (Point a, double k) {
 74
        return a /= k;
 75
    }
 76
 77 Point operator *(Point a, double k) {
 78
        return a *= k;
 79
 80
 81
    Point operator *(double k, Point a) {
 82
        return a *= k;
 83
    }
 84
 85 double det(const Point &a, const Point &b) {
 86
        return a.x * b.y - b.x * a.y;
 87 }
 88
 89 double dot(const Point &a, const Point &b) {
 90
        return a.x * b.x + a.y * b.y;
 91 }
 92
 93 bool parallel(const Point &a, const Point &b, const Point &c, const Point &d) {
 94
        return sign(det(b - a, d - c)) == 0;
 95 }
 96
 97 Point intersect(const Point &a, const Point &b, const Point &c, const Point &d) {
 98
        double s1 = det(b - a, c - a);
99
        double s2 = det(b - a, d - a);
100
        return (c * s2 - d * s1) / (s2 - s1);
101
    }
102
103 bool Point::on(const Point &a, const Point &b) const {
104
        const Point &p = *this;
105
        return sign(det(p-a, p-b)) == 0 \&\& sign(dot(p-a, p-b)) <= 0;
106
    }
107
108 bool Point::in(const vector<Point> &polygon) const {
109
        const Point &p = *this;
110
        int n = polygon.size();
111
        int count = 0;
112
        for (int i = 0; i < n; ++ i) {
113
            const Point &a = polygon[i];
114
            const Point &b = polygon[(i + 1) % n];
115
            if (p.on(a, b)){
116
                 return false;
```

3.4. FARMLAND 完全体

37

```
117
             }
118
             int t0 = sign(det(a - p, b - p));
             int t1 = sign(a.y - p.y);
119
120
             int t2 = sign(b.y - p.y);
             count += t0 > 0 \&\& t1 <= 0 \&\& t2 > 0;
121
122
             count -= t0 < 0 && t2 <= 0 && t1 > 0;
123
124
        return count != 0;
125 }
126
127 struct eglist {
128
         int other[MAXE], succ[MAXE], last[MAXE], sum;
129
         set<pair<int, int> > Edges;
         void clear() {
130
131
             memset(last, -1, sizeof(last));
132
             sum = 0;
133
             Edges.clear();
134
135
        void addEdge(int a, int b) {
136
             if (Edges.count(make pair(a, b)))
137
                 return;
138
             Edges.insert(make pair(a, b));
139
             other[sum] = b, succ[sum] = last[a], last[a] = sum;
140
             sum++;
141
142
         void _addEdge(int a, int b) {
143
             addEdge(a, b);
144
             addEdge(b, a);
145
146 }e, topo;
147
148 vector<Point> Points;
149
150 Point segments[MAXE][2];
151 double W, H;
152 int n, next[MAXE];
153 vector<double> areas, allAreas;
154 vector<vector<Point> > regions;
155
156 void addSegment(Point a, Point b) {
157
         segments[n][0] = a;
158
         segments[n][1] = b;
159
        n++;
160 }
161
162 int getPointID(const Point &p) {
         return lower_bound(Points.begin(), Points.end(), p) - Points.begin();
163
164
    }
165
```

```
166 const int VERTEX = 0;
167
    const int EDGE = 1;
168 const int REGION = 2;
169
170
    int getID(int type, int id) {
171
         if (type == VERTEX) {
172
             return id;
173
174
         if (type == EDGE) {
175
             return id + Points.size();
176
177
         if (type == REGION) {
178
             return id + Points.size() + e.sum / 2;
179
180
         assert(false);
181
    }
182
183
    double getArea(int id) {
184
         id -= Points.size() + e.sum / 2;
         return id < 0 ? 0 : areas[id];</pre>
185
186
    }
187
188
    int locate(const Point &p) {
189
         for (int i = 0; i < e.sum; i += 2) {</pre>
190
             if (p.on(Points[e.other[i]], Points[e.other[i ^ 1]])) {
191
                 return getID(EDGE, i >> 1);
192
             }
193
194
         int best = -1;
         for (int i = 0; i < regions.size(); ++i) {</pre>
195
             if (p.in(regions[i]) && (best == -1 || allAreas[best] > allAreas[i])) {
196
197
                 best = i;
198
             }
199
         }
200
         return getID(REGION, best);
201
202
203
    vector<string> colorNames;
204 map<string, int> colorIDs;
205
206 int getColorID(const char *color) {
207
         if (!colorIDs.count(color)) {
208
             colorNames.push back(color);
209
             int newID = colorIDs.size();
210
             colorIDs[color] = newID;
211
212
         return colorIDs[color];
213
    }
214
```

3.4. FARMLAND 完全体 39

```
215 int color[MAXV * 10];
216
217
    void paint(const Point &p, const char * c) {
218
         int start = locate(p);
219
         int old = color[start];
220
         int cid = getColorID(c);
221
         if (old == cid)
222
             return;
223
         queue<int> q;
224
         q.push(start);
225
         color[start] = cid;
226
         while(!q.empty()) {
227
             int x = q.front();
228
             q.pop();
229
             for (int i = topo.last[x]; ~i; i = topo.succ[i]) {
230
                  int y = topo.other[i];
231
                  if (color[y] == old) {
232
                      color[y] = cid;
233
                      q.push(y);
234
                  }
235
             }
236
         }
237
    }
238
239
    int main() {
240
         freopen("input.txt", "r", stdin);
241
         //freopen("output.txt", "w", stdout);
242
         scanf("%lf_{\perp}%lf_{\perp}%d", &W, &H, &n);
         for (int i = 0; i < n; i++) {</pre>
243
             scanf("%lf_{\sqcup}%lf_{\sqcup}%lf", \&segments[i][0].x, \&segments[i][0].y, \&segments[i][0].y]
244
                 ][1].x, &segments[i][1].y);
245
         }
246
         addSegment(Point(0, 0), Point(W, 0));
         addSegment(Point(W, 0), Point(W, H));
247
248
         addSegment(Point(W, H), Point(0, H));
         addSegment(Point(0, H), Point(0, 0));
249
250
251
         for (int i = 0; i < n; i++) {
252
             Points.push_back(segments[i][0]);
253
             Points.push back(segments[i][1]);
254
             for (int j = 0; j < i; j++) {
255
                  if (!parallel(segments[i][0], segments[i][1], segments[j][0], segments[j
                     ][1])) {
256
                      Point p = intersect(segments[i][0], segments[i][1], segments[j][0],
                          segments[j][1]);
257
                      if (p.on(segments[i][0], segments[i][1]) && p.on(segments[j][0],
                          segments[j][1])) {
258
                          Points.push_back(p);
259
                      }
```

```
260
                 }
261
             }
262
         sort(Points.begin(), Points.end());
263
         Points.erase(unique(Points.begin(), Points.end()), Points.end());
264
265
266
         e.clear();
267
         for (int i = 0; i < n; i++) {</pre>
268
             vector<pair<double, int> > pairs;
269
             for (int j = 0; j < Points.size(); j++) {</pre>
270
                  if (Points[j].on(segments[i][0], segments[i][1]))
271
                      pairs.push_back(make_pair((Points[j] - segments[i][0]).norm(), j));
272
             }
273
             sort(pairs.begin(), pairs.end());
274
             for (int i = 1; i < pairs.size(); i++) {</pre>
275
                 e.addEdge(pairs[i - 1].second, pairs[i].second);
276
                 e.addEdge(pairs[i].second, pairs[i - 1].second);
277
             }
278
         }
279
280
         for (int u = 0; u < Points.size(); u++) {</pre>
281
             vector<pair<double, int> > pairs;
282
             for (int iter = e.last[u]; ~iter; iter = e.succ[iter]) {
283
                 pairs.push_back(make_pair((Points[e.other[iter]] - Points[u]).arg(), iter
284
285
             sort(pairs.begin(), pairs.end());
286
             for(int i = 0; i < pairs.size(); i++) {</pre>
287
                 next[pairs[(i + 1) % pairs.size()].second ^ 1] = pairs[i].second;
288
             }
289
         }
290
291
         vector<pair<Point, double> > waits;
292
         static bool visit[MAXV];
293
         memset(visit, 0, sizeof(visit));
294
         for (int start = 0; start < e.sum; ++start) {</pre>
295
             if (!visit[start]) {
296
                 int v = start;
297
                 double totalArea = 0;
298
                 vector <Point> region;
299
                 for(; !visit[v]; v = next[v]) {
300
                      visit[v] = true;
                      totalArea += det(Points[e.other[v ^ 1]], Points[e.other[v]]);
301
302
                      region.push back(Points[e.other[v]]);
303
                 }
304
305
                 if (sign(totalArea) > 0) {
306
                      regions.push_back(region);
307
                      areas.push_back(totalArea);
```

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```
308
                      allAreas.push back(totalArea);
309
                  } else {
310
                      waits.push back(make pair(region.front(), -totalArea));
311
312
             }
313
         }
314
315
         //build
316
         topo.clear();
317
         for (int i = 0; i < e.sum; i++) {</pre>
             topo. addEdge(getID(EDGE, i >> 1), getID(VERTEX, e.other[i]));
318
319
         for (int i = 0; i < regions.size(); i++) {</pre>
320
321
             topo._addEdge(getID(REGION, i), getID(VERTEX, getPointID(regions[i].front()))
                 );
322
323
         for (int iter = 0; iter < waits.size(); iter++) {</pre>
324
             const Point &p = waits[iter].first;
325
             int best = -1;
             for (int i = 0; i < regions.size(); i++) {</pre>
326
                  if (p.in(regions[i]) \&\& (best == -1 || allAreas[best] > allAreas[i])) {
327
328
                      best = i;
329
                  }
330
             }
331
             if (best !=-1) {
332
                  areas[best] -= waits[iter].second;
333
                  topo._addEdge(getID(REGION, best), getID(VERTEX, getPointID(p)));
334
             }
335
         }
336
337
         getColorID("white");
338
339
         getColorID("blake");
         getColorID("__COLOR__");
340
341
         for (int i = 0; i < regions.size(); i++) {</pre>
342
343
             color[getID(REGION, i)] = getColorID("white");
344
345
         for (int i = 0; i < Points.size(); i++) {</pre>
346
             color[getID(VERTEX, i)] = getColorID("black");
347
348
         for(int i = 0; i < e.sum / 2; i++) {</pre>
             color[getID(EDGE, i)] = getColorID("black");
349
350
         paint(Point(0, 0), "__COLOR_ ");
351
         int m;
352
         scanf("%d", &m);
353
354
         while (m --) {
355
             Point p;
```

```
356
             char buffer[16];
357
              scanf("%lf_{\square}%lf_{\square}%s", &p.x, &p.y, buffer);
358
             paint(p, buffer);
359
         }
360
361
         map<string, double> answer;
362
         for (int i = 0; i < Points.size() + (e.sum >> 1) + regions.size(); ++i) {
363
             const string &name = colorNames[color[i]];
364
              if (name != "__COLOR__") {
365
                  answer[name] += getArea(i);
366
              }
367
368
         for (map<string, double> :: iterator iter = answer.begin(); iter != answer.end();
369
             printf("%s<sub>\u00e4</sub>%.8lf\n", iter->first.c_str(), 0.5 * iter->second);
370
         }
371 }
```

3.5 半平面交

```
1
   struct Border {
 2
       point p1, p2; double alpha;
 3
       Border(): p1(), p2(), alpha(0.0) {}
 4
       Border(const point &a, const point &b): p1(a), p2(b), alpha( atan2(p2.y - p1.y,
           p2.x - p1.x) ) {}
 5
       bool operator == (const Border &b) const {
 6
            return sign(alpha - b.alpha) == 0;
 7
 8
       bool operator < (const Border &b) const {</pre>
 9
            int c = sign(alpha - b.alpha); if (c != 0) return c > 0;
10
            return sign(det(b.p2 - b.p1, p1 - b.p1)) >= 0;
11
       }
12 };
   point isBorder(const Border &a, const Border &b) { // a and b should not be parallel
13
14
       point is;
15
        lineIntersect(a.p1, a.p2, b.p1, b.p2, is);
16
       return is;
17
   }
18 bool checkBorder(const Border &a, const Border &b, const Border &me) {
19
       point is;
20
        lineIntersect(a.p1, a.p2, b.p1, b.p2, is);
       return sign(det(me.p2 - me.p1, is - me.p1)) > 0;
21
22
   }
23
   double HPI(int N, Border border[]) {
24
        static Border que[MAXN * 2 + 1]; static point ps[MAXN];
25
        int head = 0, tail = 0, cnt = 0; // [head, tail)
26
        sort(border, border + N);
27
       N = unique(border, border + N) - border;
```

3.6. 三维绕轴旋转 43

```
28
        for (int i = 0; i < N; ++i) {</pre>
29
            Border &cur = border[i];
30
            while (head + 1 < tail && !checkBorder(que[tail - 2], que[tail - 1], cur))</pre>
31
                ---tail;
32
            while (head + 1 < tail && !checkBorder(que[head], que[head + 1], cur))</pre>
33
                ++head;
34
            que[tail++] = cur;
35
       while (head + 1 < tail && !checkBorder(que[tail - 2], que[tail - 1], que[head]))
36
37
            --tail;
       while (head + 1 < tail && !checkBorder(que[head], que[head + 1], que[tail - 1]))</pre>
38
39
            ++head;
40
        if (tail - head <= 2)
41
            return 0.0;
42
        //Foru(i, a, b) : a <= i < b
43
        Foru(i, head, tail)
44
            ps[cnt++] = isBorder(que[i], que[(i + 1 == tail) ? (head) : (i + 1)]);
45
        double area = 0;
46
        Foru(i, 0, cnt)
47
            area += det(ps[i], ps[(i + 1) % cnt]);
        return fabs(area * 0.5); // or (-area * 0.5)
48
49 }
```

3.6 三维绕轴旋转

```
1 const double pi = acos(-1.0);
 2 int n, m; char ch1; bool flag;
 3 double a[4][4], s1, s2, x, y, z, w, b[4][4], c[4][4];
 4 double sqr(double x)
5
6
        return x*x;
7 }
8 int main()
9
        scanf("%d\n", &n);
10
11
        memset(b, 0, sizeof(b));
        b[0][0] = b[1][1] = b[2][2] = b[3][3] = 1; //initial matrix
12
13
        for(int i = 1; i <= n; i++)</pre>
14
15
            scanf("%c", &ch1);
            if(ch1 == 'T')
16
17
                scanf("%lf_{\ \ \ }lf_{\ \ \ \ }n", \ \&x, \ \&y, \ \&z);//plus each coordinate by a number (x,
18
                     y, z)
19
                memset(a, 0, sizeof(a));
2.0
                a[0][0] = 1; a[3][0] = x;
21
                a[1][1] = 1; a[3][1] = y;
22
                a[2][2] = 1; a[3][2] = z;
```

```
23
                                                               a[3][3] = 1;
                                               }else if(ch1 == 'S')
2.4
25
                                                               scanf("\$lf_{\sqcup}\$lf_{\sqcup}\$lf', \&x, \&y, \&z); //multiply \ each \ coordinate \ by \ a \ number
26
                                                                                 (x, y, z)
27
                                                               memset(a, 0, sizeof(a));
28
                                                               a[0][0] = x;
29
                                                               a[1][1] = y;
30
                                                               a[2][2] = z;
31
                                                               a[3][3] = 1;
32
                                               }else
33
                                                               scanf("%lf_{\sqcup}%lf_{\sqcup}%lf_{\backslash}%lf_{\backslash}%x, &x, &y, &z, &w);
34
                                                               //大拇指指向x轴正方向时,4指弯曲由y轴正方向指向z轴正方向
35
36
                                                               //大拇指沿着原点到点 (x, y, z) 的向量, 4指弯曲方向旋转 w度
37
                                                               w = w*pi/180;
                                                              memset(a, 0, sizeof(a));
38
39
                                                               s1 = x*x+y*y+z*z;
40
                                                               a[3][3] = 1;
41
                                                               a[0][0] = ((y*y+z*z)*cos(w)+x*x)/s1;
                                                                                                                                                                                                                                                                a[0][1] = x*y*(1-cos(w))/
                                                                             s1+z*sin(w)/sqrt(s1); a[0][2] = x*z*(1-cos(w))/s1-y*sin(w)/sqrt(s1);
42
                                                               a[1][2] = y*z*(1-cos(w))/s1+x*sin(w)/sqrt(s1);
                                                                            w)+y*y)/s1;
43
                                                               a[2][0] = x*z*(1-cos(w))/s1+y*sin(w)/sqrt(s1); a[2][1] = y*z*(1-cos(w))/s1+y*sin(w)/sqrt(s1); a[2][1] = y*z*(1-cos(w))/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*sin(w)/s1+y*s
                                                                            s1-x*sin(w)/sqrt(s1); a[2][2] = ((x*x+y*y)*cos(w)+z*z)/s1;
44
                                               memset(c, 0, sizeof(c));
45
46
                                               for(int i = 0; i < 4; i++)
47
                                                                for(int j = 0; j < 4; j++)
48
                                                                               for(int k = 0; k < 4; k++)
49
                                                                                               c[i][j] += b[i][k]*a[k][j];
50
                                              memcpy(b, c, sizeof(c));
51
52
                              scanf("%d", &m);
53
                               for(int i = 1; i <= m; i++)</pre>
54
                                               scanf("%lf%lf%lf", &x, &y, &z);//initial vector
55
56
                                               printf("%lf_{L}%lf_{N}, x*b[0][0]+y*b[1][0]+z*b[2][0]+b[3][0], x*b[0][1]+y*b[0][1]+y*b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]+b[1][0]
                                                             [1][1]+z*b[2][1]+b[3][1], x*b[0][2]+y*b[1][2]+z*b[2][2]+b[3][2]);
57
58
                              return 0;
59
              }
```

3.7 点到凸包切线

3.8. 直线凸包交点 45

3.8 直线凸包交点

```
1 int n;
2 double eps(1e-8);
   int sign(const double & x) {
        return (x > eps) - (x + eps < 0);
5
   }
 6
   struct Point {
7
       double x, y;
8
       void scan() {
9
            scanf("%lf%lf", &x, &y);
10
       void print() {
11
12
           printf("%lf\sqcup%lf\setminusn", x, y);
13
14
       Point() {
15
        }
       Point(const double & x, const double & y) : x(x), y(y) {
16
17
18 };
19 Point operator + (const Point & a, const Point & b) {
       return Point(a.x + b.x, a.y + b.y);
20
21 }
22 Point operator - (const Point & a, const Point & b) {
23
       return Point(a.x - b.x, a.y - b.y);
24 }
25 Point operator * (const double & a, const Point & b) {
       return Point(a * b.x, a * b.y);
26
27 }
28 double operator * (const Point & a, const Point & b) {
29
       return a.x * b.y - a.y * b.x;
30 }
31 bool isUpper(const Point & a) {
       return sign(a.x) < 0 or sign(a.x) == 0 and sign(a.y > 0);
33 }
34 Point crs(const Point & as, const Point & at, const Point & bs, const Point & bt) {
35
        if(sign((at - as) * (bt - bs)) == 0) {
36
            return bs;
37
        double lambda((bs - as) * (bt - bs) / ((at - as) * (bt - bs)));
38
39
        return as + lambda * (at - as);
40 }
41 struct reca {
       Point a[50000];
42
43
       double s[50000];
44
       Point & operator [] (int x) {
45
           assert(x % n < 50000);
46
           return a[x % n];
47
        }
```

```
void init() {
48
49
            s[0] = a[0] * a[1];
            for(int i(1); i < n; i++) {</pre>
50
51
                s[i] = s[i - 1] + a[i] * (i == n - 1?a[0]:a[i + 1]);
52
            }
53
        }
54
55
        double getS(int le, int ri) {
56
            if(le > ri)
57
                return 0;
58
            le %= n;
59
            ri %= n;
60
            if(le <= ri) {
61
                return s[ri] - (le?s[le - 1]:0);
            }else {
62
63
                return getS(le, n - 1) + getS(0, ri);
64
65
        }
   } a;
66
67
   int lowerBound(int le, int ri, const Point & dir) {
68
        while(le < ri) {</pre>
69
70
            int mid((le + ri) / 2);
71
            if(sign((a[mid + 1] - a[mid]) * dir) >= 0) {
72
                le = mid + 1;
73
            }else {
74
                ri = mid;
75
            }
76
        }
77
        return le;
78
   }
79
   int boundLower(int le, int ri, const Point & s, const Point & t) {
        while(le < ri) {</pre>
80
81
            int mid((le + ri + 1) / 2);
82
            if(sign((a[mid] - s) * (t - s)) >= 0) {
83
                le = mid;
            }else {
84
85
                ri = mid - 1;
86
87
        }
88
        return le;
89
   }
90
   bool check(const Point & a, const Point & b, const Point & c, const Point & d) {
91
        return sign((a - c) * (d - c)) * sign((b - c) * (d - c)) <= 0;
92
   }
   bool f[55555];
93
   int main() {
94
95
        scanf("%d", &n);
96
        for(int i(0); i < n; i++) {</pre>
```

3.8. 直线凸包交点 47

```
97
              //printf("%d\n", n);
 98
             a[i].scan();
 99
             //return 0;
100
         //return 0;
101
         for(int i(0); i < n; i++) {</pre>
102
103
              int d(sign((a[i + 1] - a[i]) * (a[i + 2] - a[i + 1])));
104
             if(d) {
105
                  if(d < 0) {
106
                      reverse(a.a, a.a + n);
107
108
                  break;
109
             }
110
         for(int i(0); i < n; i++) {</pre>
111
112
             if(!sign(a[i].x - a[i + 1].x)) and !sign(a[i].y - a[i + 1].y)) {
113
                  f[i] = false;
114
             }else {
115
                  f[i] = true;
116
117
118
         int n1(0);
119
         for(int i(0); i < n; i++) {</pre>
120
             if(f[i]) {
121
                  a[n1++] = a[i];
122
             }
123
         }
124
         n = n1;
         //现在a必须是严格逆时针凸包
125
126
         a.init();
127
         int i1, j1;
128
         for(int i(0); i < n; i++) {</pre>
              if(isUpper(a[i + 1] - a[i]))  {
129
                  for(int j(i + 1); j != i; ++j %= n) {
130
131
                      if(!isUpper(a[j + 1] - a[j])) 
132
                           i1 = i; j1 = j;
133
                           break;
134
                      }
135
                  }
136
                  break;
137
             }
138
         if(i1 > j1) {
139
140
             j1 += n;
141
142
         int m;
143
         scanf("%d", &m);
144
         for(int i(0); i < m; i++) {</pre>
145
             Point s, t;
```

```
146
             s.scan(); t.scan();
147
             if(!isUpper(t - s)) {
148
                 swap(t, s);
149
             int i3(lowerBound(i1, j1, t - s));
150
151
             int j3(lowerBound(j1, i1 + n, s - t));
152
             int i4(boundLower(i3, j3, s, t));
153
             int j4(boundLower(j3, i3 + n, t, s));
154
             if(check(a[i4], a[i4 + 1], s, t)) {
155
                 Point p1(crs(s, t, a[i4], a[i4 + 1]));
156
                 Point p2(crs(s, t, a[j4], a[j4 + 1]));
                 if(sign(p1.x - p2.x) or sign(p1.y - p2.y)) {
157
                     assert(i4 % n != j4 % n);
158
159
                     double areal(p1 * a[i4 + 1] + a.getS(i4 + 1, j4 - 1) + a[j4] * p2 +
                         p2 * p1);
160
                     double area2(p2 * a[j4 + 1] + a.getS(j4 + 1, i4 + n - 1) + a[i4] * p1
                          + p1 * p2);
161
                     printf("%.6f\n", min(fabs(area1), fabs(area2)) / 2);
                 }else {
162
                     printf("0.000000\n");
163
164
                 }
165
             }else {
166
                 printf("0.000000\n");
167
             }
168
         }
169
    }
```

3.9 exhausted robot 凸多边形卡壳 + 凸多边形交

```
1 double eps(1e-8);
   int sign(const double & x) {
 2
 3
        return (x > eps) - (x + eps < 0);
 4
   }
 5
   bool equal(const double & x, const double & y) {
 6
        return x + eps > y and y + eps > x;
 7
   }
 8
   struct Point {
 9
        double x, y;
10
        Point () {
11
12
        Point(const double & x, const double & y) : x(x), y(y) {
13
14
        void scan() {
15
            scanf("%lf%lf", &x, &y);
16
17
        double sqrlen() const {
18
            return x * x + y * y;
19
        }
```

```
20
       double len() const {
21
           return sqrt(sqrlen());
22
23
       Point zoom(const double & 1) const {
           double lambda(1 / len());
24
25
            return Point(lambda * x, lambda * y);
26
27
       Point rev() const {
28
           return Point(-y, x);
29
30
       void print() const {
31
            printf("(%f_{\sqcup}%f)\n", x, y);
32
        }
33 };
34
35 vector<Point> blocks[22], denied[22], robot;
36
37 vector<pair<double, int> > vec;
38
39 bool f[111];
40
41 Point operator - (const Point & a, const Point & b) {
42
       return Point(a.x - b.x, a.y - b.y);
43 }
44 Point operator + (const Point & a, const Point & b) {
45
       return Point(a.x + b.x, a.y + b.y);
46 }
47 Point operator * (const double & a, const Point & b) {
48
       return Point(a * b.x, a * b.y);
49 }
50 double operator * (const Point & a, const Point & b) {
       return a.x * b.y - a.y * b.x;
51
52 }
53 double operator % (const Point & a, const Point & b) {
54
       return a.x * b.x + a.y * b.y;
55 }
56
57 bool operator < (const Point & a, const Point & b) {
58
       if(!equal(a.x, b.x))
59
           return a.x < b.x;</pre>
       else if(!equal(a.y, b.y));
60
61
           return a.y < b.y;</pre>
       return false;
62
63 }
64 bool operator == (const Point & a, const Point & b) {
65
        return equal(a.x, b.x) and equal(a.y, b.y);
66 }
67
68 void scan(vector<Point> & vec) {
```

```
69
                         vec.clear();
  70
                         int x;
  71
                         scanf("%d", &x);
  72
                         for(int i(0); i < x; i++) {</pre>
  73
                                     Point tmp;
  74
                                     tmp.scan();
   75
                                     vec.push_back(tmp);
  76
                         }
  77
             }
  78
  79
             Point intersect(const Point & as, const Point & ad, const Point & bs, const Point &
  80
                         double lambda((bs - as) * bd / (ad * bd));
  81
                         return as + lambda * ad;
  82
             }
  83
  84
             void cut(vector<Point> & vec, const Point & s, const Point & d) {
  85
                         vector<Point> vec1;
  86
                         for(int i(0); i < (int)vec.size(); i++) {</pre>
  87
                                     if(sign((vec[i] - s) * d) \le 0) {
  88
                                                vec1.push back(vec[i]);
  89
  90
                                     if(sign((vec[i] - s) * d) * sign((vec[(i + 1) % (int)vec.size()] - s) * d) < function (vec[i] - s) * d) * (int)vec[i] + (in
                                                vec1.push back(intersect(s, d, vec[i], vec[(i + 1) % (int)vec.size()] -
  91
                                                          vec[i]));
  92
                                     }
  93
                          }
  94
                         vec = vec1;
  95
             }
  96
  97
             int mi;
  98
  99
             Point getMax(const Point & norm) {
100
                         Point res(robot[0]);
101
                         mi = 0;
102
                         for(int i(0); i < (int)robot.size(); i++) {</pre>
103
                                     if(sign(robot[i] % norm - res % norm) > 0) {
104
                                                res = robot[i];
                                                mi = i;
105
106
                                     }
107
                         }
108
                         return res;
109
             }
110
             bool vecCmp(const pair<double, int> & a, const pair<double, int> & b) {
111
                         if(!equal(a.first, b.first))
112
113
                                     return a.first < b.first;</pre>
114
                         else
```

```
115
             return a.second > b.second;
116
    }
117
    bool vecEql(const pair<double, int> & a, const pair<double, int> & b) {
118
119
         return equal(a.first, b.first) and a.second == b.second;
120
121
122
    void print(const vector<Point> & vec) {
123
         printf("print:\n");
124
         for(int i(0); i < (int)vec.size(); i++) {</pre>
125
             vec[i].print();
126
127
         printf("endprint\n");
128
    }
129
130 void getConvex(vector<Point> & vec) {
131
         sort(vec.begin(), vec.end());
132
         vector<Point> vec1;
133
         for(int i(0); i < (int)vec.size(); i++) {</pre>
134
             while(vec1.size() >= 2 and sign((vec1.back() - vec1[(int)vec1.size() - 2]) *
                 (\text{vec}[i] - \text{vec1.back}())) \le 0)
135
                  vec1.pop back();
136
             vec1.push_back(vec[i]);
137
138
         vector<Point> vec2;
         for(int i((int)vec.size() - 1); i \ge 0; i--) {
139
             while(vec2.size() >= 2 and sign((vec2.back() - vec2[(int)vec2.size() - 2]) *
140
                 (\text{vec}[i] - \text{vec2.back}())) \le 0)
141
                  vec2.pop_back();
             vec2.push_back(vec[i]);
142
143
         }
144
         vec.clear();
145
         for(int i(0); i + 1 < (int)vec1.size(); i++)</pre>
146
             vec.push_back(vec1[i]);
         for(int i(0); i + 1 < (int)vec2.size(); i++)</pre>
147
             vec.push_back(vec2[i]);
148
149
     }
150
151 int main() {
152
         int tst;
153
         scanf("%d", &tst);
154
         for(int qq(1); qq <= tst; qq++) {</pre>
155
             int n;
              scanf("%d", &n);
156
157
              for(int i(0); i < n; i++)</pre>
158
                  scan(blocks[i]);
159
             scan(robot);
160
             double x1, y1, x2, y2;
161
              scanf("%lf%lf%lf%lf", &x1, &y1, &x2, &y2);
```

```
162
             x1 += robot[0].x - getMax(Point(-1, 0)).x;
163
             y1 += robot[0].y - getMax(Point(0, -1)).y;
164
             x2 = getMax(Point(1, 0)).x - robot[0].x;
             y2 -= getMax(Point(0, 1)).y - robot[0].y;
165
             double ans((x2 - x1) * (y2 - y1));
166
167
             for(int i(0); i < n; i++) {</pre>
168
                 int siz(blocks[i].size());
169
                 denied[i].clear();
170
                 int p1, p2;
171
                 p1 = 0;
172
                 getMax((blocks[i][1] - blocks[i][0]).rev());
173
                 p2 = mi;
174
                 denied[i].push_back(blocks[i][0] + robot[0] - robot[mi]);
175
                 for(int j1(1), j2(mi); j1 != p1 or j2 != p2; ) {
                      denied[i].push_back(blocks[i][j1] + robot[0] - robot[j2]);
176
177
                     Point dir((blocks[i][(j1 + 1) % (int)blocks[i].size()] - blocks[i][j1
                         ]).rev());
178
                      getMax(dir);
                      if(equal(robot[j2] % dir, robot[mi] % dir))
179
180
                          ++j1 %= (int)blocks[i].size();
181
                      else
182
                          ++j2 %= (int)robot.size();
183
                 }
184
185
             for(int i(0); i < n; i++) {</pre>
                 cut(denied[i], Point(x1, y1), Point(x2 - x1, 0));
186
187
                 cut(denied[i], Point(x2, y1), Point(0, y2 - y1));
188
                 cut(denied[i], Point(x2, y2), Point(x1 - x2, 0));
                 cut(denied[i], Point(x1, y2), Point(0, y1 - y2));
189
                 for(int j(0); j < (int)denied[i].size(); j++) {</pre>
190
191
                      f[j] = !(denied[i][j] == denied[i][(j + 1) % (int)denied[i].size()]);
192
                 }
193
                 getConvex(denied[i]);
194
                 denied[i].push_back(denied[i].front());
195
             for(int i(0); i < n; i++) {</pre>
196
197
                 for(int j(0); j + 1 < (int)denied[i].size(); j++) {</pre>
                     vec.clear();
198
199
                     vec.push_back(make_pair(0., 0));
200
                     vec.push back(make pair(1., 0));
201
                     Point norm(denied[i][j + 1] - denied[i][j]);
202
                     Point a(denied[i][j]), b(denied[i][j + 1]);
203
                     norm = norm.zoom(1 / norm.len());
                      for(int k(0); k < n; k++) if(k != i) {
204
                          int sz(vec.size());
205
206
                          for(int 1(0); 1 + 1 < (int)denied[k].size(); 1++) {</pre>
207
                              Point c(denied[k][l]), d(denied[k][l + 1]);
208
                              int s1(sign((c - a) * norm));
209
                              int s2(sign((d - a) * norm));
```

```
210
                               if(!s1 \text{ and } !s2 \text{ and } k < i \text{ and } sign((d - c) % norm) > 0) {
211
                                   vec.push back(make pair((c - a) % norm, 1));
212
                                   vec.push back(make pair((d - a) % norm, -1));
213
                               } else if(s1 \le 0 and s2 > 0 or s1 > 0 and s2 \le 0) {
214
                                   double a1((d - c) * (a - c));
215
                                   double a2((d - c) * (b - c));
216
                                   vec.push\_back(make\_pair(a1 / (a1 - a2), (s1 < 0 or s2 >
                                       0)?1:-1));
217
                               }
218
                           }
219
                      }
220
                      sort(vec.begin(), vec.end(), vecCmp);
221
                      int cnt(0);
222
                      double tot(0);
223
                      for(int k(0); k + 1 < (int)vec.size(); k++) {</pre>
224
                           cnt += vec[k].second;
225
                           if(cnt == 0 and sign(vec[k].first) >= 0 and sign(vec[k + 1].first
                               -1) <= 0) {
226
                               tot += vec[k + 1].first - vec[k].first;
227
                           }
228
                      }
229
                      ans -= tot * (denied[i][j] * denied[i][j + 1]) / 2;
230
                  }
231
232
              printf("Case_#%d:_%.3f\n", qq, ans);
233
         }
234 }
```

3.10 判断圆存在交集 O(nlogk)

传入 n 个圆, 圆心存在 cir 中, 半径存在 radius 中, nlogk 判断是否存在交集

```
1 int n;
 2 double sx, sy, d;
 3 vector<Point> cir;
  vector<double> radius;
   int isIntersectCircleToCircle(Point c1, double r1, Point c2, double r2)
7
   {
8
       double dis = c1.distTo(c2);
9
       return sign(dis - (r1 + r2)) \le 0;
10
   }
11
   void getRange(double x, Point &c, double r, double &retl, double &retr)
12
13
14
       double tmp = sqrt(max(r * r - (c.x - x) * (c.x - x), 0.0));
15
       retl = c.y - tmp; retr = c.y + tmp;
16
   }
17
```

```
18 int checkInLine(double x)
19
20
        double minR = INF, maxL = -INF;
21
        double tmpl, tmpr;
        for(int i = 0; i < n; ++ i) {</pre>
22
23
            if (sign(cir[i].x + radius[i] - x) < 0 \mid | sign(cir[i].x - radius[i] - x) > 0)
24
                return false;
25
            getRange(x, cir[i], radius[i], tmpl, tmpr);
26
            maxL = max(tmpl, maxL);
27
            minR = min(tmpr, minR);
28
            if (maxL > minR) return false;
29
30
        return true;
31
   }
32
33
   int shouldGoLeft(double x)
34 {
35
        if (checkInLine(x)) return 2;
36
        int onL = 0, onR = 0;
37
        for(int i = 0; i < n; ++ i) {</pre>
38
            if (sign(cir[i].x + radius[i] - x) < 0) onL = 1;
39
            if (sign(cir[i].x - radius[i] - x) > 0) onR = 1;
40
41
        if (onL && onR) return -1;
42
        if (onL) return 1;
43
        if (onR) return 0;
44
45
        double minR = INF, maxL = -INF, tmpl, tmpr;
46
        int idMinR, idMaxL;
47
48
        for(int i = 0; i < n; ++ i) {</pre>
49
            getRange(x, cir[i], radius[i], tmpl, tmpr);
50
            if (tmpr < minR) {</pre>
51
                minR = tmpr;
52
                idMinR = i;
53
54
            if (tmpl > maxL) {
55
                maxL = tmpl;
56
                idMaxL = i;
57
58
        if (! isIntersectCircleToCircle(cir[idMinR], radius[idMinR], cir[idMaxL], radius[
59
           idMaxL]))
60
            return -1;
        Point p1, p2;
61
        intersectionCircleToCircle(cir[idMinR], radius[idMinR], cir[idMaxL], radius[
62
            idMaxL], p1, p2);
63
        return (p1.x < x);
64 }
```

3.11. 最小覆盖球 55

```
65
66 int hasIntersectionCircles()
67 {
68
        double l = -INF, r = INF, mid;
        for(int i = 0; i < 100; ++ i) {</pre>
69
70
            mid = (1 + r) * 0.5;
71
            int tmp = shouldGoLeft(mid);
72
            if (tmp < 0) return 0;</pre>
73
            if (tmp == 2) return 1;
            if (tmp) r = mid;
74
75
            else 1 = mid;
76
77
        mid = (1 + r) * 0.5;
78
        return checkInLine(mid);
79 }
```

3.11 最小覆盖球

```
1 double eps(1e-8);
   int sign(const double & x) {
3
        return (x > eps) - (x + eps < 0);
4 }
5 bool equal(const double & x, const double & y) {
6
       return x + eps > y and y + eps > x;
7 }
8 struct Point {
9
       double x, y, z;
10
       Point() {
11
12
       Point(const double & x, const double & y, const double & z) : x(x), y(y), z(z)
13
14
       void scan() {
15
           scanf("%lf%lf%lf", &x, &y, &z);
16
17
        double sqrlen() const {
18
           return x * x + y * y + z * z;
19
20
       double len() const {
21
           return sqrt(sqrlen());
22
23
       void print() const {
           printf("(%lf_{\sqcup}%lf_{\sqcup}%lf)\n", x, y, z);
2.4
25
26 } a[33];
27 Point operator + (const Point & a, const Point & b) {
28
       return Point(a.x + b.x, a.y + b.y, a.z + b.z);
29 }
30 Point operator - (const Point & a, const Point & b) {
```

```
31
       return Point(a.x - b.x, a.y - b.y, a.z - b.z);
32 }
33 Point operator * (const double & x, const Point & a) {
       return Point(x * a.x, x * a.y, x * a.z);
34
35
36
   double operator % (const Point & a, const Point & b) {
37
       return a.x * b.x + a.y * b.y + a.z * b.z;
38 }
39 Point operator * (const Point & a, const Point & b) {
40
       return Point(a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y * b.x)
           ;
41
   }
   struct Circle {
42
43
       double r;
       Point o;
44
45
       Circle() {
46
            o.x = o.y = o.z = r = 0;
47
48
       Circle(const Point & o, const double & r) : o(o), r(r) {
49
50
       void scan() {
51
            o.scan();
52
            scanf("%lf", &r);
53
54
        void print() const {
55
            o.print();
56
            printf("%lf\n", r);
57
        }
58
   };
59
   struct Plane {
60
       Point nor;
61
       double m;
62
       Plane(const Point & nor, const Point & a) : nor(nor){
63
            m = nor % a;
64
65
   };
66
   Point intersect(const Plane & a, const Plane & b, const Plane & c) {
67
       Point c1(a.nor.x, b.nor.x, c.nor.x), c2(a.nor.y, b.nor.y, c.nor.y), c3(a.nor.z, b
           .nor.z, c.nor.z), c4(a.m, b.m, c.m);
       return 1 / ((c1 * c2) % c3) * Point((c4 * c2) % c3, (c1 * c4) % c3, (c1 * c2) %
68
           c4);
69
   }
70
   bool in(const Point & a, const Circle & b) {
71
       return sign((a - b.o).len() - b.r) \le 0;
72
   }
73
   bool operator < (const Point & a, const Point & b) {</pre>
74
        if(!equal(a.x, b.x)) {
75
            return a.x < b.x;</pre>
76
        }
```

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```
77
                     if(!equal(a.y, b.y)) {
  78
                              return a.y < b.y;</pre>
  79
  80
                     if(!equal(a.z, b.z)) {
  81
                              return a.z < b.z;</pre>
  82
  83
                    return false;
  84
          }
          bool operator == (const Point & a, const Point & b) {
  85
  86
                    return equal(a.x, b.x) and equal(a.y, b.y) and equal(a.z, b.z);
  87
          }
  88 vector<Point> vec;
          Circle calc() {
  89
                     if(vec.empty()) {
  90
  91
                               return Circle(Point(0, 0, 0), 0);
  92
                     }else if(1 == (int)vec.size()) {
  93
                              return Circle(vec[0], 0);
  94
                     }else if(2 == (int)vec.size()) {
                              return Circle(0.5 * (vec[0] + vec[1]), 0.5 * (vec[0] - vec[1]).len());
  95
  96
                     }else if(3 == (int)vec.size()) {
                              double r((vec[0] - vec[1]).len() * (vec[1] - vec[2]).len() * (vec[2] - vec[2]).len() * (vec[
  97
                                       [0]).len() / 2 / fabs(((vec[0] - vec[2]) * (vec[1] - vec[2])).len()));
  98
                              return Circle(intersect(Plane(vec[1] - vec[0], 0.5 * (vec[1] + vec[0])),
  99
                                                                      Plane(vec[2] - vec[1], 0.5 * (vec[2] + vec[1])),
100
                                                            Plane((vec[1] - vec[0]) * (vec[2] - vec[0]), vec[0]), r);
101
                     }else {
102
                              Point o(intersect(Plane(vec[1] - vec[0], 0.5 * (vec[1] + vec[0])),
                                                       Plane(vec[2] - vec[0], 0.5 * (vec[2] + vec[0])),
103
                                                       Plane(vec[3] - vec[0], 0.5 * (vec[3] + vec[0])));
104
105
                              return Circle(o, (o - vec[0]).len());
106
                     }
107
108 Circle miniBall(int n) {
109
                    Circle res(calc());
                     for(int i(0); i < n; i++) {</pre>
110
                               if(!in(a[i], res)) {
111
112
                                        vec.push back(a[i]);
113
                                        res = miniBall(i);
114
                                        vec.pop_back();
115
                                         if(i) {
116
                                                  Point tmp(a[i]);
117
                                                  memmove(a + 1, a, sizeof(Point) * i);
118
                                                  a[0] = tmp;
119
                                        }
120
                              }
121
122
                    return res;
123
          }
124
         int main() {
```

```
125
         int n;
126
         for(;;) {
127
             scanf("%d", &n);
128
             if(!n) {
129
                  break;
130
131
             for(int i(0); i < n; i++) {</pre>
132
                  a[i].scan();
133
134
             sort(a, a + n);
135
             n = unique(a, a + n) - a;
136
             vec.clear();
137
             printf("%.10f\n", miniBall(n).r);
138
         }
139 }
```

3.12 最小覆盖圆

```
1 #include < cmath >
 2 #include<cstdio>
 3 #include<algorithm>
 4 using namespace std;
 5 const double eps=1e-6;
 6 struct couple
 7
       double x, y;
 8
 9
       couple(){}
       couple(const double &xx, const double &yy)
10
11
12
            x = xx; y = yy;
13
   } a[100001];
14
15
   int n;
   bool operator < (const couple & a, const couple & b)</pre>
16
17
       return a.x < b.x - eps or (abs(a.x - b.x) < eps and a.y < b.y - eps);
18
19
20 bool operator == (const couple & a, const couple & b)
21
   {
22
       return !(a < b) and !(b < a);
23
   }
   inline couple operator - (const couple &a, const couple &b)
24
25
   {
26
       return couple(a.x-b.x, a.y-b.y);
27
28
   inline couple operator + (const couple &a, const couple &b)
29
   {
30
       return couple(a.x+b.x, a.y+b.y);
```

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```
31 }
32 inline couple operator * (const couple &a, const double &b)
33
34
       return couple(a.x*b, a.y*b);
35 }
36
   inline couple operator / (const couple &a, const double &b)
37
38
       return a*(1/b);
39 }
40 inline double operator * (const couple &a, const couple &b)
41
42
       return a.x*b.y-a.y*b.x;
43
44
   inline double len(const couple &a)
45
46
       return a.x*a.x+a.y*a.y;
47
48 inline double di2(const couple &a, const couple &b)
49
       return (a.x-b.x)*(a.x-b.x)+(a.y-b.y)*(a.y-b.y);
50
51 }
52
   inline double dis(const couple &a, const couple &b)
53
       return sqrt((a.x-b.x)*(a.x-b.x)+(a.y-b.y)*(a.y-b.y));
54
55 }
56 struct circle
57
58
        double r; couple c;
59
60 inline bool inside(const couple & x)
61
   {
        return di2(x, cir.c) < cir.r*cir.r+eps;</pre>
62
63 }
64 inline void p2c(int x, int y)
65
       cir.c.x = (a[x].x+a[y].x)/2;
66
67
       cir.c.y = (a[x].y+a[y].y)/2;
68
       cir.r = dis(cir.c, a[x]);
69
   }
70 inline void p3c(int i, int j, int k)
71 {
72
       couple x = a[i], y = a[j], z = a[k];
73
       cir.r = sqrt(di2(x,y)*di2(y,z)*di2(z,x))/fabs(x*y+y*z+z*x)/2;
74
        couple t1((x-y).x, (y-z).x), t2((x-y).y, (y-z).y), t3((len(x)-len(y))/2, (len(y)-
           len(z))/2);
75
       cir.c = couple(t3*t2, t1*t3)/(t1*t2);
76 }
77 inline circle mi()
78 {
```

```
79
         sort(a + 1, a + 1 + n);
 80
         n = unique(a + 1, a + 1 + n) - a - 1;
81
         if(n == 1)
82
83
             cir.c = a[1];
84
             cir.r = 0;
85
             return cir;
86
87
         random_shuffle(a + 1, a + 1 + n);
88
         p2c(1, 2);
89
         for(int i = 3; i <= n; i++)</pre>
90
              if(!inside(a[i]))
 91
 92
                  p2c(1, i);
 93
                  for(int j = 2; j < i; j++)</pre>
94
                      if(!inside(a[j]))
95
                       {
96
                           p2c(i, j);
97
                           for(int k = 1; k < j; k++)
98
                               if(!inside(a[k]))
99
                                    p3c(i,j,k);
100
                      }
101
              }
102
         return cir;
103
```

3.13 圆交 $O(n^2 \log n)$ 计算面积和重心

```
1
   double pi = acos(-1.0), eps = 1e-12;
 2
   double sqr(const double & x) {
 3
        return x * x;
 4
   }
 5 double ans[2001];
 6
   int sign(const double & x) {
 7
        return x < -eps?-1:x > eps;
 8
   }
   struct Point {
 9
10
        double x, y;
11
        Point(){}
        Point(const double & x, const double & y) : x(x), y(y) {}
12
        void scan() {scanf("%lf%lf", &x, &y);}
13
14
        double sqrlen() {return sqr(x) + sqr(y);}
15
        double len() {return sqrt(sqrlen());}
16
        Point rev() {return Point(y, -x);}
17
        void print() {printf("f_{\square}f_{\square}f \n", x, y);}
18
        Point zoom(const double & d) {double lambda = d / len(); return Point(lambda * x,
            lambda * y);}
   } dvd, a[2001];
```

```
20 Point centre[2001];
21 double atan2(const Point & x) {
22
       return atan2(x.y, x.x);
23 }
24 Point operator - (const Point & a, const Point & b) {
       return Point(a.x - b.x, a.y - b.y);
27 Point operator + (const Point & a, const Point & b) {
28
       return Point(a.x + b.x, a.y + b.y);
29 }
30 double operator * (const Point & a, const Point & b) {
31
       return a.x * b.y - a.y * b.x;
32 }
33 Point operator * (const double & a, const Point & b) {
34
       return Point(a * b.x, a * b.y);
35 }
36 double operator % (const Point & a, const Point & b) {
37
       return a.x * b.x + a.y * b.y;
38 }
39 struct circle {
      double r; Point o;
40
41
       circle() {}
       void scan() {
42
43
           o.scan();
44
           scanf("%lf", &r);
45
       }
46 } cir[2001];
47 struct arc {
48
       double theta;
49
       int delta;
50
       Point p;
51
       arc() {};
52
       arc(const double & theta, const Point & p, int d) : theta(theta), p(p), delta(d)
53 } vec[4444];
54 int nV;
55 inline bool operator < (const arc & a, const arc & b) {
56
       return a.theta + eps < b.theta;</pre>
57 }
58 int cnt;
59 inline void psh(const double t1, const Point p1, const double t2, const Point p2) {
60
       if(t2 + eps < t1)
61
           cnt++;
       vec[nV++] = arc(t1, p1, 1);
62
63
       vec[nV++] = arc(t2, p2, -1);
64 }
65 inline double cub(const double & x) {
66
       return x * x * x;
67 }
```

```
68
    inline void combine(int d, const double & area, const Point & o) {
 69
         if(sign(area) == 0) return;
70
         centre[d] = 1 / (ans[d] + area) * (ans[d] * centre[d] + area * o);
71
        ans[d] += area;
72
73
    bool equal(const double & x, const double & y) {
        return x + eps > y and y + eps > x;
74
75
    }
76
    bool equal(const Point & a, const Point & b) {
77
        return equal(a.x, b.x) and equal(a.y, b.y);
78
    }
79
    bool equal(const circle & a, const circle & b) {
80
        return equal(a.o, b.o) and equal(a.r, b.r);
81
    bool f[2001];
82
    int main() {
83
84
         //freopen("hdu4895.in", "r", stdin);
85
         int n, m, index;
        while(EOF != scanf("%d%d%d", &m, &n, &index)) {
86
87
             index--;
             for(int i(0); i < m; i++) {</pre>
88
89
                 a[i].scan();
90
91
             for(int i(0); i < n; i++) {</pre>
 92
                 cir[i].scan();//n个圆
93
             for(int i(0); i < n; i++) {//这一段在去重圆 能加速 删掉不会错
 94
95
                 f[i] = true;
96
                 for(int j(0); j < n; j++) if(i != j) {</pre>
97
                     if(equal(cir[i], cir[j]) and i < j or !equal(cir[i], cir[j]) and cir[</pre>
                         i].r < cir[j].r + eps and (cir[i].o - cir[j].o).sqrlen() < sqr(cir
                         [i].r - cir[j].r) + eps) {
98
                         f[i] = false;
99
                         break;
100
                     }
101
                 }
102
103
             int n1(0);
104
             for(int i(0); i < n; i++)</pre>
105
                 if(f[i])
106
                     cir[n1++] = cir[i];
107
             n = n1; // 去重圆结束
             fill(ans, ans + n + 1, 0);//ans[i]表示被圆覆盖至少i次的面积
108
109
             fill(centre, centre + n + 1, Point(0, 0));//centre[i]表示上面ans[i]部分的重心
110
             for(int i(0); i < m; i++)</pre>
                 combine(0, a[i] * a[(i + 1) % m] * 0.5, 1. / 3 * (a[i] + a[(i + 1) % m]))
111
             for(int i(0); i < n; i++) {</pre>
112
113
                 dvd = cir[i].o - Point(cir[i].r, 0);
```

```
114
                 nV = 0;
                 vec[nV++] = arc(-pi, dvd, 1);
115
116
                 cnt = 0;
117
                 for(int j(0); j < n; j++) if(j != i) {</pre>
118
                     double d = (cir[j].o - cir[i].o).sqrlen();
119
                     if(d < sqr(cir[j].r - cir[i].r) + eps) {
120
                         if(cir[i].r + i * eps < cir[j].r + j * eps)</pre>
121
                             psh(-pi, dvd, pi, dvd);
                     }else if(d + eps < sqr(cir[j].r + cir[i].r)) {</pre>
122
123
                         double lambda = 0.5 * (1 + (sqr(cir[i].r) - sqr(cir[j].r)) / d);
                         Point cp(cir[i].o + lambda * (cir[j].o - cir[i].o));
124
125
                         Point nor((cir[j].o - cir[i].o).rev().zoom(sqrt(sqr(cir[i].r) - (
                             cp - cir[i].o).sqrlen()));
                         Point frm(cp + nor);
126
                         Point to(cp - nor);
127
128
                         psh(atan2(frm - cir[i].o), frm, atan2(to - cir[i].o), to);
129
                     }
130
                 }
                 sort(vec + 1, vec + nV);
131
                 vec[nV++] = arc(pi, dvd, -1);
132
                 for(int j = 0; j + 1 < nV; j++) {
133
                     cnt += vec[j].delta;
134
                     //if(cnt == 1) {//如果只算ans[1]和centre[1], 可以加这个if加速.
135
136
                         double theta(vec[j + 1].theta - vec[j].theta);
137
                         double area(sqr(cir[i].r) * theta * 0.5);
                         combine(cnt, area, cir[i].o + 1. / area / 3 * cub(cir[i].r) *
138
                             Point(sin(vec[j + 1].theta) - sin(vec[j].theta), cos(vec[j].
                             theta) -\cos(\text{vec}[j + 1].\text{theta})));
139
                         combine(cnt, -sqr(cir[i].r) * sin(theta) * 0.5, 1. / 3 * (cir[i].
                             o + vec[j].p + vec[j + 1].p));
140
                         combine(cnt, vec[j].p * vec[j + 1].p * 0.5, 1. / 3 * (vec[j].p +
                             vec[j + 1].p));
141
                     //}
142
             }//板子部分结束 下面是题目
143
             combine(0, -ans[1], centre[1]);
144
             for(int i = 0; i < m; i++) {</pre>
145
146
                 if(i != index)
147
                     (a[index] - Point((a[i] - a[index]) * (centre[0] - a[index]), (a[i] -
                          a[index]) % (centre[0] - a[index])).zoom((a[i] - a[index]).len())
                         ).print();
148
                 else
149
                     a[i].print();
150
             }
151
152
153
         fclose(stdin);
154
         return 0;
155
    }
```

3.14 三维跨立实验 + 点到线段的垂足在线段上 + 分数类

```
long long gcd(long long a, long long b) {
 2
       return b?qcd(b, a % b):a;
 3
   }
 4
   struct frac {
        long long x, y;
 5
        frac() {}
 6
 7
        frac(const long long & xx, const long long & yy) : x(xx), y(yy) {
 8
            long long d(gcd(x, y));
            x /= d; y /= d;
 9
10
            if(y < 0)
11
                y = -y, x = -x;
12
13
       void print() const {
14
            printf("(%lld/%lld)\n", x, y);
15
16
   };
17
   frac operator + (const frac & a, const frac & b) {
        //long\ long\ y = a.y\ /\ gcd(a.y,\ b.y)\ *\ b.y;
18
        //return frac(y / a.y * a.x + y / b.y * b.x, y);//这里可以减小中间结果, 以避免爆
19
           long long.
20
       return frac(a.x * b.y + b.x * a.y, a.y * b.y);
21
22 frac operator - (const frac & a, const frac & b) {
23
        //long\ long\ y = a.y\ /\ gcd(a.y,\ b.y)\ *\ b.y;
        //return frac(y / a.y * a.x - y / b.y * b.x, y);
24
       return frac(a.x * b.y - b.x * a.y, a.y * b.y);
25
26
2.7
  frac operator * (const frac & a, const frac & b) {
28
        //long long v(gcd(a.x, b.y)), w(gcd(a.y, b.x));
29
        //return frac((a.x / v) * (b.x / w), (a.y / w) * (b.y / v));
30
       return frac(a.x * b.x, a.y * b.y);
31 }
32 frac operator / (const frac & a, const frac & b) {
33
        //long long v(gcd(a.x, b.x)), w(gcd(a.y, b.y));
        //return \ frac((a.x / v) * (b.y / w), (a.y / w) * (b.x / v));
34
35
       return frac(a.x * b.y, a.y * b.x);
36 }
37 bool operator < (const frac & a, const frac & b) {
38
       return a.x * b.y < b.x * a.y;</pre>
39
   bool operator == (const frac & a, const frac & b) {
40
       return a.x * b.y == b.x * a.y;
41
42
   }
43 bool operator <= (const frac & a, const frac & b) {
       return a.x * b.y <= b.x * a.y;
44
45 }
```

```
46
47
   frac sqr(const frac & a) {
48
       return a * a;
49 }
50 struct Point {
       frac x, y, z;
51
52
       Point () {}
53
       void scan() {cin >> x.x >> y.x >> z.x; x.y = y.y = z.y = 1;}
54
       Point(const frac & x, const frac & y, const frac & z) :x(x), y(y), z(z) {}
55
       frac sqrlen() {return x * x + y * y + z * z;}
       void print() const {printf("{");x.print(); y.print(); z.print();printf("}\n");}
57 } a, b, c, d;
58 Point operator - (const Point & a, const Point & b) {
59
       return Point(a.x - b.x, a.y - b.y, a.z - b.z);
60 }
61 Point operator + (const Point & a, const Point & b) {
62
       return Point(a.x + b.x, a.y + b.y, a.z + b.z);
63 }
64 Point operator * (const frac & a, const Point & b) {
       return Point(a * b.x, a * b.y, a * b.z);
65
66 }
67
   frac operator % (const Point & a, const Point & b) {
68
       return a.x * b.x + a.y * b.y + a.z * b.z;
69 }
70 Point operator * (const Point & a, const Point & b) {
       return Point(a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z, a.x * b.y - a.y * b.x)
72 }
73
   bool _ (const Point & a) {
       return a.x == frac(0, 1) and a.y == frac(0, 1) and a.z == frac(0, 1);
75 }
76 void check(frac & ans, const Point & a, const Point & s, const Point & t) {
77
       if(sign((a - s) % (t - s)) * sign((a - t) % (t - s)) <= 0) \{//\}
           点到线段的垂足在线段上(端点含)
78
           ans = min(ans, ((a - s) * (t - s)).sqrlen() / (t - s).sqrlen());//
               点到直线距离
79
80 }
81 int sign(const frac & a) {
       return a.x < 0?-1:a.x > 0;
82
83
84
   int main() {
85
       int tst;
86
       scanf("%d", &tst);
87
       for(int qq = 1; qq <= tst; qq++) {</pre>
88
           a.scan(); b.scan();
           c.scan(); d.scan();//线段(a->b), (c->d)
89
90
           frac ans = (a - c).sqrlen();
91
           ans = min(ans, (a - d).sqrlen());
```

```
92
            ans = min(ans, (b - c).sqrlen());
93
            ans = min(ans, (b - d).sqrlen());
94
            Point nor;
            if(!_(nor = (b - a) * (d - c)))//线段平行
95
                 if(sign((c - a) * (d - a) % nor) * sign((c - b) * (d - b) % nor) <= 0 and
96
                     sign((a - c) * (b - c) % nor) * sign((a - d) * (b - d) % nor) <= 0)//
                     三维跨立实验
97
                     ans = min(ans, sqr(nor % (c - a)) / nor.sqrlen());
            check(ans, a, c, d);
98
99
            check(ans, b, c, d);
100
            check(ans, c, a, b);
101
            check(ans, d, a, b);
            cout << ans.x << '_{\sqcup}' << ans.y << endl;
102
103
        }
104
        return 0;
105 }
```

3.15 平面图形的转动惯量计算

```
1 int n, m;
   double eps = 1e-8;
 3
   int sign(const double & x) {
 4
       return x < -eps?-1:x > eps;
 5
   }
 6
   struct Point {
 7
       double x, y;
 8
        void scan() {
 9
            scanf("%lf%lf", &x, &y);
10
11
       void print() {
12
            printf("(%f_{\sqcup}%f)\n", x, y);
13
       Point(const double & x, const double & y) : x(x), y(y) {}
14
15
       Point() {}
16
       double len() {return sqrt(x * x + y * y);}
17
       Point rev() {return Point(-y, x);}
18 } a[222], b[222];
19
   Point operator + (const Point & a, const Point & b) {
       return Point(a.x + b.x, a.y + b.y);
20
21
22 Point operator - (const Point & a, const Point & b) {
23
       return Point(a.x - b.x, a.y - b.y);
24
25
   Point operator * (const double & a, const Point & b) {
       return Point(a * b.x, a * b.y);
26
27
28 double operator % (const Point & a, const Point & b) {
```

```
29
        return a.x * b.x + a.y * b.y;
30 }
31 double operator * (const Point & a, const Point & b) {
        return a.x * b.y - a.y * b.x;
33 }
34 double sqr(const double & x) {
35
        return x * x;
36 }
37 double cub(const double & x) {
38
        return x * x * x;
39 }
40 double calc(const double & Y, const double & c0, const double & c1, const double & c2
       , const double & c3) {
        return Y * c0 + 0.5 * Y * Y * c1 + Y * Y * Y * c2 / 3 + Y * Y * Y * C3 / 4;
41
42
   }
   int main() {
43
44
        scanf("%d%d", &n, &m);
45
        for(int i = 1; i <= n; i++) {</pre>
46
            a[i].scan();
47
48
        a[0] = a[n];
49
        double area(0);
50
        for(int i = 1; i <= n; i++) {</pre>
            area += (a[i - 1] * a[i]);
51
52
53
        for(int i = 1; i <= m; i++) {</pre>
54
            b[i].scan();
55
56
        double ans(0);
        for(int i = 1; i <= m; i++) {</pre>
57
58
            vector<Point> vec(a + 1, a + 1 + n);
59
            for(int j = 1; j <= m; j++) if(j != i) {</pre>
60
                vector<Point> vec1;
61
                Point mid(0.5 * (b[i] + b[j])), dir((b[j] - b[i]).rev());
                for(int k = 0; k < (int)vec.size(); k++) {
62
                     if(sign((vec[k] - mid) * dir) \le 0)
63
64
                         vec1.push back(vec[k]);
65
                    Point dir1(vec[(k + 1) % (int)vec.size()] - vec[k]);
66
                     if(sign((vec[k] - mid) * dir) * sign((vec[(k + 1) % (int)vec.size())]
                        - \min) * \dim) < 0) {
67
                         double lambda((mid - vec[k]) * dir / (dir1 * dir));
68
                         vec1.push back(vec[k] + lambda * dir1);
69
                     }
70
                }
71
                vec = vec1;
72
73
            for(int j = 0; j < (int)vec.size(); j++)</pre>
74
                vec[j] = vec[j] - b[i];
75
            for(int j = 0; j < (int)vec.size(); j++){</pre>
```

```
76
              double X1(vec[j].len()), X(vec[(j + 1) % (int)vec.size()] % vec[j] / vec[
                  j].len()), Y(vec[j] * vec[(j + 1) % (int)vec.size()] / vec[j].len());
               //若是vec[j].len()为0 或者 Y为0 则转动惯量为0
77
78
               //旋转中心在原点 三角形((0,0), vec[j], vec[j + 1])的转动惯量, 其中若vec[
                  j] * vec[j + 1] < 0求出来的是转动惯量的相反数.
79
              ans += calc(Y, cub(X1) / 3, sqr(X1) * (X - X1) / Y, X1 * sqr((X - X1) / Y)
                  ), (cub((X - X1) / Y) - cub(X / Y)) / 3);
              ans += calc(Y, 0, 0, X1, -X1 / Y);
80
81
           }
82
83
       }
84
85
       printf("%.10f\n", ans / area * 2);
86
       fclose(stdin);
87
       return 0;
88 }
```

3.16 凸多边形内的最大圆 $O(n \log n)$

```
1 double eps(1e-8);
 2
   int sign(const double & x) {
 3
        return x < -eps?-1:x > eps;
 4
   struct Point {
 6
        double x, y;
 7
        Point() {
 8
        Point(const double & x, const double & y) : x(x), y(y) {
 9
10
11
        double sqrlen() const {
12
            return x * x + y * y;
13
14
        double len() const {
15
            return sqrt(sqrlen());
16
        void scan() {
17
18
            scanf("%lf%lf", &x, &y);
19
20
        void print() const {
21
            printf("(%f_{\sqcup}%f)\n", x, y);
22
23
   };
24
   Point operator + (const Point & a, const Point & b) {
25
        return Point(a.x + b.x, a.y + b.y);
26
27
   Point operator - (const Point & a, const Point & b) {
        return Point(a.x - b.x, a.y - b.y);
```

```
29 }
30 Point operator * (const double & a, const Point & b) {
       return Point(a * b.x, a * b.y);
32 }
33 double operator * (const Point & a, const Point & b) {
34
       return a.x * b.y - a.y * b.x;
35 }
36 struct Line {
37
       Point s, d;
38
       Line() {
39
40
       Line(const Point & s, const Point & d) : s(s), d(d) {
41
42 };
43 Point crs(const Line & a, const Line & b) {
44
       double lambda((b.s - a.s) * b.d / (a.d * b.d));
45
        return a.s + lambda * a.d;
46 }
47 struct reca {
48
       Point a, b;
        int prv, nxt;
49
50
       Point d() const {
51
           return b - a;
52
53
        double calc();
54 } a[11111];
55 reca (&c)[11111](a);
   double reca::calc() {
        if(sign(d() * c[prv].d()) and sign(d() * c[nxt].d())) {
57
58
            double len1(c[prv].d().len()), len2(d().len()), len3(c[nxt].d().len());
59
            Point cp(crs(Line(a, 1 / (len1 + len2) * (len2 * c[prv].a + len1 * b) - a),
               Line(b, 1 / (len2 + len3) * (len3 * a + len2 * c[nxt].b) - b)));
60
            return fabs((cp - a) * d() / d().len());
       }else
61
62
           return 1e100;
63
64 }
65 double val[11111];
66 bool f[11111];
67 int main() {
68
        int n;
        scanf("%d", &n);
69
        for(int i(0); i < n; i++) {</pre>
70
71
            a[i].a.scan();
72
73
        for(int i(0); i < n; i++) {</pre>
74
            a[i].b = a[(i + 1) % n].a;
75
            a[i].prv = (i + n - 1) % n;
76
            a[i].nxt = (i + 1) % n;
```

```
77
        }
78
        priority queue<pair<double, int>, vector<pair<double, int> >, greater<pair<double
           , int> > > hp;
79
        for(int i(0); i < n; i++) {</pre>
80
            hp.push(make_pair(val[i] = a[i].calc(), i));
81
        for(int i(1); i \le n - 3; i++) {
82
83
            int prv(a[hp.top().second].prv), nxt(a[hp.top().second].nxt);
84
            a[prv].nxt = nxt;
85
            a[nxt].prv = prv;
86
            if(sign(a[prv].d() * a[nxt].d()))
87
                a[prv].b = a[nxt].a = crs(Line(a[prv].a, a[prv].d()), Line(a[nxt].a, a[
                   nxt].d()));
88
            f[hp.top().second] = true;
89
            hp.pop();
90
            hp.push(make_pair(val[prv] = a[prv].calc(), prv));
91
            hp.push(make_pair(val[nxt] = a[nxt].calc(), nxt));
92
            while(f[hp.top().second] or val[hp.top().second] != hp.top().first)
93
                hp.pop();
94
95
        int y(hp.top().second);
96
        printf("%f\n", min(min(val[a[y].prv], val[a[y].nxt]), val[y]));
97
   }
```

3.17 三维凸包

```
1 const double eps = 1e-8;
 2 int mark[1005][1005];
 3 Point info[1005];
 4 int n, cnt;
 5 double mix(const Point &a, const Point &b, const Point &c) {
 6
       return a.dot(b.cross(c));}
 7
   double area(int a, int b, int c) {
 8
       return ((info[b] - info[a]).cross(info[c] - info[a])).length();}
   double volume(int a, int b, int c, int d) {
 9
10
       return mix(info[b] - info[a], info[c] - info[a], info[d] - info[a]);}
   struct Face {
11
12
       int a, b, c;
13
       Face() {}
14
       Face(int a, int b, int c): a(a), b(b), c(c) {}
15
       int &operator [](int k) { return k==0?a:k==1?b:c; }
16 };
17
   vector <Face> face;
18
   inline void insert(int a, int b, int c) { face.push_back(Face(a, b, c));}
19
   void add(int v) {
20
       vector <Face> tmp;
21
       int a, b, c;
22
       cnt++;
```

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```
for (int i = 0; i < SIZE(face); i++) {</pre>
23
24
            a = face[i][0]; b = face[i][1]; c = face[i][2];
25
            if (Sign(volume(v, a, b, c)) < 0)
26
                mark[a][b] = mark[b][a] = mark[b][c] = mark[c][b] = mark[c][a] =
27
                          mark[a][c] = cnt;
28
            else tmp.push back(face[i]);
29
30
        face = tmp;
31
        for (int i = 0; i < SIZE(tmp); i++) {</pre>
32
            a = face[i][0]; b = face[i][1]; c = face[i][2];
33
            if (mark[a][b] == cnt) insert(b, a, v);
34
            if (mark[b][c] == cnt) insert(c, b, v);
            if (mark[c][a] == cnt) insert(a, c, v);
35
36
        }
37
   }
   int Find() {
38
39
        for (int i = 2; i < n; i++) {</pre>
40
            Point ndir = (info[0] - info[i]).cross(info[1] - info[i]);
41
            if (ndir == Point()) continue;
42
            swap(info[i], info[2]);
            for (int j = i + 1; j < n; j++)
43
44
                if (Sign(volume(0, 1, 2, j)) != 0) {
45
                     swap(info[j], info[3]);
46
                     insert(0, 1, 2); insert(0, 2, 1);
47
                    return 1;
48
                }
49
50
       return 0;
51
   int main() {
52
53
        for (; scanf("%d", &n) == 1; ) {
54
            for (int i = 0; i < n; i++)</pre>
55
                info[i].Input();
56
            sort(info, info + n);
57
            n = unique(info, info + n) - info;
58
            face.clear();
59
            random shuffle(info, info + n);
60
            if (Find()) {
61
                memset(mark, 0, sizeof(mark));
62
                cnt = 0;
63
                for (int i = 3; i < n; i++) add(i);
64
                vector<Point> Ndir;
                for (int i = 0; i < SIZE(face); ++i) {</pre>
65
                    Point p = (info[face[i][0]] - info[face[i][1]]).cross
66
67
                             (info[face[i][2]] - info[face[i][1]]);
68
                    p = p / p.length();
69
                    Ndir.push_back(p);
70
                }
71
                sort(Ndir.begin(), Ndir.end());
```

72 CHAPTER 3. 计算几何

```
int ans = unique(Ndir.begin(), Ndir.end()) - Ndir.begin();
printf("%d\n", ans);

else {
    printf("1\n");
}
```

3.18 点在多边形内

```
1
   bool in_polygon(const point &p, const vector<point> &poly) {
 2
        int n = (int)poly.size();
 3
        int counter = 0;
 4
        for (int i = 0; i < n; ++i) {</pre>
 5
            point a = poly[i], b = poly[(i + 1) % n];
 6
            if (point on line(p, line(a, b)))
 7
                return false; // bounded excluded
 8
            int x = sign(det(p - a, b - a));
 9
            int y = sign(a.y - p.y);
            int z = sign(b.y - p.y);
10
            if (x > 0 \&\& y \le 0 \&\& z > 0)
11
12
                counter++;
13
            if (x < 0 \&\& z \le 0 \&\& y > 0)
14
                counter--;
15
16
        return counter != 0;
17
   }
```

3.19 三角形的内心

```
point incenter(const point &a, const point &b, const point &c) {

double p = (a - b).length() + (b - c).length() + (c - a).length();

return (a * (b - c).length() + b * (c - a).length() + c * (a - b).length()) / p;
}
```

3.20 三角形的外心

```
point circumcenter(const point &a, const point &b, const point &c) {
    point p = b - a, q = c - a, s(dot(p, p) / 2, dot(q, q) / 2);

double d = det(p, q);

return a + point(det(s, point(p.y, q.y)), det(point(p.x, q.x), s)) / d;
}
```

3.21. 三角形的垂心 73

3.21 三角形的垂心

39

for (int i = 0; i < nfree; ++i)</pre>

```
1 point orthocenter(const point &a, const point &b, const point &c) {
      return a + b + c - circumcenter(a, b, c) * 2.0;
3 }
  3.22 V 图
1 const int AIX = 5;
2 const int MAXM = AIX * MAXN;
3
4 struct point {
5
      double x, y;
6
      int index;
7
      struct Edge *in;
8
      point(double _x = 0, double _y = 0) : x(_x), y(_y) {}
9 };
```

```
10 inline bool operator< (const point &a, const point &b) {</pre>
       return a.x < b.x \mid | (sgn(a.x - b.x) == 0 && a.y < b.y);
11
12
13 inline double cross(const point &a, const point &b, const point &c) { return det
14
            (b - a, c - a); }
15 struct Edge {
       point *Org, *Dest;
       Edge *Onext, *Oprev, *Dnext, *Dprev;
17
18 };
   inline point* Other(const Edge *e, const point *p) { return e->Org == p ?
19
20
            e->Dest : e->Org; }
21 inline Edge* Next(const Edge *e, const point *p) { return e->Org == p ? e->Onext
22
             : e->Dnext; }
23 inline Edge* Prev(const Edge *e, const point *p) { return e->Org == p ? e->Oprev
24
             : e->Dprev; }
25 struct gEdge {
26
       int u, v;
27
       double w;
28
       gEdge() {}
29
       gEdge(int _u, int _v, double _w) : u(_u), v(_v), w(_w) {}
30 };
31 inline bool operator< (const gEdge &a, const gEdge &b) { return a.w < b.w; }
32 point p[MAXN], *Q[MAXN];
33 Edge mem[AIX * MAXN], *elist[AIX * MAXN];
34 static int nfree;
   //Alloc memory
36 inline void Alloc Memory(const int &n) {
37
       nfree = AIX * n;
       Edge *e = mem;
38
```

CHAPTER 3. 计算几何

```
40
             elist[i] = e++;
41
   }
42
   //Add an edge to a ring of edges
43 inline void Splice(Edge *a, Edge *b, point *v) {
44
        Edge *next;
45
        if (a\rightarrow 0rg == v)
46
             next = a \rightarrow 0next, a \rightarrow 0next = b;
47
        else
48
             next = a->Dnext, a->Dnext = b;
49
        if (next->Org == v)
50
             next->Oprev = b;
51
        else
52
             next->Dprev = b;
53
        if (b\rightarrow 0rq == v)
54
             b->Onext = next, b->Oprev = a;
55
        else
56
             b->Dnext = next, b->Dprev = a;
57
   }
58
   //Initialise a new edge
59
    inline Edge *MakeEdge(point *u, point *v) {
        Edge *e = elist[--nfree];
60
61
        e->Onext = e->Oprev = e->Dnext = e->Dprev = e;
62
        e\rightarrow 0rg = u, e\rightarrow Dest = v;
63
        if (!u->in)
64
             u\rightarrow in = e;
65
        if (!v->in)
             v\rightarrow in = e;
66
67
        return e;
68
    }
69
    //Creates a new edge and adds it to two rings of edges.
70
    inline Edge *Join(Edge *a, point *u, Edge *b, point *v, int side) {
71
        Edge *e = MakeEdge(u, v);
72
        if (side == 1) {
73
             if (a\rightarrow 0rq == u)
74
                  Splice(a->Oprev, e, u);
75
             else
76
                  Splice(a->Dprev, e, u);
77
             Splice(b, e, v);
78
        }
        else {
79
80
             Splice(a, e, u);
81
             if (b\rightarrow 0rg == v)
82
                  Splice(b->Oprev, e, v);
83
             else
84
                  Splice(b->Dprev, e, v);
85
         }
86
        return e;
87
    //Remove an edge
```

3.22. V图 75

```
89
    inline void Remove(Edge *e) {
 90
         point *u = e->Org, *v = e->Dest;
 91
         if (u->in == e)
 92
             u->in = e->0next;
 93
         if (v\rightarrow in == e)
 94
             v->in = e->Dnext;
 95
         if (e->Onext->Org == u)
 96
             e->Onext->Oprev = e->Oprev;
 97
         else
 98
             e->Onext->Dprev = e->Oprev;
 99
         if (e->0prev->0rg == u)
100
             e->Oprev->Onext = e->Onext;
101
         else
102
             e->Oprev->Dnext = e->Onext;
103
         if (e->Dnext->Org == v)
104
             e->Dnext->Oprev = e->Dprev;
105
         else
106
             e->Dnext->Dprev = e->Dprev;
         if (e->Dprev->Org == v)
107
108
             e->Dprev->Onext = e->Dnext;
109
         else
110
             e->Dprev->Dnext = e->Dnext;
111
         elist[nfree++] = e;
112
113
    //Determines the lower tangent of two triangulations
    inline void Low_tangent(Edge *e_1, point *o_1, Edge *e_r, point *o_r, Edge
              **l low, point **OL, Edge **r_low, point **OR) {
115
116
         point *d_l = Other(e_l, o_l), *d_r = Other(e_r, o_r);
117
         while (true) {
118
             if (cross(*o_l, *o_r, *d_l) < -EPS) {</pre>
119
                 e_l = Prev(e_l, d_l);
120
                 o_1 = d_1;
121
                 d_1 = Other(e_1, o_1);
122
             else if (cross(*o_1, *o_r, *d_r) < -EPS) {</pre>
123
124
                 e_r = Next(e_r, d_r);
125
                 or = dr;
126
                 d_r = Other(e_r, o_r);
127
             }
128
             else
129
                 break;
130
         *OL = o 1, *OR = o r;
131
         *1 low = e 1, *r low = e r;
132
133
    inline void Merge(Edge *lr, point *s, Edge *rl, point *u, Edge **tangent) {
134
135
         double cot_L, cot_R, N1, cot_N, P1, cot_P;
136
         point 11, 12, r1, r2, uu, vv;
137
         point *O, *D, *OR, *OL;
```

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```
138
         Edge *B, *L, *R;
139
         Low tangent(lr, s, rl, u, &L, &OL, &R, &OR);
140
         *tangent = B = Join(L, OL, R, OR, 0);
141
         O = OL, D = OR;
         do {
142
143
             Edge *El = Next(B, O), *Er = Prev(B, D), *next, *prev;
144
             point *l = Other(El, O), *r = Other(Er, D);
145
             11 = *0 - *1, 12 = *D - *1, r1 = *0 - *r, r2 = *D - *r;
             double c1 = det(11, 12), cr = det(r1, r2);
146
147
             bool BL = cl > EPS, BR = cr > EPS;
148
             if (!BL && !BR)
149
                 break;
             if (BL) {
150
151
                 double dl = dot(11, 12);
152
                 cot_L = dl / cl;
                 do {
153
154
                     next = Next(E1, 0);
155
                     uu = *0 - *Other(next, 0);
                     vv = *D - *Other(next, O);
156
                     N1 = det(uu, vv);
157
                     if (!(N1 > EPS))
158
159
                          break;
160
                     cot_N = dot(uu, vv) / N1;
161
                     if (cot_N > cot_L)
162
                         break;
163
                     Remove(El);
                     El = next;
164
165
                     cot_L = cot_N;
166
                 }
167
                 while (true);
168
             if (BR) {
169
170
                 double dr = dot(r1, r2);
                 cot_R = dr / cr;
171
172
                 do {
173
                     prev = Prev(Er, D);
174
                     uu = *0 - *Other(prev, D);
175
                     vv = *D - *Other(prev, D);
176
                     P1 = det(uu, vv);
                     if (!(P1 > EPS))
177
178
                         break;
179
                     cot P = dot(uu, vv) / P1;
                     if (\cot P > \cot R)
180
181
                          break;
182
                     Remove(Er);
183
                     Er = prev;
184
                     cot_R = cot_P;
185
186
                 while (true);
```

3.22. V图 77

```
187
188
             l = Other(El, O); r = Other(Er, D);
             if (!BL || (BL && BR && cot_R < cot_L)) {</pre>
189
190
                 B = Join(B, O, Er, r, 0);
191
                 D = r;
192
             }
             else {
193
194
                 B = Join(El, l, B, D, 0);
195
                 0 = 1;
196
             }
197
198
         while (true);
199
200
    inline void Divide(int s, int t, Edge **L, Edge **R) {
201
         Edge *a, *b, *c, *ll, *lr, *rl, *rr, *tangent;
202
         int n = t - s + 1;
203
         if (n == 2)
204
             *L = *R = MakeEdge(Q[s], Q[t]);
         else if (n == 3) {
205
             a = MakeEdge(Q[s], Q[s + 1]);
206
207
             b = MakeEdge(Q[s + 1], Q[t]);
208
             Splice(a, b, Q[s + 1]);
209
             double v = cross(*Q[s], *Q[s + 1], *Q[t]);
210
             if (v > EPS) {
211
                 c = Join(a, Q[s], b, Q[t], 0);
212
                 *L = a, *R = b;
213
             else if (v < -EPS) {
214
                 c = Join(a, Q[s], b, Q[t], 1);
215
216
                 *L = c, *R = c;
217
             }
218
             else
219
                 *L = a, *R = b;
220
221
         else if(n > 3) {
             int split = (s + t) / 2;
222
223
             Divide(s, split, &ll, &lr);
             Divide(split + 1, t, &rl, &rr);
224
225
             Merge(lr, Q[split], rl, Q[split + 1], &tangent);
226
             if (tangent->Org == Q[s])
227
                 11 = tangent;
228
             if (tangent->Dest == Q[t])
229
                 rr = tangent;
             *L = 11; *R = rr;
230
231
         }
232
233 int task, n, m, k, root[MAXN];
234
    gEdge E[MAXM], MST[MAXN];
235 inline int Make_Graph() {
```

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```
236
         Edge *start, *e;
237
         int M = 0;
238
         point *u, *v;
239
         for(int i = 0; i < n; ++i) {</pre>
240
             u = p + i;
241
             start = e = u \rightarrow in;
242
             do {
243
                  v = Other(e, u);
                 if (u < v)
244
245
                      E[M++] = gEdge(u - p + 1, v - p + 1, dis(*u, *v));
246
                 e = Next(e, u);
247
             while(e != start);
248
249
         }
250
         return M;
251
    }
252
    int find_root(const int &x) { return root[x] ? root[x] = find_root(root[x]) : x;
253
254
    inline bool merge(const int &x, const int &y) {
255
         int p = find root(x), q = find root(y);
         if (p != q) {
256
257
             root[p] = q;
258
             return true;
259
260
         else
261
             return false;
262
263
    inline void kruskal(gEdge *E, int m, int n, gEdge* MST) {
264
         for (int i = 1; i <= n; ++i)</pre>
265
             root[i] = 0;
266
         sort(E, E + m);
267
         int tot = 0;
268
         for (int i = 0; i < m; ++i)
269
             if (merge(E[i].u, E[i].v))
270
                 MST[tot++] = E[i];
271
272
    inline void MinimumEuclideanSpaningTree(point* p, int n, gEdge* MST) {
273
         Alloc_Memory(n);
274
         sort(p, p + n);
275
         for (int i = 0; i < n; ++i)
             Q[i] = p + i;
276
277
         Edge *L, *R;
         Divide(0, n - 1, &L, &R);
278
279
         m = Make Graph();
280
         kruskal(E, m, n, MST);
281
    }
    int main() {
282
283
         for (scanf("%d", &task); task--; ) {
284
             scanf("%d", &k);
```

3.22. V 图 79

```
285
            for (n = 0; scanf("%lf", &p[n].x) == 1 && p[n].x != -1; ++n) {
                scanf("%lf", &p[n].y);
286
                p[n].in = NULL;
287
288
                p[n].index = n;
289
             if (n == 1) {
290
291
                printf("0\n");
292
                continue;
293
            MinimumEuclideanSpaningTree(p, n, MST);
294
            printf("%d\n", int(ceil(k > n ? 0 : MST[n - k - 1].w) + EPS));
295
296
        }
297 }
```

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Chapter 4

数据结构

4.1 KD 树

```
1
   曼哈顿距离版,欧几里得只需要把sqr改成x*x即可。
2
   tested on bzoj 2648, 2626
3
5
   namespace k_dimensional_tree {
6
       int const N = ;
7
8
       struct point {
9
           int x, y, id;
10
11
12
       inline long long sqr(const long long &x) {
13
           return abs(x);
14
15
16
       inline long long dist(const point &a, const point &b) {
17
           return sqr(a.x - b.x) + sqr(a.y - b.y);
18
19
       struct rectangle {
20
21
           int lx, rx, ly, ry;
22
           inline void set(const point &p) {
23
                lx = rx = p.x;
24
               ly = ry = p.y;
25
26
           inline void mergy(const point &p) {
27
                lx = min(lx, p.x);
28
               rx = max(rx, p.x);
29
               ly = min(ly, p.y);
               ry = max(ry, p.y);
30
31
           }
```

```
32
            inline void mergy(const rectangle &r) {
33
                lx = min(lx, r.lx);
34
                rx = max(rx, r.rx);
35
                ly = min(ly, r.ly);
36
                ry = max(ry, r.ry);
37
38
            /* minimum distance
39
            inline long long dist(const point &p) {
40
                if (p.x <= lx && p.y <= ly) {</pre>
41
                    return sqr(p.x - lx) + sqr(p.y - ly);
42
43
                if (p.x <= rx && p.y <= ly) {</pre>
44
                    return sqr(p.y - ly);
45
46
                if (p.x >= rx && p.y <= ly) {</pre>
47
                    return sqr(p.x - rx) + sqr(p.y - ly);
48
49
                if (p.x >= rx && p.y <= ry) {</pre>
50
                    return sqr(p.x - rx);
51
                if (p.x >= rx && p.y >= ry) {
52
53
                    return sqr(p.x - rx) + sqr(p.y - ry);
54
55
                if (p.x >= lx && p.y >= ry) {
56
                    return sqr(p.y - ry);
57
58
                if (p.x <= lx && p.y >= ry) {
59
                    return sqr(p.x - lx) + sqr(p.y - ry);
60
61
                if (p.x <= lx && p.y >= ly) {
62
                    return sqr(p.x - lx);
63
64
                return 0;
65
            /* maximum distance
66
            inline long long dist(const point &p) {
67
68
                long long ret = 0;
69
                ret += max(sqr(rx - p.x), sqr(lx - p.x));
70
                ret += max(sqr(ry - p.y), sqr(ly - p.y));
71
                return ret;
72
            }
73
        };
74
75
        struct node {
            int child[2];
76
77
            point p;
78
            rectangle r;
79
            inline void set(const point &_p) {
80
                p = _p;
```

4.1. KD 树

```
81
                 r.set(p);
 82
                 child[0] = child[1] = 0;
 83
             }
 84
         };
 85
 86
         int size;
 87
         point a[N];
 88
         node tree[N];
 89
 90
         inline bool xcompare(const point &a, const point &b) {
 91
             return a.x < b.x || a.x == b.x && a.y < b.y;
 92
 93
 94
         inline bool ycompare(const point &a, const point &b) {
 95
             return a.y < b.y || a.y == b.y && a.x < b.x;
 96
 97
 98
         inline int build(int left, int right, bool dim = 0) {
 99
             int x = ++size, mid = left + right >> 1;
             nth element(a + left, a + mid, a + right, dim ? xcompare : ycompare);
100
101
             tree[x].set(a[mid]);
102
             if (left < mid) {</pre>
103
                 tree[x].child[0] = build(left, mid, dim ^ 1);
104
                 tree[x].r.mergy(tree[tree[x].child[0]].r);
105
106
             if (mid + 1 < right) {
107
                 tree[x].child[1] = build(mid + 1, right, dim ^ 1);
108
                 tree[x].r.mergy(tree[tree[x].child[1]].r);
109
110
             return x;
111
         }
112
113
         inline int insert(int x, const point &p, bool dim = 0) {
             if (x == 0) {
114
115
                 tree[++size].set(p);
116
                 return size;
117
118
             tree[x].r.mergy(p);
119
             if (dim && xcompare(p, tree[x].p) || !dim && ycompare(p, tree[x].p)) {
120
                 tree[x].child[0] = insert(tree[x].child[0], p, dim ^ 1);
121
             } else {
122
                 tree[x].child[1] = insert(tree[x].child[1], p, dim ^ 1);
123
124
             return x;
125
         }
126
             query minimum
127
128
         inline void query(int x, const point &p, long long &ret, bool dim = 0) {
129
             if (tree[x].r.dist(p) >= ret) {
```

```
130
                 return;
131
             }
132
             ret = min(ret, dist(tree[x].p, p));
133
             if (dim && xcompare(p, tree[x].p) | !dim && ycompare(p, tree[x].p)) {
134
                 if (tree[x].child[0]) {
135
                     query(tree[x].child[0], p, ret, dim ^ 1);
136
137
                 if (tree[x].child[1]) {
138
                     query(tree[x].child[1], p, ret, dim ^ 1);
139
                 }
140
             } else {
141
                 if (tree[x].child[1]) {
142
                     query(tree[x].child[1], p, ret, dim ^ 1);
143
144
                 if (tree[x].child[0]) {
145
                     query(tree[x].child[0], p, ret, dim ^ 1);
146
                 }
147
             }
148
         }
149
150
         /* query maximum
151
         inline void query(int x, const point &p, long long &ret, bool dim = 0) {
152
             if (tree[x].r.dist(p) <= ret) {</pre>
153
                 return;
154
             ret = max(ret, dist(tree[x].p, p));
155
             if (dim && xcompare(p, tree[x].p) || !dim && ycompare(p, tree[x].p)) {
156
157
                 if (tree[x].child[1]) {
                     query(tree[x].child[1], p, ret, dim ^ 1);
158
159
                 }
                 if (tree[x].child[0]) {
160
161
                     query(tree[x].child[0], p, ret, dim ^ 1);
162
                 }
163
             } else {
164
                 if (tree[x].child[0]) {
                     query(tree[x].child[0], p, ret, dim ^ 1);
165
166
167
                 if (tree[x].child[1]) {
168
                     query(tree[x].child[1], p, ret, dim ^ 1);
169
                 }
170
             }
171
         }
172
         /* query kth-minimum
173
174
         inline void query(int x, const point &p, int k, pair<long long, int> ret[], bool
            dim = 0) {
175
             if (tree[x].r.dist(p) > ret[k].first) {
176
                 return;
177
             }
```

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```
178
             pair<long long, int> val = make pair(dist(tree[x].p, p), tree[x].p.id);
179
             for (int i = 1; i <= k; ++i) {
                 if (val < ret[i]) {
180
181
                      for (int j = k + 1; j > i; — j) {
                          ret[j] = ret[j - 1];
182
183
                      }
184
                     ret[i] = val;
185
                     break;
186
                 }
187
             if (dim && xcompare(p, tree[x].p) || !dim && ycompare(p, tree[x].p)) {
188
189
                 if (tree[x].child[0]) {
                     query(tree[x].child[0], p, k, ret, dim ^ 1);
190
191
192
                 if (tree[x].child[1]) {
193
                     query(tree[x].child[1], p, k, ret, dim ^ 1);
194
                 }
195
             } else {
196
                 if (tree[x].child[1]) {
197
                     query(tree[x].child[1], p, k, ret, dim ^ 1);
198
199
                 if (tree[x].child[0]) {
200
                     query(tree[x].child[0], p, k, ret, dim ^ 1);
201
                 }
202
             }
203
         }
204
205
             query kth-maximum
                                  */
         inline void query(int x, const point &p, int k, pair<long long, int> ret[], bool
206
            dim = 0) {
207
             if (tree[x].r.dist(p) < ret[k].first) {</pre>
208
                 return;
209
210
             pair<long long, int> val = make_pair(dist(tree[x].p, p), -tree[x].p.id);
             for (int i = 1; i <= k; ++i) {</pre>
211
                 if (val > ret[i]) {
212
                     for (int j = k + 1; j > i; ---j) {
213
214
                          ret[j] = ret[j - 1];
215
216
                     ret[i] = val;
217
                     break;
218
                 }
219
             if (dim && xcompare(p, tree[x].p) || !dim && ycompare(p, tree[x].p)) {
220
                 if (tree[x].child[1]) {
221
222
                     query(tree[x].child[1], p, k, ret, dim ^ 1);
223
                 if (tree[x].child[0]) {
224
225
                     query(tree[x].child[0], p, k, ret, dim ^ 1);
```

```
226
                 }
227
             } else {
228
                  if (tree[x].child[0]) {
229
                      query(tree[x].child[0], p, k, ret, dim ^ 1);
230
                 if (tree[x].child[1]) {
231
232
                      query(tree[x].child[1], p, k, ret, dim ^ 1);
233
                 }
234
             }
235
         }
236
237
         inline void clear() {
238
             size = 0;
239
         }
240
    }
```

4.2 树链剖分

```
namespace heavy_light_decomposition {
 1
 2
        int const N = ;
 3
 4
        int n;
 5
        vector<int> adj[N];
 6
        int father[N], height[N], size[N], son[N], top[N], idx[N], num[N];
 7
 8
        inline void prepare() {
 9
            vector<int> queue;
10
            queue.push back(1);
11
            father[1] = height[1] = 0;
12
            for (int head = 0; head < (int)queue.size(); ++head) {</pre>
13
                 int x = queue[head];
14
                 for (int i = 0; i < (int)adj[x].size(); ++i) {</pre>
15
                     int y = adj[x][i];
16
                     if (y != father[x]) {
17
                         queue.push_back(y);
18
                         height[y] = height[x] + 1;
19
                         father[y] = x;
20
                     }
21
                 }
22
23
            for (int i = n - 1; i \ge 0; —i) {
24
                int x = queue[i];
25
                size[x] = 1;
26
                son[x] = -1;
                 for (int j = 0; j < (int)adj[x].size(); ++j) {</pre>
27
28
                     int y = adj[x][j];
29
                     if (y != father[x]) {
30
                         size[x] += size[y];
```

4.3. 可持久化左偏树 87

```
31
                         if (son[x] == -1 \mid | size[son[x]] < size[y]) {
32
                              son[x] = y;
33
                         }
34
                     }
35
                 }
36
37
            int tot = 0;
38
            fill(top + 1, top + n + 1, 0);
39
            for (int i = 0; i < n; ++i) {</pre>
40
                 int x = queue[i];
                 if (top[x] == 0) {
41
42
                     for (int y = x; y != -1; y = son[y]) {
43
                         top[y] = x;
44
                         idx[y] = ++tot;
45
                         num[tot] = //data[y];
46
                     }
47
                 }
48
            }
49
            build(1, 1, n);
50
51
52
        inline void handle(int x, int y) {
53
            for (; true; ) {
54
                 if (top[x] == top[y]) {
                     if (x == y) {
55
56
                         handle(1, 1, n, idx[x], idx[x]);
57
                     } else {
                         if (height[x] < height[y]) {</pre>
58
59
                              handle(1, 1, n, idx[x], idx[y]);
60
                         } else {
61
                              handle(1, 1, n, idx[y], idx[x]);
62
                         }
63
                     }
64
                     break;
65
                 if (height[top[x]] > height[top[y]]) {
66
                     handle(1, 1, n, idx[top[x]], idx[x]);
67
                     x = father[top[x]];
68
69
                 } else {
70
                     handle(1, 1, n, idx[top[y]], idx[y]);
71
                     y = father[top[y]];
72
                 }
73
            }
74
        }
75
   }
```

4.3 可持久化左偏树

```
Node * persiMerge(Node * a, Node * b) {
 1
        if(!a) return b;
 2
 3
        if(!b) return a;
 4
        Node * res;
 5
        if(a\rightarrow v < b\rightarrow v)  {
 6
            res = new Node(*a);
 7
            res->s[1] = persiMerge(b, res->s[1]);
 8
        }else {
 9
            res = new Node(*b);
10
            res->s[1] = persiMerge(a, res->s[1]);
11
12
        if(!res->s[0] or res->s[1] and res->s[0]->1 < res->s[1]->1)
13
            swap(res->s[0], res->s[1]);
14
        res->1 = res->s[1]?res->s[1]->1 + 1:0;
15
        return res;
16 }
    4.4
           treap
   namespace treap {
        struct node {
 2
 3
            node *left, *right;
 4
            int key;
 5
            int size, count, aux;
 6
            inline node(int aux) {
 7
                left = right = 0;
 8
                key = size = count = 0;
 9
                aux = _aux;
10
11
            inline void update() {
12
                this->size = this->left->size + this->count + this->right->size;
13
            }
14
        };
15
16
        node *null;
17
        inline void print(node *&x) {
18
19
            if (x == null) {
20
                return;
21
            }
22
            print(x->left);
23
            printf("%d_{\sqcup}", x->key);
24
            print(x->right);
25
        }
```

26 27

28

29

inline node* create(int key) {

x->key = key;

node *x = new node(rand() % INT MAX);

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```
30
             x\rightarrow count = x\rightarrow size = 1;
31
             x\rightarrow left = x\rightarrow right = null;
32
             return x;
33
         }
34
         inline void left_rotate(node *&x) {
35
36
             node *y = x->right;
37
             x->right = y->left;
38
             y\rightarrow left = x;
39
             x->update();
40
             y->update();
41
             x = y;
42
         }
43
44
         inline void right_rotate(node *&x) {
45
             node *y = x\rightarrowleft;
46
             x\rightarrow left = y\rightarrow right;
47
             y->right = x;
48
             x->update();
49
             y->update();
50
             x = y;
51
         }
52
53
         inline void insert(node *&x, int key) {
54
             if (x == null) {
55
                  x = create(key);
56
                  return;
57
58
             if (x->key == key) {
59
                  x->count++;
60
             } else if (x->key > key) {
61
                  insert(x->left, key);
62
                  if (x->left->aux < x->aux) {
63
                       right_rotate(x);
64
             } else {
65
66
                  insert(x->right, key);
67
                  if (x->right->aux < x->aux) {
68
                       left_rotate(x);
69
                  }
70
             }
             x->update();
71
72
73
74
         inline void erase(node *&x, int key) {
             if (x == null) {
75
76
                  return;
77
78
             if (x->key == key) {
```

```
79
                  if (x\rightarrow count > 1) {
80
                      x->count--;
81
                  } else if (x->left == null && x->right == null) {
82
                      delete(x);
83
                      x = null;
84
                      return;
85
                  \} else if (x->left->aux < x->right->aux) {
86
                      right_rotate(x);
87
                      erase(x->right, key);
88
                  } else {
89
                      left_rotate(x);
90
                      erase(x->left, key);
91
              } else if (x->key > key) {
92
93
                  erase(x\rightarrowleft, key);
94
              } else {
95
                  erase(x->right, key);
96
97
             x->update();
98
         }
99
100
         inline void prepare() {
101
             null = new node(INT MAX);
102
         }
103 }
```

4.5 functional treap

```
namespace functional_treap {
 1
 2
        struct node {
 3
            int size;
 4
            node *left, *right;
 5
            inline node(node *_left, node *_right) {
 6
                left = _left;
                right = _right;
 7
 8
            inline node* update() {
 9
10
                size = left->size + 1 + right->size;
11
                return this;
12
13
            inline pair<node*, node*> split(int);
14
        };
15
        node* null;
16
17
18
        inline bool random(int x, int y) {
19
            return rand() % (x + y) < x;
20
        }
```

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```
21
22
        inline node* mergy(node* x, node* y) {
23
            if (x == null) {
24
                return y;
25
26
            if (y == null) {
27
                return x;
28
29
            if (random(x->size, y->size)) {
30
                x\rightarrow right = mergy(x\rightarrow right, y);
31
                return x->update();
32
33
            y->left = mergy(x, y->left);
34
            return y->update();
35
        }
36
37
        inline pair<node*, node*> node::split(int n) {
38
            if (this == null) {
39
                return make pair(null, null);
40
            if (n <= left->size) {
41
                pair<node*, node*> ret = left->split(n);
42
43
                left = null;
44
                return make_pair(ret.first, mergy(ret.second, this->update()));
45
46
            pair<node*, node*> ret = right->split(n - left->size);
47
            right = null;
48
            return make_pair(mergy(this->update(), ret.first), ret.second);
49
        }
50
51
        inline void prepare() {
52
            null = new node(null, null);
53
            null->left = null->right = null;
54
        }
55 }
```

4.6 LCT

```
1
   namespace link_cut_tree {
2
        struct node {
3
            node *child[2], *father;
 4
            bool head, rev;
            int val, sum, size;
5
 6
            inline node() {
                head = rev = val = sum = size = 0;
7
8
9
            inline void set(node *temp, int dir) {
10
                child[dir] = temp;
```

```
11
                temp->father = this;
12
            inline int which() {
13
14
                return father->child[1] == this;
15
16
            inline void update() {
17
                sum = val + child[0]->sum + child[1]->sum;
18
                size = 1 + child[0]->size + child[1]->size;
19
20
            inline void release() {
21
                if (rev) {
22
                    child[0]->reverse();
23
                    child[1]->reverse();
24
                    rev = 0;
25
                }
26
            }
27
            inline void reverse() {
28
                if (size == 0) {
29
                    return;
30
                rev ^= 1;
31
32
                swap(child[0], child[1]);
33
            }
34
        };
35
36
        node *null, *tree[N];
37
38
        inline node* create(int val) {
39
            node *temp = new node();
40
            temp->val = temp->sum = val;
            temp->size = 1;
41
42
            temp->child[0] = temp->child[1] = temp->father = null;
43
            temp->head = true;
44
            return temp;
45
        }
46
47
        inline void rotate(node *root) {
48
            node *father = root->father;
49
            father->release();
50
            root->release();
51
            int dir = root->which();
52
            father->set(root->child[!dir], dir);
53
            if (father->head) {
54
                father->head = false;
55
                root->head = true;
56
                root->father = father->father;
57
            } else {
58
                father->father->set(root, father->which());
59
```

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```
60
             root->set(father, !dir);
 61
             father->update();
 62
         }
 63
         inline void splay(node *root) {
 64
 65
             for (root->release(); !root->head; ) {
 66
                 if (root->father->head) {
 67
                     rotate(root);
68
                 } else {
 69
                     root->which() == root->father->which() ? (rotate(root->father),
                         rotate(root)) : (rotate(root), rotate(root));
 70
 71
             }
 72
             root->update();
 73
         }
 74
 75
         inline void access(node *root) {
 76
             for (node *temp = null; root != null; temp = root, root = root->father) {
 77
                 splay(root);
 78
                 root->child[1]->head = true;
 79
                 root->child[1] = temp;
 80
                 root->child[1]->head = false;
 81
                 root->update();
 82
             }
 83
         }
 84
 85
         inline void link(int son, int father) {
 86
             access(tree[son]);
 87
             splay(tree[son]);
 88
             tree[son]->father = tree[father];
 89
             tree[son]->reverse();
 90
         }
 91
 92
         inline void cut(int x, int y) {
 93
             access(tree[y]);
 94
             splay(tree[x]);
 95
             if (tree[x]->father == tree[y]) {
 96
                 tree[x]->father = null;
 97
             } else {
98
                 access(tree[x]);
99
                 splay(tree[y]);
100
                 if (tree[y]->father == tree[x]) {
                     tree[y]->father = null;
101
102
                 }
103
             }
104
         }
105
106
         inline void handle(int x, int y) {
```

107

access(tree[x]);

```
108
             node *root = tree[y];
109
             for (node *temp = null; root != null; temp = root, root = root->father) {
110
                 splay(root);
111
                 if (root->father == null) {
112
113
114
                 root->child[1]->head = true;
115
                 root->child[1] = temp;
116
                 root->child[1]->head = false;
117
                 root->update();
118
             }
119
         }
120
121
         inline void init(int n, int val[]) {
122
             for (int i = 1; i <= n; ++i) {</pre>
123
                 tree[i] = create(val[i]);
124
             }
125
         }
126
127
         inline void prepare() {
             null = new node();
128
129
             null->child[0] = null->child[1] = null->father = null;
130
         }
131 }
```

4.7 Splay

```
1 namespace splay {
        struct node {
 2
 3
            node *child[2], *father;
            int val, sum, size;
 4
 5
            inline node() {
 6
                val = sum = size = 0;
 7
 8
            inline int which() {
 9
                return father->child[1] == this;
10
11
            inline void set(node *temp, int dir) {
12
                child[dir] = temp;
13
                temp->father = this;
14
15
            inline void update() {
16
                sum = val + child[0]->sum + child[1]->sum;
17
                size = 1 + child[0]->size + child[1]->size;
18
19
            inline void release() {
20
21
            }
```

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```
22
        };
23
24
        node *null, *head;
25
26
        inline void print(node *root) {
27
            if (root == null) {
28
                return;
29
30
            print(root->child[0]);
31
            printf("%d<sub>\(\)</sub>", root—>val);
            print(root->child[1]);
32
33
34
        inline node* create(int val = 0) {
35
36
            node *temp = new node();
37
            temp->val = val;
            temp->child[0] = temp->child[1] = temp->father = null;
38
39
            return temp;
40
        }
41
        inline void rotate(node *root) {
42
43
            node *father = root->father;
44
            int dir = root->which();
45
            father->release();
46
            root->release;
47
            father->set(root->child[!dir], dir);
48
            father->father->set(root, father->which());
49
            root->set(father, !dir);
50
            if (father == head) {
51
                head = root;
52
53
            father->update();
54
        }
55
56
        inline void splay(node *root, node *target) {
57
            for (root->release(); root->father != target; ) {
58
                if (root->father->father == target) {
59
                     rotate(root);
60
                } else {
61
                     root->which() == root->father->which() ? (rotate(root->father),
                        rotate(root)) : (rotate(root), rotate(root));
62
                }
63
            }
64
            root->update();
65
66
67
        inline int rank(node *root) {
68
            splay(root, null);
69
            return root->child[0]->size + 1;
```

```
70
         }
 71
 72
         inline node* find(int rank) {
 73
             node *now = head;
 74
             for (; now->child[0]->size + 1 != rank; ) {
 75
                 now->release();
 76
                 if (now->child[0]->size + 1 > rank) {
 77
                      now = now->child[0];
 78
                  } else {
 79
                      rank -= now->child[0]->size + 1;
 80
                      now = now->child[1];
 81
                  }
 82
             }
 83
             return now;
 84
         }
 85
 86
         inline void splay(int left, int right) {
 87
             splay(find(right), null);
 88
             splay(find(left), head);
 89
         }
 90
 91
         inline node* insert(int pos, int val) {
 92
             splay(pos, pos + 1);
 93
             node *now = head->child[0];
 94
             node *cur = create(val);
 95
             now->set(cur, 1);
 96
             splay(cur, null);
 97
             return head;
 98
         }
 99
100
         inline void insert(int pos, int n, int val[]) {
101
             splay(pos, pos + 1);
102
             node *now = head->child[0];
103
             for (int i = 1; i <= n; ++i) {</pre>
104
                 node *cur = create(val[i]);
105
                 now->set(cur, 1);
106
                 now = cur;
107
108
             splay(now, null);
109
110
111
         inline void erase(node *root) {
112
             int pos = rank(root);
113
             splay(pos - 1, pos + 1);
114
             head->child[0]->child[1] = null;
115
             head->child[0]->update();
116
             head->update();
117
         }
118
```

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```
119
        inline int query(int left, int right) {
120
             splay(left - 1, right + 1);
121
            return head->child[0]->child[1]->sum;
122
        }
123
        inline void prepare() {
124
125
            null = new node();
126
            head = create();
127
            node *tail = create();
128
            head->set(tail, 1);
129
            splay(tail, null);
130
        }
131 }
```

Chapter 5

图论

5.1 Gabow 算法求点双连通分量 (非递归)

```
边 (u, v) 属于 min(color[u], color[v]) 这个点双连通分量.
```

```
1 int color[222222], siz[222222], cnt[222222];
2 long long ans[222222];
3 vector<int> edges[222222];
4 vector<pair<int, int> > st0, st2;
5 vector<int> st1;
6 void psh(int v) {
7
        st0.push back(make pair(v, 0));
        color[v] = st1.size();
8
9
        st1.push_back(v);
  }
10
   int main() {
11
12
        freopen("travel.in", "r", stdin);
        freopen("travel.out", "w", stdout);
13
14
        int n, m;
        scanf("%d%d", &n, &m);
15
        for(int i(1); i <= m; i++) {</pre>
16
17
            int x, y;
            scanf("%d%d", &x, &y);
18
19
            edges[x].push_back(y);
20
            edges[y].push_back(x);
21
        }
22
        int c(n);
23
        fill(color + 1, color + 1 + n, 0);
        fill(ans + 1, ans + 1 + n, 0);
24
25
        fill(cnt + 1, cnt + 1 + n, 0);
26
        fill(siz + 1, siz + 1 + n, 0);
        for(int i(1); i <= n; i++) if(!color[i]) {</pre>
27
28
            psh(i);
            while(!st0.empty()) {
29
30
```

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```
31
                int v(st0.back().first), p(st0.back().second++);
32
                if(p != (int)edges[v].size()) {
33
                    int y(edges[v][p]);
34
                    if(!color[y]) {
35
                        psh(y);
36
                        st2.push back(make pair(color[v], color[y]));
37
                    }else
38
                        while(!st2.empty() and st2.back().first > color[y])
39
                            st2.pop_back();
40
                }else {
41
                    st0.pop_back();
42
                    siz[v]++;
43
                    if(color[v] == 1)
44
                        color[v] = c;
                    else {
45
46
                        int fa(st0.back().first);
47
                        if(st2.back().second == color[v]) {
48
                            st2.pop_back();
49
                            color[v] = ++c;
50
                            while(st1.back() != v) {
51
                                 color[st1.back()] = c;
52
                                 st1.pop back();
53
                             }
54
                            st1.pop_back();
55
                            ans[fa] += (long long)cnt[fa] * siz[v];
56
                            cnt[fa] += siz[v];
57
58
                        siz[fa] += siz[v];
59
60
                    ans[v] += (long long)(n - cnt[v]) * cnt[v] + n - cnt[v] - 1;
61
                }
62
            }
63
64
        for(int i(1); i <= n; i++) {</pre>
            cout << ans[i] << endl;//ans[i]:删去点i后, 无法连通的{a, b}数, 其中a, b
65
               为图中不同节点且无序.
66
67
       fclose(stdin);
68
        fclose(stdout);
69
       return 0;
70
```

5.2 Hopcroft Karp 求二分图最大匹配 $O(EV^{0.5})$

```
    // hint :: 全部都是 Obase
    // 用的时候, 建好边, 左边n个点, 右边m个点, 直接调用 maxMatch即可
```

```
4 const int N = 3333;
5
6 vector<int> e[N];
7 int pairx[N], pairy[N], level[N];
8 int n, m;
9
10 bool dfs(int x) {
11
        for(int i = 0; i < (int)e[x].size(); i++) {</pre>
12
            int y = e[x][i];
13
            int w = pairy[y];
            if (w == -1 \mid | level[x] + 1 == level[w] && dfs(w)) {
14
15
                 pairx[x] = y;
16
                 pairy[y] = x;
17
                 return true;
18
            }
19
20
        level[x] = -1;
21
        return false;
22 }
23
24 int maxMatch() {
25
        fill(pairx, pairx + n, -1);
26
        fill(pairy, pairy + m, -1);
27
        for(int answer = 0; ; ) {
28
            vector<int> queue;
29
            for(int i = 0; i < n; i++) {</pre>
30
31
                 if (pairx[i] == -1) {
                     level[i] = 0;
32
33
                     queue.push_back(i);
34
                 } else {
35
                     level[i] = -1;
36
                 }
37
            }
38
            for(int head = 0; head < (int)queue.size(); head++) {</pre>
39
40
                 int x = queue[head];
41
                 for(int i = 0; i < (int)e[x].size(); i++) {</pre>
42
                     int y = e[x][i];
43
                     int w = pairy[y];
44
                     if (w != -1 \&\& level[w] < 0) {
                         level[w] = level[x] + 1;
45
                         queue.push back(w);
46
47
                     }
48
                 }
49
            }
50
51
            int delta = 0;
52
            for(int i = 0; i < n; i++) {</pre>
```

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```
53
                 if (pairx[i] == -1 \&\& dfs(i)) {
54
                      delta++;
55
                 }
56
57
             if (delta == 0) {
58
                 return answer;
59
             } else {
60
                 answer += delta;
61
             }
62
        }
63
    }
64
65
    int solve() {
66
        int timing;
67
        scanf("%d", &timing);
68
69
        static int x[N], y[N], s[N];
70
        scanf("%d", &n);
71
        for(int i = 0; i < n; i++) {</pre>
             scanf("%d_{\perp}%d_{\parallel}%d", &x[i], &y[i], &s[i]);
72
73
             e[i].clear();
74
        }
75
76
        scanf("%d", &m);
77
        for(int i = 0; i < m; i++) {</pre>
78
             int xx, yy;
79
             scanf("%d_{\square}%d", &xx, &yy);
             for(int j = 0; j < n; j++) {</pre>
80
                 if (timing * timing * s[j] * s[j] >= (xx - x[j]) * (xx - x[j]) + (yy - y[
81
                     j]) * (yy - y[j])) {
82
                     e[j].push_back(i);
83
                 }
84
             }
85
        }
86
87
        return maxMatch();
88
    }
89
90
   int main() {
91
        freopen("input.txt", "r", stdin);
92
        int test;
        scanf("%d", &test);
93
94
        while(test---) {
95
             static int testCount = 0;
96
             printf("Scenario_#%d:\n", ++testCount);
97
             printf("%d\n", solve());
98
            puts("");
99
```

100

return 0;

5.3. 最小树形图 103

101 }

5.3 最小树形图

```
const int maxn=1100;
1
3
   int n,m , g[maxn][maxn] , used[maxn] , pass[maxn] , eg[maxn] , more , queue[maxn];
 4
 5
   void combine (int id , int &sum ) {
 6
        int tot = 0 , from , i , j , k ;
7
        for ( ; id!=0 && !pass[ id ] ; id=eg[id] ) {
8
            queue[tot++]=id ; pass[id]=1;
9
        for ( from=0; from<tot && queue[from]!=id ; from++);</pre>
10
11
        if (from==tot) return;
12
        more = 1;
13
        for ( i=from ; i<tot ; i++) {</pre>
14
            sum+=g[eg[queue[i]]][queue[i]] ;
            if ( i!=from ) {
15
16
                 used[queue[i]]=1;
17
                 for ( j = 1 ; j <= n ; j++) if ( !used[j] )</pre>
18
                     if ( g[queue[i]][j]<g[id][j] ) g[id][j]=g[queue[i]][j] ;</pre>
19
            }
2.0
21
        for ( i=1; i<=n ; i++) if ( !used[i] && i!=id ) {</pre>
22
            for ( j=from ; j<tot ; j++){</pre>
23
                k=queue[j];
                 if ( g[i][id]>g[i][k]-g[eg[k]][k] ) g[i][id]=g[i][k]-g[eg[k]][k];
24
25
            }
26
        }
27
   }
28
29
   int mdst( int root ) { // return the total length of MDST
30
        int i , j , k , sum = 0 ;
        memset ( used , 0 , sizeof ( used ) ) ;
31
        for ( more =1; more ; ) {
32
33
            more = 0;
34
            memset (eg,0,sizeof(eg));
35
            for ( i=1 ; i <= n ; i ++) if ( !used[i] && i!=root ) {</pre>
36
                 for ( j=1 , k=0 ; j <= n ; j ++) if ( !used[j] && i!=j )</pre>
                     if ( k==0 || g[j][i] < g[k][i] ) k=j;</pre>
37
38
                eg[i] = k ;
39
40
            memset(pass,0,sizeof(pass));
            for ( i=1; i<=n ; i++) if ( !used[i] && !pass[i] && i!= root ) combine ( i ,</pre>
41
                sum ) ;
42
        for ( i =1; i<=n ; i ++) if ( !used[i] && i!= root ) sum+=g[eg[i]][i];</pre>
43
```

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```
44
        return sum ;
45
   }
46
47
48
   int main(){
       freopen("input.txt", "r", stdin);
49
50
       freopen("output.txt","w",stdout);
51
       int i,j,k,test,cases;
52
       cases=0;
53
       scanf("%d", &test);
       while (test){
54
55
            test--;
56
            //if (n==0) break;
57
            scanf("%d%d",&n,&m);
58
   //
            memset(g,60,sizeof(g));
59
            foru(i,1,n)
60
              foru(j,1,n) g[i][j]=1000001;
61
            foru(i,1,m) {
                scanf("%d%d",&j,&k);
62
63
                j++;k++;
                scanf("%d",&g[j][k]);
64
65
            }
66
            cases++;
            printf("Case_#%d:_",cases);
67
68
            k=mdst(1);
69
            if (k>1000000) printf("Possums!\n"); //===no
70
            else printf("%d\n",k);
71
        }
72
73
       return 0;
74 }
```

5.4 KM

```
1 #include <cstdio>
 2 #include <cstdlib>
   #include <algorithm>
 4 #include <vector>
 5 #include <cstring>
 6
  #include <string>
 7
   #include <iostream>
 8
   #define foreach(e, x) for(__typeof(x.begin()) e = x.begin(); e != x.end(); ++e)
 9
10
11 using namespace std;
12
13 const int N = 333;
14 const int INF = (1 << 30);
```

5.4. KM 105

```
15
   int mat[N][N], lx[N], ly[N], vx[N], vy[N], slack[N];
16
17
   int n, match[N];
18
   bool find(int x) {
19
20
        vx[x] = 1;
21
        for(int i = 1; i <= n; i++) {</pre>
22
            if (vy[i]) {
23
                 continue;
24
25
            int temp = lx[x] + ly[i] - mat[x][i];
26
            if (temp == 0) {
                 vy[i] = 1;
27
                 if (match[i] == -1 \mid | find(match[i])) {
28
29
                     match[i] = x;
30
                     return true;
31
                 }
32
            } else {
33
                 slack[i] = min(slack[i], temp);
34
35
36
        return false;
37
38
39
   int KM() {
40
        for(int i = 1; i <= n; i++) {</pre>
41
            lx[i] = -INF;
42
            ly[i] = 0;
            match[i] = -1;
43
44
            for(int j = 1; j <= n; j++) {</pre>
45
                 lx[i] = max(lx[i], mat[i][j]);
46
            }
47
48
        for(int i = 1; i <= n; i++) {</pre>
49
            for(int j = 1; j <= n; j++) {</pre>
50
                 slack[j] = INF;
51
52
            for(; ;) {
53
                 memset(vx, 0, sizeof(vx));
54
                 memset(vy, 0, sizeof(vy));
55
                 for(int j = 1; j <= n; j++) {
                     slack[j] = INF;
56
57
58
                 if (find(i)) {
59
                     break;
60
61
                 int delta = INF;
62
                 for(int j = 1; j <= n; j++) {</pre>
63
                     if (!vy[j]) {
```

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```
64
                          delta = min(delta, slack[j]);
65
                      }
66
                 }
67
                 for(int j = 1; j <= n; j++) {</pre>
                      if (vx[j]) {
68
69
                          lx[j] -= delta;
70
71
                      if (vy[j]) {
72
                          ly[j] += delta;
73
                      } else {
74
                          slack[j] -= delta;
75
                      }
76
                 }
77
             }
78
        }
79
        int answer = 0;
80
        for(int i = 1; i <= n; i++) {</pre>
81
             answer += mat[match[i]][i];
82
83
        return answer;
84
    }
85
86
    int main() {
        while(scanf("%d", &n) != EOF) {
87
88
             for(int i = 1; i <= n; i++) {</pre>
89
                 for(int j = 1; j <= n; j++) {</pre>
                      scanf("%d", &mat[i][j]);
90
91
                 }
92
             }
93
             printf("%d\n", KM());
94
        }
95
        return 0;
96 }
```

5.5 扩展 KM

```
#include <cstdio>
#include <cstdlib>
#include <algorithm>
#include <iostream>
#include <cstring>
using namespace std;

const int N = 205;
const int inf = 100000000;

int a[N], b[N], c[N][N], vx[N], vy[N], w[N][N], dx[N], dy[N];
int ans, m, n, slack[N], lk[N], next[N];
```

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```
13
14 bool hungary(int x) {
15
        vx[x] = 1;
        for(int i = 1; i <= n; i++) {</pre>
16
17
            if (vy[i])
18
                continue;
19
            int delta = dx[x] + dy[i] - w[x][i];
20
            if (delta == 0) {
21
                vy[i] = 1;
22
                if (b[i]) {
                     lk[x] = i;
23
24
                     next[x] = 0;
25
                     return true;
26
27
                for(int j = 1; j <= m; j++) {</pre>
28
                     if (vx[j])
29
                         continue;
30
                     if (c[j][i] && hungary(j)) {
31
                         lk[x] = i;
32
                         next[x] = j;
33
                         return true;
34
                     }
35
                }
36
            } else {
                slack[i] = min(slack[i], delta);
37
38
            }
39
        }
40
        return false;
41
   }
42
43
   void travel(int x) {
44
        int flow = a[x];
45
        for(int i = x; i; i = next[i]) {
46
            if (next[i])
                flow = min(flow, c[next[i]][lk[i]]);
47
48
            else
                flow = min(flow, b[lk[i]]);
49
50
51
        a[x] = flow;
52
        for(int i = x; i; i = next[i]) {
53
            if (next[i])
54
                c[next[i]][lk[i]] -= flow;
55
            else
56
                b[lk[i]] -= flow;
57
            c[i][lk[i]] += flow;
58
        }
59
   }
60
61 int Main() {
```

```
scanf("%d_{\sqcup}%d", &m, &n);
 62
 63
          for(int i = 1; i <= m; i++)</pre>
 64
              scanf("%d", &a[i]);
         for(int i = 1; i <= n; i++)</pre>
 65
              scanf("%d", &b[i]);
 66
 67
          for(int i = 1; i <= m; i++)</pre>
 68
              for(int j = 1; j <= n; j++) {</pre>
                  scanf("%d", &w[i][j]);
 69
 70
                  w[i][j] *= -1;
 71
                  c[i][j] = 0;
 72
 73
         memset(dy, 0, sizeof(dy));
 74
          for(int i = 1; i <= m; i++) {</pre>
 75
              dx[i] = -inf;
 76
              for(int j = 1; j <= n; j++)</pre>
 77
                  dx[i] = max(dx[i], w[i][j]);
 78
 79
          for(int i = 1; i <= m; i++) {
 80
              while(1) {
                  for(int j = 1; j <= n; j++)</pre>
 81
 82
                       slack[j] = inf;
                  while (a[i]) {
 83
 84
                       fill(vx + 1, vx + m + 1, 0);
 85
                       fill(vy + 1, vy + n + 1, 0);
 86
                       if (hungary(i))
 87
                            travel(i);
 88
                       else
 89
                           break;
 90
 91
                  if (!a[i])
                       break;
 92
 93
                   int delta = inf;
 94
                   for(int j = 1; j \le n; j++)
 95
                       if (!vy[j])
 96
                           delta = min(delta, slack[j]);
                   for(int j = 1; j <= m; j++)</pre>
 97
 98
                       if (vx[j])
 99
                           dx[j] = delta;
100
                   for(int j = 1; j <= n; j++)</pre>
101
                       if (vy[j])
102
                           dy[j] += delta;
103
              }
104
105
         long long ans = 0;
106
          for(int i = 1; i <= m; i++)</pre>
107
              for(int j = 1; j <= n; j++) {</pre>
108
                  ans += (long long)c[i][j] * w[i][j];
109
110
         cout << -ans << endl;</pre>
```

5.6. 度限制生成树 109

```
111
         return 0;
112
    }
113
114 int main() {
115
         int testCount;
116
         scanf("%d", &testCount);
117
         while(testCount--) {
118
             Main();
119
120
         return 0;
121 }
```

5.6 度限制生成树

```
1 const int N = 55, M = 1010, INF = 1e8;
 2 int n, m, S, K, ans, cnt, Best[N], fa[N], FE[N];
 3 int f[N], p[M], t[M], c[M], o, Cost[N];
 4 bool u[M], d[M];
5 pair<int, int> MinCost[N];
 6 struct Edge {
7
        int a, b, c;
       bool operator < (const Edge & E) const { return c < E.c; }</pre>
8
9 }E[M];
10 vector<int> SE;
11 inline int F(int x) { return fa[x] == x ? x : fa[x] = F(fa[x]); }
12 inline void AddEdge(int a, int b, int C) {
        p[++o] = b; c[o] = C;
13
       t[o] = f[a]; f[a] = o;
14
15 }
16 void dfs(int i, int father) {
17
        fa[i] = father;
18
        if (father == S) Best[i] = -1;
19
        else {
20
            Best[i] = i;
21
            if (Cost[Best[father]] > Cost[i]) Best[i] = Best[father];
22
        for (int j = f[i]; j; j = t[j])
23
24
        if (!d[j] && p[j] != father) {
25
            Cost[p[j]] = c[j];
26
            FE[p[j]] = j;
27
            dfs(p[j], i);
28
        }
29
30
   inline void Kruskal() {
31
       cnt = n - 1; ans = 0; o = 1;
32
       for (int i = 1; i <= n; i++) fa[i] = i, f[i] = 0;</pre>
        sort(E + 1, E + m + 1);
33
34
        for (int i = 1; i <= m; i++) {
```

```
35
            if (E[i].b == S) swap(E[i].a, E[i].b);
36
            if (E[i].a != S && F(E[i].a) != F(E[i].b)) {
                fa[F(E[i].a)] = F(E[i].b);
37
38
                ans += E[i].c;
39
                cnt--;
40
                u[i] = true;
41
                AddEdge(E[i].a, E[i].b, E[i].c);
42
                AddEdge(E[i].b, E[i].a, E[i].c);
43
            }
44
45
        for (int i = 1; i <= n; i++) MinCost[i] = make_pair(INF, INF);</pre>
46
        for (int i = 1; i <= m; i++)</pre>
        if (E[i].a == S) {
47
48
            SE.push back(i);
49
            MinCost[F(E[i].b)] = min(MinCost[F(E[i].b)], make_pair(E[i].c, i));
50
51
        for (int i = 1; i <= n; i++)</pre>
52
        if (i != S && fa[i] == i) {
53
            dfs(E[MinCost[i].second].b, S);
54
            u[MinCost[i].second] = true;
55
            ans += MinCost[i].first;
56
        }
57
   }
58 bool Solve() {
59
        Kruskal();
60
        for (int i = cnt + 1; i <= K && i <= n; i++) {
61
            int MinD = INF, MinID = -1;
62
            for (int j = (int) SE.size() - 1; j \ge 0; j--)
63
            if (u[SE[j]])
64
                SE.erase(SE.begin() + j);
65
            for (int j = 0; j < (int) SE.size(); j++) {</pre>
66
                int tmp = E[SE[j]].c - Cost[Best[E[SE[j]].b]];
67
                if (tmp < MinD) {</pre>
68
                     MinD = tmp;
69
                     MinID= SE[j];
70
                }
71
72
            if (MinID == -1) return false;
73
            if (MinD >= 0) break;
74
            ans += MinD;
75
            u[MinID] = true;
            d[FE[Best[E[MinID].b]]] = d[FE[Best[E[MinID].b]] ^ 1] = true;
76
77
            dfs(E[MinID].b, S);
78
79
        return true;
80 }
```

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5.7 一般图匹配

```
1 const int N = 300;
 2 int n, Next[N], f[N], mark[N], visited[N], Link[N], Q[N], head, tail;
 3 vector <int> E[N];
 4 int getf(int x) { return f[x] == x ? x : f[x] = getf(f[x]); }
 5 void merge(int x, int y) { x = getf(x); y = getf(y); if (x != y) f[x] = y; }
 6 int LCA(int x, int y) {
 7
         static int flag = 0;
 8
         flag++;
 9
         for (; ; swap(x, y)) if (x != -1) {
10
             x = getf(x);
             if (visited[x] == flag) return x;
11
12
             visited[x] = flag;
13
             if (Link[x] != -1) x = Next[Link[x]];
14
             else x = -1;
15
16 }
17 void go(int a, int p) {
        while (a != p) {
18
19
             int b = Link[a], c = Next[b];
20
             if (getf(c) != p) Next[c] = b;
21
             if (mark[b] == 2) mark[Q[tail++] = b] = 1;
22
             if (mark[c] == 2) mark[Q[tail++] = c] = 1;
23
             merge(a, b); merge(b, c); a = c;
24
         }
25 }
26 void find(int s) {
         for (int i = 0; i < n; i++) {</pre>
27
             Next[i] = -1; f[i] = i;
28
29
             mark[i] = 0; visited[i] = -1;
30
31
         head = tail = 0; Q[tail++] = s; mark[s] = 1;
         for (; head < tail && Link[s] == -1; ) {
32
33
             for (int i = 0, x = Q[head++]; i < (int)E[x].size(); i++) {
                   \textbf{if} \ (\texttt{Link}[\texttt{x}] \texttt{!= E}[\texttt{x}][\texttt{i}] \texttt{ \&\& getf}(\texttt{x}) \texttt{ != getf}(\texttt{E}[\texttt{x}][\texttt{i}]) \texttt{ \&\& mark}[\texttt{E}[\texttt{x}][\texttt{i}]] \texttt{ != 2) } 
34
                       {
35
                       int y = E[x][i];
36
                       if (mark[y] == 1) {
37
                           int p = LCA(x, y);
38
                           if (getf(x) != p) Next[x] = y;
39
                           if (getf(y) != p) Next[y] = x;
40
                           go(x, p);
41
                           go(y, p);
42
43
                       else if (Link[y] == -1) {
44
                           Next[y] = x;
45
                           for (int j = y; j != -1; ) {
46
                                int k = Next[j];
```

```
47
                             int tmp = Link[k];
48
                             Link[j] = k;
49
                             Link[k] = j;
50
                             j = tmp;
51
52
                         break;
53
                     }
54
                     else {
55
                         Next[y] = x;
56
                         mark[Q[tail++] = Link[y]] = 1;
57
                         mark[y] = 2;
58
                     }
59
                }
60
            }
61
        }
62
   }
63
   int main() {
64
        for (int i = 0; i < n; i++) Link[i] = -1;
        for (int i = 0; i < n; i++) if (Link[i] == -1) {
65
66
            find(i);
67
68
        int ans = 0;
69
        for (int i = 0; i < n; i++) ans += Link[i] != -1;
70
        return ans;
71
```

5.8 无向图最小割

```
1 const int V = 100;
 2 #define typec int
 3 const typec inf = 0x3f3f3f; // max of res
 4 const typec maxw = 1000; // maximum edge weight
 5 typec g[V][V], w[V]; //g[i][j] = g[j][i]
 6 int a[V], v[V], na[V];
 7
   typec mincut(int n) {
 8
        int i, j, pv, zj;
 9
       typec best = maxw * n * n;
10
        for (i = 0; i < n; i++) v[i] = i; // vertex: 0 ~ n-1</pre>
11
       while (n > 1) {
12
            for (a[v[0]] = 1, i = 1; i < n; i++) {
13
                a[v[i]] = 0; na[i - 1] = i;
                w[i] = g[v[0]][v[i]];
14
15
            for (pv = v[0], i = 1; i < n; i++) {
16
                for (zj = -1, j = 1; j < n; j++)
17
18
                    if (!a[v[j]] && (zj < 0 || w[j] > w[zj]))
19
                        zj = j;
20
                a[v[zj]] = 1;
```

5.9. HAMILTON 回路 113

```
21
                if (i == n - 1) {
22
                     if (best > w[zj]) best = w[zj];
23
                     for (i = 0; i < n; i++)
24
                         g[v[i]][pv] = g[pv][v[i]] +=
25
                             g[v[zj]][v[i]];
26
                     v[zj] = v[--n];
27
                     break;
28
                }
29
                pv = v[zj];
30
                for (j = 1; j < n; j++)
31
                     if(!a[v[j]])
32
                         w[j] += g[v[zj]][v[j]];
33
            }
34
35
        return best;
36 }
```

5.9 Hamilton 回路

```
1 bool graph[N][N];
 2 int n, l[N], r[N], next[N], last[N], s, t;
   char buf[10010];
 4 void cover(int x) { l[r[x]] = l[x]; r[l[x]] = r[x]; }
5 int adjacent(int x) {
 6
        for (int i = r[0]; i <= n; i = r[i]) if (graph[x][i]) return i;</pre>
7
        return 0;
   }
8
9
   int main() {
10
        scanf("%d\n", &n);
11
        for (int i = 1; i <= n; ++i) {</pre>
12
            gets(buf);
13
            string str = buf;
14
            istringstream sin(str);
15
            int x;
16
            while (\sin >> x) {
17
                 graph[i][x] = true;
18
19
            1[i] = i - 1;
20
            r[i] = i + 1;
21
22
        for (int i = 2; i <= n; ++i)</pre>
23
            if (graph[1][i]) {
24
                 s = 1;
25
                t = i;
26
                cover(s);
27
                cover(t);
28
                next[s] = t;
29
                break;
```

```
30
            }
31
        while (true) {
            int x;
32
33
            while (x = adjacent(s)) {
34
                next[x] = s;
35
                s = x;
36
                cover(s);
37
38
            while (x = adjacent(t)) {
39
                next[t] = x;
40
                t = x;
41
                cover(t);
42
            if (!graph[s][t]) {
43
44
                 for (int i = s, j; i != t; i = next[i])
45
                     if (graph[s][next[i]] && graph[t][i]) {
46
                         for (j = s; j != i; j = next[j])
47
                              last[next[j]] = j;
48
                         j = next[s];
49
                         next[s] = next[i];
50
                         next[t] = i;
51
                         t = j;
52
                         for (j = i; j != s; j = last[j])
53
                              next[j] = last[j];
54
                         break;
55
                     }
56
57
            next[t] = s;
58
            if (r[0] > n)
59
                break;
60
            for (int i = s; i != t; i = next[i])
61
                if (adjacent(i)) {
62
                     s = next[i];
                     t = i;
63
64
                     next[t] = 0;
65
                     break;
66
                }
67
68
        for (int i = s; ; i = next[i]) {
69
            if (i == 1) {
                printf("%d", i);
70
71
                for (int j = next[i]; j != i; j = next[j])
                     printf("⊔%d", j);
72
73
                printf("_{\sqcup}%d\n", i);
74
                break;
75
76
            if (i == t)
77
                break;
78
        }
```

5.10. 弦图判定 115

79 }

5.10 弦图判定

```
1 int n, m, first[1001], 1, next[2000001], where[2000001],f[1001], a[1001], c[1001], L
       [1001], R[1001],
 2 v[1001], idx[1001], pos[1001];
 3 bool b[1001][1001];
5 int read(){
 6
       char ch;
7
        for (ch = getchar(); ch < '0' || ch > '9'; ch = getchar());
8
        int cnt = 0;
9
        for (; ch >= '0' && ch <= '9'; ch = getchar()) cnt = cnt * 10 + ch - '0';
10
        return(cnt);
11 }
12
13
   inline void makelist(int x, int y){
14
       where[++1] = y;
        next[l] = first[x];
15
16
        first[x] = 1;
17
   }
18
19 bool cmp(const int &x, const int &y){
       return(idx[x] < idx[y]);</pre>
21 }
22
23 int main(){
       //freopen("1015.in", "r", stdin);
24
25
       // freopen("1015.out", "w", stdout);
        for (;;)
26
27
        {
28
            n = read(); m = read();
29
            if (!n && !m) return 0;
30
            memset(first, 0, sizeof(first)); 1 = 0;
31
            memset(b, false, sizeof(b));
            for (int i = 1; i <= m; i++)</pre>
32
33
            {
34
                int x = read(), y = read();
35
                if (x != y \&\& !b[x][y])
36
37
                   b[x][y] = true; b[y][x] = true;
38
                   makelist(x, y); makelist(y, x);
39
                }
40
41
            memset(f, 0, sizeof(f));
42
            memset(L, 0, sizeof(L));
43
            memset(R, 255, sizeof(R));
```

```
44
            L[0] = 1; R[0] = n;
45
            for (int i = 1; i <= n; i++) c[i] = i, pos[i] = i;</pre>
            memset(idx, 0, sizeof(idx));
46
            memset(v, 0, sizeof(v));
47
            for (int i = n; i; --i)
48
49
50
                int now = c[i];
51
                R[f[now]]--;
52
                if (R[f[now]] < L[f[now]]) R[f[now]] = -1;
53
                idx[now] = i; v[i] = now;
54
                for (int x = first[now]; x; x = next[x])
55
                    if (!idx[where[x]])
56
                     {
57
                        swap(c[pos[where[x]]], c[R[f[where[x]]]]);
58
                        pos[c[pos[where[x]]]] = pos[where[x]];
59
                        pos[where[x]] = R[f[where[x]]];
60
                        L[f[where[x]] + 1] = R[f[where[x]]] --;
61
                        if (R[f[where[x]]] < L[f[where[x]]]) R[f[where[x]]] = -1;
                        if (R[f[where[x]] + 1] == -1)
62
                            R[f[where[x]] + 1] = L[f[where[x]] + 1];
63
64
                        ++f[where[x]];
65
                     }
66
            bool ok = true;
67
            //v是完美消除序列.
68
69
            for (int i = 1; i <= n && ok; i++)</pre>
70
71
                int cnt = 0;
72
                for (int x = first[v[i]]; x; x = next[x])
73
                     if (idx[where[x]] > i) c[++cnt] = where[x];
74
                sort(c + 1, c + cnt + 1, cmp);
75
                bool can = true;
76
                for (int j = 2; j <= cnt; j++)</pre>
77
                    if (!b[c[1]][c[j]])
78
                     {
79
                         ok = false;
80
                         break;
81
82
83
            if (ok) printf("Perfect\n");
84
            else printf("Imperfect\n");
85
            printf("\n");
86
        }
87
   }
```

5.11 弦图求团数

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```
int n, m, first[100001], next[2000001], where[2000001], l, L[100001], R[100001], c
       [100001], f[100001],
   pos[100001], idx[100001], v[100001], ans;
 4
   inline void makelist(int x, int y){
 5
        where[++1] = y;
 6
        next[l] = first[x];
7
        first[x] = 1;
8
   }
9
10 int read(){
11
        char ch;
12
        for (ch = getchar(); ch < '0' || ch > '9'; ch = getchar());
13
        for (; ch >= '0' && ch <= '9'; ch = getchar()) cnt = cnt * 10 + ch - '0';
14
15
        return(cnt);
16
   }
17
18 int main(){
        freopen("1006.in", "r", stdin);
freopen("1006.out", "w", stdout);
19
20
21
        memset(first, 0, sizeof(first)); 1 = 0;
22
        n = read(); m = read();
23
        for (int i = 1; i <= m; i++)</pre>
24
25
            int x, y;
26
            x = read(); y = read();
27
            makelist(x, y); makelist(y, x);
28
29
        memset(L, 0, sizeof(L));
30
        memset(R, 255, sizeof(R));
31
        memset(f, 0, sizeof(f));
32
        memset(idx, 0, sizeof(idx));
33
        for (int i = 1; i <= n; i++) c[i] = i, pos[i] = i;
        L[0] = 1; R[0] = n; ans = 0;
34
        for (int i = n; i; —i)
35
36
37
            int now = c[i], cnt = 1;
38
            idx[now] = i; v[i] = now;
39
            if (--R[f[now]] < L[f[now]]) R[f[now]] = -1;
40
            for (int x = first[now]; x; x = next[x])
41
                if (!idx[where[x]])
42
                     swap(c[pos[where[x]]], c[R[f[where[x]]]]);
43
44
                     pos[c[pos[where[x]]]] = pos[where[x]];
45
                     pos[where[x]] = R[f[where[x]]];
46
                     L[f[where[x]] + 1] = R[f[where[x]]] --;
47
                     if (R[f[where[x]]] < L[f[where[x]]]) R[f[where[x]]] = -1;
```

```
 \textbf{if} \ (\texttt{R[f[where[x]] + 1] == -1}) \ \texttt{R[f[where[x]] + 1] = L[f[where[x]] +} \\ 
48
                              1];
49
                         ++f[where[x]];
50
                    }
51
                    else ++cnt;
52
               ans = max(ans, cnt);
53
54
         printf("%d\n", ans);
55
    }
```

5.12 有根树的同构

```
//http://acm.sdut.edu.cn/judgeonline/showproblem?problem id=1861 ÓÐ ùÊ÷µÄͬ¹¹
 1
   const int mm=1051697,p=4773737;
   int m,n,first[101],where[10001],next[10001],1,hash[10001],size[10001],pos[10001];
 3
   long long f[10001],rt[10001];
 5 bool in[10001];
 6
 7
   inline void makelist(int x,int y){
 8
        where[++1]=y;
 9
        next[l]=first[x];
10
        first[x]=l;
11
   }
12
13
14
   inline void hashwork(int now){
15
        int a[1001],v[1001],tot=0;
16
        size[now]=1;
        for (int x=first[now];x;x=next[x])
17
18
19
            hashwork(where[x]);
20
            a[++tot]=f[where[x]];
21
            v[tot]=size[where[x]];
22
            size[now]+=size[where[x]];
23
24
        a[++tot]=size[now];
25
        v[tot]=1;
26
        int len=0;
27
        for (int i=1;i<=tot;i++)</pre>
28
           for (int j=i+1; j<=tot; j++)</pre>
29
              if (a[j]<a[i])
30
31
                  int u=a[i];a[i]=a[j];a[j]=u;
32
                 u=v[i];v[i]=v[j];v[j]=u;
33
              }
34
        f[now]=1;
35
        for (int i=1;i<=tot;i++)</pre>
36
           {
```

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```
f[now]=((f[now]*a[i])%p*rt[len])%p;
37
38
                   len+=v[i];
39
            }
40
    }
41
42
   int main(){
        //freopen("1.txt","r",stdin);
43
44
        //freopen("2.txt","w",stdout);
45
        scanf("%d%d",&n,&m);
46
        rt[0]=1;
47
        for (int i=1;i<=100;i++)</pre>
48
             rt[i]=(rt[i-1]*mm)%p;
49
        for (int i=1;i<=n;i++)</pre>
50
        {
51
             memset(first,0,sizeof(first));
52
             memset(in,false,sizeof(in));
53
             1=0;
54
             for (int j=1; j<m; j++)</pre>
55
56
                 int x,y;
                 scanf("%d%d",&x,&y);
57
58
                 makelist(x,y);
59
                 in[y]=true;
60
             }
61
             int root=0;
62
             for (int j=1; j<=m; j++)</pre>
63
             if (!in[j])
64
             {
65
                 root=j;
66
                 break;
67
             }
68
             memset(size,0,sizeof(size));
69
             memset(f,0,sizeof(f));
70
             hashwork(root);
71
             hash[i]=f[root];
72
73
        for (int i=1;i<=n;i++) pos[i]=i;</pre>
74
        memset(in,false,sizeof(in));
75
        for (int i=1;i<=n;i++)</pre>
         if (!in[i])
76
77
          {
                      printf("%d",i);
78
79
                      for (int j=i+1; j<=n; j++)</pre>
80
                      if (hash[j]==hash[i])
81
                      {
82
                           in[j]=true;
83
                           printf("=%d",j);
84
85
                      printf("\n");
```

```
86 }
87 }
```

5.13 zkw 费用流

```
1 #include <cstdio>
 2 #include <cstdlib>
 3 #include <algorithm>
 4 #include <cstring>
 5 #include <cmath>
 6 using namespace std;
 7
 8 const int N = 105 \ll 2, M = 205 * 205 * 2;
 9
   const int inf = 1000000000;
10
11
   struct eglist {
12
        int other[M], succ[M], last[N], cap[M], cost[M], sum;
13
        void clear() {
14
            memset(last, -1, sizeof(last));
15
            sum = 0;
16
17
        void _addEdge(int a, int b, int c, int d) {
18
            other[sum] = b, succ[sum] = last[a], last[a] = sum, cost[sum] = d, cap[sum++]
                = c;
19
        void addEdge(int a, int b, int c, int d) {
20
21
            _addEdge(a, b, c, d);
22
            addEdge(b, a, 0, -d);
23
        }
24
   }e;
25
26
   int n, m, S, T, tot, totFlow, totCost;
27
   int dis[N], slack[N], visit[N], cur[N];
28
29
   int modlable() {
30
        int delta = inf;
        for(int i = 1; i <= T; i++) {</pre>
31
32
            if (!visit[i] && slack[i] < delta)</pre>
33
                delta = slack[i];
34
            slack[i] = inf;
35
            cur[i] = e.last[i];
36
        if (delta == inf)
37
38
            return 1;
39
        for(int i = 1; i <= T; i++)</pre>
40
            if (visit[i])
41
                dis[i] += delta;
42
        return 0;
```

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```
43
   }
44
45
   int dfs(int x, int flow) {
46
        if (x == T) {
            totFlow += flow;
47
48
            totCost += flow * (dis[S] - dis[T]);
49
            return flow;
50
51
        visit[x] = 1;
52
        int left = flow;
53
        for(int &i = cur[x]; ~i; i = e.succ[i])
54
            if (e.cap[i] > 0 && !visit[e.other[i]]) {
55
                int y = e.other[i];
                if (dis[y] + e.cost[i] == dis[x]) {
56
57
                     int delta = dfs(y, min(left, e.cap[i]));
58
                     e.cap[i] -= delta;
59
                     e.cap[i ^ 1] += delta;
60
                     left -= delta;
61
                     if (!left)
62
                         return flow;
63
                } else {
64
                     slack[y] = min(slack[y], dis[y] + e.cost[i] - dis[x]);
65
66
            }
67
        return flow - left;
68 }
69
70 pair<int, int> minCost() {
71
        totFlow = 0, totCost = 0;
72
        fill(dis + 1, dis + T + 1, 0);
        for(int i = 1; i <= T; i++)</pre>
73
74
            cur[i] = e.last[i];
75
        do {
76
            do {
77
                fill(visit + 1, visit + T + 1, 0);
78
            } while(dfs(S, inf));
79
        } while(!modlable());
80
        return make_pair(totFlow, totCost);
81
   }
82
83
   void run() {
        scanf("%d_%d", &m, &n);
84
85
        e.clear();
        S = m + n + 1, T = m + n + 2;
86
87
        tot = 0;
        for(int i = 1; i <= m; i++) {</pre>
88
89
            int times;
90
            scanf("%d", &times);
91
            e.addEdge(S, i, times, 0);
```

```
92
 93
         for(int i = 1; i <= n; i++) {</pre>
 94
             int times;
 95
             scanf("%d", &times);
 96
             e.addEdge(i + m, T, times, 0);
 97
 98
         for(int i = 1; i <= m; i++)</pre>
 99
             for(int j = 1; j <= n; j++) {</pre>
100
                 int cost;
101
                  scanf("%d", &cost);
102
                 e.addEdge(i, j + m, inf, cost);
103
         pair<int, int> tmp = minCost();
104
105
         printf("%d\n", tmp.second);
106 }
107
108 int main() {
109
         int Test;
110
         scanf("%d", &Test);
111
         for(; Test--; run());
         return 0;
112
113 }
```

Chapter 6

字符串

6.1 扩展 KMP

```
传入字符串 s 和长度 N, next[i]=LCP(s, s[i..N-1])
 1 void z(char *s, int *next, int N)
2
   {
3
        int j = 0, k = 1;
 4
       while (j + 1 < N \&\& s[j] == s[j + 1]) ++ j;
       next[0] = N - 1; next[1] = j;
        for(int i = 2; i < N; ++ i) {</pre>
 6
7
            int far = k + next[k] - 1, L = next[i - k];
8
            if (L < far - i + 1) next[i] = L;
9
            else {
10
                j = max(0, far - i + 1);
                while (i + j < N \&\& s[j] == s[i + j]) ++ j;
11
                next[i] = j; k = i;
12
13
            }
14
       }
15 }
```

6.2 后缀数组

字符串后面会自动加上一个最小字符 \0.

```
const int N = 4 * int(1e5) + 10;

int n, m;
int sa[N], ta[N], tb[N], *rank = ta, *tmp = tb;
int height[N], myLog[N], f[N][20];
int str[N];

bool cmp(int i, int j, int l) {
   return tmp[i] == tmp[j] && tmp[i + 1] == tmp[j + 1];
}
```

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```
11
12
   void radixSort() {
13
        static int w[N];
14
        fill(w, w + m, 0);
        for (int i = 0; i < n; i++) {</pre>
15
16
            w[rank[i]]++;
17
18
        for (int i = 1; i < m; i++) {</pre>
19
            w[i] += w[i - 1];
20
21
        22
            sa[--w[rank[tmp[i]]]] = tmp[i];
23
        }
24
   }
25
   void suffixArray() {
26
27
        for (int i = 0; i < n; i++) {</pre>
28
            rank[i] = str[i];
29
            tmp[i] = i;
30
31
        radixSort();
32
        for (int j = 1, i, p; j < n; j <<= 1, m = p) {</pre>
33
            for (i = n - j, p = 0; i < n; i++) {
34
                tmp[p++] = i;
35
36
            for (i = 0; i < n; i++) {
                if (sa[i] >= j) {
37
38
                    tmp[p++] = sa[i] - j;
39
                }
40
            }
41
            radixSort();
42
            for (swap(tmp, rank), rank[sa[0]] = 0, i = p = 1; i < n; i++) {
43
                rank[sa[i]] = cmp(sa[i-1], sa[i], j) ? p-1 : p++;
44
            }
45
        for (int i = 0, j, k = 0; i < n; ++i, k = max(k - 1, 0)) {
46
47
            if (rank[i]) {
                j = sa[rank[i] - 1];
48
49
                for (; str[i + k] == str[j + k]; k++);
50
                height[rank[i]] = k;
51
            }
52
53
        for (int i = 2; i <= n; i++) {</pre>
54
            myLog[i] = myLog[i >> 1] + 1;
55
56
        for (int i = 1; i < n; i++) {</pre>
57
            f[i][0] = height[i];
58
59
        for (int j = 1; 1 << j <= n; j++) {
```

6.2. 后缀数组 125

```
60
             for (int i = 1; i + (1 << j) <= n; i++) {</pre>
 61
                  f[i][j] = min(f[i][j-1], f[i+(1 << j-1)][j-1]);
 62
             }
 63
         }
 64
 65
 66
    int lcp(int 1, int r) {
 67
         if (1 > r) {
 68
             return 0;
 69
 70
         int len = myLog[r - l + 1];
 71
         return min(f[l][len], f[r - (1 << len) + 1][len]);
 72
    }
 73
 74 int nBase, mBase;
 75 int cnt[N];
 76 char buf[N];
77
 78
    int pos(int x) {
79
         return x / (mBase << 1 | 1 );
 80
 81
 82
    int main() {
83
         n = 0;
 84
         m = 256;
 85
         scanf("%d%d", &nBase, &mBase);
         for (int i = 0; i < nBase; i++) {</pre>
 86
             scanf("%s", buf);
 87
             for (int j = 0; j < mBase; j++) {
 88
 89
                  str[n++] = buf[j];
90
 91
             for (int j = 0; j < mBase; j++) {</pre>
 92
                 str[n++] = buf[j];
 93
94
             str[n++] = i < nBase - 1 ? m++ : 0;
95
96
         suffixArray();
97
         int result = 0, total = 0;
98
         for (int i = 0, j = 0; i < n; i++) {</pre>
99
             for (; j < n && total < nBase; j++) {</pre>
100
                 int p = pos(sa[j]);
                 total += cnt[p]++ == 0;
101
102
             if (total == nBase) {
103
                 result = max(result, lcp(i + 1, j - 1));
104
105
106
             int p = pos(sa[i]);
107
             total -= --cnt[p] == 0;
108
         }
```

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```
109
         result = min(result, mBase);
110
         printf("%d\n", result);
111
         vector <int> ans(n);
112
         total = 0;
         memset(cnt, 0, sizeof(cnt));
113
114
         for (int i = 0, j = 0; i < n; i++) {
115
             for (; j < n && total < nBase; j++) {</pre>
116
                 int p = pos(sa[j]);
117
                 total += cnt[p]++ == 0;
118
119
             if (total == nBase && lcp(i + 1, j - 1) >= result) {
120
                  for (int k = i; k < j; k++) {
                      int p = pos(sa[k]);
121
122
                      ans[p] = sa[k] % (mBase << 1 | 1);
123
                 }
124
                 break;
125
             }
126
             int p = pos(sa[i]);
127
             total -= --cnt[p] == 0;
128
         for (int i = 0; i < nBase; i++) {</pre>
129
130
             printf("%d\n", ans[i] % mBase + 1);
131
         }
132
```

6.3 DC3

```
1 //`DC3 待排序的字符串放在r 数组中,从r[0]到r[n-1],长度为n,且最大值小于m.`
2 // 约定除r[n-1]外所有的r[i]都大于0, r[n-1]=0。
   //`函数结束后, 结果放在sa 数组中,从sa[0]到sa[n-1]。`
 4 //`r必须开长度乘3`
5 #define maxn 10000
6 #define F(x) ((x)/3+((x)%3==1?0:tb))
7
   #define G(x) ((x)<tb?(x)*3+1:((x)-tb)*3+2)
8
9
   int wa[maxn],wb[maxn],wv[maxn],wss[maxn];
10
   int s[maxn*3],sa[maxn*3];
11
   int c0(int *r,int a,int b)
12
13
       return r[a]==r[b]&&r[a+1]==r[b+1]&&r[a+2]==r[b+2];
14
   }
   int c12(int k,int *r,int a,int b)
15
16
17
       if(k==2) return r[a]<r[b]||r[a]==r[b]&&c12(1,r,a+1,b+1);</pre>
18
       else return r[a] < r[b] | | r[a] == r[b] \& wv[a+1] < wv[b+1];
19
20 void sort(int *r,int *a,int *b,int n,int m)
```

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```
21
   {
22
        int i;
23
        for(i=0;i<n;i++) wv[i]=r[a[i]];</pre>
24
        for(i=0;i<m;i++) wss[i]=0;</pre>
25
        for(i=0;i<n;i++) wss[wv[i]]++;</pre>
26
        for(i=1;i<m;i++) wss[i]+=wss[i-1];</pre>
27
        for(i=n-1;i>=0;i--) b[--wss[wv[i]]]=a[i];
28
   }
29 void dc3(int *r,int *sa,int n,int m)
30
   {
        int i,j,*rn=r+n,*san=sa+n,ta=0,tb=(n+1)/3,tbc=0,p;
31
32
        r[n]=r[n+1]=0;
33
        for(i=0;i<n;i++)</pre>
34
            if(i%3!=0) wa[tbc++]=i;
35
        sort(r+2,wa,wb,tbc,m);
36
        sort(r+1,wb,wa,tbc,m);
37
        sort(r,wa,wb,tbc,m);
38
        for(p=1,rn[F(wb[0])]=0,i=1;i<tbc;i++)</pre>
39
            rn[F(wb[i])]=c0(r,wb[i-1],wb[i])?p-1:p++;
40
        if (p<tbc) dc3(rn,san,tbc,p);</pre>
        else for (i=0;i<tbc;i++) san[rn[i]]=i;</pre>
41
42
        for (i=0;i<tbc;i++)</pre>
43
            if(san[i]<tb) wb[ta++]=san[i]*3;</pre>
44
        if(n%3==1) wb[ta++]=n-1;
45
        sort(r,wb,wa,ta,m);
        for(i=0;i<tbc;i++)</pre>
46
47
            wv[wb[i]=G(san[i])]=i;
48
        for(i=0,j=0,p=0;i<ta && j<tbc;p++)</pre>
49
            sa[p]=c12(wb[j]%3,r,wa[i],wb[j])?wa[i++]:wb[j++];
50
        for(;i<ta;p++) sa[p]=wa[i++];</pre>
51
        for(; j < tbc; p++) sa[p] = wb[j++];</pre>
52
   }
53
54
   int main(){
55
        int n, m=0;
        scanf("%d",&n);
56
57
        for (int i=0;i<n;i++) scanf("%d",&s[i]),s[i]++,m=max(s[i]+1,m);</pre>
58
        printf("%d\n",m);
59
        s[n++]=0;
60
        dc3(s,sa,n,m);
61
        62 }
```

6.4 AC 自动机

```
1 namespace aho_corasick_automation {
2    int const N = ;
3    struct node {
```

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```
4
            node *next[N], *fail;
 5
            int count;
             inline node() {
 6
 7
                 memset(next, 0, sizeof(next));
 8
                 fail = 0;
 9
                 count = 0;
10
            }
11
        };
12
13
        node *root;
14
15
        inline int idx(char x) {
16
            return x - 'a';
17
18
19
        inline void insert(node *x, char *str) {
20
             int len = (int)strlen(str);
21
             for (int i = 0; i < len; ++i) {</pre>
22
                 int c = idx(str[i]);
23
                 if (!x->next[c]) {
24
                     x->next[c] = new node();
25
26
                 x = x->next[c];
27
28
            x->count++;
29
        }
30
31
        inline void build() {
32
            vector<node*> queue;
            queue.push_back(root->fail = root);
33
34
             for (int head = 0; head < (int)queue.size(); ++head) {</pre>
35
                 node* x = queue[head];
36
                 for (int i = 0; i < N; ++i) {</pre>
37
                     if (x->next[i]) {
                          x->next[i]->fail = (x == root) ? root : x->fail->next[i];
38
39
                          x->next[i]->count += x->next[i]->fail->count;
40
                          queue.push back(x->next[i]);
41
                      } else {
42
                          x\rightarrow next[i] = (x == root) ? root : x\rightarrow fail\rightarrow next[i];
43
                      }
44
                 }
45
             }
46
        }
47
48
        inline void prepare() {
49
            root = new node();
50
        }
51 }
```

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6.5 极长回文子串

```
1 //CF17 - E
2 typedef long long int64;
3 const int N = 4 * int(1e6) + 111;
 4 const int mod = 51123987;
5 int n;
6 int input[N];
7 int start[N], finish[N];
8 int f[N];
9 int64 ans;
10 void prepare() {
11
        int k = 0;
12
        for (int i = 0; i < n; ++i) {
            if (k + f[k] < i) {
13
14
                int &1 = f[i] = 0;
15
                for (; i - 1 - 1 \ge 0 && i + 1 + 1 < n && input[i - 1 - 1] ==
16
                          input[i + 1 + 1]; l++);
17
                k = i;
18
            } else {
                int &l = f[i] = f[k - (i - k)];
19
                if (i + 1 >= k + f[k]) {
20
21
                     1 = \min(1, k + f[k] - i);
22
                     for (; i - 1 - 1 \ge 0 && i + 1 + 1 < n && input[i - 1 - 1] ==
23
                              input[i + 1 + 1]; l++);
24
                    k = i;
25
                }
26
            int 1 = i - f[i], r = i + f[i];
27
            1 += 1 & 1;
28
29
            r -= r & 1;
            if (1 <= r) {
30
31
                1 /= 2;
32
                r /= 2;
33
                int mid1 = 1 + r >> 1;
34
                int mid2 = mid1 + ((1 + r) & 1);
35
                start[1]++;
36
                start[mid1 + 1]--;
37
                finish[mid2]++;
38
                finish[r + 1] --;
39
                ans = (ans + (r - 1) / 2 + 1) \% mod;
40
            }
41
        }
42
43
   int main() {
        scanf("%d_{\sqcup}", \&n);
44
45
        for (int i = 0; i < n; ++i) {
            input[i << 1] = getchar();</pre>
46
47
            if (i < n - 1)
```

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```
48
                 input[i << 1 | 1] = '*';
49
        }
50
        n = n * 2 - 1;
51
        prepare();
        ans = ans * (ans - 1) / 2 \% mod;
52
53
        n = (n + 1) / 2;
54
        int sum = 0;
55
        for (int i = 0; i < n; ++i) {</pre>
56
            if (i) {
57
                 start[i] = (start[i] + start[i - 1]) % mod;
58
                 finish[i] = (finish[i] + finish[i - 1]) % mod;
59
            ans = (ans - (int64)start[i] * sum % mod) % mod;
60
61
            sum = (sum + finish[i]) % mod;
62
        }
63
        cout << (ans + mod) % mod << endl;</pre>
64
   }
```

6.6 后缀自动机 --多个串的最长公共子串

1

```
const int N = 255555;
 3 const int C = 36;
 4
 5
   struct Node {
 6
        Node *next[C], *fail;
        int count, len, dp, dp2;
 7
        void clear() {
 8
 9
             for(int i = 0; i < C; i++)</pre>
10
                 next[i] = NULL;
11
             len = count = 0;
12
             fail = NULL;
13
        }
14
    };
15
    Node *tail, *q[N * 2], pool[N * 2], *head;
16
    int used = 0, top = 0;
17
   char bufer[N * 2];
18
19
20
   Node *newNode() {
21
        pool[used++].clear();
22
        return &pool[used - 1];
23
    }
24
    void add(int x) {
25
26
        Node *np = newNode(), *p = tail;
27
        tail = np;
        np \rightarrow len = p \rightarrow len + 1;
```

```
29
        for(; p && !p->next[x]; p = p->fail)
30
             p->next[x] = np;
31
        if (!p)
32
             np->fail = head;
33
        else if (p\rightarrow len + 1 == p\rightarrow next[x]\rightarrow len)
34
             np->fail = p->next[x];
35
        else {
36
             Node *q = p->next[x], *nq = newNode();
37
             *nq = *q;
38
             nq \rightarrow len = p \rightarrow len + 1;
39
             q->fail = np->fail = nq;
40
             for(; p && p->next[x] == q; p = p->fail)
41
                 p\rightarrow next[x] = nq;
42
        }
43
   }
44
45
   int main() {
46
        scanf("%s", bufer);
47
        int length = strlen(bufer);
48
        head = tail = newNode();
49
        for(int i = 0; i < length; i++)</pre>
50
             add(bufer[i] - 'a');
51
        for(int i = 0; i < used; i++)</pre>
52
             pool[i].count = 0, pool[i].dp = pool[i].len;
53
        int number = 0;
54
        while(scanf("%s", bufer) == 1) {
55
             number++;
56
             length = strlen(bufer);
57
             Node *iter = head;
58
             int cur = 0;
             top = 0;
59
60
             for(int i = 0; i < length; i++) {</pre>
61
                 int x = bufer[i] - 'a';
62
                 while(iter != head && !iter->next[x])
                      iter = iter->fail, cur = iter->len;
63
                 if (iter->next[x]) {
64
65
                      cur++;
                      iter = iter->next[x];
66
67
68
                 q[top++] = iter;
69
                 if (iter->count == number - 1) {
70
                      iter->count = number;
71
                      iter->dp2 = cur;
72
                 } else if (iter->count == number) {
73
                      iter->dp2 = max(iter->dp2, cur);
74
                 } else {
75
                      top--;
76
                 }
77
             }
```

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```
78
            for(int i = 0; i < top; i++) {</pre>
79
                 q[i]->dp = min(q[i]->dp, q[i]->dp2);
80
81
82
        int ans = 0;
83
        for(int i = 0; i < used; i++)</pre>
84
             if (pool[i].count == number)
85
                 ans = max(ans, pool[i].dp);
        printf("%d\n", ans);
86
87
        return 0;
88 }
```

6.7 后缀自动机 --多次询问串在母串中的出现次数

```
1
 2
   const int N = 2555555;
 3 const int C = 36;
 5 struct Node {
        Node *next[C], *fail;
 6
 7
        int count, len;
        void clear() {
 8
 9
             for(int i = 0; i < C; i++)</pre>
10
                  next[i] = NULL;
11
             len = count = 0;
12
             fail = NULL;
13
        }
14
    };
15
16 Node *tail, *q[N * 2], pool[N * 2], *head;
17 int used = 0;
18 char bufer[N * 2];
19 int buc[N * 2], f[N * 2];
20
21 Node *newNode() {
22
        pool[used++].clear();
23
        return &pool[used - 1];
24
   }
25
26
   void add(int x) {
27
        Node *np = newNode(), *p = tail;
28
        tail = np;
29
        np\rightarrow len = p\rightarrow len + 1;
30
        for(; p \&\& !p \rightarrow next[x]; p = p \rightarrow fail)
31
             p->next[x] = np;
32
        if (!p)
33
             np->fail = head;
         else if (p\rightarrow len + 1 == p\rightarrow next[x]\rightarrow len)
```

6.8. 循环串的最小表示

```
35
             np->fail = p->next[x];
36
        else {
37
             Node *q = p->next[x], *nq = newNode();
38
             *nq = *q;
             nq->len = p->len + 1;
39
40
             q->fail = np->fail = nq;
41
             for(; p && p->next[x] == q; p = p->fail)
42
                 p->next[x] = nq;
43
        }
44
   }
45
46
   int main() {
        scanf("%s\n", bufer);
47
48
        int length = strlen(bufer);
        head = tail = newNode();
49
50
        for(int i = 0; i < length; i++)</pre>
51
             add(bufer[i] - 'a');
52
        for(int i = 0; i < used; ++i)</pre>
53
             ++buc[pool[i].len];
        for(int i = 1; i <= length; i++)</pre>
54
             buc[i] += buc[i - 1];
55
        for(int i = used - 1; i >= 0; i--)
56
57
             q[--buc[pool[i].len]] = &pool[i];
        Node *iter = head;
58
        for(int i = 0; i < length; ++i)</pre>
59
60
             (iter = iter->next[bufer[i] - 'a'])->count++;
        for(int i = used - 1; i > 0; --i) {
61
62
             f[q[i]\rightarrow len] = max(f[q[i]\rightarrow len], q[i]\rightarrow count);
63
             q[i]->fail->count += q[i]->count;
64
        for(int i = length - 1; i > 0; —i) {
65
66
             f[i] = max(f[i + 1], f[i]);
67
68
        for(int i = 1; i <= length; i++)</pre>
69
            printf("%d\n", f[i]);
70
        return 0;
71
   }
```

6.8 循环串的最小表示

```
1 struct cyc_string
2 {
3    int n, offset;
4    char str[max_length];
5    char & operator [] (int x)
6    {return str[((offset + x) % n)];}
7    cyc_string(){offset = 0;}
8 };
```

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```
9 void minimum_circular_representation(cyc_string & a)
10
11
       int i = 0, j = 1, dlt = 0, n = a.n;
12
       while(i < n and j < n and dlt < n)
13
         if(a[i + dlt] == a[j + dlt]) dlt++;
14
15
         else
16
17
           if(a[i + dlt] > a[j + dlt]) i += dlt + 1; else j += dlt + 1;
18
           dlt = 0;
19
         }
20
       }
21
       a.offset = min(i, j);
22
   }
23 int main()
24 {return 0;}
```

Chapter 7

Others

7.1 快速求逆

```
1 int inverse(int x, int modulo) {
2     if(x == 1)
3        return 1;
4     return (long long)(modulo - modulo / x) * inverse(modulo % x, modulo) % modulo;
5 }
```

7.2 求某年某月某日星期几

```
1 int whatday(int d, int m, int y)
2
3
        int ans;
        if (m == 1 | | m == 2) {
4
5
           m += 12; y --;
 6
7
        if ((y < 1752) \mid | (y == 1752 \&\& m < 9) \mid | (y == 1752 \&\& m == 9 \&\& d < 3))
            ans = (d + 2 * m + 3 * (m + 1) / 5 + y + y / 4 + 5) % 7;
8
       else ans = (d + 2 * m + 3 * (m + 1) / 5 + y + y / 4 - y / 100 + y / 400) % 7;
9
10
       return ans;
11 }
```

7.3 LL*LL%LL

```
1 LL multiplyMod(LL a, LL b, LL P) { // `需要保证 a 和 b 非负`
2 LL t = (a * b - LL((long double)a / P * b + 1e-3) * P) % P;
3 return t < 0 : t + P : t;
4 }
```

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7.4 next_nCk

```
void nCk(int n, int k) {
       for (int comb = (1 << k) - 1; comb < (1 << n); ) {
2
3
           // ...
4
           {
5
               int x = comb & -comb, y = comb + x;
6
               comb = (((comb & ~y) / x) >> 1) | y;
7
           }
8
       }
9
  }
```

7.5 单纯形

```
test on uva 12567
```

```
1 const double eps = 1e-8;
   // max{c * x | Ax <= b, x >= 0}的解, 无解返回空的vector, 否则就是解.
   vector<double> simplex(vector<vector<double> > &A, vector<double> b, vector<double> c
 4
        int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
 5
       vector<vector<double> > D(n + 2, vector<double>(m + 1));
 6
       vector<int> ix(n + m);
 7
        for(int i = 0; i < n + m; i++) {</pre>
 8
            ix[i] = i;
 9
10
        for(int i = 0; i < n; i++) {</pre>
            for(int j = 0; j < m - 1; j++) {
11
12
                D[i][j] = -A[i][j];
13
14
            D[i][m-1] = 1;
15
            D[i][m] = b[i];
16
            if (D[r][m] > D[i][m]) {
17
                r = i;
18
            }
19
       }
20
21
        for(int j = 0; j < m - 1; j++) {
22
            D[n][j] = c[j];
23
24
       D[n + 1][m - 1] = -1;
        for(double d; ;) {
25
26
            if (r < n) {
27
                swap(ix[s], ix[r + m]);
28
                D[r][s] = 1. / D[r][s];
29
                for(int j = 0; j <= m; j++) {</pre>
30
                    if (j != s) {
31
                        D[r][j] *= -D[r][s];
```

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```
32
                      }
33
34
                 for(int i = 0; i <= n + 1; i++) {</pre>
35
                      if (i != r) {
                          for(int j = 0; j <= m; j++) {</pre>
36
                               if (j != s) {
37
38
                                   D[i][j] += D[r][j] * D[i][s];
39
40
                          D[i][s] *= D[r][s];
41
42
                      }
43
                 }
44
             }
45
             r = -1, s = -1;
             for(int j = 0; j < m; j++) {</pre>
46
47
                 if (s < 0 | | ix[s] > ix[j]) {
48
                      if (D[n + 1][j] > eps | | D[n + 1][j] > -eps && D[n][j] > eps) {
49
                          s = j;
50
                      }
51
                 }
52
53
             if (s < 0) {
54
                 break;
55
             for(int i = 0; i < n; i++) {</pre>
56
57
                 if (D[i][s] < -eps) {</pre>
                      if (r < 0 | | (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -eps
58
59
                           | | d < eps && ix[r + m] > ix[i + m])  {
60
61
                          r = i;
62
                      }
63
                 }
64
             }
65
66
             if (r < 0) {
                 return vector<double> ();
67
68
69
70
        if (D[n + 1][m] < -eps) {
71
             return vector<double> ();
72
        }
73
74
        vector<double> x(m-1);
        for(int i = m; i < n + m; i++) {</pre>
75
76
             if (ix[i] < m - 1) {
77
                 x[ix[i]] = D[i - m][m];
78
             }
79
        }
80
        return x;
```

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81 }

7.6 曼哈顿最小生成树

```
1
   `只需要考虑每个点的 pi/4*k \longrightarrow pi/4*(k+1)的区间内的第一个点, 这样只有4n条无向边。`
 2
   */
 3
 4 const int maxn = 100000+5;
 5 const int Inf = 1000000005;
 6 struct TreeEdge
 7
 8
        int x,y,z;
 9
       void make( int _x,int _y,int _z ) { x=_x; y=_y; z=_z; }
10
   } data[maxn*4];
11
12
   inline bool operator < ( const TreeEdge& x,const TreeEdge& y ) {</pre>
13
        return x.z<y.z;
14
15
   int x[maxn],y[maxn],px[maxn],py[maxn],id[maxn],tree[maxn],node[maxn],val[maxn],fa[
       maxn];
   int n;
17
18 inline bool compare1( const int a, const int b ) { return x[a]<x[b]; }
   inline bool compare2( const int a,const int b ) { return y[a]<y[b]; }</pre>
20 inline bool compare3( const int a, const int b) { return (y[a]-x[a]<y[b]-x[b] | y[a
       ]-x[a]==y[b]-x[b] && y[a]>y[b]); }
21
   inline bool compare4( const int a, const int b) { return (y[a]-x[a]>y[b]-x[b] | y[a
       ]-x[a]==y[b]-x[b] && x[a]>x[b]); }
22
   inline bool compare5( const int a,const int b ) { return (x[a]+y[a]>x[b]+y[b] | | x[a
       ]+y[a]==x[b]+y[b] && x[a]<x[b]); }
23
   inline bool compare6( const int a, const int b) { return (x[a]+y[a]<x[b]+y[b] | x[a
       ]+y[a]==x[b]+y[b] && y[a]>y[b]); }
24
   void Change_X()
25
   {
26
        for(int i=0;i<n;++i) val[i]=x[i];</pre>
27
        for(int i=0;i<n;++i) id[i]=i;</pre>
28
        sort(id,id+n,compare1);
29
        int cntM=1, last=val[id[0]]; px[id[0]]=1;
30
        for(int i=1;i<n;++i)</pre>
31
32
            if(val[id[i]]>last) ++cntM, last=val[id[i]];
33
            px[id[i]]=cntM;
34
        }
35
   }
   void Change Y()
36
37
   {
38
        for(int i=0;i<n;++i) val[i]=y[i];</pre>
```

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```
39
        for(int i=0;i<n;++i) id[i]=i;</pre>
40
        sort(id,id+n,compare2);
        int cntM=1, last=val[id[0]]; py[id[0]]=1;
41
42
        for(int i=1;i<n;++i)</pre>
43
44
            if(val[id[i]]>last) ++cntM, last=val[id[i]];
45
            py[id[i]]=cntM;
46
        }
47 }
48 inline int absValue( int x ) { return (x<0)?-x:x; }
49 inline int Cost( int a,int b ) { return absValue(x[a]-x[b])+absValue(y[a]-y[b]); }
50 int find( int x ) { return (fa[x]==x)?x:(fa[x]=find(fa[x])); }
51 int main()
52
53
   //
        freopen("input.txt", "r", stdin);
54
   //
        freopen("output.txt", "w", stdout);
55
56
        int test=0;
        while( scanf("%d",&n)!=EOF && n )
57
58
            for(int i=0;i<n;++i) scanf("%d%d",x+i,y+i);</pre>
59
60
            Change X();
61
            Change_Y();
62
            int cntE = 0;
63
            for(int i=0;i<n;++i) id[i]=i;</pre>
64
65
            sort(id,id+n,compare3);
66
            for(int i=1;i<=n;++i) tree[i]=Inf,node[i]=-1;</pre>
67
            for(int i=0;i<n;++i)</pre>
68
            {
69
                 int Min=Inf, Tnode=-1;
70
                 for(int k=py[id[i]];k<=n;k+=k&(-k)) if(tree[k]<Min) Min=tree[k],Tnode=</pre>
                    node[k];
71
                if(Tnode>=0) data[cntE++].make(id[i],Tnode,Cost(id[i],Tnode));
72
                 int tmp=x[id[i]]+y[id[i]];
73
                 for(int k=py[id[i]];k;k-=k&(-k)) if(tmp<tree[k]) tree[k]=tmp,node[k]=id[i</pre>
                    ];
74
75
            sort(id,id+n,compare4);
            for(int i=1;i<=n;++i) tree[i]=Inf,node[i]=-1;</pre>
76
77
            for(int i=0;i<n;++i)</pre>
78
                 int Min=Inf, Tnode=-1;
79
                 for(int k=px[id[i]];k<=n;k+=k&(-k)) if(tree[k]<Min) Min=tree[k],Tnode=</pre>
80
                    node[k];
81
                 if(Tnode>=0) data[cntE++].make(id[i],Tnode,Cost(id[i],Tnode));
82
                 int tmp=x[id[i]]+y[id[i]];
83
                 for(int k=px[id[i]];k;k-=k&(-k)) if(tmp<tree[k]) tree[k]=tmp,node[k]=id[i</pre>
                    ];
```

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```
84
85
            sort(id,id+n,compare5);
86
            for(int i=1;i<=n;++i) tree[i]=Inf,node[i]=-1;</pre>
            for(int i=0;i<n;++i)</pre>
87
88
89
                int Min=Inf, Tnode=-1;
90
                ];
                if(Tnode>=0) data[cntE++].make(id[i],Tnode,Cost(id[i],Tnode));
91
92
                int tmp=-x[id[i]]+y[id[i]];
93
                for(int k=px[id[i]];k \le n;k + = k&(-k)) if(tmp \le tree[k]) tree[k] = tmp,node[k] =
                   id[i];
94
            }
95
            sort(id,id+n,compare6);
96
            for(int i=1;i<=n;++i) tree[i]=Inf,node[i]=-1;</pre>
            for(int i=0;i<n;++i)</pre>
97
98
            {
99
                int Min=Inf, Tnode=-1;
100
                for(int k=py[id[i]];k<=n;k+=k&(-k)) if(tree[k]<Min) Min=tree[k],Tnode=</pre>
                   node[k];
101
                if(Tnode>=0) data[cntE++].make(id[i],Tnode,Cost(id[i],Tnode));
102
                int tmp=-x[id[i]]+y[id[i]];
103
                for(int k=py[id[i]];k;k-=k&(-k)) if(tmp<tree[k]) tree[k]=tmp,node[k]=id[i</pre>
                   ];
104
            }
105
106
            long long Ans = 0;
107
            sort(data,data+cntE);
108
            for(int i=0;i<n;++i) fa[i]=i;</pre>
109
            for(int i=0;i<cntE;++i) if(find(data[i].x)!=find(data[i].y))</pre>
110
111
                Ans += data[i].z;
112
                fa[fa[data[i].x]]=fa[data[i].y];
113
            }
114
            115
116
        }
117
        return 0;
118
    }
```

7.7 最长公共子序列

7.7.1 最长公共子序列

```
1 const int dx[]={0,-1,0,1};
2 const int dy[]={1,0,-1,0};
3 const string ds="ENWS";
4 char G[52][52];
```

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```
5 char A[22222], B[22222], buf[22222];
 6 int n, m;
8 typedef unsigned long long 11;
9
10 const int M = 62;
11 const int maxn = 20010;
12 const int maxt = 130;
13 const int maxl = maxn / M + 10;
14 const ll Top = ((ll) 1 << (M));
15 const 11 Topless = Top -1;
16 const 11 underTop = ((11) 1 << (M - 1));
17 typedef ll bitarr[maxl];
18 bitarr comp[maxt], row[2], X;
19
20 void get(char *S){
21
        int L,x,y,sz=0;
22
        scanf("%d%d%d",&L,&x,&y),x--,y--;
23
        //scanf(" %s",buf);
24
        S[sz++]=G[x][y];
        for(int i=0;i<L;i++){</pre>
25
26
            char ch;
27
            scanf("_{\sqcup}%c", \&ch);
28
            int pos=ds.find(ch);
29
            x+=dx[pos],y+=dy[pos];
30
            if (x < 0 | y < 0 | x >= n | y >= m) for (;;);
            S[sz++]=G[x][y];
31
32
33
        S[sz]=0;
34
   }
35
36 bool calc[maxt];
37
38 void prepare() {
39
40
        int u, p;
       memset(calc, 0, sizeof(calc));
41
42
        for (int i = 0; i < m; i++) {
43
            u = B[i];
            if (calc[u]) continue; //=====仅对所有字符集 , 每次一次
44
45
            calc[u] = 1;
46
           memset(comp[u], 0, sizeof(comp[u]));
47
            for (p = 0; p < n; p++) if (u == A[p]) comp[u][p / M] ^= ((11) 1 << (p % M));
48
        }
49
   }
50
51 void solve() {
52
       prepare();
53
       memset(row, 0, sizeof(row));
```

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```
54
         int prev, curt;
55
         int i, u, p, c, cc;
56
         int Ln = (n / M) + 1;
57
         prev = 0;
         for (i = 0; i < m; i++) {
58
59
             curt = 1 - prev; u = B[i];
 60
             for (p = 0; p < Ln; p++) X[p] = row[prev][p] | comp[u][p];</pre>
 61
             c = 0;
 62
             for (p = 0; p < Ln; p++) {
 63
                 cc = (row[prev][p] & underTop) > 0;
 64
                 row[prev][p] = ((row[prev][p] & (underTop - 1)) << 1) + c;
 65
                 c = cc;
 66
 67
             for (p = 0; p < Ln; p++) {
 68
                  if (row[prev][p] != Topless) {
 69
                      row[prev][p]++;
70
                      break;
71
                 }
72
                 row[prev][p] = 0;
73
             }
74
             c = 0;
75
             for (p = 0; p < Ln; p++) {
 76
                 if (X[p] >= row[prev][p] + c)
 77
                      row[prev][p] = X[p] - (row[prev][p] + c), c = 0;
 78
                 else
 79
                      row[prev][p] = Top + X[p] - (row[prev][p] + c), c = 1;
 80
81
             for (p = 0; p < Ln; p++)
                 row[curt][p] = X[p] & (row[prev][p] ^ X[p]);
82
83
             prev = curt;
84
85
         int ret = 0;
86
         for (i = 0; i < n; i++)</pre>
87
             if (row[prev][i / M] & ((ll) 1 << (i % M))) ret++;</pre>
88
    // printf("%d %d %d\n", n, m, ret);
     //=====ret 就是最长公共子序列。
89
         printf("%d_{\square}%d_{\square}", n - ret, m - ret);
90
91
92
93
    int main(){
94
         int tests=0,T;
         scanf("%d",&T);
95
         while(T--){
96
97
             scanf("%d%d",&n,&m);
98
             for(int i=0;i<n;i++)</pre>
99
                  for (int j = 0; j < m; j++)
100
                      scanf("\c",&G[i][j]);
101
             get(A),get(B);
102
```

7.8. 环状最长公共子序列

```
103
                printf("Case<sub>\(\sigma\)</sub>%d:<sub>\(\sigma\)</sub>", ++tests);
104 //
                printf("A = %s \setminus n, B = %s \setminus n", A, B);
105
                n = strlen(A), m = strlen(B);
106
                //n = 20000; m = 20000;
                //for (int i = 0; i < m; i++) A[i] = B[i] = 'A';
107
108
                //A[m] = B[m] = 0;
109
                solve();
110
           }
111 }
```

7.8 环状最长公共子序列

```
1 const int N = 2222;
3 int a[N], b[N];
   int n, dp[N][N], from[N][N];
5
   int run() {
7
        scanf("%d", &n);
        for(int i = 1; i <= n; i++) {</pre>
8
9
            scanf("%d", &a[i]);
10
            a[i + n] = a[i];
11
            b[n - i + 1] = a[i];
12
13
       memset(from, 0, sizeof(from));
14
        int ans = 0;
        for(int i = 1; i <= 2 * n; i++) {
15
            from[i][0] = 2;
16
17
            int upleft = 0, up = 0, left = 0;
18
            for(int j = 1; j <= n; j++) {</pre>
19
                upleft = up;
20
                if (a[i] == b[j]) {
21
                     upleft++;
22
                } else {
                     upleft = INT_MIN;
23
24
25
                if (from[i-1][j])
26
                     up++;
27
                int mm = max(up, max(left, upleft));
                if (mm == left) {
28
29
                     from[i][j] = 0;
30
                } else if (mm == upleft)
31
                     from[i][j] = 1;
32
                else
33
                     from[i][j] = 2;
34
                left = mm;
35
36
            if (i >= n) {
```

```
37
                 int count = 0;
38
                 for(int x = i, y = n; y; ) {
                     if (from[x][y] == 1) {
39
40
                         x--; y--;
41
                         count++;
42
                     } else if (from[x][y] == 0)
43
                         y--;
44
                     else
45
                         x--;
46
                 }
47
                 ans = max(ans, count);
48
                 int x = i - n + 1;
49
                 from[x][0] = 0;
50
                 int y = 0;
51
                 for(; y <= n && from[x][y] == 0; y++);</pre>
52
                 for(; x <= i; x++) {</pre>
53
                     from[x][y] = 0;
54
                     if (x == i) {
55
                         break;
56
57
                     for(; y <= n; ++y) {</pre>
58
                          if (from[x + 1][y] == 2) {
59
                              break;
60
61
                          if (y + 1 \le n \&\& from[x + 1][y + 1] == 1) {
62
                              y++;
63
                              break;
64
                          }
65
                     }
66
                 }
67
            }
68
        if (n)
69
70
            printf("%d\n", ans);
71
        return n;
72
    }
73
74
   int main() {
75
        for(; run(); );
76
        return 0;
77
   }
```

7.9 长方体表面两点最近距离

```
1 int r;
2 void turn(int i, int j, int x, int y, int z,int x0, int y0, int L, int W, int H) {
3    if (z==0) {
4       int R = x*x+y*y;
```

7.10. 插头 DP 145

```
5
            if (R<r) r=R;
 6
        }
7
        else{
8
            if(i>=0 && i< 2)
                turn(i+1, j, x0+L+z, y, x0+L-x, x0+L, y0, H, W, L);
9
10
            if(j>=0 \&\& j< 2)
                turn(i, j+1, x, y0+W+z, y0+W-y, x0, y0+W, L, H, W);
11
12
            if(i<=0 && i>-2)
13
                turn(i-1, j, x0-z, y, x-x0, x0-H, y0, H, W, L);
14
            if(j \le 0 \&\& j \ge -2)
                turn(i, j-1, x, y0-z, y-y0, x0, y0-H, L, H, W);
15
16
        }
17
   int main(){
18
19
        int L, H, W, x1, y1, z1, x2, y2, z2;
20
        cin >> L >> W >> H >> x1 >> y1 >> z1 >> x2 >> y2 >> z2;
21
        if (z1!=0 && z1!=H)
22
        if (y1==0 | y1==W)
23
            swap(y1,z1), std::swap(y2,z2), std::swap(W,H);
24
        else
25
            swap(x1,z1), std::swap(x2,z2), std::swap(L,H);
26
        if (z1==H) z1=0, z2=H-z2;
27
        r=0x3fffffff; turn(0,0,x2-x1,y2-y1,z2,-x1,-y1,L,W,H);
28
        cout<<r<<endl;
29
        return 0;
30 }
```

7.10 插头 DP

```
1 #include <cstdio>
 2 #include <cstdlib>
 3 #include <algorithm>
 4 #include <vector>
5 #include <iostream>
6 using namespace std;
7
8 typedef long long int64;
9 typedef pair<int, long long> State;
10 const int MAXN = 8;
11
12 char map[MAXN + 10][MAXN + 10];
13 int n, m, lastx, lasty;
14 int64 ans;
15 vector<State> vec[2];
16
17
18 void mergy(int cur) {
19
       sort(vec[cur].begin(), vec[cur].end());
```

```
20
        int size = 0;
21
        for(int i = 0, j = 0; i < vec[cur].size(); i = j) {</pre>
22
            vec[cur][size] = vec[cur][i];
23
            j = i + 1;
            while(j < vec[cur].size() && vec[cur][j].first == vec[cur][size].first)</pre>
24
25
                vec[cur][size].second += vec[cur][j].second, j++;
26
            size++;
27
        }
28
        vec[cur].resize(size);
29
   }
30
31
   void next_line(int cur) {
32
        int size = 0;
33
        for(int i = 0; i < vec[cur].size(); i++) {</pre>
34
            int sta = vec[cur][i].first;
35
            if ((sta >> (m << 1)) == 0) {</pre>
36
                vec[cur][size] = vec[cur][i];
37
                vec[cur][size].first <<= 2;</pre>
38
                size++;
39
            }
40
41
        vec[cur].resize(size);
42
43
44
   inline int replace(int sta, int pos, int v) {
45
        return (sta & (~(3 << (pos << 1)))) | (v << (pos << 1));
46 }
47
   inline int replace(int &sta, int pos, int v1, int v2) {
48
49
        int res = replace(sta, pos, v1);
50
        res = replace(res, pos + 1, v2);
51
        return res;
52
   }
53
54
   int Trans(int sta, int pos) {
55
        int cnt = 1, v = (sta >> (pos << 1) & 3);</pre>
56
        if (v == 1) {
57
            sta = replace(sta, pos, 0, 0);
58
            for(int i = pos + 2; ; i++) {
59
                if ((sta >> (i << 1) & 3) == 1)
60
61
                else if ((sta >> (i << 1) & 3) == 2)
62
                     cnt--;
                if (cnt == 0)
63
64
                     return replace(sta, i, 1);
65
            }
66
        } else {
67
            sta = replace(sta, pos, 0, 0);
68
            for(int i = pos - 1; ; i--) {
```

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```
69
                 if ((sta >> (i << 1) & 3) == 1)
 70
                      cnt--;
 71
                 else if ((sta >> (i << 1) & 3) == 2)
 72
                      cnt++;
 73
                 if (cnt == 0)
 74
                      return replace(sta, i, 2);
 75
             }
 76
         }
 77
    }
 78
 79
    void dp block(int i, int j, int cur) {
 80
         for(int s = 0; s < vec[cur].size(); s++) {</pre>
             int sta = vec[cur][s].first;
 81
             int64 val = vec[cur][s].second;
 82
 83
             int left = (sta >> (j << 1)) & 3, up = (sta >> ((j + 1) << 1)) & 3;</pre>
 84
             if (left == 0 && up == 0) {
 85
                 vec[cur ^ 1].push_back(State(sta, val));
 86
             }
 87
         }
 88
    }
 89
 90 void dp_blank(int i, int j, int cur) {
91
         for(int s = 0; s < vec[cur].size(); s++) {</pre>
92
             int sta = vec[cur][s].first;
93
             int64 val = vec[cur][s].second;
 94
             int left = (sta >> (j << 1)) & 3, up = (sta >> ((j + 1) << 1)) & 3, ns = 0;
             if (left && up) {
95
 96
                 if (left == 2 && up == 1) {
                      vec[cur ^ 1].push_back(State(replace(sta, j, 0, 0), val));
 97
                 } else if (left == 1 && up == 2) {
98
99
                      if (replace(sta, j, 0, 0) == 0 && i == lastx && j == lasty)
100
                          ans += val;
101
                 } else if (left == 1 && up == 1) {
102
                      vec[cur ^ 1].push_back(State(Trans(sta, j), val));
                 } else if (left == 2 && up == 2) {
103
                     vec[cur ^ 1].push_back(State(Trans(sta, j), val));
104
105
106
             } else if (left || up) {
107
                 vec[cur ^ 1].push_back(State(sta, val));
108
                 vec[cur ^ 1].push back(State(replace(sta, j, up, left), val));
109
             } else {
110
                 vec[cur ^ 1].push back(State(replace(sta, j, 1, 2), val));
111
             }
112
         }
113 }
114
115 void show(int cur) {
116
         for(int i = 0; i < vec[cur].size(); i++)</pre>
117
             printf("%d<sub>\\\\</sub>8I64d\n", vec[cur][i].first, vec[cur][i].second);
```

```
118
         printf("step\n");
119
120
121
     int main() {
         freopen("input.txt", "r", stdin);
122
123
         while(scanf("%d_{\square}%d", &n, &m) == 2) {
124
              ans = 0;
125
              lastx = lasty = -1;
126
              gets(map[0]);
127
              for(int i = 0; i < n; i++) {
128
                  scanf("%s", map[i]);
129
                  for(int j = 0; j < m; j++) {</pre>
                       if (map[i][j] == '.') {
130
                           lastx = i, lasty = j;
131
132
                       }
133
                  }
134
135
              if (lastx == -1) {
136
                  printf("0\n");
137
                  continue;
138
139
              int cur = 0;
140
              vec[cur].clear();
141
              vec[cur].push_back(State(0, 1));
142
              for(int i = 0; i < n; i++) {</pre>
143
                  for(int j = 0; j < m; j++) {</pre>
                      vec[cur ^ 1].clear();
144
145
                      if (map[i][j] == '.')
                           dp_blank(i, j, cur);
146
147
                      else
148
                           dp_block(i, j, cur);
149
                      cur ^= 1;
150
                      mergy(cur);
151
                       //show(cur);
152
153
                  next_line(cur);
154
155
              cout << ans << endl;</pre>
156
         }
157
         return 0;
158
     }
```

7.11 最大团搜索

1

```
Int g[][] 为图的邻接矩阵。MC(V) 表示点集 V 的最大团令 Si=vi, vi+1, ..., vn, mc[i] 表示 MC(Si) 倒着算 mc[i], 那么显然 MC(V)=mc[1] 此外有 mc[i]=mc[i+1] or mc[i]=mc[i+1]+1 void init(){
    int i, j;
```

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```
for (i=1; i<=n; ++i) for (j=1; j<=n; ++j) scanf("%d", &g[i][j]);
3
 4
   }
   void dfs(int size){
        int i, j, k;
 6
7
        if (len[size]==0) {
8
            if (size>ans) {
9
                 ans=size; found=true;
10
11
            return;
12
        for (k=0; k<len[size] && !found; ++k) {</pre>
13
14
            if (size+len[size]-k<=ans) break;</pre>
15
            i=list[size][k];
16
            if (size+mc[i]<=ans) break;</pre>
            for (j=k+1, len[size+1]=0; j<len[size]; ++j)</pre>
17
18
            if (g[i][list[size][j]]) list[size+1][len[size+1]++]=list[size][j];
19
            dfs(size+1);
20
        }
21 }
22 void work(){
23
        int i, j;
24
        mc[n]=ans=1;
25
        for (i=n-1; i; ---i) {
26
            found=false;
27
            len[1]=0;
28
            for (j=i+1; j<=n; ++j) if (g[i][j]) list[1][len[1]++]=j;</pre>
29
            dfs(1);
30
            mc[i]=ans;
31
        }
32 }
33 void print(){
        printf("%d\n", ans);
34
35 }
```

7.12 Dancing Links

```
namespace dancing_links {
1
2
        int const N = , M = , G = ;
3
 4
        struct node {
 5
            int col, row, left, right, up, down;
 6
            inline void clear() {
7
                col = row = left = right = up = down = 0;
8
            }
9
        } grid[G];
10
11
        int n, m, tot;
12
        int cnt[M], head[N], tail[N];
```

```
13
14
        inline void prepare() {
15
            tot = m + 1;
16
            for (int i = 1; i <= n; ++i) {</pre>
                head[i] = tail[i] = 0;
17
18
19
            for (int i = 1; i <= m + 1; ++i) {</pre>
20
                grid[i].col = i;
21
                grid[i].left = i - 1;
                grid[i].right = i + 1;
22
23
                grid[i].up = i;
                grid[i].down = i;
24
25
                cnt[i] = 0;
26
27
            grid[1].left = m + 1;
28
            grid[m + 1].right = 1;
29
        }
30
31
        inline void remove(int x) {
32
            grid[grid[x].right].left = grid[x].left;
33
            grid[grid[x].left].right = grid[x].right;
34
            for (int y = grid[x].down; y != x; y = grid[y].down) {
35
                for (int z = grid[y].right; z != y; z = grid[z].right) {
36
                     cnt[grid[z].col]--;
37
                     grid[grid[z].down].up = grid[z].up;
38
                     grid[grid[z].up].down = grid[z].down;
39
                }
40
            }
41
        }
42
        inline void resume(int x) {
43
44
            for (int y = grid[x].up; y != x; y = grid[y].up) {
45
                 for (int z = grid[y].left; z != y; z = grid[z].left) {
46
                     cnt[grid[z].col]++;
47
                     grid[grid[z].up].down = z;
48
                     grid[grid[z].down].up = z;
49
                 }
50
            }
51
            grid[grid[x].right].left = x;
52
            grid[grid[x].left].right = x;
53
        }
54
55
        inline void add(int x, int y) {
56
            tot++;
57
            cnt[y]++;
58
            if (!head[x]) {
59
                head[x] = tot;
60
61
            if (!tail[x]) {
```

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```
62
                 tail[x] = tot;
 63
             }
 64
             grid[tot].row = x; grid[tot].col = y;
 65
             grid[tot].up = grid[y].up; grid[grid[y].up].down = tot;
66
             grid[tot].down = y; grid[y].up = tot;
 67
             grid[tot].left = tail[x]; grid[tail[x]].right = tot;
 68
             grid[tot].right = head[x]; grid[head[x]].left = tot;
 69
             tail[x] = tot;
 70
 71
 72
         inline bool dfs(int dep) {
 73
             if (grid[m + 1].right == m + 1) {
 74
                 return true;
 75
             int x = grid[m + 1].right;
 76
 77
             for (int i = x; i != m + 1; i = grid[i].right) {
 78
                 if (cnt[i] < cnt[x]) {</pre>
 79
                     x = i;
 80
                 }
 81
             if (!cnt[x]) {
 82
 83
                 return false;
 84
85
             remove(x);
             for (int i = grid[x].down; i != x; i = grid[i].down) {
 86
 87
                 for (int j = grid[i].right; j != i; j = grid[j].right) {
 88
                      remove(grid[j].col);
 89
                 if (dfs(dep + 1)) {
 90
 91
                      return true;
 92
 93
                 for (int j = grid[i].left; j != i; j = grid[j].left) {
 94
                      resume(grid[j].col);
 95
                 }
96
 97
             resume(x);
98
             return false;
99
100
101
         inline void clear() {
102
             for (int i = 1; i <= tot; ++i) {</pre>
103
                 grid[i].clear();
104
             }
105
         }
106 }
```

7.13 极大团计数

```
Bool g[][] 为图的邻接矩阵, 图点的标号由 1 至 n。
    void dfs(int size){
 1
 2
        int i, j, k, t, cnt, best = 0;
 3
        bool bb;
 4
        if (ne[size] == ce[size]){
 5
             if (ce[size]==0) ++ans;
 6
            return;
 7
 8
        for (t=0, i=1; i<=ne[size]; ++i) {</pre>
             for (cnt=0, j=ne[size]+1; j<=ce[size]; ++j)</pre>
 9
10
             if (!g[list[size][i]][list[size][j]]) ++cnt;
11
             if (t==0 || cnt<best) t=i, best=cnt;</pre>
12
13
        if (t && best<=0) return;</pre>
14
        for (k=ne[size]+1; k<=ce[size]; ++k) {</pre>
15
             if (t>0){
                 for (i=k; i<=ce[size]; ++i) if (!g[list[size][t]][list[size][i]]) break;</pre>
16
17
                 swap(list[size][k], list[size][i]);
18
             }
19
            i=list[size][k];
20
            ne[size+1]=ce[size+1]=0;
21
             for (j=1; j<k; ++j)if (g[i][list[size][j]]) list[size+1][++ne[size+1]]=list[</pre>
                size][j];
22
            for (ce[size+1]=ne[size+1], j=k+1; j<=ce[size]; ++j)</pre>
23
            if (g[i][list[size][j]]) list[size+1][++ce[size+1]]=list[size][j];
24
            dfs(size+1);
25
            ++ne[size];
26
            --best;
            for (j=k+1, cnt=0; j<=ce[size]; ++j) if (!g[i][list[size][j]]) ++cnt;</pre>
27
28
            if (t==0 || cnt<best) t=k, best=cnt;</pre>
29
            if (t && best<=0) break;</pre>
30
        }
31
   }
    void work(){
32
        int i;
33
34
        ne[0]=0; ce[0]=0;
35
        for (i=1; i<=n; ++i) list[0][++ce[0]]=i;</pre>
36
        ans=0;
37
        dfs(0);
38
    }
```

Chapter 8

Hints

8.1 积分表

$$\arcsin x \to \frac{1}{\sqrt{1-x^2}}$$

$$\arccos x \to -\frac{1}{\sqrt{1-x^2}}$$

$$\arctan x \to \frac{1}{1+x^2}$$

$$a^x \to \frac{a^x}{\ln a}$$

$$\sin x \to -\cos x$$

$$\cos x \to \sin x$$

$$\tan x \to -\ln\cos x$$

$$\sec x \to \ln\tan(\frac{x}{2} + \frac{\pi}{4})$$

$$\tan^2 x \to \tan x - x$$

$$\csc x \to \ln\tan\frac{x}{2}$$

$$\sin^2 x \to \frac{x}{2} - \frac{1}{2}\sin x \cos x$$

$$\cos^2 x \to \frac{x}{2} + \frac{1}{2}\sin x \cos x$$

$$\sec^2 x \to \tan x$$

$$\frac{1}{\sqrt{a^2 - x^2}} \to \arcsin\frac{x}{a}$$

$$\csc^2 x \to -\cot x$$

$$\frac{1}{a^2 - x^2}(|x| < |a|) \to \frac{1}{2a}\ln\frac{a + x}{a - x}$$

$$\frac{1}{x^2 - a^2}(|x| > |a|) \to \frac{1}{2a}\ln\frac{x - a}{x + a}$$

$$\sqrt{a^2-x^2} \rightarrow \frac{x}{2}\sqrt{a^2-x^2} + \frac{a^2}{2}\arcsin\frac{x}{a}$$

$$\frac{1}{\sqrt{x^2+a^2}} \rightarrow \ln(x+\sqrt{a^2+x^2})$$

$$\sqrt{a^2+x^2} \rightarrow \frac{x}{2}\sqrt{a^2+x^2} + \frac{a^2}{2}\ln(x+\sqrt{a^2+x^2})$$

$$\frac{1}{\sqrt{x^2-a^2}} \rightarrow \ln(x+\sqrt{x^2-a^2})$$

$$\sqrt{x^2-a^2} \rightarrow \frac{x}{2}\sqrt{x^2-a^2} - \frac{a^2}{2}\ln(x+\sqrt{x^2-a^2})$$

$$\frac{1}{x\sqrt{a^2-x^2}} \rightarrow -\frac{1}{a}\ln\frac{a+\sqrt{a^2-x^2}}{x}$$

$$\frac{1}{x\sqrt{a^2+x^2}} \rightarrow -\frac{1}{a}\ln\frac{a+\sqrt{a^2+x^2}}{x}$$

$$\frac{1}{\sqrt{2ax-x^2}} \rightarrow \arccos(1-\frac{x}{a})$$

$$\frac{x}{ax+b} \rightarrow \frac{x}{a} - \frac{b}{a^2}\ln(ax+b)$$

$$\sqrt{2ax-x^2} \rightarrow \frac{x-a}{2}\sqrt{2ax-x^2} + \frac{a^2}{2}\arcsin(\frac{x}{a}-1)$$

$$\frac{1}{x\sqrt{ax+b}}(b<0) \rightarrow \frac{2}{\sqrt{-b}}\arctan\sqrt{\frac{ax+b}{-b}}$$

$$x\sqrt{ax+b} \rightarrow \frac{2(3ax-2b)}{15a^2}(ax+b)^{\frac{3}{2}}$$

$$\frac{1}{x\sqrt{ax+b}}(b>0) \rightarrow \frac{1}{\sqrt{b}}\ln\frac{\sqrt{ax+b}-\sqrt{b}}{\sqrt{ax+b}+\sqrt{b}}$$

$$\frac{x}{\sqrt{ax+b}} \rightarrow \frac{2(ax-2b)}{3a^2}\sqrt{ax+b}$$

$$\frac{1}{x^2\sqrt{ax+b}} \rightarrow -\frac{\sqrt{ax+b}}{bx} - \frac{a}{2b}\int\frac{dx}{x\sqrt{ax+b}}$$

$$\frac{1}{x^2\sqrt{ax+b}} \rightarrow 2\sqrt{ax+b} + b\int\frac{dx}{x\sqrt{ax+b}}$$

$$\frac{1}{\sqrt{(ax+b)^n}}(n>2) \rightarrow \frac{-2}{a(n-2)} \cdot \frac{1}{\sqrt{(ax+b)^{n-2}}}$$

$$\frac{1}{ax^2+c}(a>0,c>0) \rightarrow \frac{1}{\sqrt{ac}}\ln(ax^2+c)$$

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$$\frac{1}{ax^{2}+c}(a+,c-) \to \frac{1}{2\sqrt{-ac}} \ln \frac{x\sqrt{a}-\sqrt{-c}}{x\sqrt{a}+\sqrt{-c}}$$

$$\frac{1}{x(ax^{2}+c)} \to \frac{1}{2c} \ln \frac{x^{2}}{ax^{2}+c}$$

$$\frac{1}{ax^{2}+c}(a-,c+) \to \frac{1}{2\sqrt{-ac}} \ln \frac{\sqrt{c}+x\sqrt{-a}}{\sqrt{c}-x\sqrt{-a}}$$

$$x\sqrt{ax^{2}+c} \to \frac{1}{3a}\sqrt{(ax^{2}+c)^{3}}$$

$$\frac{1}{(ax^{2}+c)^{n}}(n>1) \to \frac{x}{2c(n-1)(ax^{2}+c)^{n-1}} + \frac{2n-3}{2c(n-1)} \int \frac{dx}{(ax^{2}+c)^{n-1}}$$

$$\frac{x^{n}}{ax^{2}+c}(n\neq 1) \to \frac{x^{n-1}}{a(n-1)} - \frac{c}{a} \int \frac{x^{n-2}}{ax^{2}+c} dx$$

$$\frac{1}{x^{2}(ax^{2}+c)^{n}} (n\geq 2) \to \frac{1}{c} \int \frac{dx}{x^{2}(ax^{2}+c)^{n-1}} - \frac{a}{c} \int \frac{dx}{(ax^{2}+c)^{n}}$$

$$\sqrt{ax^{2}+c}(a>0) \to \frac{x}{2}\sqrt{ax^{2}+c} + \frac{c}{2\sqrt{a}} \ln(x\sqrt{a}+\sqrt{ax^{2}+c})$$

$$\sqrt{ax^{2}+c}(a<0) \to \frac{x}{2}\sqrt{ax^{2}+c} + \frac{c}{2\sqrt{-a}} \arcsin(x\sqrt{\frac{-a}{c}})$$

$$\frac{1}{\sqrt{ax^{2}+c}}(a>0) \to \frac{1}{\sqrt{a}} \ln(x\sqrt{a}+\sqrt{ax^{2}+c})$$

$$\frac{1}{\sqrt{ax^{2}+c}}(a<0) \to \frac{1}{\sqrt{-a}} \arcsin(x\sqrt{\frac{a}{c}})$$

$$\sin^{2}ax \to \frac{x}{2} - \frac{1}{4a} \sin 2ax$$

$$\cos^{2}ax \to \frac{x}{2} + \frac{1}{4a} \sin 2ax$$

$$\cos^{2}ax \to \frac{x}{2} + \frac{1}{4a} \sin 2ax$$

$$\cos^{2}ax \to \frac{1}{a} \ln \tan \frac{ax}{2}$$

$$\frac{1}{\cos ax} \to \frac{1}{a} \ln \tan \frac{ax}{2}$$

$$\frac{1}{\cos ax} \to \frac{1}{a} \ln \tan (\frac{\pi}{4} + \frac{ax}{2})$$

$$\ln(ax) \to x \ln(ax) - x$$

$$\sin^{3}ax \to \frac{-1}{a} \cos ax + \frac{1}{3a} \cos^{3}ax$$

$$\cos^{3}ax \to \frac{1}{a} \sin ax - \frac{1}{3a} \sin^{3}ax$$

$$\frac{1}{\sin^{2}ax} \to -\frac{1}{a} \cot ax$$

$$\begin{split} x\ln(ax) &\rightarrow \frac{x^2}{2}\ln(ax) - \frac{x^2}{4} \\ \cos ax &\rightarrow \frac{1}{a}\sin ax \\ x^2e^{ax} &\rightarrow \frac{e^{ax}}{a^3}(a^2x^2 - 2ax + 2) \\ (\ln(ax))^2 &\rightarrow x(\ln(ax))^2 - 2x\ln(ax) + 2x \\ x^2\ln(ax) &\rightarrow \frac{x^3}{3}\ln(ax) - \frac{x^3}{9} \\ x^n\ln(ax) &\rightarrow \frac{x^{n+1}}{n+1}\ln(ax) - \frac{x^{n+1}}{(n+1)^2} \\ \sin(\ln ax) &\rightarrow \frac{x}{2}[\sin(\ln ax) - \cos(\ln ax)] \\ \cos(\ln ax) &\rightarrow \frac{x}{2}[\sin(\ln ax) + \cos(\ln ax)] \end{split}$$

数学公式 8.2

组合公式

• fibonacci

 $f_0 = 0, f_1 = 1$ $f_{n+2}f_n - f_{n+1}^2 = (-1)^{n+1}$ $f_{-n} = (-1)^{n-1}f_n$ $f_{n+k} = f_k f_{n+1} + f_{k-1} f_n$ $gcd(f_m, f_n) = f_{gcd(m,n)}$ $f_m | f_n^2 \Leftrightarrow n f_n | m$

• $\sum_{k=1}^{n} (2k-1)^2 = \frac{n(4n^2-1)}{3}$

• $\sum_{k=1}^{n} k^3 = (\frac{n(n+1)}{2})^2$

• $\sum_{k=1}^{n} (2k-1)^3 = n^2(2n^2-1)$

• $\sum_{k=1}^{n} k^4 = \frac{n(n+1)(2n+1)(3n^2+3n-1)}{30}$

• $\sum_{k=1}^{n} k^5 = \frac{n^2(n+1)^2(2n^2+2n-1)}{12}$

• $\sum_{k=1}^{n} k(k+1) = \frac{n(n+1)(n+2)}{3}$

• $\sum_{k=1}^{n} k(k+1)(k+2) = \frac{n(n+1)(n+2)(n+3)}{4}$

• $\sum_{k=1}^{n} k(k+1)(k+2)(k+3) = \frac{n(n+1)(n+2)(n+3)(n+4)}{5}$

• 错排: $D_n = n!(1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} + \dots + \frac{(-1)^n}{n!}) = (n-1)(D_{n-2} - D_{n-1})$

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8.3 平面几何公式

三角形

- 1. 半周长 P = (a+b+c)/2
- 2. 面积 $S = aH_a/2 = ab\sin(C)/2 = \sqrt{P(P-a)(P-b)(P-c)}$
- 3. 中线 $M_a = \sqrt{2(b^2+c^2)-a^2}/2 = \sqrt{b^2+c^2+2bc\cos(A)}/2$
- 4. 角平分线 $T_a = \sqrt{bc((b+c)^2 a^2)}/(b+c) = 2bc\cos(A/2)/(b+c)$
- 5. 高线 $H_a = b\sin(C) = c\sin(B) = \sqrt{b^2 ((a^2 + b^2 c^2)/(2a))^2}$
- 6. 内切圆半径

$$\begin{split} r &= S/P = \arcsin(B/2)\sin(C/2)/\sin((B+C)/2) = 4R\sin(A/2)\sin(B/2)\sin(C/2) \\ &= \sqrt{(P-a)(P-b)(P-c)/P} = P\tan(A/2)\tan(B/2)\tan(C/2) \end{split}$$

7. 外接圆半径 $R = abc/(4S) = a/(2\sin(A)) = b/(2\sin(B)) = c/(2\sin(C))$

四边形

D1, D2 为对角线, M 对角线中点连线, A 为对角线夹角

- 1. $a^2 + b^2 + c^2 + d^2 = D1^2 + D2^2 + 4M^2$
- 2. $S = D1D2\sin(A)/2$
- 3. 圆内接四边形 ac + bd = D1D2
- 4. 圆内接四边形, P 为半周长 $S = \sqrt{(P-a)(P-b)(P-c)(P-d)}$

正n边形

R 为外接圆半径,r 为内切圆半径

- 1. 中心角 $A=2\pi/n$
- 2. 内角 $C = (n-2)\pi/n$
- 3. 边长 $a = 2\sqrt{R^2 r^2} = 2R\sin(A/2) = 2r\tan(A/2)$
- 4. 面积 $S = nar/2 = nr^2 \tan(A/2) = nR^2 \sin(A)/2 = na^2/(4\tan(A/2))$

员

- 1. 弧长 l=rA
- 2. 弦长 $a = 2\sqrt{2hr h^2} = 2r\sin(A/2)$
- 3. 弓形高 $h=r-\sqrt{r^2-a^2/4}=r(1-\cos(A/2))=\arctan(A/4)/2$
- 4. 扇形面积 $S1 = rl/2 = r^2A/2$
- 5. 弓形面积 $S2 = (rl a(r h))/2 = r^2(A \sin(A))/2$

棱柱

- 1. 体积 V = Ah, A 为底面积, h 为高
- 2. 侧面积 S = lp, l 为棱长, p 为直截面周长
- 3. 全面积 T = S + 2A

棱锥

- 1. 体积 V = Ah, A 为底面积, h 为高
- 2. 正棱锥侧面积 $S=lp,\ l$ 为棱长, p 为直截面周长
- 3. 正棱锥全面积 T = S + 2A

棱台

- 1. 体积 $V = (A1 + A2 + \sqrt{A1A2})h/3$, A1, A2 为上下底面积, h 为高
- 2. 正棱台侧面积 $S=(p1+p2)l/2,\ p1,p2$ 为上下底面周长, l 为斜高
- 3. 正棱台全面积 T = S + A1 + A2

圆柱

- 1. 侧面积 $S=2\pi rh$
- 2. 全面积 $T = 2\pi r(h+r)$
- 3. 体积 $V=\pi r^2 h$

圆锥

- 1. 母线 $l = \sqrt{h^2 + r^2}$
- 2. 侧面积 $S = \pi r l$
- 3. 全面积 $T = \pi r(l+r)$
- 4. 体积 $V = \pi r^2 h/3$

圆台

- 1. 母线 $l = \sqrt{h^2 + (r1 r2)^2}$
- 2. 侧面积 $S = \pi(r1 + r2)l$
- 3. 全面积 $T = \pi r 1(l + r 1) + \pi r 2(l + r 2)$
- 4. 体积 $V = \pi(r1^2 + r2^2 + r1r2)h/3$

8.4. 网络流 HINTS 159

球

- 1. 全面积 $T = 4\pi r^2$
- 2. 体积 $V = 4\pi r^3/3$

球台

- 1. 侧面积 $S=2\pi rh$
- 2. 全面积 $T = \pi(2rh + r1^2 + r2^2)$
- 3. 体积 $V = \pi h(3(r1^2 + r2^2) + h^2)/6$

球扇形

- 1. 全面积 $T = \pi r(2h + r0)$, h 为球冠高, r0 为球冠底面半径
- 2. 体积 $V = 2\pi r^2 h/3$

8.4 网络流 Hints

下界: (u, v) 下界为 c: 超级源到 t 建流量为 c, s 到超级汇建流量为 c, (原来的汇到原来的源建无穷, 如果有), 流一遍超级源出边满了就存在可行流.

下界最大流 (有源汇): 上面的搞完从原来的源到原来的汇流一遍下界最小流 (有源汇): 上面的搞完从原来的汇到原来的源流一遍

8.5 2-SATHints

每对点都选择强连通时 color 较小的

8.6 二分图相关 Hints

二分图最小覆盖集: 从右边的所有没有匹配过的点出发走增广路, 右边所有没有打上记号的点, 加上左边已经有记号的点.

最小覆盖数 = 最大匹配数.

8.7 java hints

旧

```
1 import java.io.*;
2 import java.util.*;
3 import java.math.*;
4
5 class InputReader {
```

```
6
        BufferedReader buff;
 7
        StringTokenizer tokenizer;
 8
 9
        InputReader(InputStream stream) {
10
            buff = new BufferedReader(new InputStreamReader(stream));
11
            tokenizer = null;
12
13
        boolean hasNext() {
            while (tokenizer == null || !tokenizer.hasMoreTokens())
14
15
                try {
                    tokenizer = new StringTokenizer(buff.readLine());
16
17
18
                catch (Exception e) {
19
                    return false;
20
                }
21
            return true;
22
        }
23
        String next() {
24
            if (!hasNext())
25
                throw new RuntimeException();
26
            return tokenizer.nextToken();
27
28
        int nextInt() { return Integer.parseInt(next()); }
29
        long nextLong() { return Long.parseLong(next()); }
30
   }
31
32
   class Node implements Comparable<Node> {
33
        int key;
34
        public int compareTo(Node o) {
35
            if (key != o.key)
36
                return key < o.key ? -1 : 1;
37
            return 0;
38
39
        public boolean equals(Object o) { return false; }
40
        public String toString() { return ""; }
41
        public int hashCode() { return key; }
42
   }
43
44 class MyComparator implements Comparator<Node> {
45
        public int compare(Node a, Node b) {
46
            if (a.key != b.key)
47
                return a.key < b.key ? -1:1;
48
            return 0;
49
        }
50
   }
51
52
   public class Main {
53
        public static void main(String[] args) {
54
            new Main().run();
```

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```
55
56
       void run() {
57
           PriorityQueue<Integer> Q = new PriorityQueue<Integer>();
58
           Q.offer(1); Q.poll(); Q.peek(); Q.size();
59
60
           HashMap<Node, Integer> dict = new HashMap<Node, Integer>();
61
           dict.entrySet(); dict.put(new Node(), 0); dict.containsKey(new Node());
62
            //Map.Entry e = (Map.Entry)it.next(); e.getValue(); e.getKey();
63
64
           HashSet<Node> h = new HashSet<Node>();
65
           h.contains(new Node()); h.add(new Node()); h.remove(new Node());
66
67
           Random rand = new Random();
68
           rand.nextInt(); rand.nextDouble();
69
70
           int temp = 0;
71
           BigInteger a = BigInteger.ZERO, b = new BigInteger("1"), c =
72
                     BigInteger.valueOf(2);
73
           a.remainder(b); a.modPow(b, c); a.pow(temp); a.intValue();
74
           a.isProbablePrime(temp); // 1 - 1 / 2 ^ certainty
75
           a.nextProbablePrime();
76
77
           Arrays.asList(array);
           Arrays.sort(array, fromIndex, toIndex, comparator);
78
79
           Arrays.fill(array, fromIndex, toIndex, value);
80
           Arrays.binarySearch(array, key, comparator); // found ? index : -
81
                    (insertPoint) - 1
82
           Arrays.equals(array, array2);
83
           Collection.toArray(arrayType[]);
84
           Collections.copy(dest, src);
85
86
           Collections.fill(collection, value);
87
           Collections.max(collection, comparator);
88
           Collections.replaceAll(list, oldValue, newValue);
89
           Collections.reverse(list);
90
           Collections.reverseOrder();
91
           Collections.rotate(list, distance); // -
92
           Collections.shuffle(list); // random_shuffle
93
       }
94
  }
   新
 1 import java.io.*;
 2 import java.util.*;
3 import java.math.*;
 4
5 public class Main {
       public static void main(String[] args) {
```

```
7
            InputStream inputStream = System.in;
 8
            OutputStream outputStream = System.out;
 9
            InputReader in = new InputReader(inputStream);
10
            PrintWriter out = new PrintWriter(outputStream);
11
            Task solver = new Task();
12
            solver.solve(1, in, out);
13
            out.close();
14
        }
15
   }
16
17
   class Task {
18
        public void solve(int testNumber, InputReader in, PrintWriter out) {
19
20
        }
21
   }
22
   class InputReader {
23
24
        public BufferedReader reader;
25
        public StringTokenizer tokenizer;
26
27
        public InputReader(InputStream stream) {
28
            reader = new BufferedReader(new InputStreamReader(stream), 32768);
29
            tokenizer = null;
30
        }
31
32
        public String next() {
            while (tokenizer == null || !tokenizer.hasMoreTokens()) {
33
34
                try {
35
                    tokenizer = new StringTokenizer(reader.readLine());
36
                } catch (IOException e) {
37
                    throw new RuntimeException(e);
38
                }
39
            }
40
            return tokenizer.nextToken();
41
        }
42
        public int nextInt() {
43
44
            return Integer.parseInt(next());
45
        }
46
47
        public long nextLong() {
48
            return Long.parseLong(next());
49
        }
50
   }
```

8.8 Usage_of_Rope

1 #include <ext/rope>