

1. Dijkstra's Limitations :

SSSP in a weighted (Positive) graph problem solve.

For negative weighted value, we can't use Dijkstra.

Negative Cycle value tends to become : $-\infty$.

To detect negative Cycle, we can't use Dijkstra.

2. Bellman-Ford Algo's Intuition & Simulation :

By doing normal brute-force iteration, we can see, its guaranteed that after $V-1$ {Number of Nodes - 1}, times iteration, all node relaxation of a graph will complete, after that, there will be no change.

So, $(v-1)$ iteration needed to get the final distances of a graph of v nodes.

3. Bellman-Ford Pseudocode & Complexity :

Input : A weighted Graph with no negative Cycle

Output : Shortest Distance from source node to all other nodes.

- Create a distance array "d" with all value to infinity.

- $d[\text{source}] = 0$

- for $i=1$ to $v-1$: **$O(n)$**

- For all edge "e(u, v, w)": **$O(e)$**

- if $d[u] + w < d[v]$ **$O(1)$**

- $d[v] = d[u] + w$ // Relaxation **$O(1)$**

- print the distance array "d". **$O(n)$**

Time Complexity : $O(|V| * |E|) :: O(|V| * n^2) :: O(n^3)$

Space Complexity : $O(n)$

4. Bellman-Ford Code : Implementation

5. Negative Cycle Detection :

No change in $d[\text{Nodes}]$ in N -th iteration Time. if any change detected that means, there is a cycle.

So if, in N 'th iteration any relaxation happens, it will have a negative cycle.

6. Negative Cycle Detection Pseudocode & Code :

- Create a distance array "d" with all value to infinity.
- $d[\text{source}] = 0$

relaxed = false.

- for $i=1$ to v :
 - For all edge "e(u, v, w)":
 - if $d[u] + w < d[v]$
 - $d[v] = d[u] + w$
 - if $i == n$:
 - relaxed = true.

If relaxed == true:

Negative Cycle Detected.