

# Formula List

## Differentiation

### *Rules of Differentiation*

1.  $\frac{d}{dx}(\text{constant}) = 0$
2.  $\frac{d}{dx}(cf(x)) = c \frac{d}{dx}f(x)$
3.  $\frac{d}{dx}(f(x) + g(x)) = \frac{d}{dx}f(x) + \frac{d}{dx}g(x)$  (Sum Rule)
4.  $\frac{d}{dx}(f(x)g(x)) = f(x) \frac{d}{dx}g(x) + g(x) \frac{d}{dx}f(x)$  (Product Formula)
5.  $\frac{d}{dx}\left(\frac{f(x)}{g(x)}\right) = \frac{g(x) \frac{d}{dx}f(x) - f(x) \frac{d}{dx}g(x)}{[g(x)]^2}$  (Quotient Rule)

### *Derivative of Algebraic Function*

1.  $\frac{d}{dx}u^n = nu^{n-1} \frac{du}{dx}$

### *Derivatives of Trigonometric Functions*

1.  $\frac{d}{dx}\sin u = \cos u \frac{du}{dx}$
2.  $\frac{d}{dx}\cos u = -\sin u \frac{du}{dx}$
3.  $\frac{d}{dx}\tan u = \sec^2 u \frac{du}{dx}$
4.  $\frac{d}{dx}\sec u = \sec u \tan u \frac{du}{dx}$
5.  $\frac{d}{dx}\csc u = -\csc u \cot u \frac{du}{dx}$
6.  $\frac{d}{dx}\cot u = -\csc^2 u \frac{du}{dx}$

### *Derivatives of Inverse Trigonometric Functions*

1.  $\frac{d}{dx}\sin^{-1}u = \frac{1}{\sqrt{1-u^2}} \frac{du}{dx}$
2.  $\frac{d}{dx}\cos^{-1}u = -\frac{1}{\sqrt{1-u^2}} \frac{du}{dx}$
3.  $\frac{d}{dx}\tan^{-1}u = \frac{1}{1+u^2} \frac{du}{dx}$
4.  $\frac{d}{dx}\sec^{-1}u = \frac{1}{|u|\sqrt{u^2-1}} \frac{du}{dx}$
5.  $\frac{d}{dx}\csc^{-1}u = -\frac{1}{|u|\sqrt{u^2-1}} \frac{du}{dx}$

$$6. \frac{d}{dx} \cot^{-1} u = -\frac{1}{1+u^2} \frac{du}{dx}$$

### ***Derivative of Logarithmic Function***

$$1. \frac{d}{dx} \ln u = \frac{1}{u} \frac{du}{dx}$$

### ***Derivative of Exponential Function***

$$1. \frac{d}{dx} e^u = e^u \frac{du}{dx}$$

### ***Derivatives of Hyperbolic Functions***

$$1. \frac{d}{dx} \sinh u = \cosh u \frac{du}{dx}$$

$$2. \frac{d}{dx} \cosh u = \sinh u \frac{du}{dx}$$

$$3. \frac{d}{dx} \tanh u = \operatorname{sech}^2 u \frac{du}{dx}$$

$$4. \frac{d}{dx} \operatorname{sech} u = -\operatorname{sech} u \tanh u \frac{du}{dx}$$

$$5. \frac{d}{dx} \operatorname{cosech} u = -\operatorname{cosech} u \coth u \frac{du}{dx}$$

$$6. \frac{d}{dx} \coth u = -\operatorname{cosech}^2 u \frac{du}{dx}$$

### ***Derivatives of Inverse Hyperbolic Functions***

$$1. \frac{d}{dx} \sinh^{-1} u = \frac{1}{\sqrt{1+u^2}} \frac{du}{dx}$$

$$2. \frac{d}{dx} \cosh^{-1} u = \frac{1}{\sqrt{u^2-1}} \frac{du}{dx}, u > 1$$

$$3. \frac{d}{dx} \tanh^{-1} u = \frac{1}{1-u^2} \frac{du}{dx}, |u| < 1$$

$$4. \frac{d}{dx} \operatorname{csch}^{-1} u = -\frac{1}{|u|\sqrt{1+u^2}} \frac{du}{dx}, u \neq 0$$

$$5. \frac{d}{dx} \coth^{-1} u = \frac{1}{1-u^2} \frac{du}{dx}, |u| < 1$$

Where  $u$  is a function of  $x$