

**1. Introduction to Heap / Priority Queue : A Powerful Simple Data Structure based on Binary Tree. Heap is a Complete Binary Tree.**

- a. Insert :  $O(\log N)$
- b. Max / Min :  $O(1)$
- c. Delete :  $O(\log N)$

**2. Heap Insertion : Theory**

- a. Max heap for finding maximum value  $O(1)$ ,
- b. Min heap for finding minimum value  $O(1)$ .
- c. For **Max** heap all child nodes are equal or **less** than their parent.
- d. For **Min** heap all child nodes are equal or **greater** than their parent.
- e. So Max / Min value will be on the root. That 's why  $O(1)$

Max Heap Insert : Up-heapify (compare with parent & swap)  $O()$

**3. Heap Insertion : Implementation**

$O(\log N)$ : [ Height =  $\log N$ , Complete Binary Tree ]

- A. Using Dynamic Array
- B. Left Child :  $i = 2i + 1$
- C. Right Child :  $i = 2i - 1$
- D. parent =  $i-1/2$

**4. Heap Delete : Theory [For Max Heap]**

Swap with last node. then delete the last node  $O(1)$ , Then call down-heapify

Down-heapify : compare parent with its two children and swap downward.

Complexity :  $O(\log N)$

**5. Heap Delete : Implementation**

**6. Heap Max Operations : Other Operations : getMax, ExtractMax().**