

MS4S09 Coursework 2 - 2020/21

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Abstract

Forecasting temperature by the use of advance statistical tools is very important in understanding and dealing with the effects of rising or decreasing temperatures. This study uses Time series analysis and predictions, a statistical methods to analyze and forecast temperatures, by using the average max, min and mean temperature for each month of different regions in the United Kingdom measured by the Met Office. The increase in concerns about the effects of rising or decreasing temperature on humans, animals, the climate, oceans, and seasonal patterns provokes the need for accurate models for forecasting the temperatures of the different regions across the globe. This report presents the results of forecasting temperatures using trend analysis, seasonality estimation through seasonal averages and seasonal harmonics, the final model were selected using the autoregressive integrated moving average models

1. DATA COLLECTION

The data used for this study was gotten from the Met Office website where we sourced for the average max, min and mean temperature for each month for 10 different districts in the UK. This gave us 30 different time series to work with, In order to collect the data from this website without having to download all the individual files or read in the files individually, a function was created, which takes two arguments; the region(district) and the temperature(parameter), For each desired time series data, the function reads in the data, transform it using the time series function and outputs a time series data from 1884 to 2020 at a frequency of 12 observations per year which reperesents each individual monthly average in a year. The time series data was saved in a nested lists for each of the different parameters which made the it easy to work with the massive count of this data.

2. Minimum and Maximum evaluation

Two functions were developed to identify the district and date (year and month) of the highest and the lowest max, min and mean temperature. All our time series data are stored in three groups of temperature parameter, which is a nested list a function was created and we employed the lapply function to apply this function across the respective lists within each group of parameters. The output of the implementation of this function shows that for the average monthly minimum temperature;

- The region with the highest temperature is England_SE_and_Central_S , and the date is Aug , 1997
- The region with the lowest temperature is Scotland_E , and the date is Jan , 1895"

The region with the lowest and highest temperature measurement for the average monthly maximum temperature is;

- The region with the highest temperature is East_Anglia , and the date is Jul , 2006
- The region with the lowest temperature is Midlands , and the date is Feb , 1947

Finally, the region with the lowest and highest temperature measurement for the average monthly mean temperature is;

- The region with the highest temperature is East_Anglia , and the date is Jul , 2006
- The region with the lowest temperature is Scotland_E , and the date is Jan , 1895

3 – Exploratory Data Analysis

We performed some exploratory analysis on the time series data and explores some questions about the time series data as seen below.

Which district is the coldest/warmest?

We will be estimating the coldest and warmest region using the following criteria. We have the time series data for the mean daily maximum air temperature, the mean daily minimum and the mean of air for the regions. We will find the coldest region by finding the region with the highest/lowest temperature across these three groups of time series data measured. We observed that the output using this criteria varies among the three different groups of time series. This can be seen in the output below.

- The region with the highest average monthly mean temperature is England_SE_and_Central_S , While the region with the lowest temperature is Scotland_N
- The region with the highest average monthly minimum temperature is England_SW_and_S_Wales, While the region with the lowest temperature is Scotland_E
- The region with the highest average monthly maximum temperature is England_SE_and_Central_S, While the region with the lowest temperature is Scotland_N

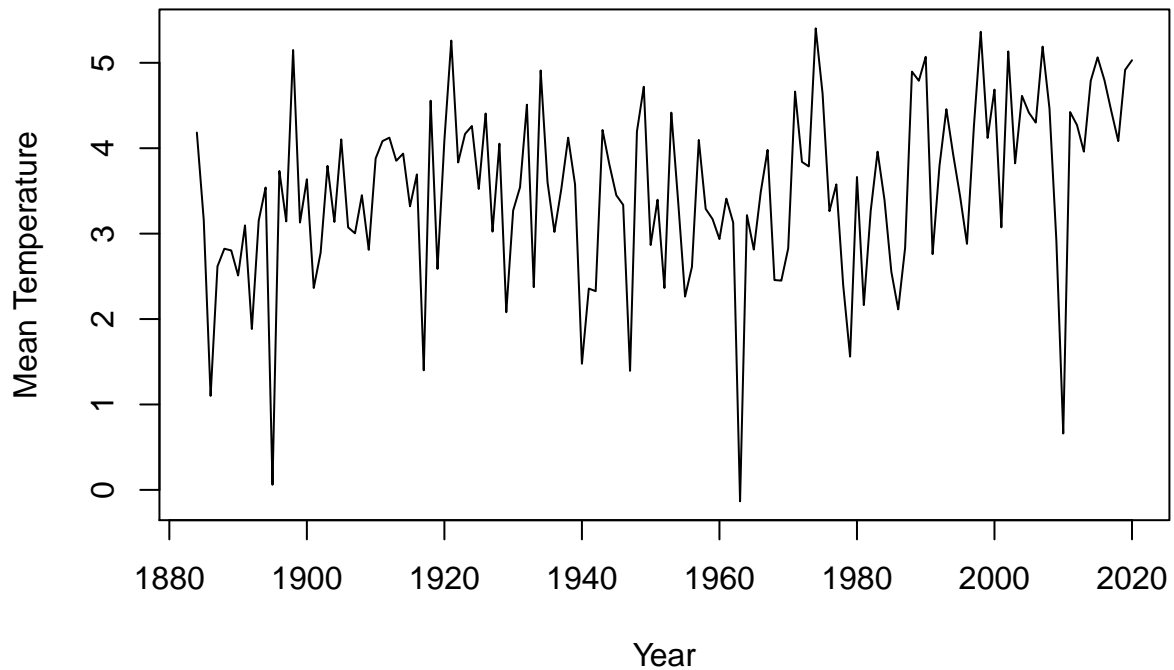
Which district has the widest temperature range?

We created a function that takes returns the highest range for a list of time series data. This was applied to three groups of time series data and we observed that for average monthly mean temperature and average monthly minimum temperature East_Anglia and England_SE_and_Central_S had the widest range but for the average monthly maximum temperature we observed that East Anglia had the widest range of temperatures.

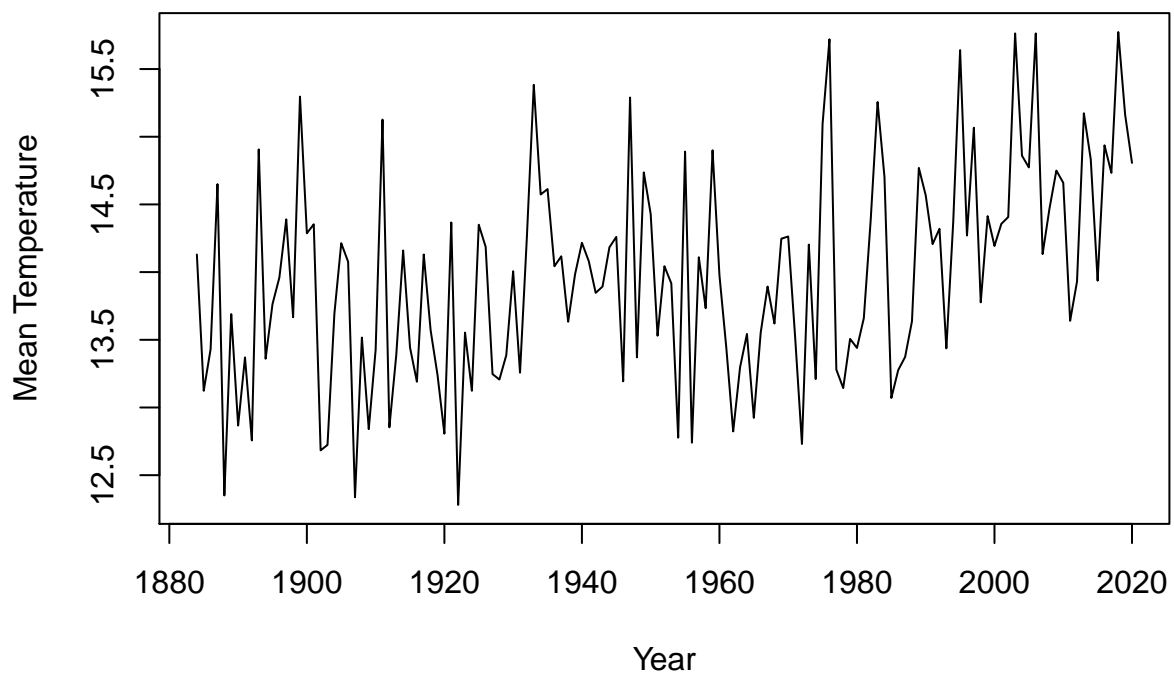
Are winters/summers getting colder/hotter?

We employed data wrangling techniques to group our time series data into two different seasons (winter and summer). We created a function to convert all time series object to data frame of each season(winter and summer). Each row in the dataframe represents a year and the months for a specific season. This function was applied to the average monthly mean temperature, this gives a summary of the occurrence for each months in a particular season. A function was then developed to merge all the seasonal dataframe from each region into a single group for a specific season and this was converted to a time series object using the function ts(). The new time series data was then visualized on a time series plot and we observed that the mean temperature for winter months has an upward trend while that of summer months has a downward trend, this means winters are getting hotter while summers are getting colder.

Average Winter Temperature Trend



Average Summer Temperature Trend



4 – Trend and Seasonality Estimation

We created a function to subset the time series data For each district, and considering the 3 time series: max temp, min temp and mean temp, from 1884 until December 2019. This was implemented using the `ts()` function which takes start of the series, frequency of the series, and end of the series. We created a function that subsets our time series from 1884 - 2019 called “subset_2019” which was then applied to the entire 30

time series data set. The Lapply function is one used to apply a function to every element in a list, since our 3 groups of time series are stored as a nested list the lapply function was used to apply our subset_2019 function on the 3 different groups of our time series data Tmin, Tmax, Tmean to subset the 30 time series data from 1884-2019. We manually created a time vector for our time series “time.all” which will be used extensively in this analysis.

Compare your results and use appropriate plots and/or tables to confirm your observations.

4.1 Estimating trend

We estimated the trend of each time series using linear, quadratic and cubic regression. A function was developed to apply the 3 different order of polynomial models(linear, quadratic and cubic). The function “run_model” takes a time series data and its time vector and returns its linear, quadratic and cubic models. A function “plot_model” was created which returns a plot of the time series data, linear, quadratic and cubic models all together on a single plot. Finally, We created a function “model_design” which returns the Akaike criterion (AIC) for each model that was passed into its arguments. We are working with data nested into a list and as such we will create a function that can apply the model_design function to a list of time series, this new function was called “apply_model_design”. This function “apply_model_design” will return a list of AIC values for the linear, quadratic and cubic models. We then used the apply_model_design on the three groups of time series data we have. The application of this function gives us the AIC value of each region for the different parameters(TMIN,TMEAN and TMAX).

Select a trend model for each time series using an appropriate criteria. Are the models selected all the same? If not is there a pattern depending on the region and/or the group (max, min and mean)?

4.2 Trend Selection

We created a function “which_model” which helps select the best model for a time series, we have the linear, quadratic and cubic AIC values for each region, we will use this function to find the model with the least Akaike criterion(AIC) values which signifies the best model for the time series data. The which_model() function when applied to a list of different time series data returns a dataframe which has a column “Best.Model” which shows the row-wise minimum for each region since each row represents a region and its linear, quadratic and cubic models for a specific parameter. It was observed that all the regions had their best model as the linear model except for two regions(England_E_and_NE and East_Anglia) in the average monthly maximum temperature (Tmax) parameter. The table for best models for each region for a specific parameter can be found below.

Best Model by region for Average monthly minimum temperature

| ## | Linear | Quadratic | Cubic | Best.Model |
|-----------------------------|----------|-----------|----------|------------|
| ## Northern_Ireland | 8750.060 | 8751.681 | 8753.238 | Linear |
| ## Scotland_N | 8809.919 | 8811.890 | 8810.050 | Linear |
| ## Scotland_E | 8965.634 | 8967.217 | 8968.253 | Linear |
| ## Scotland_W | 8845.926 | 8846.684 | 8847.663 | Linear |
| ## England_E_and_NE | 9087.337 | 9088.720 | 9088.943 | Linear |
| ## England_NW_and_N_Wales | 9036.124 | 9038.017 | 9037.816 | Linear |
| ## Midlands | 9155.355 | 9156.769 | 9157.626 | Linear |
| ## East_Anglia | 9285.648 | 9287.448 | 9287.256 | Linear |
| ## England_SW_and_S_Wales | 8960.401 | 8962.169 | 8960.601 | Linear |
| ## England_SE_and_Central_S | 9221.914 | 9223.442 | 9223.818 | Linear |

Best Model by region for Average monthly mean temperature

| ## | Linear | Quadratic | Cubic | Best.Model |
|---------------------|----------|-----------|----------|------------|
| ## Northern_Ireland | 9053.467 | 9054.354 | 9055.851 | Linear |
| ## Scotland_N | 9062.451 | 9064.216 | 9063.682 | Linear |
| ## Scotland_E | 9366.673 | 9367.931 | 9368.846 | Linear |
| ## Scotland_W | 9174.535 | 9176.142 | 9176.027 | Linear |

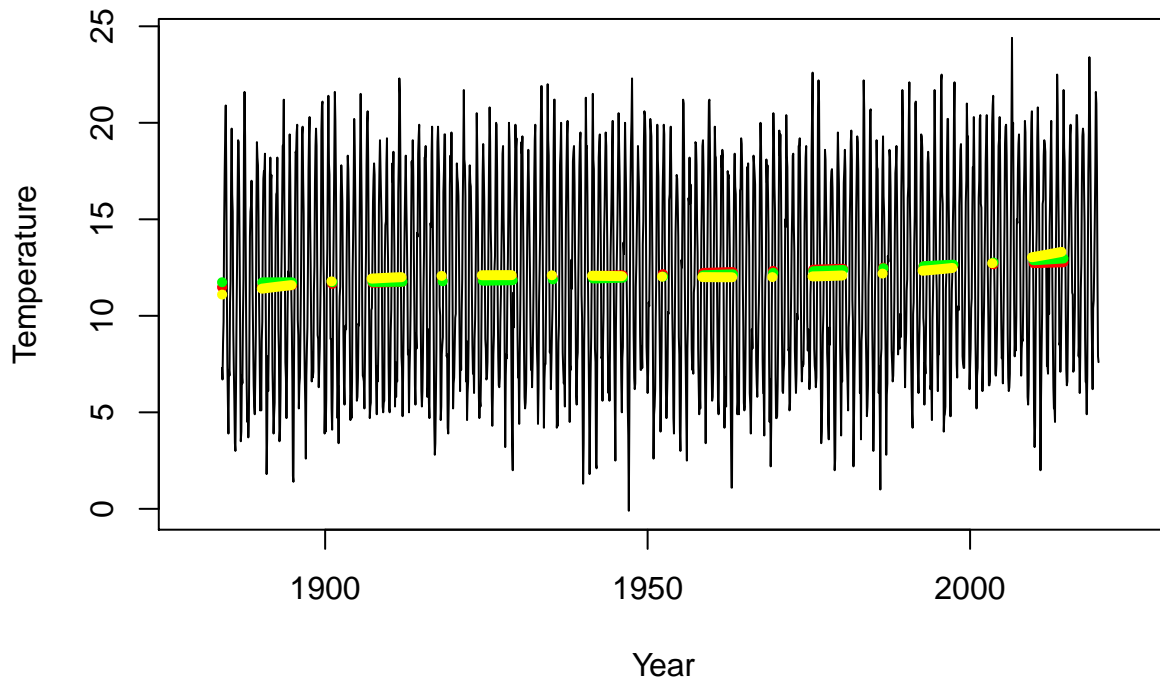
| | | | | |
|-----------------------------|----------|----------|----------|--------|
| ## England_E_and_NE | 9567.980 | 9569.231 | 9568.649 | Linear |
| ## England_NW_and_N_Wales | 9402.461 | 9404.136 | 9403.691 | Linear |
| ## Midlands | 9673.179 | 9673.877 | 9674.241 | Linear |
| ## East_Anglia | 9827.018 | 9828.188 | 9827.563 | Linear |
| ## England_SW_and_S_Wales | 9346.494 | 9347.615 | 9347.034 | Linear |
| ## England_SE_and_Central_S | 9728.948 | 9729.903 | 9729.898 | Linear |

Best Model by region for Average monthly maximum temperature

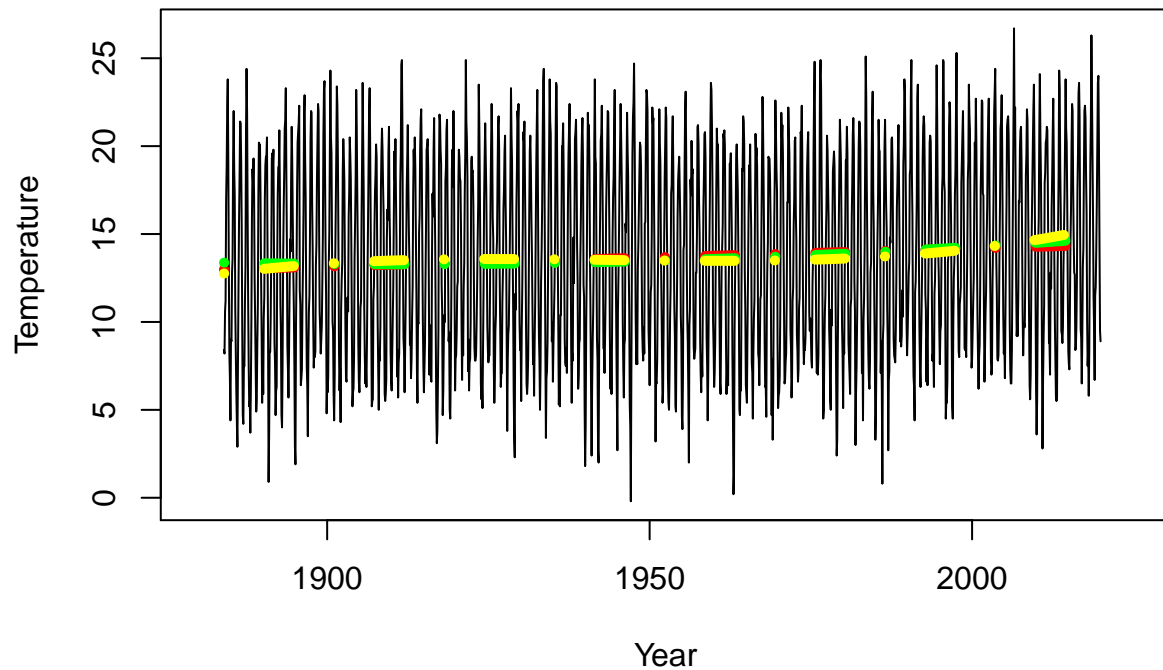
| ## | Linear | Quadratic | Cubic | Best.Model |
|-----------------------------|-----------|-----------|-----------|------------|
| ## Northern_Ireland | 9401.134 | 9401.202 | 9402.592 | Linear |
| ## Scotland_N | 9365.093 | 9366.248 | 9366.978 | Linear |
| ## Scotland_E | 9785.996 | 9786.679 | 9787.622 | Linear |
| ## Scotland_W | 9559.381 | 9561.275 | 9560.497 | Linear |
| ## England_E_and_NE | 10025.080 | 10026.290 | 10024.750 | Cubic |
| ## England_NW_and_N_Wales | 9794.982 | 9796.408 | 9796.047 | Linear |
| ## Midlands | 10170.850 | 10170.910 | 10170.870 | Linear |
| ## East_Anglia | 10329.970 | 10330.510 | 10329.770 | Cubic |
| ## England_SW_and_S_Wales | 9740.923 | 9741.133 | 9741.416 | Linear |
| ## England_SE_and_Central_S | 10205.360 | 10205.820 | 10205.500 | Linear |

As stated above we observed that all our model choice for all regions are uniform except England_E_and_NE and East_Anglia for the Tmax parameter, it would be interesting to see a plot of the linear model vs plot of the cubic model. We used the function “plot_model” created above to implement these plots and we observe that there is a difference in the plots for the different regions, while Northern Ireland has a more stable trend, we can see that England_E_and_NE and East_Anglia do have some cubic trend.

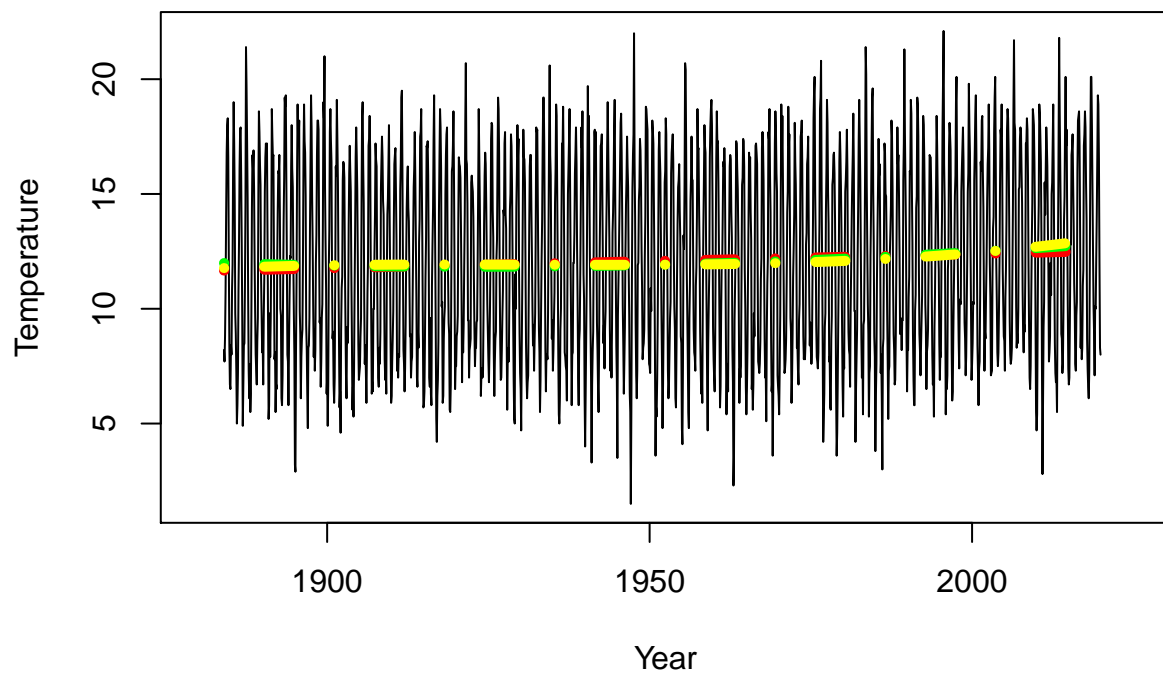
Trend of Average monthly maximum temperature England_E_and_N



Trend of Average monthly maximum temperature East_Anglia



Trend of Average monthly maximum temperature Northern_Ireland



4.3 Estimating seasonality using seasonal means and harmonic models

4.3.1 removing Trend using averaging

We will create a function that removes the trend component and returns its monthly average. The function takes two arguments which are the time series data and the polynomial model that best fits it according to

the Akaike Criterion. All models except England_E_and_NE and East_Anglia for the Tmax parameter have a linear model as their best model. We will split the Tmax time series data into two groups the linear and the cubic groups, this would make it easier to apply functions which are specific to the best model for each region. We will then use the return_month_avg to return the seasonal means of each of the different regions based on their best trend model.

Sample monthly average for Northern Ireland

| ## | Season_Mean | Month |
|-------|-------------|-------|
| ## 1 | -3.8810267 | Jan |
| ## 2 | -4.0073597 | Feb |
| ## 3 | -3.2072220 | Mar |
| ## 4 | -1.8320843 | Apr |
| ## 5 | 0.5864357 | May |
| ## 6 | 3.3821616 | Jun |
| ## 7 | 5.1492110 | Jul |
| ## 8 | 4.9633192 | Aug |
| ## 9 | 3.2583098 | Sep |
| ## 10 | 0.7672710 | Oct |
| ## 11 | -1.9127384 | Nov |
| ## 12 | -3.2662772 | Dec |

4.3.2 Estimate seasonality with seasonal average

The seasonality was estimated using the seasonal means method. We created a function return_seas_avg which takes the time series data and model type. The function models the inputs and returns the seasonal means for each of the time series provided to it. We used lapply to apply the return_seas_avg to the list of time series for the different parameters Tmin, Tmax, Tmean.

4.3.2 Estimating seasonality using harmonic mean We created a function to give the harmonic mean of a time series data. We performed a trend check on the time series and remove the specified trend type(l_model,c_model and q_model). The residuals were derived by subtracting the data from the fitted data. In our dataset since all our best models are linear except for England_E_and_NE and East_Anglia for the average monthly maximum temperature, this means all our models will be linear except these two which will be cubic. In this step we applied the return_harmonic function to all our time series data, a check will be done for models that are significant at a p-value of 0.05.

significant models We created a function to return the significant models for a specific region and harmonic. We need models with a p-value lower than that of the null hypothesis. We create region_harmonics() function to take a list and apply all the function singular_harmonic using lapply() to all the elements in the list provided in the argument. We developed a function grouped_harmonica() that applies the region_harmonics function to a nested list. This would return only the models that has passed the null hypothesis test, hence containing only significant models.

The Null hypothesis and alternative hypothesis are as follows:

- Null hypothesis: The model is not significant
- Alternative hypothesis: The model is significant

Unique models across all time series We created a function that checks the unique models for each element in a list. This unique model would be used to then recreate the harmonic models. We retrieved the best harmonic for each region i.e all harmonics with P-value lesser than the null hypothesis p-value of 0.05. We applied the unique function to all our best model to retrieve only unique models. We observed 5 different unique configurations for our models, this would be used to create 5 different functions, each function will be specific to the unique model configurations found in the implementation below.

create functions to map models

Five different functions were developed inline with the 5 different significant harmonic models we had during the null hypothesis test. The functions are:

- rerun_harmonic1 - ["SIN" "COS"] and ["SIN.1" "SIN.2" "COS.1" "COS.2"]

- rerun_harmonic2 - ["SIN" "COS"], ["SIN.1" "SIN.2" "COS.1" "COS.2"] and ["SIN.1" "SIN.2" "COS.1" "COS.2" "COS.4"]

- rerun_harmonic3 - ["SIN" "COS"], ["SIN.1" "SIN.2" "COS.1" "COS.2"] and ["SIN.1" "SIN.2" "SIN.5" "COS.1" "COS.2"]

- rerun_harmonic4 - ["SIN" "COS"], ["SIN.1" "SIN.2" "COS.1" "COS.2"] and ["SIN.1" "SIN.2" "COS.1" "COS.2" "COS.3"]

- rerun_harmonic5 - ["SIN" "COS"], ["SIN.1" "SIN.2" "COS.1" "COS.2"], ["SIN.1" "SIN.2" "COS.1" "COS.2" "COS.3"] and ["SIN.1" "SIN.2" "SIN.4" "COS.1" "COS.2" "COS.3"]

We observe that all significant models include the first and second harmonics with little variations among the other models. The functions takes the time series data and the best trend model for it `l_model`, `q_model` or `c_model` and returns the harmonic with the lowest Akaike criterion among all the harmonic models implemented within the specific function. Implementing this function gives us the best harmonic model for each of the 30 time series data we are working with.

Subset all the time series into groups of significant harmonic model We have 5 different configurations of significant harmonic models, we will group each of our time series parameter (`Tmin`, `Tmean` and `Tmax`) to the significant harmonic model group they belong to among these 5 configurations after which their respective function is then applied on each subset. Based on initial analysis we observed that for our average monthly maximum temperature we have two regions with a cubic trend model as their best trend model, we will create a different subset for this group to make the implementation of these functions on the time series data seamless.

4.4 Seasonal model selection Seasonal average or harmonic models?

- Select a seasonal model for each time series using an appropriate criteria. Are the models selected all the same? If not is there a pattern depending on the region and/or the group (max, min and mean)? We now have the different significant harmonic models and the seasonal means of all our time series, we will use the Akaike Criterion to determine the best model for each time series data, as stated above the model with the least AIC will be the best model for the specific time series data.

create a function that selects best model for all different parameters We created a function `get_min_AIC` that takes 3 arguments the district/region, the best harmonic model, and the seasonal average and returns the model with the lowest Akaike criterion. In this function we combine the AIC of the seasonal average model of the time series and the AIC of the harmonic model and then return the model with the lowest AIC.

ALI TMIN We used the `do.call` function to re-combine our different configurations for `TMIN` parameter into one list for each parameter. The `get_min_AIC` method was then applied on each time series to return the model with the lowest AIC and we observe that seasonal average was not the best for any of the time series in this group.


```
##                                Best Model Tmin
## Northern_Ireland              seas.har2
## Scotland_N                   seas.har2
## Scotland_E                   seas.har3_B
## Scotland_W                   seas.har2
## England_E_and_NE             seas.har2
## England_NW_and_N_Wales      seas.har2
## Midlands                     seas.har2
## East_Anglia                  seas.har2
## England_SW_and_S_Wales      seas.har3_C
## England_SE_and_Central_S    seas.har2
```

ALI TMEAN We used the `do.call` function to re-combine our different configurations for TMEAN parameter into one list for each parameter. The `get_min_AIC` method was then applied on each time series to return the model with the lowest AIC and we observe that seasonal average was not the best for any of the time series in this group.

```
##                                Best Models Tmean
## Northern_Ireland              seas.har2
## Scotland_N                   seas.har2
## Scotland_E                   seas.har2
## Scotland_W                   seas.har3_A
## England_E_and_NE             seas.har2
## England_NW_and_N_Wales      seas.har2
## Midlands                     seas.har2
## East_Anglia                  seas.har2
## England_SW_and_S_Wales      seas.har2
## England_SE_and_Central_S    seas.har2
```

ALL Tmax We combined the time series with a linear trend into a single list and applied the `get_min_AIC` and the same was done for time series with a cubic trend.

```
##                                Best Models Tmax
## Northern_Ireland              seas.har3_A
## Scotland_N                   seas.har3_A
## Scotland_E                   seas.har3_A
## Scotland_W                   seas.har3_A
## England_NW_and_N_Wales      seas.har3_A
## Midlands                     seas.har2
## England_SW_and_S_Wales      seas.har4
## England_SE_and_Central_S    seas.har2
## England_E_and_NE            seas.har2
## East_Anglia                  seas.har2
```

We used the `unique` function to check the unique best models for each group of our time series and we can see we have 5 different best models distributed among the different time series data. Similar to the approach used above, we will create 5 functions that models our combined trend model and seasonal models for each time series data. **Unique Models**

```
## [1] "seas.har2" "seas.har3_B" "seas.har3_C" "seas.har3_A" "seas.har4"
## [1] 5
```

4.5 Building combined model for trend and seasonality

We have 5 different best model distributed among the different groups of time series, we will create 5 functions to implement the combine models based on the groups each time series data belongs to, we will subset the time series into their respective groups and apply these functions across the respective groups. Finally, We combined all the different models for the time series into a variable called “final”.

4.6 Creating test set using a combined quadratic and sin-cosine (of order 2) models.

A function `return_quad_sin_cos` was created to Estimate trend and seasonality using a combined quadratic and sin-cosine (of order 2) models. We created a function to apply the `return_quad_sin_cos` on a nested list called `def_temp`. The final outputs were joined into a list and called `test`.

5 ARMA and Forecasting

5.1 Retrieving the residuals for test and final models

We subsetting the final and test model into subsets of the component parameters (Tmax, Tmean and Tmin), a function was created to derive the residuals for both final and test models. The `mapply` function was used to derive the residuals by subtracting the combined model(final and test) from the original time series data. We removed trend and seasonality from each of the 30 time series for both the final and test model and hence we now have 60 residuals time series.

5.2 Fit the residuals with an appropriate ARMA model.

To fit a arma model to all our time series we created a function “`fit_fun`” which takes a residual as an argument and returns a model for our residuals. This was used to create forecasts for our time series later in this study. The `lapply` function was used to apply the `fit_func` function across our nested time series in both final and test set. We assigned the outcome into 6 different lists which represents Tmax, Tmean and Tmin for final and test model.

5.3 Forecasting

We will Forecast the average max, min and mean temperature for each month of 2020. We have to forecast the trend, seasonal components and the residuals which would then be combined to give our actual forecasts. Earlier in this analysis we observed that our best model for harmonics were splitted into 5 different configurations, we will implement similar solution here creating 5 different functions based on the 5 configurations. The functions were applied to their respective group of time series data and this gave us the final predictions for our models.

-TMIN MODELS

```
## [1] 10
```

-TMEAN MODELS

```
## [1] 10
```

-TMAX MODELS

```
## [1] 10
```

5.4 Model Comparison

We will be evaluating the accuracy of our predictions using the accuracy function of the forecast library, we used the subsetting time series of 2020 data for all our time series as the actual while outcome of our

predictions for 2020 as the predicted. We are going to observe our models performance with unseen data not used when fitting the model. The mapply function was used to apply the model_accuracy function across all our different time series predictions for best test and final.

We observe the rmse for our models below, we can see the rmse for both the test model and final model, we observed that for some regions the test model performed better than the final model according to the rmse figures in the tables below.

| ## | | Tmin_rmse | Tmean_rmse | Tmax_rmse |
|----|--------------------------|-----------|------------|-----------|
| ## | East_Anglia | 1.0137703 | 1.0591556 | 1.1416514 |
| ## | England_E_and_NE | 0.7879267 | 0.8959341 | 1.1428033 |
| ## | England_NW_and_N_Wales | 0.8558855 | 0.9830944 | 1.2888542 |
| ## | England_SE_and_Central_S | 1.0640558 | 1.1230801 | 1.3518842 |
| ## | England_SW_and_S_Wales | 0.9544779 | 0.9894317 | 1.3759842 |
| ## | Midlands | 0.9261652 | 1.0519680 | 1.3738682 |
| ## | Northern_Ireland | 0.5231145 | 0.6909344 | 0.9506735 |
| ## | Scotland_E | 0.8003523 | 0.8567716 | 1.0819655 |
| ## | Scotland_N | 0.8038820 | 0.8478665 | 0.9273918 |
| ## | Scotland_W | 0.8295469 | 0.8300845 | 0.9548110 |

| ## | | Tmin_rmse | Tmean_rmse | Tmax_rmse |
|----|--------------------------|-----------|------------|-----------|
| ## | East_Anglia | 1.0057423 | 1.0363773 | 1.2934321 |
| ## | England_E_and_NE | 0.7749689 | 0.8793718 | 1.1671861 |
| ## | England_NW_and_N_Wales | 0.8349328 | 0.9472259 | 1.2555474 |
| ## | England_SE_and_Central_S | 1.0152126 | 1.0236335 | 1.3110822 |
| ## | England_SW_and_S_Wales | 0.8702804 | 0.9193448 | 1.3035392 |
| ## | Midlands | 0.8848937 | 0.9964866 | 1.3519500 |
| ## | Northern_Ireland | 0.5348322 | 0.6643862 | 0.9673044 |
| ## | Scotland_E | 0.7828467 | 0.8172999 | 1.0546422 |
| ## | Scotland_N | 0.8094486 | 0.8560443 | 0.9894496 |
| ## | Scotland_W | 0.7947144 | 0.8121647 | 1.0011004 |

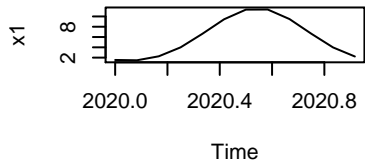
We focused our analysis on the values from the test model predictions, final model predictions and the actual predictions for the South wales and North wales region, a plot was implemented and we observe that the plots are similar for the three different variables for north and south wales.

| ## | test_predictions | final_predictions | Actual |
|-------|------------------|-------------------|--------|
| ## 1 | 1.546477 | 1.497710 | 3.2 |
| ## 2 | 1.483202 | 1.420285 | 2.6 |
| ## 3 | 2.253805 | 2.187965 | 2.0 |
| ## 4 | 3.989963 | 3.924409 | 4.4 |
| ## 5 | 6.619674 | 6.555247 | 6.2 |
| ## 6 | 9.448657 | 9.385545 | 10.2 |
| ## 7 | 11.326805 | 11.265046 | 10.8 |
| ## 8 | 11.346451 | 11.286073 | 12.2 |
| ## 9 | 9.489493 | 9.430523 | 8.6 |
| ## 10 | 6.644874 | 6.587314 | 6.5 |
| ## 11 | 3.978881 | 3.922690 | 5.2 |
| ## 12 | 2.218433 | 2.163558 | 1.9 |

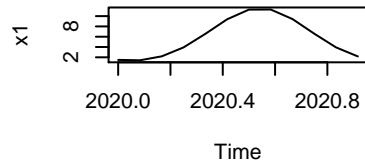
| ## | test_predictions | final_predictions | Actual |
|------|------------------|-------------------|--------|
| ## 1 | 2.369714 | 2.247397 | 3.8 |
| ## 2 | 2.292664 | 2.106081 | 4.0 |
| ## 3 | 2.973141 | 2.908926 | 3.0 |
| ## 4 | 4.636609 | 4.400516 | 5.6 |
| ## 5 | 7.224215 | 7.157505 | 6.7 |
| ## 6 | 10.031540 | 9.841134 | 10.3 |

| | | | |
|-------|-----------|-----------|------|
| ## 7 | 11.901634 | 11.757708 | 11.2 |
| ## 8 | 11.938664 | 11.841460 | 13.1 |
| ## 9 | 10.142091 | 9.922029 | 9.5 |
| ## 10 | 7.397123 | 7.348201 | 7.5 |
| ## 11 | 4.833470 | 4.616245 | 5.6 |
| ## 12 | 3.128227 | 3.036602 | 3.1 |

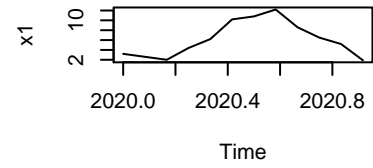
Test predictions North wales



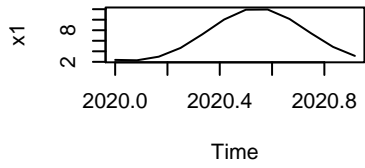
Final predictions North wales



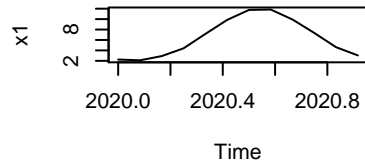
Actual North wales



Test predictions South wales



Final predictions South wales



Actual predictions South wale

