

## 1. Path Printing :

### No Cycle :

Store parent of  $v$  / parent of relaxed node =  $u$ /by which its relaxed.

Then store parents from destination to source in a vector.

The vector's reverse version will be the path for the graph.

## 2. Cycle Printing: Print the cycle.

### With Cycle :

Detect the Negative cycle. And print the Negative cycle.

In  $n$ 'th iteration, we can see changes of nodes whose are the part of the negative cycle and those nodes that can be reached from the negative cycle.

If we start tracing from a node that can be reached from the cycle. Then, we will be on the cycle in a certain period of time.

To enter in the cycle from outer part but reachable node from the cycle, we need to trace parent  $n-1$  iteration times.

## 3. Pseudocode & Complexity :

Input : A weighted Graph with no negative Cycle

Output : Shorted Distance from source node to all other nodes.

- Create a distance array "d" with all value to infinity.

- Create a parent array

- $d[\text{source}] = 0$

- `negative_cycle = false.`

- for  $i=1$  to  $v-1$  :

- For all edge " $e(u, v, w)$ ":

- if  $d[u] + w < d[v]$ :

- $d[v] = d[u] + w$

- $\text{parent}[v] = u$

- if  $i == n$ :

- `negative_cycle = true.`

- **IF `negative_cycle == false` :  $O(N)$**

- `selected_node = destination_node`

- declare a vector as named "path"

- while True :

```

    Path.push_back(selected_node)
    - selected_node = parent[selected_node]
    - If selected_node == src :
        break
- reverse the vector and print it.

- IF negative_cycle == True :  $O(N) + O(N)$ 
- create a "last_updated_node" variable. = -1
- if i == n:
    - negative_cycle = true.
    - last_updated_node = v [latest updated node]

- selected_node = last_updated_node
- for(i=1 to n-1):
    - selected_node = parent[selected_node]
- int first_updatedNode = selected_node
- declare a vector as named "cycle"
- cycle.push_back(selected_node)
- while True:
    - selected_node = parent[selected_node]
    - cycle.push_back(selected_node)
    - if ( selected_node == first_updatedNode ) :
        - break.
- reverse the cycle vector and print it.

```

Time Complexity :  $O(V * E)$  [SAME]

Space Complexity :  $O(V)$  [SAME]

#### 4. Problem Solving : Implementation in Code :

Cycle Finding : <https://cses.fi/problemset/task/1197>