

Find numerical (the first scheme against the flow) solutions of one-dimensional transport equation

$$\frac{\partial u}{\partial t} + c \frac{\partial u}{\partial x} = 0; x \in (0,1), t > 0$$

with the following conditions:

$$c = 1;$$

$$\begin{aligned} 1. \quad & u(t=0, x) = \cos\left(\frac{\pi x}{2}\right); \\ & u(t, x=0) = 1, \quad u(t, x=1) = 0. \end{aligned}$$

$$c = -1;$$

$$\begin{aligned} 2. \quad & u(t=0, x) = \cos\left(\frac{\pi x}{2}\right); \\ & u(t, x=0) = 1, \quad u(t, x=1) = 0. \end{aligned}$$

$$c = 0.5;$$

$$\begin{aligned} 3. \quad & u(t=0, x) = x; \\ & u(t, x=0) = 0, \quad u(t, x=1) = 1. \end{aligned}$$

$$c = 1;$$

$$\begin{aligned} 4. \quad & u(t=0, x) = 0; \\ & u(t, x=0) = 1, \quad u_x(t, x=1) = 0. \end{aligned}$$

$$c = -1;$$

$$\begin{aligned} 5. \quad & u(t=0, x) = x+1; \\ & u(t, x=0) = 1, \quad u(t, x=1) = 2. \end{aligned}$$

$$c = 1;$$

$$\begin{aligned} 6. \quad & u(t=0, x) = 0; \\ & u(t, x=0) = 1, \quad u(t, x=1) = 3. \end{aligned}$$

$$c = -1;$$

$$\begin{aligned} 7. \quad & u(t=0, x) = 0; \\ & u_x(t, x=0) = 0, \quad u(t, x=1) = 1. \end{aligned}$$

$$c = 2;$$

$$\begin{aligned} 8. \quad & u(t=0, x) = \cos\left(\frac{\pi x}{2}\right); \\ & u(t, x=0) = 1, \quad u(t, x=1) = 0. \end{aligned}$$

$$c = -0.5;$$

$$9. \quad u(t=0, x) = 1 - x;$$

$$u(t, x=0) = 1, \quad u(t, x=1) = 0.$$

$$c = -1;$$

$$10. \quad u(t=0, x) = x + 1;$$

$$u_x(t, x=0) = 1, \quad u(t, x=1) = 2.$$

$$c = 1;$$

$$11. \quad u(t=0, x) = 0;$$

$$u(t, x=0) = 1, \quad u(t, x=1) = 0.$$

$$c = -2;$$

$$12. \quad u(t=0, x) = x + 1;$$

$$u(t, x=0) = 1, \quad u(t, x=1) = 2.$$

$$c = 1;$$

$$13. \quad u(t=0, x) = \cos\left(\frac{\pi x}{2}\right);$$

$$u(t, x=0) = 1, \quad u_x(t, x=1) = 0.$$

$$c = -1;$$

$$14. \quad u(t=0, x) = x;$$

$$u(t, x=0) = 0, \quad u(t, x=1) = 1.$$

$$c = 1;$$

$$15. \quad u(t=0, x) = 1;$$

$$u(t, x=0) = 2, \quad u(t, x=1) = 1.$$

$$c = 1;$$

$$16. \quad u(t=0, x) = \cos\left(\frac{\pi x}{2}\right);$$

$$u(t, x=0) = 1, \quad u_x(t, x=1) = 1.$$

$$c = 1;$$

$$17. \quad u(t=0, x) = 0;$$

$$u(t, x=0) = 1, \quad u(t, x=1) = 2.$$

$$c = -1.5;$$

$$18. \quad u(t=0, x) = 0;$$

$$u(t, x=0) = 1, \quad u(t, x=1) = 0.$$

$$c = 1;$$

$$19. u(t = 0, x) = \sin(\pi x);$$

$$u(t, x = 0) = 0, \quad u(t, x = 1) = 0.$$

$$c = -1;$$

$$20. u(t = 0, x) = 0.5;$$

$$u(t, x = 0) = 0.5, \quad u(t, x = 1) = 0.$$

Draw graphs for different three time moments. Do not forget to demonstrate stability condition.