NumPy

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1 Learn NumPy

NumPy is the fundamental package for scientific computing in Python. It is a Python library that provides a multidimensional array object, various derived objects (such as masked arrays and matrices), and an assortment of routines for fast operations on arrays, including mathematical, logical, shape manipulation, sorting, selecting, I/O, discrete Fourier transforms, basic linear algebra, basic statistical operations, random simulation and much more.

NumPy arrays have a fixed size at creation, unlike Python lists (which can grow dynamically). Changing the size of an ndarray will create a new array and delete the original.

The elements in a NumPy array are all required to be of the same data type, and thus will be the same size in memory. The exception: one can have arrays of (Python, including NumPy) objects, thereby allowing for arrays of different sized elements.

NumPy arrays facilitate advanced mathematical and other types of operations on large numbers of data. Typically, such operations are executed more efficiently and with less code than is possible using Python's built-in sequences.

A growing plethora of scientific and mathematical Python-based packages are using NumPy arrays; though these typically support Python-sequence input, they convert such input to NumPy arrays prior to processing, and they often output NumPy arrays. In other words, in order to efficiently use much (perhaps even most) of today's scientific/mathematical Python-based software, just knowing how to use Python's built-in sequence types is insufficient - one also needs to know how to use NumPy arrays.

sequence size and speed are particularly important in scientific computing

NumPy's main object is the homogeneous multidimensional array. It is a table of elements (usually numbers), all of the same type, indexed by a tuple of non-negative integers. In NumPy dimensions are called axes. For example, the array for the coordinates of a point in 3D space, [1, 2, 1], has one axis. That axis has 3 elements in it, so we say it has a length of 3. In the example pictured below, the array has 2 axes. The first axis has a length of 2, the second axis has a length of 3.

1.0.1 Difference between Numpy and standard Python

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```
[305]: [[1., 0., 0.],
[0., 1., 2.]]
```

```
[305]: [[1.0, 0.0, 0.0], [0.0, 1.0, 2.0]]
```

NumPy's array class is called ndarray. It is also known by the alias array. Note that numpy.array is not the same as the Standard Python Library class array.array, which only handles one-dimensional arrays and offers les functionality. The more important attributes of an ndarray object are 1. ndarray.n:im the number of axes (dimensions) of the a

- 2. ndarray.shape: the dimensions of the array. This is a tuple of integers indicating the size of the array in each dimension. For matrix with n rows and mcolumns, shapewillbe(n,m). Theleng the oft hesha petup le ist herefo ret henumbr of axes, nd
- 3. . ndarray.:ize the total number of elements of the array. This is equal to the product of the elements of s
- 4. pe. ndarray:dtype an object describing the type of the elements in the array. One can create or specify dtype's using standard ython types. Additionally NumPy provides types of its own. numpy.int32, numpy.int16, and numpy.float64 re some
- 5. amples. ndarra:.itemsize the size in bytes of each element of the array. For example, an array of elements of type float64asitemsize 8 (=64/8), while one of type complex32 has itemsize 4 (=32/8). It is equivalent to ndray.dtype
- 6. itemsize.: ndarray.data the buffer containing the actual elements of the array. Normally, we won't need to use this attriute because we will access the elements in an array using indexing facilities.rray

```
[306]: import numpy as np np.__version__
```

```
[307]: list1 = [1,2,3,4,5] list1
```

[307]: [1, 2, 3, 4, 5]

1.0.2 Basic Attributes of the ndarray Class

```
[308]: list2 = ['mukesh', 28, 10000000, [1,2,3,4,5,6], True] list2
```

[308]: ['mukesh', 28, 10000000, [1, 2, 3, 4, 5, 6], True]

This doesnot work with massive amount of data as it will become very slow. so NumPy was introduces wich is every fast but allows to manipulate similar kind of data.

[309]: import numpy as np

[310]: #help(np.ndarray)

Attribute	Description	
Shape	A tuple that contains the number of elements (i.e., the length) for each dimension (axis) of the array.	
Size	The total number elements in the array.	
Ndim	Number of dimensions (axes).	
nbytes	Number of bytes used to store the data.	
dtype	The data type of the elements in the array.	

```
[311]: np1 = np.array([0,1,2,3,4,5,6,7,8,9]) #creatin NumPy array np1 #display the values of NumPy array
```

[311]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])

[312]: type(np1)

[312]: numpy.ndarray

[313]: np1.shape

[313]: (10,)

[314]: np1.size

[314]: 10

[315]: np1.ndim

[315]: 1

```
[316]: np1.nbytes

[316]: 80

[317]: np1.dtype
```

1.0.3 Data Types

[317]: dtype('int64')

dtype	Variants	Description
int	int8, int16, int32, int64	Integers
uint	uint8, uint16, uint32, uint64	Unsigned (nonnegative) integers
bool	Bool	Boolean (True or False)
float	float16, float32, float64, float128	Floating-point numbers
complex	complex64, complex128, complex256	Complex-valued floating-point numbers

1.0.4 3 Ways to Creating NumPy Arrays

1st method: via python list

```
[318]: mylist = [1,2,3,4,5]
mylist_from_array = np.array(mylist)
mylist_from_array
```

[318]: array([1, 2, 3, 4, 5])

```
[319]: mylist_from_array * 10
```

[319]: array([10, 20, 30, 40, 50])

2nd Method: via Python Tuples

```
[320]: # creation via Python Tuple
mytuple = (1,2,3,4,5,6,7,8,9,10)
np.array(mytuple)
```

[320]: array([1, 2, 3, 4, 5, 6, 7, 8, 9, 10])

3rd method: via NumPy arange method

[321]: np.arange(10)

[321]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])

```
np.arange(10, 23)
[322]:
[322]: array([10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22])
[323]: np.arange(10,23,5)
[323]: array([10, 15, 20])
      The following example demonstrates how to use the dtype attribute to generae arrays
      of intger-, foat-, and complex-valued elements:
[324]: npp = np.array([1,2,3,4], dtype=np.int16)
       print(npp)
      [1 2 3 4]
[325]: npp1 = np.array([1,2,3,4,5,], dtype=np.float32)
       print(npp1)
      [1. 2. 3. 4. 5.]
[326]: npp2 = np.array([1,2,3,4,5,6], dtype=np.complex64)
       npp2
[326]: array([1.+0.j, 2.+0.j, 3.+0.j, 4.+0.j, 5.+0.j, 6.+0.j], dtype=complex64)
      Once a NumPy array is created, its dtype cannot be changed
[327]: data = np.array([1, 2, 3], dtype=np.float32)
       data
[327]: array([1., 2., 3.], dtype=float32)
[328]: data.dtype
[328]: dtype('float32')
[329]: data = np.array(data, dtype=np.int32)
       data.dtype
[329]: dtype('int32')
[330]: data
[330]: array([1, 2, 3], dtype=int32)
```

It can also be changed using the astype method of the ndarray class

```
[331]: data = np.array([1, 2, 3], dtype=np.float32)
       data
[331]: array([1., 2., 3.], dtype=float32)
[332]: data.astype(np.int32)
[332]: array([1, 2, 3], dtype=int32)
[333]: d1 = np.array([1, 2, 3], dtype=float)
        d2 = np.array([1, 2, 3], dtype=complex)
       d1 + d2
[333]: array([2.+0.j, 4.+0.j, 6.+0.j])
        (d1 + d2).dtype
[334]:
[334]: dtype('complex128')
      Real and Imaginary Parts
[335]: data = np.array([1, 2, 3], dtype=complex)
       data
[335]: array([1.+0.j, 2.+0.j, 3.+0.j])
[336]: data.real
[336]: array([1., 2., 3.])
[337]: data.imag
[337]: array([0., 0., 0.])
      length of the array
[338]: len(np.arange(10,23))
[338]: 13
[339]: np.arange(10,23).size
[339]: 13
```

1.0.5 Difference between Python ad NumPy Data Structure

```
[340]: mytuple = (1,2,3,4,5,6,7,8,9,10)
       # np.array(mytuple)
       mytuple * 3
[340]: (1,
        2,
        3,
        4,
        5,
        6,
        7,
        8,
        9,
        10,
        1,
        2,
        3,
        4,
        5,
        6,
        7,
        8,
        9,
        10,
        1,
        2,
        3,
        4,
        5,
        6,
        7,
        8,
        9,
        10)
[341]: mytuple = (1,2,3,4,5,6,7,8,9,10)
       np.array(mytuple)
       np.array(mytuple) * 3
[341]: array([ 3, 6, 9, 12, 15, 18, 21, 24, 27, 30])
```

1.0.6 NumPy shape

```
[342]: np1.shape #showing the shape of array, dimentions and/or numer of values in
       →array(in the current case as it is just one dimentaional array)
[342]: (10,)
[343]: np2 = np.array([[1,2,3,4,5],[6,7,8,9,10]])
      np2.shape
[343]: (2, 5)
[344]: np2
[344]: array([[ 1, 2, 3, 4, 5],
             [6, 7, 8, 9, 10]])
[345]: np2.ravel() #returns the array, flattened
[345]: array([1, 2, 3, 4, 5, 6, 7, 8, 9, 10])
[346]: np2 = np.arange(10) #creating NumPy array with arange() with 10 values
[346]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
[347]: np3 = np.arange(0,10,2) #usin arange steps option with value 2
      np3
[347]: array([0, 2, 4, 6, 8])
[348]: np5 = np.zeros((2,10)) # creatin NumPy array with 2 dimentional with 10 items_
       ⇒in each dimention
      np5
[348]: array([[0., 0., 0., 0., 0., 0., 0., 0., 0., 0.],
             [0., 0., 0., 0., 0., 0., 0., 0., 0., 0.]
[349]: np6 = np.full((10), 6) #NumPy full(0 function to create NumPy single_
       ⇔dimentional array with 10 values and all values are 6
      np6
[349]: array([6, 6, 6, 6, 6, 6, 6, 6, 6])
[350]: np7 = np.full((2, 10), 6) #NumPy full(0 function to create NumPy two_
       ⇔dimentional array with 10 values and all values are 6
      np7
```

```
[350]: array([[6, 6, 6, 6, 6, 6, 6, 6, 6],
              [6, 6, 6, 6, 6, 6, 6, 6, 6]])
[351]: a = np.empty([2, 3, 2])
       а
[351]: array([[[1.56690889e-316, 0.00000000e+000],
               [1.03977794e-312, 9.54898106e-313],
               [1.01855798e-312, 1.03977794e-312]],
              [[1.23075756e-312, 1.14587773e-312],
               [1.10343781e-312, 9.76118064e-313],
               [1.08221785e-312, 1.90979621e-312]]])
[352]: #converting list to NumPy array
       mylist = [1,2,3,4,5]
       np8 = np.array(mylist)
       np8
[352]: array([1, 2, 3, 4, 5])
[353]: #accessing ay specific item of NumPy array
       np8[0]
[353]: 1
[354]: np8[2]
[354]: 3
[355]: #checkin the datatype of NumPy array
       np8.dtype
[355]: dtype('int64')
      1.0.7 Two dimentional arrays
[356]: my_array = np.arange(35)
      my_array.shape = (7,5)
      my_array
[356]: array([[ 0, 1, 2, 3,
              [5, 6, 7, 8, 9],
              [10, 11, 12, 13, 14],
              [15, 16, 17, 18, 19],
              [20, 21, 22, 23, 24],
              [25, 26, 27, 28, 29],
```

```
[357]: my_array[2]
[357]: array([10, 11, 12, 13, 14])
[358]: my_array[-2]
[358]: array([25, 26, 27, 28, 29])
[359]: my_array[6,2]
[359]: 32
[360]: # my_array[6][21]
      1.0.8 Three Dimentional Array
[361]: my3darray = np.arange(70)
       my3darray
[361]: array([ 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16,
              17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33,
              34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50,
              51, 52, 53, 54, 55, 56, 57, 58, 59, 60, 61, 62, 63, 64, 65, 66, 67,
              68, 69])
[362]: my3darray.shape=(2,7,5)
       my3darray
[362]: array([[[ 0, 1, 2,
                             3,
                                 4],
               [5, 6, 7,
                             8,
                                 9],
               [10, 11, 12, 13, 14],
               [15, 16, 17, 18, 19],
               [20, 21, 22, 23, 24],
               [25, 26, 27, 28, 29],
               [30, 31, 32, 33, 34]],
              [[35, 36, 37, 38, 39],
               [40, 41, 42, 43, 44],
               [45, 46, 47, 48, 49],
               [50, 51, 52, 53, 54],
               [55, 56, 57, 58, 59],
               [60, 61, 62, 63, 64],
               [65, 66, 67, 68, 69]]])
```

[30, 31, 32, 33, 34]])

1.0.9 Basic Indexing and Slicing

```
[363]: np1 = np.array([1,2,3,4,5,6,7,8,9])
[364]: np1[1:5]
[364]: array([2, 3, 4, 5])
[365]: np1[1:]
[365]: array([2, 3, 4, 5, 6, 7, 8, 9])
[366]: np1[-3:-1]
[366]: array([7, 8])
[367]: np1[1:5:2] #with stepping 2
[367]: array([2, 4])
[368]: np1[::2] #prints start to end with stepping 2
[368]: array([1, 3, 5, 7, 9])
[369]: np1[::3] #prints start to end with stepping 3
[369]: array([1, 4, 7])
[370]: arr = np.arange(10)
       arr
[370]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
[371]: arr[5]
[371]: 5
[372]: arr[5:8]
[372]: array([5, 6, 7])
[373]: arr[5:8] = 12
[374]: arr
[374]: array([ 0, 1, 2, 3, 4, 12, 12, 12, 8, 9])
```

An important first distinction from Python's built-in lists is that array slices are views on the original array. This means that the data is not copied, and any modifications to the view will be reflected in the source array.

```
[375]: arr_slice = arr[5:8]
       arr_slice
[375]: array([12, 12, 12])
[376]: arr_slice[1] = 12345
[377]: arr
[377]: array([
                  0,
                         1,
                                 2,
                                        3,
                                               4,
                                                     12, 12345,
                                                                    12,
                                                                            8,
                  9])
      The "bare" slice [:] will assign to all values in an array:
[378]: arr_slice[:] = 64
[379]: arr
[379]: array([0, 1, 2, 3, 4, 64, 64, 64, 8, 9])
[380]: #slicing multi dimentional array
       np2 = np.array([[1,2,3,4,5], [6,7,8,9,10]])
       np2[0:1,1:3]
[380]: array([[2, 3]])
[381]: np2[0:2,1:3]
[381]: array([[2, 3],
              [7, 8]])
[382]:
       arr3d = np.array([[[1, 2, 3], [4, 5, 6]], [[7, 8, 9], [10, 11, 12]]])
      1.1 Copy Vs View for NumPy
[383]: import numpy as np
       np1 = np.array([0,1,2,3,4,5])
[384]: #creating view
       np2= np1.view()
       np1 #original NP1
[384]: array([0, 1, 2, 3, 4, 5])
```

```
[385]: np2 #Original NP2
[385]: array([0, 1, 2, 3, 4, 5])
[386]: np1[0] = 41
[387]: np1 #original NP1
[387]: array([41, 1, 2, 3, 4, 5])
[388]: np2 #Original NP2
[388]: array([41, 1, 2, 3, 4,
                                    5])
      notice that the original and view both changed. It means whe we changing the original, the view
      also changes
      Aother example
[389]: rng = np.random.default_rng(seed=1701) # seed for reproducibility
       x1 = rng.integers(10, size=6) # one-dimensional array
       x1
[389]: array([9, 4, 0, 3, 8, 6])
[390]: x2 = rng.integers(10, size=(3, 4)) # two-dimensional array
       x2
[390]: array([[3, 1, 3, 7],
              [4, 0, 2, 3],
              [0, 0, 6, 9]])
[391]: x3 = rng.integers(10, size=(3, 4, 5)) # three-dimensional array
       x3
[391]: array([[[4, 3, 5, 5, 0],
               [8, 3, 5, 2, 2],
               [1, 8, 8, 5, 3],
               [0, 0, 8, 5, 8]],
              [[5, 1, 6, 2, 3],
               [1, 2, 5, 6, 2],
               [5, 2, 7, 9, 3],
               [5, 6, 0, 2, 0]],
              [[2, 9, 4, 3, 9],
               [9, 2, 2, 4, 0],
               [0, 3, 0, 0, 2],
```

```
[3, 2, 7, 4, 7]]])
[392]: x2\_sub = x2[:2, :2]
       x2_sub
[392]: array([[3, 1],
              [4, 0]])
[393]: #copy function
       np1 = np.array([0,1,2,3,4,5])
      Now if we modify this subarray, we'll see that the original array is changed!
[394]: x2\_sub[0, 0] = 99
       x2_sub
[394]: array([[99, 1],
              [4, 0]
[395]: x2
[395]: array([[99, 1,
                        3,
                            7],
              [4,0,
                        2,
                            3],
              [ 0, 0,
                            9]])
                        6,
      1.1.1 Creating a Copy
[396]: np1 = np.array([0,1,2,3,4,5])
       np2 = np1.copy()
[397]: np1 #original NP1
[397]: array([0, 1, 2, 3, 4, 5])
[398]: np2 #original NP1
[398]: array([0, 1, 2, 3, 4, 5])
[399]: np1[0] = 41
[400]: np1 #original NP1
[400]: array([41, 1, 2, 3, 4, 5])
[401]: np2 #original NP1
```

[401]: array([0, 1, 2, 3, 4, 5])

notice that when we change the original but the copy has not changed. It simply idicates the copy is a seperate copy fothe original and has no links with the original

```
# now try to change the copy version to check if the original changes
[402]:
[403]: np1 = np.array([0,1,2,3,4,5])
[404]: np2 = np1.copy()
[405]: np2
[405]: array([0, 1, 2, 3, 4, 5])
[406]: np1 #original NP1
[406]: array([0, 1, 2, 3, 4, 5])
[407]: np2[0] = 41
[408]: np1 #original NP1
[408]: array([0, 1, 2, 3, 4, 5])
[409]: np2 #original NP1
[409]: array([41, 1, 2, 3, 4,
                                    5])
      since copy is completely different array it only changes and it does not reflect the original array
      1.2 Another example
[410]: x2 = rng.integers(10, size=(3, 4)) # two-dimensional array
       x2\_sub\_copy = x2[:2, :2].copy()
       x2_sub_copy
[410]: array([[9, 3],
               [5, 0]])
      If we now modify this subarray, the original array is not touched
[411]: x2\_sub\_copy[0, 0] = 42
[412]: x2_sub_copy
[412]: array([[42, 3],
              [5, 0]])
[413]: x2
```

```
[413]: array([[9, 3, 6, 6], [5, 0, 2, 5], [6, 4, 8, 2]])
```

1.2.1 Indexing with Slices

```
[414]: arr
[414]: array([0, 1, 2, 3, 4, 64, 64, 64, 8, 9])
[415]: arr[1:6]
[415]: array([ 1, 2, 3, 4, 64])
[416]: arr2d = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
[417]: arr2d
[417]: array([[1, 2, 3],
              [4, 5, 6],
              [7, 8, 9]])
[418]: arr2d[:2]
[418]: array([[1, 2, 3],
              [4, 5, 6]])
[419]: arr2d[:2, 1:]
[419]: array([[2, 3],
              [5, 6]])
[420]: lower_dim_slice = arr2d[1, :2]
[421]: lower_dim_slice
[421]: array([4, 5])
[422]: lower_dim_slice.shape
[422]: (2,)
[423]: arr2d[:2, 2]
[423]: array([3, 6])
[424]: arr2d[:, :1]
```

```
[424]: array([[1],
              [4],
              [7]])
[425]: arr2d[:2, 1:] = 0
[426]:
        arr2d
[426]: array([[1, 0, 0],
              [4, 0, 0],
              [7, 8, 9]])
[427]: arr2d[1, :2]
[427]: array([4, 0])
[428]: my\_vector = np.array([-15, -4, 0, 3, 21, 37, 105])
       my_vector
[428]: array([-15, -4, 0, 3, 21, 37, 105])
[429]: my_vector[0]
[429]: -15
[430]: my_vector[1]
[430]: -4
[431]: | # my_vector[305]
[432]: 305 % 7
[432]: 4
[433]: my_vector[305 % 7]
[433]: 21
      check how it gives the 4th element of the my_vector array above
[434]: my_vector.size
[434]: 7
      ### Boolean Indexing
        names = np.array(["Bob", "Joe", "Will", "Bob", "Will", "Joe", "Joe"])
[435]:
```

```
[436]: names
[436]: array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'], dtype='<U4')
[437]: data = np.array([[4, 7], [0, 2], [-5, 6], [0, 0], [1, 2], [-12, -4], [3, 4]])
[438]: data
[438]: array([[ 4,
                      7],
              [ 0,
                      2],
              [ -5,
                      6],
              [ 0,
                      0],
              [ 1,
                      2],
              [-12,
                     -4],
              [ 3,
                      4]])
[439]: names == "Bob"
[439]: array([ True, False, False, True, False, False])
       data[names == "Bob"]
[440]:
[440]: array([[4, 7],
              [0, 0]])
[441]:
       data[names == "Bob", 1:]
[441]: array([[7],
              [[0]]
[442]: data[names == "Bob", 1]
[442]: array([7, 0])
[443]:
       names != "Bob"
[443]: array([False, True, True, False, True, True,
                                                        True])
[444]:
      ~(names == "Bob")
[444]: array([False, True, True, False, True, True, True])
[445]: data[~(names == "Bob")]
[445]: array([[ 0,
                      2],
              [ -5,
                      6],
              [ 1,
                      2],
```

```
[-12, -4],
              [ 3, 4]])
[446]:
       cond = names == "Bob"
[447]:
        data[~cond]
[447]: array([[ 0,
                      2],
                      6],
              [ -5,
              [ 1,
                      2],
              [-12, -4],
              [ 3,
                      4]])
[448]:
       mask = (names == "Bob") | (names == "Will")
[449]: mask
[449]: array([ True, False, True, True, True, False, False])
[450]:
       data[mask]
[450]: array([[ 4, 7],
              [-5, 6],
              [0, 0],
              [1, 2]])
       data[data < 0] = 0
[451]:
[452]: data
[452]: array([[4, 7],
              [0, 2],
              [0, 6],
              [0, 0],
              [1, 2],
              [0, 0],
              [3, 4]])
[453]:
        data[names != "Joe"] = 7
[454]: data
[454]: array([[7, 7],
              [0, 2],
              [7, 7],
              [7, 7],
              [7, 7],
```

```
[0, 0],
[3, 4]])
```

1.2.2 Another example

```
[455]: my_vector = np.array([-17, -3, 0, 4, 7, 19, 109])
[456]: my_vector
[456]: array([-17, -3, 0, 4, 7, 19, 109])
[457]: zero_mod_7_mask = 0 == (my_vector % 7)
       zero_mod_7_mask
[457]: array([False, False, True, False, True, False, False])
[458]: sub_array = my_vector[zero_mod_7_mask]
       sub_array
[458]: array([0, 7])
[459]: sub_array[sub_array > 0]
[459]: array([7])
      1.2.3 NumPy logical Operator
      ### Fancy Indexing
[460]: arr = np.zeros((8, 4))
[461]: for i in range(8):
           arr[i] = i
[462]: arr
[462]: array([[0., 0., 0., 0.],
              [1., 1., 1., 1.],
              [2., 2., 2., 2.],
              [3., 3., 3., 3.],
              [4., 4., 4., 4.],
              [5., 5., 5., 5.],
              [6., 6., 6., 6.],
              [7., 7., 7., 7.]])
[463]: arr[[4, 3, 0, 6]]
```

```
[463]: array([[4., 4., 4., 4.],
              [3., 3., 3., 3.],
              [0., 0., 0., 0.],
              [6., 6., 6., 6.]])
[464]:
       arr[[-3, -5, -7]]
[464]: array([[5., 5., 5., 5.],
              [3., 3., 3., 3.],
              [1., 1., 1., 1.]])
[465]:
        arr = np.arange(32).reshape((8, 4))
[466]: arr
[466]: array([[ 0, 1, 2, 3],
              [4, 5, 6, 7],
              [8, 9, 10, 11],
              [12, 13, 14, 15],
              [16, 17, 18, 19],
              [20, 21, 22, 23],
              [24, 25, 26, 27],
              [28, 29, 30, 31]])
[467]:
        arr[[1, 5, 7, 2], [0, 3, 1, 2]]
[467]: array([ 4, 23, 29, 10])
[468]:
       arr[[1, 5, 7, 2]][:, [0, 3, 1, 2]]
[468]: array([[4, 7, 5, 6],
              [20, 23, 21, 22],
              [28, 31, 29, 30],
              [8, 11, 9, 10]])
[469]: arr.shape
[469]: (8, 4)
      1.2.4 NumPy universal Functions
[470]: np1 = np.array([0,1,2,3,4,5,6,7,8,9])
       np1
[470]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

```
[471]: #sqrt function
       np.sqrt((np1))
[471]: array([0.
                                   , 1.41421356, 1.73205081, 2.
                                                                         ])
              2.23606798, 2.44948974, 2.64575131, 2.82842712, 3.
[472]: #abslute value function
       np1= np.array([-3,-2-1,0,1,2,3,4,5,6,7,8,9])
       np.absolute((np1))
[472]: array([3, 3, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
[473]: #exponent fujnction
       np.exp((np1))
[473]: array([4.97870684e-02, 4.97870684e-02, 1.00000000e+00, 2.71828183e+00,
              7.38905610e+00, 2.00855369e+01, 5.45981500e+01, 1.48413159e+02,
              4.03428793e+02, 1.09663316e+03, 2.98095799e+03, 8.10308393e+03])
[474]: #min and max function
       np.max((np1))
[474]: 9
[475]: np.min((np1))
[475]: -3
[476]: #dot product calculation
       11 = [1,2,3]
       12 = [4,5,6]
       a1 = np.array((11))
       a2 = np.array((12))
       print("dot product via list")
       dot =0
       for i in range(len(l1)):
           dot += 11[i] * 12[i]
       print(dot)
       print("dot poroduct via NumPy array")
       dot = np.dot(a1,a2)
       print(dot)
      dot product via list
      dot poroduct via NumPy array
```

```
[477]: #linspae function
       np.linspace(5,15,9)
[477]: array([ 5. , 6.25, 7.5 , 8.75, 10. , 11.25, 12.5 , 13.75, 15. ])
[478]: mylinspace = np.linspace(5,15,9, retstep=True)
       mylinspace
[478]: (array([ 5. , 6.25, 7.5 , 8.75, 10. , 11.25, 12.5 , 13.75, 15. ]), 1.25)
[479]: mylinspace[1]
[479]: 1.25
[480]: #zeros() function
       np.zeros(6)
[480]: array([0., 0., 0., 0., 0., 0.])
[481]: #one function
       np.ones(6)
[481]: array([1., 1., 1., 1., 1., 1.])
[482]: np.zeros((5,5))
[482]: array([[0., 0., 0., 0., 0.],
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]
              [0., 0., 0., 0., 0.]])
[483]: np.zeros((5,4,3))
[483]: array([[[0., 0., 0.],
               [0., 0., 0.],
               [0., 0., 0.],
               [0., 0., 0.]],
              [[0., 0., 0.],
               [0., 0., 0.],
               [0., 0., 0.],
               [0., 0., 0.]],
              [[0., 0., 0.],
               [0., 0., 0.],
               [0., 0., 0.],
```

```
[0., 0., 0.]],

[[0., 0., 0.],
[0., 0., 0.],
[0., 0., 0.]],

[[0., 0., 0.],
[0., 0., 0.],
[0., 0., 0.],
[0., 0., 0.],
```

1.2.5 NumPy DataTypes

```
[484]: np.zeros(11, dtype='int64')
[484]: array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0])
[485]: np.zeros(11)
[485]: array([0., 0., 0., 0., 0., 0., 0., 0., 0., 0.])
  []:
      ### Transposing Arrays and Swapping Axes
[486]: arr = np.arange(15).reshape((3, 5))
[487]: arr
[487]: array([[ 0, 1, 2, 3, 4],
              [5, 6, 7, 8, 9],
              [10, 11, 12, 13, 14]])
[488]:
       arr.T #returnsthe array, transposed
[488]: array([[ 0, 5, 10],
                   6, 11],
              [ 1,
              [2, 7, 12],
              [ 3,
                   8, 13],
              [4,
                   9, 14]])
[489]:
       arr = np.array([[0, 1, 0], [1, 2, -2], [6, 3, 2], [-1, 0, -1], [1, 0, 1]])
[490]: arr
```

```
[490]: array([[ 0, 1, 0],
             [1, 2, -2],
             [6, 3, 2],
             [-1, 0, -1],
             [1, 0, 1]
[491]: np.dot(arr.T, arr)
[491]: array([[39, 20, 12],
             [20, 14, 2],
             [12, 2, 10]])
[492]:
       arr.T @ arr
[492]: array([[39, 20, 12],
             [20, 14, 2],
             [12, 2, 10]])
[493]: arr
[493]: array([[ 0, 1, 0],
             [1, 2, -2],
             [6, 3, 2],
             [-1, 0, -1],
             [1, 0, 1]])
[494]:
      arr.swapaxes(0, 1)
[494]: array([[ 0, 1, 6, -1,
                               1],
             [1, 2, 3, 0, 0],
             [0, -2, 2, -1,
                               1]])
      1.2.6 Pseudorandom Number Generation
[495]: samples = np.random.standard_normal(size=(4, 4))
[496]: samples
[496]: array([[ 0.64388249, -0.83486572, 0.81875284, -0.96590295],
             [-2.19260694, -0.63743414, 0.07675669, -1.00403397],
             [0.22750889, 0.04179036, -0.52341692, -0.23373595],
             [-0.55381454, -0.60664394, -2.29954216, 0.56674033]]
[497]:
       from random import normal variate
[498]:
       N = 1_{000}000
```

1.2.7 NumPy Reshaping

```
[499]: np1 = np.array([1,2,3,4,5,6,7,8,9,10,11,12])
      np1
[499]: array([ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12])
[500]: np1.shape
[500]: (12,)
[501]: np2 = np1.reshape(3,4)
      np2
[501]: array([[ 1, 2, 3, 4],
             [5, 6, 7, 8],
             [ 9, 10, 11, 12]])
[502]: np2.shape
[502]: (3, 4)
[503]: np3 = np1.reshape(2,3,2)
      np3
[503]: array([[[ 1, 2],
              [3, 4],
              [5, 6]],
             [[7, 8],
              [ 9, 10],
              [11, 12]])
[504]: np3.shape
[504]: (2, 3, 2)
[505]: np4 = np3.reshape(-1)
      np4
[505]: array([ 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12])
[506]: np4.shape
[506]: (12,)
```

1.2.8 Another example

```
grid = np.arange(1, 10).reshape(3, 3)
[507]:
[507]: array([[1, 2, 3],
              [4, 5, 6],
              [7, 8, 9]])
      Note that for this to work, the size of the initial array must match the size of the reshaped array,
      and in most cases the reshape method will return a no-copy view of the initial array.
[508]: x = np.array([1,2,3])
       x.reshape((1,3))
[508]: array([[1, 2, 3]])
[509]: x.reshape((3,1))
[509]: array([[1],
              [2],
              [3]])
[510]: x[np.newaxis, :]
[510]: array([[1, 2, 3]])
        x[:, np.newaxis]
[511]:
[511]: array([[1],
               [2],
               [3]])
             Stacking together different arrays
  []:
      1.2.10 Iterate through NumPy array
[512]: np1 = np.array([1,2,3,4,5,6,7,8,91,10,11,12])
[513]: np1
[513]: array([ 1, 2, 3, 4, 5, 6, 7, 8, 91, 10, 11, 12])
```

np2 = np.array([[1,2,3,4,5],[6,7,8,9,10]]) np2

```
[514]: for x in np.nditer(np2):
           print(x)
      1
      2
      3
      4
      5
      6
      7
      8
      9
      10
      11
      12
      1.2.11 Concatenation of Arrays
[515]: x = np.array([1,2,3])
       y = np.array([3,2,1])
       np.concatenate([x,y])
[515]: array([1, 2, 3, 3, 2, 1])
[516]: z = np.array([3,5,6,8,67])
       np.concatenate([x,y,z])
[516]: array([ 1, 2, 3, 3, 2, 1, 3, 5, 6, 8, 67])
[517]: grid = np.array([[1, 2, 3], [4, 5, 6]])
       np.concatenate([grid,grid])
[517]: array([[1, 2, 3],
              [4, 5, 6],
              [1, 2, 3],
              [4, 5, 6]])
[518]:
        # concatenate along the second axis (zero-indexed
        np.concatenate([grid, grid], axis=1)
[518]: array([[1, 2, 3, 1, 2, 3],
              [4, 5, 6, 4, 5, 6]])
      For working with arrays of mixed dimensions, it can be clearer to use the np.vstack (vertical stack)
      and np.hstack (horizontal stack) functions
[519]: # vertically stack the arrays
```

np.vstack([x, grid])

```
[519]: array([[1, 2, 3],
              [1, 2, 3],
              [4, 5, 6]])
[520]: # horizontally stack the arrays
        y = np.array([[99],[99]])
        np.hstack([grid, y])
[520]: array([[ 1, 2, 3, 99],
              [4, 5, 6, 99]
      1.2.12 Splitting of Arrays
      The opposite of concatenation is splitting, which is implemented by the functions np.split, np.hsplit,
      and np.vsplit. For each of these, we can pass a list of indices giving the split points
[521]: x = [1, 2, 3, 99, 99, 3, 2, 1]
       x1, x2, x3 = np.split(x, [3,5])
[522]: x1
[522]: array([1, 2, 3])
[523]: x2
[523]: array([99, 99])
[524]: x3
[524]: array([3, 2, 1])
           Sorting NumPy array
[525]: np1 = np.array([5,1,78,9,1,5786,2,4,7,0])
       np.sort(np1)
[525]: array([
                                    2,
                                          4,
                                                5,
                                                      7,
                                                          9,
                                                                  78, 5786])
               0,
                       1,
                              1,
[526]: np2 = np.array(['Zakir', 'John', 'Tina', 'Aaron'])
       np.sort(np2)
[526]: array(['Aaron', 'John', 'Tina', 'Zakir'], dtype='<U5')
[527]: np3 = np.array([True, False, True, False, True, True, False])
       np.sort(np3)
```

True])

[527]: array([False, False, False, True, True, True,

```
[528]: np4 = np.array([[3,7,1,5,89],[3,8,90,2,90]])
      np.sort(np4)
[528]: array([[ 1, 3, 5, 7, 89],
             [2, 3, 8, 90, 90]])
[529]: grid = np.arange(16).reshape((4, 4))
       grid
[529]: array([[ 0, 1, 2, 3],
             [4, 5, 6, 7],
             [8, 9, 10, 11],
             [12, 13, 14, 15]])
[530]: upper, lower = np.vsplit(grid, [2])
      print(upper)
      print(lower)
      [[0 1 2 3]
       [4 5 6 7]]
      [[8 9 10 11]
       [12 13 14 15]]
[531]: left, right = np.hsplit(grid, [2])
       print(left)
       print(right)
      [[0 1]
       [45]
       [8 9]
      [12 13]]
      [[2 3]
       [6 7]
       [10 11]
       [14 15]]
      1.3.1 NumPy Searching
[532]: np1 = np.array([1,2,3,4,5,3,6,68678,6,78,87,78])
      print(np1)
      print(np.where(np1==3))
          1
                2
                      3
                            4
                                  5
                                        3
                                              6 68678
                                                         6
                                                              78
                                                                    87
                                                                          78]
      (array([2, 5]),)
[533]: a = np.where(np1==3)[0]
      print(a)
```

```
[2 5]
[534]: print(np1[a[0]])
      3
[535]: ## prints even numbers
      y = np.where(np1 \% 2 == 0)
      print(np1)
      print(y)
      print(y[0])
                       3
                                              6 68678
                                                          6
                                                               78
                                                                           78]
                                                                     87
      (array([ 1, 3, 6, 7, 8, 9, 11]),)
      [1 3 6 7 8 9 11]
[536]: ## prints odd numbers
      y = np.where(np1 \% 2 == 1)
      print(np1)
      print(y)
      print(y[0])
      1
                2
                      3
                                        3
                                              6 68678
                                                               78
                                                                     87
                                                                           781
                            4
      (array([ 0, 2, 4, 5, 10]),)
      [ 0 2 4 5 10]
      Filtering NumPy Arrays with Boolean Index lists
[537]: np1 = np.array([1,2,3,4,5,6,7,8,9,10])
      x = [True, True, False, False, True, False, False, False, False]
[538]: print(np1)
      print(np1[x])
      [1 2 3 4 5 6 7 8 9 10]
      [1 2 5]
[539]: filtered = []
      for thing in np1:
          if thing % 2 == 0:
              filtered.append(True)
          else:
              filtered.append(False)
      print(np1)
      print(filtered)
      new = np1[filtered]
      print(new)
```

```
[1 2 3 4 5 6 7 8 9 10]
     [False, True, False, True, False, True, False, True]
     [2 4 6 8 10]
[540]: filtered = []
      for thing in np1:
         if thing > 5:
             filtered.append(True)
         else:
             filtered.append(False)
      print(np1)
      print(filtered)
      new = np1[filtered]
      print(new)
     [1 2 3 4 5 6 7 8 9 10]
     [False, False, False, False, True, True, True, True, True]
     [678910]
[541]: filtered = np1 % 2 ==0
      print(np1)
      print(filtered)
      new = np1[filtered]
      print(new)
     [1 2 3 4 5 6 7 8 9 10]
     [False True False True False True False True]
     [ 2 4 6 8 10]
[542]: filtered = np1 > 5
      print(np1)
      print(filtered)
      new = np1[filtered]
      print(new)
     [1 2 3 4 5 6 7 8 9 10]
     [False False False False True True True True]
     [678910]
 []:
```