

RSA

# RSA

- ▶ Select at random two large prime numbers  $p, q$ .
- ▶ Compute  $n = pq$  and  $\phi(n) = (p - 1)(q - 1)$ .
- ▶ Select a small integer  $e$  such that  $\gcd(e, \phi(n)) = 1$ .
- ▶ Compute  $d = e^{-1} \bmod \phi(n)$ .
- ▶ Publish the pair  $(n, e)$  as your RSA Public Key.
- ▶ Keep secret  $d$ , your RSA Private Key. Also keep  $p, q, \phi(n)$  secret.

To encrypt a message  $M$  we find  $C = M^e \bmod n$ .

To decrypt a cyphertext  $C$  we find  $M = C^d \bmod n$ .

# RSA Examples

- Perform encryption and decryption using the RSA algorithm, for the following:
  1.  $p = 5; q = 11, e = 3; M = 9$
  2.  $p = 7; q = 11, e = 17; M = 8$
  3.  $p = 11; q = 13, e = 11; M = 7$
  4.  $p = 3; q = 11, e = 7; M = 5$