

**1. Problem Definition and example :** 0-1 Knapsack = বস্তা বা থলে  
Profit Maximization within a certain capacity. 0-1 : taken/not taken.

**2. Brute force :** Brute force way to solve this Knapsack problem.

$$\text{brute}(n) = \max \{ \text{value}[n] + \text{brute}(n-1) \}$$

	1	2	3	4	
Value :	200	250	100	80	Capacity : 13
Weight :	3	11	5	4	

**i. States :** knapsack(4, 13) (weight, value)

/(Yes) with 4th \ (No)

knapsack(3, 9)

knapsack(3, 13)

**ii. Recurrence Case will be :**

$$\text{knapsack}(n, \text{cap}) = \max \{ \begin{array}{l} \text{val}[n] + \text{knapsack}(n-1, \text{cap}-w[n]) \\ 0 + \text{knapsack}(n-1, \text{cap}) \end{array} \}$$

**iii. Base Case :**

$$\text{Knapsack}(0, \text{cap}) = 0;$$

**Time Complexity :**  $O(2^n)$

**3. DP formulation :**

$\text{Knapsack}(n, \text{cap}) = O(2^n) \rightarrow O(n * \text{cap})$ , if we use DP formulation.

Space Complexity =  $\text{dp}[n][\text{cap}] = O(n * \text{cap})$

**4. Coding with Memoization : Implementation**

atcoder Task-D : Knapsack-1 : [https://atcoder.jp/contests/dp/tasks/dp\\_d](https://atcoder.jp/contests/dp/tasks/dp_d)

**5. Coding with Tabulation : Same Task from 4.**