

# Module 3

April 13, 2021

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*You are currently looking at **version 1.0** of this notebook. To download notebooks and datafiles, as well as get help on Jupyter notebooks in the Coursera platform, visit the [Jupyter Notebook FAQ](#) course resource.*

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## 1 Applied Machine Learning: Module 3 (Evaluation)

### 1.1 Evaluation for Classification

#### 1.1.1 Preamble

```
In [1]: %matplotlib notebook
import numpy as np
import pandas as pd
import seaborn as sns
import matplotlib.pyplot as plt
from sklearn.model_selection import train_test_split
from sklearn.datasets import load_digits

dataset = load_digits()
X, y = dataset.data, dataset.target

for class_name, class_count in zip(dataset.target_names, np.bincount(dataset.target)):
    print(class_name, class_count)
```

0 178  
1 182  
2 177  
3 183  
4 181  
5 182  
6 181  
7 179  
8 174  
9 180

```
print('Original labels:\t', y[1:30])
print('New binary labels:\t', y_binary_imbalanced[1:30])
```

2



```
Support vector machine classifier (linear kernel, C=1)
[[402   5]
 [   5 38]]
```

```
In [10]: from sklearn.linear_model import LogisticRegression

lr = LogisticRegression().fit(X_train, y_train)
lr_predicted = lr.predict(X_test)
confusion = confusion_matrix(y_test, lr_predicted)

print('Logistic regression classifier (default settings)\n', confusion)
```

```
Logistic regression classifier (default settings)
[[401   6]
 [   6 37]]
```

```
In [11]: from sklearn.tree import DecisionTreeClassifier

dt = DecisionTreeClassifier(max_depth=2).fit(X_train, y_train)
tree_predicted = dt.predict(X_test)
confusion = confusion_matrix(y_test, tree_predicted)

print('Decision tree classifier (max_depth = 2)\n', confusion)
```

```
Decision tree classifier (max_depth = 2)
[[400   7]
 [  17 26]]
```

### 1.1.4 Evaluation metrics for binary classification

```
In [12]: from sklearn.metrics import accuracy_score, precision_score, recall_score,
# Accuracy = TP + TN / (TP + TN + FP + FN)
# Precision = TP / (TP + FP)
# Recall = TP / (TP + FN) Also known as sensitivity, or True Positive Rat
# F1 = 2 * Precision * Recall / (Precision + Recall)
print('Accuracy: {:.2f}'.format(accuracy_score(y_test, tree_predicted)))
print('Precision: {:.2f}'.format(precision_score(y_test, tree_predicted)))
print('Recall: {:.2f}'.format(recall_score(y_test, tree_predicted)))
print('F1: {:.2f}'.format(f1_score(y_test, tree_predicted)))
```

```
Accuracy: 0.95
Precision: 0.79
Recall: 0.60
F1: 0.68
```

```
In [13]: # Combined report with all above metrics
         from sklearn.metrics import classification_report

         print(classification_report(y_test, tree_predicted, target_names=['not 1',
                                     precision    recall  f1-score   support

not 1      0.96      0.98      0.97       407
  1         0.79      0.60      0.68        43

avg / total      0.94      0.95      0.94       450
```

```
In [ ]: print('Random class-proportional (dummy)\n',
              classification_report(y_test, y_classprop_predicted, target_names=['not 1',
              print('SVM\n',
                    classification_report(y_test, svm_predicted, target_names = ['not 1',
              print('Logistic regression\n',
                    classification_report(y_test, lr_predicted, target_names = ['not 1',
              print('Decision tree\n',
                    classification_report(y_test, tree_predicted, target_names = ['not 1',
```

### 1.1.5 Decision functions

```
In [14]: X_train, X_test, y_train, y_test = train_test_split(X, y_binary_imbalanced,
                    y_scores_lr = lr.fit(X_train, y_train).decision_function(X_test)
                    y_score_list = list(zip(y_test[0:20], y_scores_lr[0:20]))

                    # show the decision_function scores for first 20 instances
                    y_score_list
```

```
Out[14]: [(0, -23.172292973469546),
          (0, -13.542576515500063),
          (0, -21.717588760007867),
          (0, -18.903065133316439),
          (0, -19.733169947138638),
          (0, -9.7463217496747667),
          (1, 5.2327155658831135),
          (0, -19.308012306288916),
          (0, -25.099330209728528),
          (0, -21.824312362996),
          (0, -24.14378275072049),
          (0, -19.578811099762508),
          (0, -22.568371393280199),
          (0, -10.822590225240777),
          (0, -11.907918741521932),
          (0, -10.977026853802803),
          (1, 11.206811164226373),
```

```
(0, -27.64415761980748),
(0, -12.857692102545409),
(0, -25.848149140240199)]
```

```
In [15]: X_train, X_test, y_train, y_test = train_test_split(X, y_binary_imbalanced,
y_proba_lr = lr.fit(X_train, y_train).predict_proba(X_test)
y_proba_list = list(zip(y_test[0:20], y_proba_lr[0:20,1]))

# show the probability of positive class for first 20 instances
y_proba_list
```

```
Out[15]: [(0, 8.6377579220606777e-11),
(0, 1.3138118599563783e-06),
(0, 3.6997386039099529e-10),
(0, 6.1730972504865465e-09),
(0, 2.6914925394345074e-09),
(0, 5.8506057771143608e-05),
(1, 0.99468934644404694),
(0, 4.1175302368500096e-09),
(0, 1.2574750894253029e-11),
(0, 3.3252290754668869e-10),
(0, 3.2695529799373086e-11),
(0, 3.1407283576084884e-09),
(0, 1.5800864117150149e-10),
(0, 1.9943442430612578e-05),
(0, 6.7368003023860014e-06),
(0, 1.7089540581641637e-05),
(1, 0.9999864188091131),
(0, 9.8694940340195476e-13),
(0, 2.6059983600823893e-06),
(0, 5.9469113009063784e-12)]
```

### 1.1.6 Precision-recall curves

```
In [16]: from sklearn.metrics import precision_recall_curve

precision, recall, thresholds = precision_recall_curve(y_test, y_scores_lr)
closest_zero = np.argmin(np.abs(thresholds))
closest_zero_p = precision[closest_zero]
closest_zero_r = recall[closest_zero]

plt.figure()
plt.xlim([0.0, 1.01])
plt.ylim([0.0, 1.01])
plt.plot(precision, recall, label='Precision-Recall Curve')
plt.plot(closest_zero_p, closest_zero_r, 'o', markersize = 12, fillstyle = 'none')
plt.xlabel('Precision', fontsize=16)
plt.ylabel('Recall', fontsize=16)
```

```
plt.axes().set_aspect('equal')
plt.show()
```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

### 1.1.7 ROC curves, Area-Under-Curve (AUC)

```
In [17]: from sklearn.metrics import roc_curve, auc
```

```
X_train, X_test, y_train, y_test = train_test_split(X, y_binary_imbalanced
```

```
y_score_lr = lr.fit(X_train, y_train).decision_function(X_test)
fpr_lr, tpr_lr, _ = roc_curve(y_test, y_score_lr)
roc_auc_lr = auc(fpr_lr, tpr_lr)
```

```
plt.figure()
plt.xlim([-0.01, 1.00])
plt.ylim([-0.01, 1.01])
plt.plot(fpr_lr, tpr_lr, lw=3, label='LogRegr ROC curve (area = {:.2f})'.
plt.xlabel('False Positive Rate', fontsize=16)
plt.ylabel('True Positive Rate', fontsize=16)
plt.title('ROC curve (1-of-10 digits classifier)', fontsize=16)
plt.legend(loc='lower right', fontsize=13)
plt.plot([0, 1], [0, 1], color='navy', lw=3, linestyle='--')
plt.axes().set_aspect('equal')
plt.show()
```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```
In [18]: from matplotlib import cm
```

```
X_train, X_test, y_train, y_test = train_test_split(X, y_binary_imbalanced
```

```
plt.figure()
plt.xlim([-0.01, 1.00])
plt.ylim([-0.01, 1.01])
for g in [0.01, 0.1, 0.20, 1]:
    svm = SVC(gamma=g).fit(X_train, y_train)
    y_score_svm = svm.decision_function(X_test)
    fpr_svm, tpr_svm, _ = roc_curve(y_test, y_score_svm)
    roc_auc_svm = auc(fpr_svm, tpr_svm)
```

```

accuracy_svm = svm.score(X_test, y_test)
print("gamma = {:.2f}    accuracy = {:.2f}    AUC = {:.2f}".format(g, acc, roc_auc))

plt.plot(fpr_svm, tpr_svm, lw=3, alpha=0.7,
         label='SVM (gamma = {:.0.2f}), area = {:.0.2f}'.format(g, roc_auc))

plt.xlabel('False Positive Rate', fontsize=16)
plt.ylabel('True Positive Rate (Recall)', fontsize=16)
plt.plot([0, 1], [0, 1], color='k', lw=0.5, linestyle='--')
plt.legend(loc="lower right", fontsize=11)
plt.title('ROC curve: (1-of-10 digits classifier)', fontsize=16)
plt.axes().set_aspect('equal')

plt.show()

```

<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

```

gamma = 0.01    accuracy = 0.91    AUC = 1.00
gamma = 0.10    accuracy = 0.90    AUC = 0.98
gamma = 0.20    accuracy = 0.90    AUC = 0.66
gamma = 1.00    accuracy = 0.90    AUC = 0.50

```

## 1.1.8 Evaluation measures for multi-class classification

### Multi-class confusion matrix

```

In [19]: dataset = load_digits()
X, y = dataset.data, dataset.target
X_train_mc, X_test_mc, y_train_mc, y_test_mc = train_test_split(X, y, random_state=0)

svm = SVC(kernel = 'linear').fit(X_train_mc, y_train_mc)
svm_predicted_mc = svm.predict(X_test_mc)
confusion_mc = confusion_matrix(y_test_mc, svm_predicted_mc)
df_cm = pd.DataFrame(confusion_mc,
                     index = [i for i in range(0,10)], columns = [i for i in range(0,10)])

plt.figure(figsize=(5.5,4))
sns.heatmap(df_cm, annot=True)
plt.title('SVM Linear Kernel \nAccuracy:{0:.3f}'.format(accuracy_score(y_test_mc, svm_predicted_mc)))

plt.ylabel('True label')
plt.xlabel('Predicted label')

```



```

svm = SVC(kernel = 'rbf').fit(X_train_mc, y_train_mc)
svm_predicted_mc = svm.predict(X_test_mc)
confusion_mc = confusion_matrix(y_test_mc, svm_predicted_mc)
df_cm = pd.DataFrame(confusion_mc, index = [i for i in range(0,10)],
                      columns = [i for i in range(0,10)])

plt.figure(figsize = (5.5,4))
sns.heatmap(df_cm, annot=True)
plt.title('SVM RBF Kernel \nAccuracy:{0:.3f}'.format(accuracy_score(y_test_mc, svm_predicted_mc)))

plt.ylabel('True label')
plt.xlabel('Predicted label');

```

<IPython.core.display.Javascript object>

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<IPython.core.display.Javascript object>

<IPython.core.display.HTML object>

### Multi-class classification report

```
In [20]: print(classification_report(y_test_mc, svm_predicted_mc))
```

	precision	recall	f1-score	support
0	1.00	0.65	0.79	37
1	1.00	0.23	0.38	43
2	1.00	0.39	0.56	44
3	1.00	0.93	0.97	45
4	0.14	1.00	0.25	38
5	1.00	0.33	0.50	48
6	1.00	0.54	0.70	52
7	1.00	0.35	0.52	48
8	1.00	0.02	0.04	48
9	1.00	0.55	0.71	47
avg / total	0.93	0.49	0.54	450

## Micro- vs. macro-averaged metrics

```
In [21]: print('Micro-averaged precision = {:.2f} (treat instances equally)'\n              .format(precision_score(y_test_mc, svm_predicted_mc, average = 'micro'))\n          print('Macro-averaged precision = {:.2f} (treat classes equally)'\n              .format(precision_score(y_test_mc, svm_predicted_mc, average = 'macro')))
```

Micro-averaged precision = 0.49 (treat instances equally)  
Macro-averaged precision = 0.91 (treat classes equally)

```
In [22]: print('Micro-averaged f1 = {:.2f} (treat instances equally)'\n              .format(f1_score(y_test_mc, svm_predicted_mc, average = 'micro')))\n          print('Macro-averaged f1 = {:.2f} (treat classes equally)'\n              .format(f1_score(y_test_mc, svm_predicted_mc, average = 'macro')))
```

Micro-averaged f1 = 0.49 (treat instances equally)  
Macro-averaged f1 = 0.54 (treat classes equally)

### 1.1.9 Regression evaluation metrics

```
In [23]: %matplotlib notebook\nimport matplotlib.pyplot as plt\nimport numpy as np\nfrom sklearn.model_selection import train_test_split\nfrom sklearn import datasets\nfrom sklearn.linear_model import LinearRegression\nfrom sklearn.metrics import mean_squared_error, r2_score\nfrom sklearn.dummy import DummyRegressor\n\ndiabetes = datasets.load_diabetes()\n\nX = diabetes.data[:, None, 6]\ny = diabetes.target\n\nX_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)\n\nlm = LinearRegression().fit(X_train, y_train)\nlm_dummy_mean = DummyRegressor(strategy = 'mean').fit(X_train, y_train)\n\ny_predict = lm.predict(X_test)\ny_predict_dummy_mean = lm_dummy_mean.predict(X_test)\n\nprint('Linear model, coefficients: ', lm.coef_)\nprint("Mean squared error (dummy): {:.2f}".format(mean_squared_error(y_test, y_predict_dummy_mean)))\nprint("Mean squared error (linear model): {:.2f}".format(mean_squared_error(y_test, y_predict)))\nprint("r2_score (dummy): {:.2f}".format(r2_score(y_test, y_predict_dummy_mean)))
```

```

print("r2_score (linear model): {:.2f}".format(r2_score(y_test, y_predict))

# Plot outputs
plt.scatter(X_test, y_test, color='black')
plt.plot(X_test, y_predict, color='green', linewidth=2)
plt.plot(X_test, y_predict_dummy_mean, color='red', linestyle = 'dashed',
         linewidth=2, label = 'dummy')

plt.show()

```

```

Linear model, coefficients: [-698.80206267]
Mean squared error (dummy): 4965.13
Mean squared error (linear model): 4646.74
r2_score (dummy): -0.00
r2_score (linear model): 0.06

```

<IPython.core.display.Javascript object>

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### 1.1.10 Model selection using evaluation metrics

#### Cross-validation example

```

In [ ]: from sklearn.model_selection import cross_val_score
        from sklearn.svm import SVC

dataset = load_digits()
# again, making this a binary problem with 'digit 1' as positive class
# and 'not 1' as negative class
X, y = dataset.data, dataset.target == 1
clf = SVC(kernel='linear', C=1)

# accuracy is the default scoring metric
print('Cross-validation (accuracy)', cross_val_score(clf, X, y, cv=5))
# use AUC as scoring metric
print('Cross-validation (AUC)', cross_val_score(clf, X, y, cv=5, scoring =
# use recall as scoring metric
print('Cross-validation (recall)', cross_val_score(clf, X, y, cv=5, scoring

```

#### Grid search example

```

In [ ]: from sklearn.svm import SVC
        from sklearn.model_selection import GridSearchCV
        from sklearn.metrics import roc_auc_score

```

```

dataset = load_digits()
X, y = dataset.data, dataset.target == 1
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)

clf = SVC(kernel='rbf')
grid_values = {'gamma': [0.001, 0.01, 0.05, 0.1, 1, 10, 100]}

# default metric to optimize over grid parameters: accuracy
grid_clf_acc = GridSearchCV(clf, param_grid = grid_values)
grid_clf_acc.fit(X_train, y_train)
y_decision_fn_scores_acc = grid_clf_acc.decision_function(X_test)

print('Grid best parameter (max. accuracy): ', grid_clf_acc.best_params_)
print('Grid best score (accuracy): ', grid_clf_acc.best_score_)

# alternative metric to optimize over grid parameters: AUC
grid_clf_auc = GridSearchCV(clf, param_grid = grid_values, scoring = 'roc_auc')
grid_clf_auc.fit(X_train, y_train)
y_decision_fn_scores_auc = grid_clf_auc.decision_function(X_test)

print('Test set AUC: ', roc_auc_score(y_test, y_decision_fn_scores_auc))
print('Grid best parameter (max. AUC): ', grid_clf_auc.best_params_)
print('Grid best score (AUC): ', grid_clf_auc.best_score_)

```

## Evaluation metrics supported for model selection

```

In [ ]: from sklearn.metrics.scorer import SCORERS

print(sorted(list(SCORERS.keys()))))

```

### 1.1.11 Two-feature classification example using the digits dataset

#### Optimizing a classifier using different evaluation metrics

```

In [ ]: from sklearn.datasets import load_digits
        from sklearn.model_selection import train_test_split
        from adspy_shared_utilities import plot_class_regions_for_classifier_subplot
        from sklearn.svm import SVC
        from sklearn.model_selection import GridSearchCV

dataset = load_digits()
X, y = dataset.data, dataset.target == 1
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)

# Create a two-feature input vector matching the example plot above
# We jitter the points (add a small amount of random noise) in case there are
# in feature space where many instances have the same features.
jitter_delta = 0.25

```

```

X_twovar_train = X_train[:, [20, 59]] + np.random.rand(X_train.shape[0], 2) - 1
X_twovar_test = X_test[:, [20, 59]] + np.random.rand(X_test.shape[0], 2) - 1

clf = SVC(kernel = 'linear').fit(X_twovar_train, y_train)
grid_values = {'class_weight': ['balanced', {1:2}, {1:3}, {1:4}, {1:5}, {1:10}],
               'gamma': [0.001, 0.01, 0.1, 1, 10]}
plt.figure(figsize=(9,6))
for i, eval_metric in enumerate(['precision', 'recall', 'f1', 'roc_auc']):
    grid_clf_custom = GridSearchCV(clf, param_grid=grid_values, scoring=eval_metric)
    grid_clf_custom.fit(X_twovar_train, y_train)
    print('Grid best parameter (max. {0}): {1}'
          .format(eval_metric, grid_clf_custom.best_params_))
    print('Grid best score ({0}): {1}'
          .format(eval_metric, grid_clf_custom.best_score_))
plt.subplots_adjust(wspace=0.3, hspace=0.3)
plot_class_regions_for_classifier_subplot(grid_clf_custom, X_twovar_test, y_test,
                                         None, None, plt.subplot(2, 2, i+1))

plt.title(eval_metric+'-oriented SVC')
plt.tight_layout()
plt.show()

```

### Precision-recall curve for the default SVC classifier (with balanced class weights)

```

In [ ]: from sklearn.model_selection import train_test_split
        from sklearn.metrics import precision_recall_curve
        from adspy_shared_utilities import plot_class_regions_for_classifier
        from sklearn.svm import SVC

dataset = load_digits()
X, y = dataset.data, dataset.target == 1
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)

# create a two-feature input vector matching the example plot above
jitter_delta = 0.25
X_twovar_train = X_train[:, [20, 59]] + np.random.rand(X_train.shape[0], 2) - 1
X_twovar_test = X_test[:, [20, 59]] + np.random.rand(X_test.shape[0], 2) - 1

clf = SVC(kernel='linear', class_weight='balanced').fit(X_twovar_train, y_train)

y_scores = clf.decision_function(X_twovar_test)

precision, recall, thresholds = precision_recall_curve(y_test, y_scores)
closest_zero = np.argmin(np.abs(thresholds))
closest_zero_p = precision[closest_zero]
closest_zero_r = recall[closest_zero]

plot_class_regions_for_classifier(clf, X_twovar_test, y_test)
plt.title("SVC, class_weight = 'balanced', optimized for accuracy")

```

```

plt.show()

plt.figure()
plt.xlim([0.0, 1.01])
plt.ylim([0.0, 1.01])
plt.title ("Precision-recall curve: SVC, class_weight = 'balanced'")
plt.plot(precision, recall, label = 'Precision-Recall Curve')
plt.plot(closest_zero_p, closest_zero_r, 'o', markersize=12, fillstyle='none')
plt.xlabel('Precision', fontsize=16)
plt.ylabel('Recall', fontsize=16)
plt.axes().set_aspect('equal')
plt.show()
print('At zero threshold, precision: {:.2f}, recall: {:.2f}'
      .format(closest_zero_p, closest_zero_r))

```

In [ ]: