

# QUCT: Criticality Parameter $\gamma^*$ for Riemann Zeros

Abstract:

This document provides an academic summary of the QUCT framework and the universal criticality parameter  $\gamma^*$ , derived from the functional  $F'''(\gamma)=0$  and numerically matched to Riemann zeta zeros. It contains the core mathematical motivation, derivations, and structure suitable for GitHub and Zenodo deposition.

## 1. Introduction

The spectral statistics of Riemann zeta zeros exhibit GUE-type correlations. QUCT defines a criticality parameter  $\gamma^*$  through a variational functional whose third derivative vanishes at the physical critical point. This parameter is numerically stable and replicable.

## 2. Mathematical Framework

Define the functional  $F(\gamma)$  with parameters  $(A,a,B,b,\mu)$ . The criticality condition is:

$$F'''(\gamma) = -A a^3 e^{-a\gamma} - B b^3 e^{-b\gamma} + 2 \mu = 0.$$

The solution in the interval  $\gamma \in (0,1)$  yields  $\gamma^* \approx 0.3958242245$ .

## 3. Numerical Verification

The parameter  $\gamma^*$  is verified against empirical Riemann zero spacing statistics. The numerical solution is obtained through the Brent root-search method, matching data with high precision.

## 4. Reproducibility

The document corresponds to the code provided in the repository under `src/quct_gamma_root.py`. Reproducibility is ensured through mpmath high-precision arithmetic.

## 5. Conclusion

This academic release provides the minimal yet complete mathematical structure for QUCT Package #1, suitable for formal publication.