

Catalogue Information:

N_R = Number of tuples in Relation R.

B_R = Number of blocks contains in R ($\frac{N_R}{F_R}$)

S_R = Size of a tuple of R

F_R = Blocking Factor; Number of tuple from R that fit into one block.

$$\left\lfloor \frac{N_R}{B_R} \right\rfloor$$

$V(A, R)$ = Number of distinct value for attribute A in R.

$Se(A, R)$ = Selectivity of attribute A
= Avg. number of tuple R satisfy equality condition on A.
 $\frac{N_R}{V(A, R)}$

Let's understand with example :

Student

Roll	Name
1	A
2	B
3	C
4	D
5	E
6	F
7	G
8	H
9	I

2 bytes 8 bytes

block 1
block 2
block 3

$$NR = 9$$

$$BR = 3$$

$$IR = \text{Size of each Record} \\ = 2 + 8 = 10 \text{ bytes}$$

$$fr = \frac{NR}{BR} = \frac{9}{3} = 3$$

$$V(A, R) =$$

$$V(\text{Roll}, \text{Student}(R)) = 9$$

$$V(\text{Name}, u) = 9$$

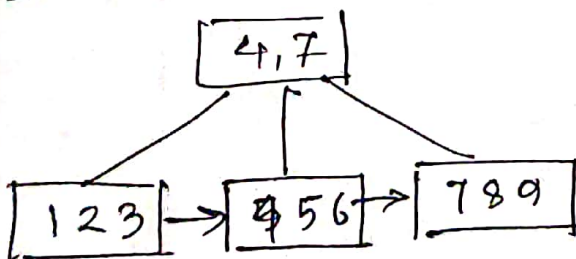
ID
a
b
c

$$V(ID, R(R)) = 3$$

here; select * from V
where Branch = 'BE'

$$S(B, R) = \frac{NR}{V(B, V)} = \frac{6}{2} = 3$$

B+ tree



Roll	Branch
1	BE
2	BE
3	ME
4	BE
5	ME
6	ME

BE/ME = 3
Equally dist.

If each value of an attribute have uniform distribution means equal probability, then selection result can be estimated to have

$$\frac{NR}{V(IR)} \text{ records}$$

Query Optimization

Complex conjugation :

S_i = the number of satisfying tuples

Student

Roll	Branch	G
1	BE	M
2	BE	F
3	ME	M
4	ME	M
5	BE	F
6	BSe	M

$$S_{BE} = 3$$

$$S_{MB} = 2$$

$$S_{BSe} = 1$$

$$S_M = 4$$

$$S_F = 2$$

$$P[BE] = \frac{3}{6} = \frac{1}{2}$$

$$P[MB] = \frac{2}{6} = \frac{1}{3}$$

$$P[BSe] = \frac{1}{6}$$

$$P[M] = \frac{4}{6} = \frac{2}{3}$$

$$P[F] = \frac{2}{6} = \frac{1}{3}$$

Select * from Student

where Branch = 'BE' & Gender = 'F'

$$\sigma_{\text{Branch} = 'BE' \wedge \text{Gender} = 'M'} (\text{Student})$$

$$= 6 \times \frac{3}{6} \times \frac{4}{6} = 2$$

$$\sigma_{\text{Branch} = 'BE' \wedge \text{Gender} = 'F'} (\text{Student})$$

$$= 6 \times \frac{3}{6} \times \frac{2}{6} = \frac{2}{3}$$

Disjunction :

select * from Student

where Branch = "BE" or Gender = "F".

$$NR * \left(1 - \left(1 - \frac{S_1}{NR} \right) \times \left(1 - \frac{S_2}{NR} \right) \times \left(1 - \frac{S_3}{NR} \right) \right)$$

$$6 * \left(1 - \left(1 - \frac{3}{6} \right) \times \left(1 - \frac{2}{6} \right) \right)$$

$$= 6 * \left(1 - \frac{3}{6} \times \frac{4}{6} \right) = 6 * \left(1 - \frac{1}{3} \right) = \frac{12}{2} = 4$$

$\sigma_{A \leq v}$ or $\sigma_{A \geq v}$ cases :

Roll	Marks
1	90
2	62
3	40
4	75
5	82

①

where marks < 39 ;

②

where marks > 90 ;

③

where marks < 50 ;

④

where marks > 80 ;

$$\min(\text{marks}) = 40$$

$$\max(\text{marks}) = 90$$

for ① & ② the values are out of range. \therefore tuples = 0

for ③

$$\text{tuples} = \frac{\text{value} - \min(R)}{\max(R) - \min(R)} \times \text{value (total tuple)}$$

$$= \frac{50 - 40}{90 - 40} \times 5$$

$$= \frac{10}{50} \times 5 = \frac{10}{10} = 1$$

for ④

$$\text{tuples} = 5 \times \frac{80 - 40}{90 - 40}$$

$$= 5 \times \frac{40}{50}$$

$$= 4 \quad \text{Ans}$$

2nd table at 2nd Q of 5 tuples = $NR/2$

2nd

Negation :

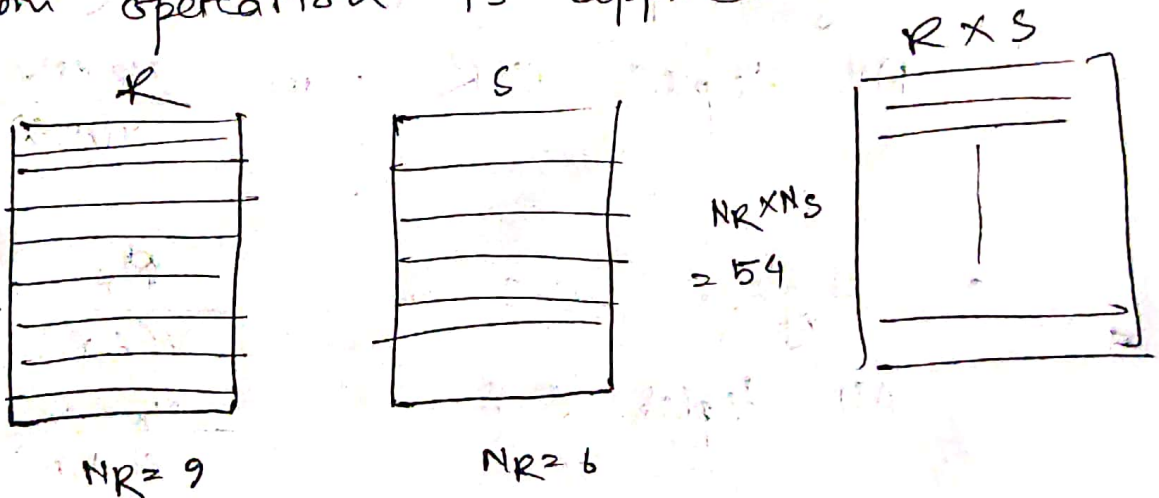
Select * from Student
where Branch != "BE";

$$\begin{aligned} N_R - \text{size}(\sigma_{\theta}(R)) &\Rightarrow N_R - \text{size}(\sigma_{BE}(SH)) \\ &= N_R - \frac{N_R}{V(\text{Branch}, SH)} \\ &= 6 - \frac{6}{3} = 6 - 2 = 4 \quad (\text{Ans}) \end{aligned}$$

estimated number of records present in Br.

Join size Estimation :

Determine the size of table after join operation is applied



① $R \cap S = \emptyset$ (No attr. is common).

$\{a, b, c, d\} \cap \{c, d, e\} = \emptyset$ (a, b, c, d are attr.)

② $R \cap S = \text{key of } R/S \text{ table.}$

(or)
A record of S (or R) will join with at most one record from R (or S).

यदि Foreign key \rightarrow Table \in NR \rightarrow \rightarrow
 आमतौर join table का size $2(N+1)$

③ $R \cap S = X$ where X is not key of
 neither R or S .

Roll	Sid
1	S ₁
2	S ₂
3	S ₃
4	S ₄

$N_R = 4$

Sid	Topics
S ₁	T ₁
S ₂	T ₂
S ₃	T ₃

$N_S = 3$

Sid	SName
S ₁	Phy
S ₂	chem
S ₃	Math
S ₄	BIO

Rules:

• single tuple $\in R$ produces $\frac{N_S}{V(A, S)}$ tuples in $R \cap S$

All tuples $\in R$ " $\frac{N_R \times N_S}{V(A, S)}$

• single tuple $\in S$ " " " "

All tuples $\in S$ " " " "

$\frac{N_R}{V(A, R)}$ " " "
 $\frac{N_R \times N_S}{V(A, R)}$ " " "

Now, in the given example.

For tuple $\in R$,

$$\frac{4 \times 3}{3} = \frac{12}{3} = 4$$

$A = R \cap S = 2 \text{ Sid}$

For tuple $\in S$,

$$\frac{4 \times 3}{4} = \frac{12}{4} = 3$$

Ans = $\min(4, 3) = 3$

* primary key বরাবর খুঁজলে $\log_2(NR)$ টিকে লাগে

কয়টি block Access করবে?

→ formula = ~~total~~ total blocks + tuple access time within block

$$= \left\lceil \frac{\frac{NR}{V(A,R)}}{F_r} \right\rceil + \log_2 \left(\frac{NR}{F_r} \right)$$

যদি binary search
২২৫

যদি B+ tree ২২৫

Tree height + 1] Primary index, equality on key

Tree height + $\left\lceil \frac{NR}{\frac{V(A,R)}{F_r}} \right\rceil$ গড়

যদি $\sigma_A = 5$ মান

Primary index but not equality on key.

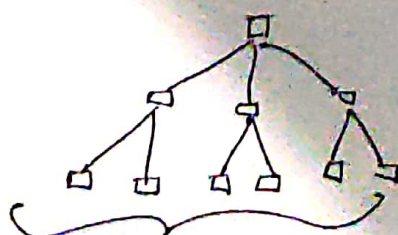
time to Access the index(block)

Access the tuples in the specified index

Searching index
এটি index table থেকে index find করার জন্য

এটি specified index এ tuple খোঁজে যেখানে মেজাজে আছে

access the blocks



index table is leaf node এ মান (Tree height)

then ২২৫ tuple খুঁজবে