

1. All Pair Shortest Path :

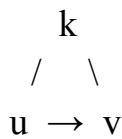
Every nodes single source shortest path. For this we need Floyd - Warshall Algorithm. **It is an Incremental Algorithm.**

For this we will use Adjacency-Matrix.

Intermediate node = not using the direct edge, by using other bypassable nodes from u to v node are the intermediate nodes.

2. Floyd-Warshall Simulation part 1 :

$d[u][v] = d[u][k] + d[k] + d[v]$ // k is the intermediate node.



$d[u][v] = \min(d[u][v], d[u][k] + d[k][v])$

3. Floyd-Warshall Simulation part 2 :

Increasing the intermediate nodes number will produce the more shortest distance of each node.

4. Pseudocode & Complexity :

- Input \rightarrow A weighted graph as an adjacency matrix.
- Output \rightarrow All pair shortest path/distance.
- Create a distance matrix, d. Where $d[i][j] = x$, where there is a direct edge from i to j which cost is x.
- for all node "i" $d[i][i] = 0$.
- for all nodes i & j where there isn't any direct edge from $i \rightarrow j$: $d[i][j] = \text{INF}$
- for all node "k" :
 - for all node u:
 - for all node v:
 - $d[u][v] = \min(d[u][v], d[u][k] + d[k][v])$
- output all pair shortest distance, 'd'

Time Complexity : $O(V^3)$

Space Complexity : $O(V^2)$

5. Floyd Warshall Code : Implementation

6. Problem Solving : From CSES

Shortest Routes II : <https://cses.fi/problemset/task/1672>